Functional Programming – Laboratory 5 Tail recursion, Control

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1 Concepts

- Tail recursion
- when, unless, let, let*
- block, tagbody, loop
- \bullet progn, prog1, prog2
- prog, prog*
- do, do*, dolist, dotimes

2 Questions from Laboratory 4

- How many types of recursion do you know? Which one is the most efficient?
- How do we recognize a tail recursive function? What is the method used for writing tail recursive functions? Give one example of a tail recursive function (write the definition of the function in LISP).
- Simulate (trace function name), where function name is the name of your own function.

3 Control

3.1 when, unless

```
> (when (= 8 9) 4 9)
> (when (< 8 9) (print 'azi) 4 9)
> (when (> 10 9))
> (unless (> 10 9) 100 'nothing)
```

```
> (unless (> 10 9) 100 (print 'nothing))
> (unless (< 10 9) 100 (print 'nothing))
> (unless (< 10 9) (print 'nothing) 100)
   when and unless are equivalent with:
 (unless p a b c) = (cond ((not p) a b c))
 (\mathbf{unless} \ p \ a \ b \ c) = (\mathbf{when} \ (\mathbf{not} \ p) \ a \ b \ c)
 (when p \ a \ b \ c) == (cond (p a b c))
 (\mathbf{when} \ \mathbf{p} \ \mathbf{a} \ \mathbf{b} \ \mathbf{c}) = (\mathbf{unless} \ (\mathbf{not} \ \mathbf{p}) \ \mathbf{a} \ \mathbf{b} \ \mathbf{c})
3.2 block, tagbody, loop
; construction of a block — the structure
(block block_name <form1> <form2> .... <formn>)
; < form1 > < form2 > \dots < formn > are optional
; in the case of missing it will return NIL
> (block_block_name (print 'expr1) (print 'expr2) (print 'expr3))
> (block block_name 1 2 3 4)
> (block block_name 2)
; Blocks with abrupt exit
; for this we use
; return-form or return.
; When return-form block_name is evaluated the program exits
; the block\ block\_name\ with\ the\ value\ resulted\ from\ the
; evaluation of the second argument (which is optional
; < form1 > < form2 > \ldots < formn >),
; if this is missing, then we get \mathit{NIL}.
> (block block_name3
           (setq x 1)
           (print (1+ x))
           (return-from block_name3 (1+ x))
           (print 4))
> (block_block_name33
         (\text{setq x 1})
         (\mathbf{print} (1+ x))
         (\operatorname{setq} x (1+ x))
```

```
(return-from block_name33 (1+ x))
       (print 4))
; return is used in order to exit blocks with the name {\it NIL}
; do, dolist, dotimes and loop include implicitly a
; block with the name nil):
> (dolist (x '(1 2 3)))
> (dolist (x '(1 2 3)) (print x))
> (dolist (x '(2 3 -7 5))
          (print x)
          (if (< x 0) (return 'done)))
; Any function definition is a block with the name the name of the function
; from the body of the function we exit using
; return-from
> (defun f()
       (print 'a)
       (return-from f 10)
       (print 'b))
> (f)
; Blocks within which you can use gotos
> (tagbody again
          (\operatorname{setq} x (1+ x))
          (if (< x 5) (go again)
                       (go end)
          )
          end
       (print x)
> (tagbody lala (setq v 9) (print v))
; read a number until that number is greater than 0
> (tagbody retake
          (print 'Introduce >)
          (if (plusp (read))
                      (go retake)
                      'done
          )
INTRODUCE>
23
```

```
INTRODUCE>
INTRODUCE>
INTRODUCE>
-90
NIL
> (block some
       (setq d (1+ 3))
       (print d)
       (if (< d 4) (go some)
                    (return-from some 100)
       (print 'somethingStrage)
> (tagbody some
       (setq d (1+ 3))
       (print d)
       (if (< d 4) (go some)
                    (return 100)
       (print 'somethingStrage)
> (tagbody some
       (setq d (1+ 3))
       (print d)
       (if (< d 4) (go some)
                    (go lala)
       lala
       (print 'somethingStrage)
```

Conclusions:

- (block block-name expression-1 expression-2 ... expression-n)
- (return [result])
- (return-from name [result])
- (return value) == (return-from nil value)
- $\bullet\,$ tagbody accepts symbols they are not evaluated.
- $\bullet\,$ If we reach the end of a tagbody nil is returned.
- loop repeatedly evaluates his parameters.
- \bullet We exit a loop using return or throw.

• Advise: try to not use go!

3.3 progn, prog1, prog2

```
> (setq w 11 xx 22)
> (values w xx)
> (values 1 2 3 4)
> (values '(1 2 3 4))
> (progn 10 (print 20) 30)
> (progn 10 (print 20) 30 (values 10 20 30))
> (progn 100 200 300 (values 10 20 30))
> (progn 1 2 3 4 5 6 7)
> (prog1 1 2 3 4 5 6 7)
> (prog2 1 2 3 4 5 6 7)
> (prog2 'la (values 2 3 4) 9)
> (prog2 'la (values '(2 3 4) 90) 9)
> (prog1 (+ 2 3) (+ 3 5) (+ 11 22))
> (prog2 (+ 2 3) (+ 3 5) (+ 11 22))
```

Conclusions:

- progn returns the last evaluation form (if the last evaluation returns multiple values, then progn will return them all);
- $\bullet\ prog1$ returns the first form evaluation (only its first value).
- $\bullet \ (prog2abc...z) == (progna(prog1bc...z))$

3.4 let, let*

let is used to group expressions and performs parallel binding of local variables to values.

let* performs sequential binding of local variables to values.

