

Question 2.

a. Using Q4.3:

- Op1A = 5.7

$5.7 \times 2^3 = 45.6_{10} \xrightarrow{45} 0010\ 1101_2$

So Op1A = 00101.101

- Op2A = 7.2

$7.2 \times 2^3 = 57.6_{10} \xrightarrow{57} 0011\ 1001_2$

So Op2A = 00011.001

45 : 2 = 22	1	2 : 2 = 1	0
22 : 2 = 11	0		
11 : 2 = 5	1		
5 : 2 = 2	1		
↪ 101101 ₂			
57 : 2 = 28	1	3 : 2 = 1	1
28 : 2 = 14	0		
14 : 2 = 7	0		
7 : 2 = 3	1		
↪ 111001 ₂			

b. $(5.7 + 7.2) =$

$$\begin{array}{r} 111\ 001 \\ 0010\ 1101 \\ + \\ 0011\ 1001 \\ \hline \end{array}$$

B. 01100110 → B = +1100.110

c. $0110\ 0110_2 = + (1 \times 2^3 + 1 \times 2^2 + 1 \times 2^{-1} + 1 \times 2^{-2})$
 $= 12.75_{10}$

So C = 12.8

Question 3:

a. Using Q5.2:

- Op1A = 10.04

$10.04 \times 2^2 = 40.16_{10} \xrightarrow{40} 0010\ 1000_2$

So Op1A = 001010.00₂

40 : 2 = 20	0
20 : 2 = 10	0
10 : 2 = 5	0
5 : 2 = 2	1
2 : 2 = 1	0
↪ 101000 ₂	

$$- \text{Op2A} = 0.01$$

$$0.01 \times 2^2 = 0.04 \xrightarrow{0} 0000\ 0000_2$$

$$\text{So Op2A} = .000000.00$$

$$\text{b. } 10.04 + 0.01$$

$$\begin{array}{r} 001010.00 \\ + 000000.00 \\ \hline 001010.00_2 \end{array}$$

$$\text{So B} = +01010.00$$

$$\text{c. We have B} = 001010.00_2$$

$$= + (1 \times 2^3 + 1 \times 2^1) = 10_{10}$$

$$\text{So C} = 10.00$$

Question 4:

a. Using 4.3 format:

$$- \text{Op1A} = -5.9$$

$$= - (5.9 \times 2^3) = - (47.2) \xrightarrow{4} - (0010\ 1111)_2$$

$$47: 2 = 23 \mid 1$$

$$23: 2 = 11 \mid 1$$

$$11: 2 = 5 \mid 1$$

$$5: 2 = 2 \mid 1$$

$$2: 2 = 1 \mid 0$$

$$\hookrightarrow 00101111_2$$

$$\text{Convert bit: } 11010000$$

$$\text{Add 1: } 11010001$$

$$\text{So } -5 \text{ Op1A} = 11010001_2$$

$$\text{In } -Op2A = 5.7$$

$$= 5.7 \times 2^3 = 45.6_{10} \xrightarrow{45} 0010 \ 1101$$

$$45:2 = 22 \mid 1 \quad 2:2 = 1 \mid 0$$

$$22:2 = 11 \mid 0$$

$$11:2 = 5 \mid 1$$

$$5:2 = 2 \mid 1$$

$$\hookrightarrow 101101_2$$

$$\text{So } Op2A = 0010 \ 1101_2$$

$$b. (-5.9) - (5.7)$$

I would use the cal: $(-5.9) + (-5.7)$

$$\begin{aligned} -(5.7) &= -(0010 \ 1101)_2 = (1101 \ 0010 + 1)_2 \\ &= 1101 \ 0011_2 \end{aligned}$$

$$\begin{array}{r} 1101 \ 0001 \\ + 1101 \ 0011 \\ \hline \end{array}$$

$$110100100$$

$$\text{So } B =$$

$$1010 \ 0100$$

$$00101$$

$$1100$$

c. We can see the sign bit = 1.

Perform 2's complement

$$11010 \ 0100$$

$$11010 \ 0011$$

$$\text{Convert: } 00101 \ 1100$$

$$\begin{aligned} 00101 \ 1100_2 &= 1 \times 2^3 + 1 \times 2^1 + 1 \times 2^0 + 1 \times 2^{-1} \\ &= 11.5 \end{aligned}$$

$$\text{So } C = -11.5$$

Question 5:

a. floating point: 6000 mmmm.

$$OpA = -3.5$$

Since we have 3 exp bit, the exp. offset is: $2^{3-1} = 3$

$$(3.5) \times 2^4 = 56_{10} = 0111000_2$$

$$56 : 2 = 28 \mid 0$$

$$3 : 2 = 1 \mid 1$$

$$28 : 2 = 14 \mid 0$$

$$14 : 2 = 7 \mid 0$$

$$7 : 2 = 3 \mid 1$$

$$\hookrightarrow 111000$$

$$\text{and} = 1.1100 \times 2^1 = (-1)^1 \times 1.1100 \times 2^{4-3} \hookrightarrow 100$$

$$\text{So } OpA = 11001100$$

b. We have: $(-1)^1 \times (1 + 2^{-1} + 2^{-2}) \times 2^1 = -3.5$

$$\text{So } OpB = -3.5$$

Question 6:

a. floating point: 5000 mmmm.

$$OpA = 0.41$$

Since we have 3 exp bit, the exp. offset is $2^{3-1} = 3$

$$0.41 \times 2^4 = 6.56 \xrightarrow{b} 0110_2$$

$$6 : 2 = 3 \mid 0$$

$$3 : 2 = 1 \mid 1$$

$$\hookrightarrow 110_2$$

$$\text{and} = 1.1000 \times 2^{-2} = 1.1000 \times 2^{1-3} \hookrightarrow 001$$

$$\text{So } OpA = 0001000$$

0.0110

b. We have 00011000

$$\hookrightarrow (-1)^0 \times (1 + 2^{-1}) \times 2^{-2} = 0.375$$

So $B = 0.38$

Question 7. $(-6) < (-35)$

At $A = -6_{10} = 0xFA$,

$B = -35_{10} = 0xDD$

$C = 0x22$

$D = 0x00$

$$E = 0x1C = A + C = \begin{array}{r} 0xFA \\ + 0x22 \\ \hline 0x11C \end{array}$$

and E is 8bit so it will return 0x1C with 1 on Car of overflow.

$F = 0xFA$

$G = 0x22$

$H = 0x00$

$I = 0x01$

Question 8. $(46) < (16)$

$A = 0x2E (= 46)$

$B = 0x10 (= 16)$

$C = 0xEF$

$D = 0x00$

$E = 0x1D$ where $E = A + C$

$$\begin{array}{r} 0x2E \\ \times 0xEF \\ \hline 0x1D \end{array}$$

$F = 0x2E$

$G = 0xEF$

$H = 0x00$

$I = 0x01$

so E will be returned as 1D and an overflow in the ADDER