

Aquaculture

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Overview

Introduction

What is aquaculture?

What is the current problem?

Solution

Defining our model

Adjusting the model

Cost function

Optimal harvesting time

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What is aquaculture

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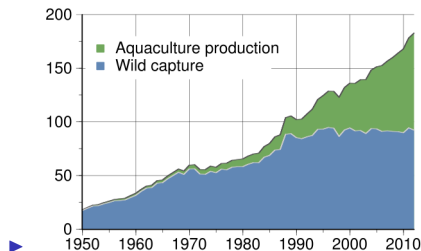


Figure: Global production of aquatic organisms in million tonnes, since 1950, as reported by the FAO

What is aquaculture

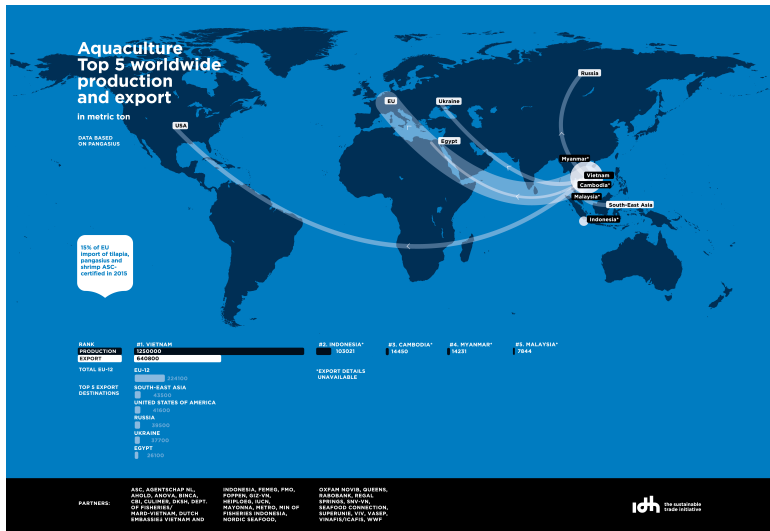


Figure: Aquaculture production and exports

What is aquaculture

Today will talk about farming fish!

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We can help by determining the best time for harvesting the fish.

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Defining our model

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Biologists often refer to equation (1) as the **allometric equation**

Defining our model

We can solve the equation for $\alpha \neq 1$

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$$W(t) = [(1 - \alpha) Kt + C]^{\frac{1}{1-\alpha}}$$

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$$\frac{dW}{dt} = KW^\alpha S \quad (2)$$

$$S = 1 - \left(\frac{W}{W_{max}}\right)^\mu$$

Adjusting our model

We can find $W(t)$ using some constant given for t measured in months ($K = 10$, $\alpha = \frac{3}{4}$, $\mu = \frac{1}{4}$, $W_{max} = 81$ ounces and $W(0) = 1$ ounce).

$$\frac{dW}{dt} = 10W^\alpha - \left(\frac{10W}{3}\right)$$

$$W(t) = e^{\frac{-10}{3}t} \left(3e^{\frac{5t}{6}} - 2\right)^4$$

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We can find the function $C(t)$ using some empiric constants: $K_1 = 0.4$, $K_2 = 0.1$, $C(0) = 1.1$ (dollars), and $W(t)$ we determined already.

Cost function

$$\frac{dC}{dt} = K_1 + K_2 \frac{dW}{dt} \text{ (integrate the equation)}$$

$$C(t) = K_1 t + K_2 W(t) + K_3$$

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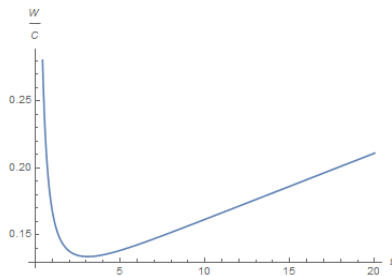


Figure: Cost / Weight ratio.

Optimal harvesting time

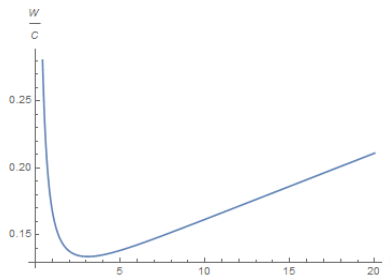


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Optimal time to harvest the fish is around **3 months** (3.0853) with a cost ratio of **0.13**.

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Bibliography I



R.K. Nagle, E.B. Snaff, A.D. Sieder

Fundamentals of Differential Equations and Boundary Value Problems.

Addison-Wesley, 2012.



S. Balint, L. Braescu, E. Kaslik

Ordinary and Partial Differential Equations Lecture Notes
West University of Timisoara, 2006. 2000.