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VARIA

Outcome Variable	Are the observations independent or correlated?		Alternatives (assumptions violated)
	independent	correlated	
Continuous (e.g. pain scale, cognitive function)	Ttest ANOVA Linear correlation Linear regression	Paired ttest Repeated-measures ANOVA Mixed models/GEE modeling	Wilcoxon sign-rank test Wilcoxon rank-sum test Kruskal-Wallis test Spearman rank correlation coefficient
Binary or categorical (e.g. fracture yes/no)	Risk difference/Relative risks Chi-square test Logistic regression	McNemar's test Conditional logistic regression GEE modeling	Fisher's exact test McNemar's exact test
Count data	Poisson regression Negative binomial regression	GEE modeling	
Time-to-event (e.g. time to fracture)	Rate ratio Kaplan-Meier statistics (Parametric regression) Cox regression	Frailty model	Time-varying effects if PH assumption violated



Modelling counts

the Poisson distribution

- Famous example by von Bortkiewicz (1898): observe the number of soldiers in the Prussian army who got kicked by horses over a number of years and corps

# kicks (=k)	# soldiers	fraction	Expected fraction
0	109	0.545	0.543
1	65	0.325	0.331
2	22	0.110	0.101
3	3	0.015	0.021
4	1	0.005	0.003

- Average nr of horsekicks per soldier:

$$\bar{X} = \frac{0*109+1*65+2*22+3*3+4*1}{200} = 0.61$$

- The probability that the nr of kicks=k

$$P(X = k) = \frac{\lambda^k e^{-\lambda}}{k!} \qquad \hat{\lambda} = \bar{X}$$

Generalized linear models (GLM)

- A glm consists of 3 parts
 - A ***distribution***, specifying the conditional distribution of the the response Y given the predictor variables

$$\eta = \beta_0 + \beta_1 x_1 + \dots + \beta_p x_p$$

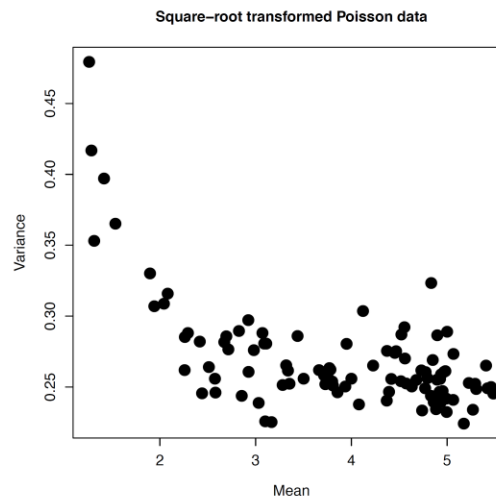
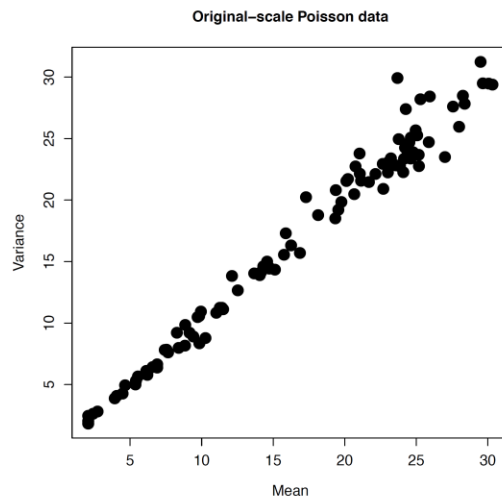
- A ***linear predictor***

$$g(E[Y|X]) = \eta$$

- A ***link function*** g , linking the conditional expected value of Y to η

Poisson regression: link function

- Distribution: Poisson
- Link function: log
 - The link function transforms the mean, not the observed values
$$\log(E[Y|X]) \neq E[\log(Y|X)]$$
 - Transforming the observed values changes the association between mean and variance



offset

- Incorporate normalization factor as offset
 - Eg in lateral root data: count nr of lateral roots and normalize by root length

$$\log(E[Y|X]) = \beta_0 + \beta_1 X_1 + \log(\text{rootlength})$$

- The counts are not explicitly scaled

$$\log(E[\frac{Y}{\text{rootlength}}|X]) = \beta_0 + \beta_1 x_1$$

Longitudinal analysis

- Measurements on the same subject ifo time
- Measurements done on the same subjects are correlated

Logistic regression

- Binary response
- The residuals are non-normal and heteroscedastic
- Predictions can take values >1 or <0
- Logit model $\ln[p/(1-p)] = \beta_0 + \beta_1 X + \varepsilon$ solves this problem
- p the probability of $Y=1$ $P(Y=1 | X)$
- $p/(1-p)$ =odds ratio
- $\ln[p/(1-p)] = \ln(\text{odds ratio}) = \text{“logit”}$

Survival analysis

- Binary response
- Analyses time to event
- Censored data
- examples:
 - Time till death
 - Time till recidivism
 - Time until 70% of the machines break down
- The survival function is the probability to survive beyond $S(t)$
- Univariate
 - Kaplan-Meier curve
- Multivariate
 - Cox proportional hazards

Looking for courses or consulting

- @UGent
 - Faculty of Medicine:
<https://www.ugent.be/ge/en/services/biostatistics-unit>
 - Faculty of Veterinary Medicine: contact [Luc Duchateau](#)
 - Department of Plant Biotechnology and Bioinformatics,
contact: [Veronique Storme](#)
 - Faculty of Psychology and Educational Sciences - [Statistics support](#)
 - Other faculties: [FIRE](#)
- <https://lstat.kuleuven.be/consulting>
- <https://www.uantwerpen.be/en/research-and-innovation/research-at-uantwerp/core-facilities/core-facilities/statua/who-we-are/>
- <https://www.flames-statistics.com/>! Flames Summer School @UGent
- <https://www.ugent.be/we/en/services/ICES>

Useful R links

- <https://onlinecourses.science.psu.edu/stat464/>
- <http://www.r-tutor.com/>
- <http://www.cookbook-r.com/>
- <https://www.datacamp.com/>
- <http://www.statmethods.net/index.html>
- <http://www.rdocumentation.org/>
- <https://www.zoology.ubc.ca/~schluter/R/>
- <http://www.sr.bham.ac.uk/~ajrs/R/index.html>
- <http://www.r-bloggers.com/>
- <http://r4stats.com/>
- <http://www.ats.ucla.edu/stat/r/>
- <http://manuals.bioinformatics.ucr.edu/home>