

# Magnetic Field Models for Geospace Particle Tracing

AMPS Interface Documentation

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## 1 Total field representation

AMPS typically represents the magnetic field as

$$\mathbf{B}(\mathbf{r}, t) = \mathbf{B}_{\text{int}}(\mathbf{r}, t) + \mathbf{B}_{\text{ext}}(\mathbf{r}, t), \quad (1)$$

where  $\mathbf{B}_{\text{int}}$  is the internal (main) field and  $\mathbf{B}_{\text{ext}}$  is the magnetospheric current system contribution.

## 2 Internal field (IGRF / dipole)

For most applications,  $\mathbf{B}_{\text{int}}$  is modeled using IGRF (or a dipole approximation for sensitivity testing). The internal field provides the dominant contribution near Earth and controls low-altitude cutoffs.

## 3 Empirical external field models (Tsyganenko family)

Empirical models represent  $\mathbf{B}_{\text{ext}}$  using parametrizations constrained by spacecraft observations. Typical inputs are solar-wind dynamic pressure, IMF  $B_y/B_z$ , Dst, and/or Kp.

### T96

Tsyganenko (1996) provides a widely used external field model suitable for many cutoff studies.

### TS05 (Tsyganenko & Sitnov 2005) / TA15 (Tsyganenko–Andreeva 2015)

Storm-time models incorporate additional drivers and are designed to capture disturbed intervals. For SEP cutoff calculations, these models are often preferred for event-realistic reconstructions and strong-storm sensitivity tests.

**Driver sets.** In this interface, the "TS05" model is configured with the common scalar drivers (Dst or SYM-H, solar-wind dynamic pressure  $P_{\text{dyn}}$ , IMF  $B_x/B_y/B_z$ , solar-wind  $V_x$  and density  $N$ ) and an EPOCH time tag. The underlying TS05 formulation is *dynamical*: the magnitudes of major current systems are driven by six history-dependent variables  $W_1..W_6$ , each computed as a relaxation integral/sum over the prior solar-wind/IMF conditions. Tsyganenko & Sitnov (2005) define (their Eq. (7–8)) a generic form

$$W(t_i) = \frac{r}{12} \sum_{k=1}^i S_k \exp \left[ \frac{r}{60} (t_k - t_i) \right], \quad S_k = \left( \frac{N_k}{5} \right)^\ell \left( \frac{V_k}{400} \right)^b \left( \frac{B_{s,k}}{5} \right)^g, \quad (2)$$

with module-specific exponents and relaxation rates. This is why TS05 is best driven from an OMNI-style time series (5-min cadence).

**OMNI/TS05 record format.** A commonly used dataset is distributed as yearly files `YYYY_OMNI_5m_with_TS05.v` where each 5-min record contains IMF ( $B_x, B_y, B_z$ ), solar-wind velocity components, density, temperature, SYM-H, availability flags, dipole tilt angle (radians),  $P_{dyn}$  (nPa), and the six TS05 driving variables  $W_1..W_6$ .

**Parameter presets (order-of-magnitude).** Quiet solar wind typically corresponds to  $P_{dyn} \sim 1\text{--}3$  nPa,  $|B_z| \lesssim 5$  nT,  $V_x \sim -400$  km/s,  $N \sim 3\text{--}10$  cm $^{-3}$ ; storm main-phase intervals commonly reach  $P_{dyn} \sim 5\text{--}15$  nPa,  $B_z \sim -10$  to  $-30$  nT,  $V_x \sim -600$  to  $-800$  km/s, and Dst/SYM-H  $\lesssim -100$  nT.

## 4 MHD-driven fields (BATSRUS / GAMERA)

For highest fidelity, AMPS can ingest a 3D time-dependent magnetic field from a global MHD model. In this mode:

- The MHD solution provides  $\mathbf{B}(\mathbf{r}, t)$  (and optionally  $\mathbf{E}$ ).
- Particle tracing uses spatio-temporal interpolation on the MHD grid.
- Boundary surfaces (magnetopause, inner boundary) should be consistent with the MHD domain.

This option is computationally heavier but can reproduce event-specific structures not captured by analytic fits.

## 5 Notes for cutoff calculations

- Using a storm-time external model (e.g., TS05/T15) can change  $R_C$  by several GV at mid-latitudes.
- Time dependence can be critical during rapid Dst changes; ensure  $\Delta t$  in tracing resolves the driver cadence.
- Consistency with the electric field model matters for drift trajectories, especially in the inner magnetosphere.

## 6 References (selected)

- Tsyganenko, N. A. (1996). “Effects of the solar wind conditions on the global magnetosphere configuration...” *JGR*.
- Tsyganenko, N. A., & Sitnov, M. I. (2005). (TS05). *JGR*.
- Tsyganenko, N. A., & Andreeva, V. A. (2015). (T15). *JGR*.