$$\begin{array}{ccc} (\,\mathbf{let}\,[\,\ast\,] & (\\ & (\,\mathrm{var}\!-\!1 \ \mathrm{value}\!-\!1\,) \end{array}$$

```
(var-2 value-2)
                    (var-m value-m)
               )
               expression-1
               expression-2
               expression-n)
> (let ((x 1) (y 2) (z 3)) (setq w (+ x y z)) (list x y z w))
> (let* ((x 1) (y (+ x 1)) (z (+ y 1))) (list x y z))
      prog, prog*
3.5
      (\mathbf{prog} \ (\mathbf{var}-1 \ \mathbf{var}-2 \ (\mathbf{var}-3 \ \mathbf{init}-3) \ \mathbf{var}-4 \ (\mathbf{var}-5 \ \mathbf{init}-5))
             expression-1
          value-1
             expression-2
              expression-3
              expression-4
          value-2
             expression-5
              . . .
       )
       prog\ is\ a\ combination\ between\ block , tagbody\ and\ let*
       prog opens implicitly a nil block, therefore
                       in order to exit we use return [result].
; \quad Example:
> (prog (i (sum 0))
          retake
          (\,\mathbf{print}\ 'Introduce>)
          (setq i (read))
          (if (> i 0)
                  (progn (setq sum (+ sum i)) (go retake))
                  (return sum)
          )
INTRODUCE>
34
INTRODUCE>
23
\hbox{INTRODUCE}\!\!>
11
INTRODUCE>
4.5
INTRODUCE>
```

```
-3
72.5
; use catch and throw
; Example: if x is greater than 0 returns ok,
; otherwise the result is the value of x
> (defun f1 (x)
       (catch 'ex1 (f2 x)))
> (defun f2 (x)
       (if (minusp x)
               (throw 'ex1 x)
     'ok
> (f1 2)
> (f1 -2)
;; the mechanism of catch and throw is:
; - when throw is evaluated, it does not evaluate the
      forms after throw, but it takes up the forms
      (located in the interpreter stack)
       until it reaches catch with the same label as
       throw (the second argument). In this moment the
 result of throw is the value returned by catch.
```

- Concluzii:
- In blocks like block we use return from or return in order to force the exit;
- In blocks like *tagbody* we have *go*;
- The definition of a function is a block with the name of the function;
- For non-local gotos use catch and throw
- sequential blocks are: progn, prog1, prog2
- \bullet prog is a combination between block, tagbody, let*

3.6 loop,do,do*

Iteration statements in Lisp can be done in multiple ways. The most commonly used id do. The general form is:

```
(do ({(<var> [<init> [<step>]])}*)
  (<test-end> {<result>}*)
  <body>
```

```
)
; or
(do ( (var1 init1 step1)
       (var2 init2 step2)
       (varn initn stepn))
    (test-end result)
  body)
  The difference between do and do* is that do is used for binding in parallel
and do* is used for binding sequential (similar with psetq and let, or setq or
; prints the natural numbers between two values:
> (defun printing (start ending)
        (do ((i start (1+ i)))
            ((> i ending))
          (\mathbf{print} \ i)
> (printing 2 10)
; if we want to return some values
; then we write the function:
> (defun printing2 (start ending)
        (do ((i start (1+ i)))
            ((> i ending) 'done)
          (print i)
> (printing 2 2 8)
> (defun factorial (n)
        (\mathbf{do}* ((i \ 1 \ (1+i)))
         (result 1 (* result i)))
        ((= i n) result)
> (factorial 8)
; using loop
> (loop (print 10) (print 20) (print 30) (return))
```

```
> (loop (print '>)
         (if (eq (read) 'stop)
                  (return 'exit)
256
7896540
>
9
>
-980
>
lalala
stop
EXIT
>(loop for i from 1 to 6 do (print i))
> (\mathbf{do} ((x 1 (1+ x)) (y 1 (* x y))) ((> x 5) y))
  DOTIMES is a version of the function DO and is equivalent with FOR. The
syntax is:
  (DOTIMES (variable counter result) body)
  Equivalent with:
FOR variabe=0 until counter-1 DO
       body
RETURN result
  Examples:
> (dotimes (i 10 (1+ i)) (print 'today))
> (dotimes (i 10 (1+ i)) (prin1 i) (princ ""))
> (dotimes (i 4 (* i 2)))
> (dotimes (i 4 (* i 2)) (print 'one))
> (dotimes (i 4 (* i 2)) (1+ 89))
> (dotimes (i 4 (* i 2)) (print (1+ 89)))
> (dotimes (i 5 (* i i)) (prin1 i))
> (dotimes (i 5 (* i i)) (prin1 i) (princ "_"))
```

```
> (dotimes (i 10 (* i i)) (prin1 i) (princ ""))
```

DOLIST is similar to DOTIMES but when using DOTIMES the variable receives values between 0 to counter-1, and when using DOLIST the variable receives all the values of the elements from the list.

```
The syntax is:
(DOLIST (variable my-list result) body)
Equivalent to:

FOR variable=first elem from the list
UNTIL the last element from the list DO
body
RETUR result
Examples:

> (dolist (var '(1 2 3)) (print var))

> (dolist (x '(a b c)) (prin1 x) (princ "-"))
```

4 Homework - deadline: next lab

1. Write a recursive function which returns a list with all the atoms from a list given as parameter:

```
(squash '(a b c (d e) ((f) g)))

=> (a b c d e f g)

(squash '(a b))

=> (a b)

(squash '(() ((((a)))) ()))

=> (a)
```

2. Write a non-recursive function which calculates the sum of squares of the elements from a list.

$$(square-sum '(1 2 3)) => 14$$