

Logic Programming

An Introduction to Prolog

October 7, 2015

Contents of this lecture

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- Part 2: A review of the theoretical basis of logic programming. Based on corresponding topics in [Ben-Ari, 2001] and [Nilsson and Maluszynski, 2000].
- Part 3: Advanced topics in logic programming/Prolog. Based on corresponding topics in [Ben-Ari, 2001] and [Nilsson and Maluszynski, 2000].

Organizatorial items

- ▶ Lecturer and TA: Isabela Drămnesc
- ▶ Course webpage: <http://web.info.uvt.ro/~idramnesc>
 - ▶ 7 Courses
 - ▶ 14 Labs: working with Prolog
- ▶ Handouts: will be posted on the webpage of the lecture
- ▶ Grading:
 - ▶ 50% : weekly seminar assignments
 - ▶ 50% : 1 written exam (colloquy) at the end of the semester (during the last lecture)

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 - ▶ **implementation of the solutions (mundane and tedious).**

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- ▶ In logic programming
 - ▶ **program** = set of axioms,
 - ▶ **computation** = constructive proof of a goal statement.

Logic programming: some history

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- ▶ Kurt Gödel's incompleteness theorem (1931): any theory containing arithmetic cannot prove its own consistency.
- ▶ Alonzo Church and Alan Turing (independently, 1936): undecidability - no mechanical method to decide truth (in general).

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- ▶ 1981 Japanese Fifth Generation Computer project: project to build the next generation computers with advanced AI capabilities (using a concurrent Prolog as the programming language).

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 - ▶ personnel planning: StaffPlan (airports in Barcelona, Madrid; Hovedstaden region in Denmark).
 - ▶ information management for disasters: ARGOS - crisis management in CBRN (chemical, biological, radiological and nuclear) incidents – used by Australia, Brasil, Canada, Ireland, Denmark, Sweden, Norway, Poland, Estonia, Lithuania and Montenegro.

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- ▶ Use Prolog to solve problems that involve **objects** and **relations** between objects.
- ▶ Examples:
 - ▶ Objects: “John”, “book”, “jewel”, etc.
 - ▶ Relations: “John owns the book”, “The jewel is valuable”.
 - ▶ Rules: “Two people are sisters if they are both females and they have the same parents”.

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- ▶ Programming in Prolog: a conversation with the Prolog interpreter.

Facts

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- ▶ Arbitrary numbers of arguments are allowed.
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- ▶ Facts are part of the Prolog database (knowledge base).

Queries

- ▶ A query in Prolog:

`?- owns(mary , book).`

Prolog searches in the knowledge base for facts that match the question:

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- ▶ Otherwise the answer is false :
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 - ▶ **Attention: false may not mean that the answer is false (but more like “not derivable from the knowledge”).**

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- ▶ Instead of:

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?- likes(john, apples).

?- likes(john, candy).

ask something like “What does John like?” (i.e. give everything that John likes).

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- ▶ In Prolog variables start with **CAPITAL LETTERS**:

```
?- likes(john, X).
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Prolog computation: example

- Consider the following facts in a Prolog knowledge base:

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likes(john , mary ).  
likes(paul , mary ).  
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```

- To the query

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?-likes(john , X).
```

Prolog will answer

```
X = flowers
```

and wait for further instructions.

Prolog answer computation

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- ▶ In the example above, two more “; Enter” will determine Prolog to answer:

`X = mary.`
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false

- ▶ When no (more) matching facts are found in the knowledge base, Prolog answers false.

Conjunctions: more complex queries

- ▶ Consider the following facts:

likes (mary , food).

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likes (john , wine).

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`likes (john , mary).`

- ▶ And the query:

`?-likes (john , mary) , likes (mary , john) .`

- ▶ the query reads “does john like mary and does mary like john?”

Conjunctions: more complex queries

- ▶ Consider the following facts:

```
likes (mary , food ).  
likes (mary , wine ).  
likes (john , wine ).  
likes (john , mary ).
```

- ▶ And the query:

```
?- likes (john , mary) , likes (mary , john ) .
```

- ▶ the query reads “does john like mary **and** does mary like john?”
- ▶ **Prolog will answer false**: it searches for each goal in turn (all goals have to be satisfied, if not, it will fail, i.e. answer false).

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- ▶ Prolog: try to satisfy the first goal (if it is satisfied put a placemaker), then try to satisfy the second goal (if yes, put a placemaker).
- ▶ If at any point there is a failure, backtrack to the last placemaker and try alternatives.

Example: conjunction, backtracking

The way Prolog computes the answer to the above query is represented:

- ▶ In Figure 1, the first goal is satisfied, Prolog attempts to find a match for the second goal (with the variable instantiated).
- ▶ The failure to find a match in the knowledge base causes backtracking, see Figure 2.
- ▶ The new alternative tried is successful for both goals, see Figure 3.

?-likes (mary, X), likes(john, X).

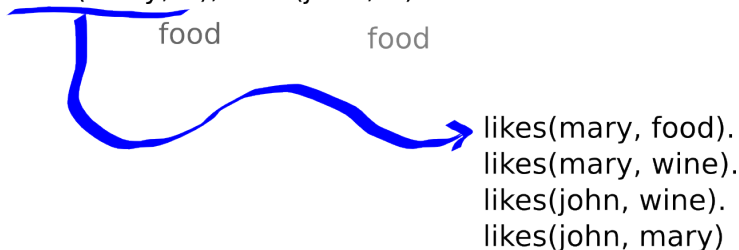


Figure : Success for the first goal.

?-likes (mary, X), likes(john, X).

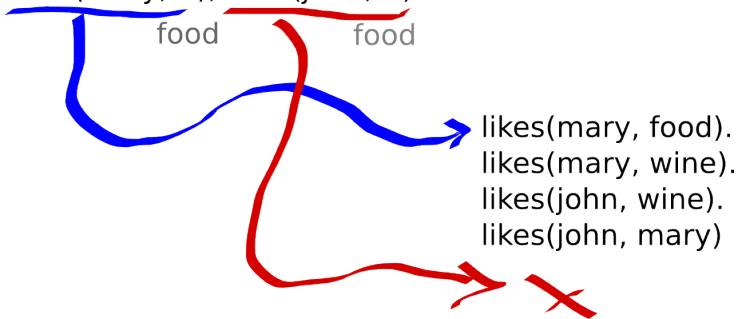


Figure : Second goal failure causes backtracking.

?-likes (mary, X), likes(john, X).

wine

wine

likes(mary, food).
likes(mary, wine).
likes(john, wine).
likes(john, mary)



Figure : Success with alternative instantiation.

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likes(john, bertrand).  
likes(john, charles).  
likes(john, david).  
...
```

but this is tedious!!!

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- ▶ Enter **rules**: “John likes any object, but only that which is a person” is a rule about what (who) John likes.
- ▶ **Rules express that a fact depends on other facts.**

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 - ▶ but there may be other ways (i.e. other rules with the same head) to detect such predicates,
 - ▶ in order to have full definitions “iff” is needed instead of “if”.
- ▶ Rules are general statements about objects and their relationships (in general variables occur in rules, but not always).

Rules in Prolog

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- ▶ **Example:**

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likes(john , X) :-  
    likes(X, wine).  
likes(john , X) :-  
    likes(X, wine), likes(X, food).  
likes(john , X) :-  
    female(X), likes(X, wine).
```


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likes(john, X) :-  
    likes(X, wine), likes(X, food).  
likes(john, X) :-  
    female(X), likes(X, wine).
```

- ▶ **Attention!** The scope of the variables that occur in a rule is the rule itself (rules do not share variables).

Example (royals)

► Knowledge base:

```
male(albert).  
male(edward).  
female(alice).  
female(victoria).  
parents(alice, albert, victoria).  
parents(edward, albert, victoria).  
sister_of(X, Y):—  
    female(X),  
    parents(X, M, F).  
    parents(Y, M, F).
```

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sister_of(X, Y):-  
    female(X),  
    parents(X, M, F).  
    parents(Y, M, F).
```

► Goals:

```
?-sister_of(alice, edward).  
?-sister_of(alice, X).
```

Exercise (thieves)

- Consider the following:

```
/*1*/ thief(john).
```

```
/*2*/ likes(mary, food).
```

```
/*3*/ likes(mary, wine).
```

```
/*4*/ likes(john, X):- likes(X, wine).
```

```
/*5*/ may_steal(X, Y) :-  
        thief(X), likes(X, Y).
```

- Explain how the query

```
?- may_steal(john, X).
```

is executed by Prolog.

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- ▶ Constants are of 2 types:
 - ▶ atoms,
 - ▶ numbers: integers, rationals (with special libraries), reals (floating point representation).

Examples of atoms

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 - ▶ likes ,

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- ▶ Examples: `X`, `Input`, `_something`, `_` (the last one called anonymous variable).
- ▶ Anonymous variables need not have consistent interpretations (they need not be bound to the same value):

`?-likes (_,john).` % does anybody like John?

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- ▶ A structure is specified by its functor (name) and its components

```
owns(john , book( wuthering_heights , bronte ) ).  
book( wuthering_heights , author( emily , bronte ) ).
```

```
?-owns(john , book(X, author(Y, bronte ) ) ).  
% does John own a book (X) by Bronte (Y, bronte)?
```

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- ▶ **Remark:** ' ' allows the use of any character.

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- ▶ Example: $3+4$ (structure) does not have the same meaning with 7 (term).
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- ▶ The result of the evaluation is that X is assigned the value 7.

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 - ▶ Associativity: What is $x + y + z$? $x + (y + z)$ or $(x + y) + z$?

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- ▶ Arithmetic operators are left associative.

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- ▶ Remark on terminology: while in some Prolog sources the term “matching” is used, note that in the (logic) literature matching is used for the situation where one of the terms is ground (i.e. contains no variables). What = does is unification.

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- ▶ If $T1$ and $T2$ are instantiated variables, then decide according to their value (they unify - if they have the same value, otherwise not);
- ▶ If $T1$ is a structure: $f(X_1, X_2, \dots, X_n)$ and $T2$ has the same **functor** (name): $f(Y_1, Y_2, \dots, Y_n)$ and the same number of arguments, then unify these arguments recursively ($X_1 = Y_1$, $X_2 = Y_2$, etc.). If all the arguments unify, then the answer is true, otherwise the answer is false (unification fails);
- ▶ **In any other case, unification fails.**

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- ▶ In fact this is due to the fact that according to the unification procedure, the result is
 $X = f(X) = f(f(X)) = \dots = f(f(\dots(f(X)\dots)))$ - an infinite loop would be generated.

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- ▶ A predicate complementary to unification:
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 - ▶ i.e. **$T1 \backslash = T2$ cannot be unified.**

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- ▶ Note that variables have to be instantiated in most cases (with the exception of the first two above, where unification is performed in the case of uninstantiation).

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- ▶ Prolog also provides arithmetic operators (functions), e.g.:
+, −, *, /, mod, rem, abs, max, min, random, floor, ceiling
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- ▶ The Prolog evaluator is has the form:

X is Expr.

where X is an uninstantiated variable, and Expr is an arithmetic expression, where all variables must be instantiated (Prolog has no equation solver).

Example (with arithmetic(1))

```
reigns(rhondri , 844, 878).
reigns(anarawd , 878, 916).
reigns(hywel_dda , 916, 950).
reigns(lago_ap_idwal , 950, 979).
reigns(hywel_ap_ieuaf , 979, 985).
reigns(cadwallon , 985, 986).
reigns(maredudd , 986, 999).
prince(X, Y):-
    reigns(X, A, B),
    Y >= A,
    Y <= B.
```

```
?- prince(cadwallon , 986).
true
?- prince(X, 979).
X = lago_ap_idwal ;
X = hywel_ap_ieuaf
```

Example (with arithmetic(2))

```
pop(place1 , 203).  
pop(place2 , 548).  
pop(place3 , 800).  
pop(place4 , 108).
```

```
area(place1 , 3).  
area(place2 , 1).  
area(place3 , 4).  
area(place4 , 3).  
density(X, Y):-  
    pop(X, P),  
    area(X, A),  
    Y is P/A.
```

```
?-density(place3 , X).  
X = 200  
true
```

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 - ▶ Arithmetic in Prolog,
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 - ▶ Subtle point: occurs check.

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- ▶ Read: Chapter 1 and Chapter 2 (including exercises section) of [Clocksin and Mellish, 2003].



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