# Clustering

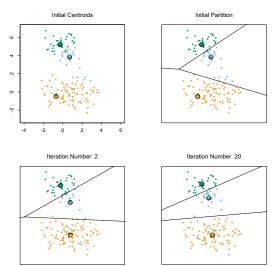
Data Mining Prof. Dawn Woodard School of ORIE Cornell University

# **Outline**

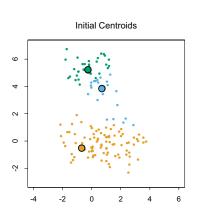
1 Clustering

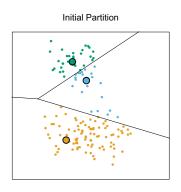
# K-Means Clustering

Figure 14.6 in the Hastie et al. text:

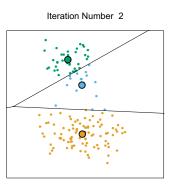


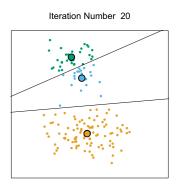
# **K-Means Clustering**





# **K-Means Clustering**





#### **Public Utilities Data**

- Recall the data on public utilities (Shmueli, Patel, and Bruce, 2007)
- Wish to group based on financial factors
- Used for e.g. a study on the impact of deregulation
- Could pick one "typical" utility in each group and study in detail the potential effect of deregulation on that utility
- Scale up to estimate impact for all utilities
- This is less costly than studying in detail the effect of deregulation on every single utility

#### Data on public utilities (Shmueli, Patel, and Bruce, 2007):

| 1 |                |      |      |     |      |               |       |      |       |
|---|----------------|------|------|-----|------|---------------|-------|------|-------|
|   |                |      |      |     |      | Demand.growth |       |      |       |
|   | 1 Arizona      | 1.06 | 9.2  | 151 | 54.4 | 1.6           | 9077  | 0.0  | 0.628 |
|   | 2 Boston       | 0.89 | 10.3 | 202 | 57.9 | 2.2           | 5088  | 25.3 | 1.555 |
|   | 3 Central      | 1.43 | 15.4 | 113 | 53.0 | 3.4           | 9212  | 0.0  | 1.058 |
|   | 4 Commonwealth | 1.02 | 11.2 | 168 | 56.0 | 0.3           | 6423  | 34.3 | 0.700 |
|   | 5 NY           | 1.49 | 8.8  | 192 | 51.2 | 1.0           | 3300  | 15.6 | 2.044 |
|   | 6 Florida      | 1.32 | 13.5 | 111 | 60.0 | -2.2          | 11127 | 22.5 | 1.241 |
|   | 7 Hawaiian     | 1.22 | 12.2 | 175 | 67.6 | 2.2           | 7642  | 0.0  | 1.652 |
|   | 8 Idaho        | 1.10 | 9.2  | 245 | 57.0 | 3.3           | 13082 | 0.0  | 0.309 |
|   | 9 Kentucky     | 1.34 | 13.0 | 168 | 60.4 | 7.2           | 8406  | 0.0  | 0.862 |
| 1 | 0 Madison      | 1.12 | 12.4 | 197 | 53.0 | 2.7           | 6455  | 39.2 | 0.623 |
| 1 | 1 Nevada       | 0.75 | 7.5  | 173 | 51.5 | 6.5           | 17441 | 0.0  | 0.768 |
| 1 | 2 New England  | 1.13 | 10.9 | 178 | 62.0 | 3.7           | 6154  | 0.0  | 1.897 |
| 1 |                | 1.15 | 12.7 | 199 | 53.7 | 6.4           | 7179  | 50.2 | 0.527 |
| 1 | 4 Oklahoma     | 1.09 | 12.0 | 96  | 49.8 | 1.4           | 9673  | 0.0  | 0.588 |
| 1 | 5 Pacific      | 0.96 | 7.6  | 164 | 62.2 | -0.1          | 6468  | 0.9  | 1.400 |
| 1 | 6 Puget        | 1.16 | 9.9  | 252 | 56.0 | 9.2           | 15991 | 0.0  | 0.620 |
| 1 | 7 San Diego    | 0.76 | 6.4  | 136 | 61.9 | 9.0           | 5714  | 8.3  | 1.920 |
| 1 | 8 Southern     | 1.05 | 12.6 | 150 | 56.7 | 2.7           | 10140 | 0.0  | 1.108 |
| 1 | 9 Texas        | 1.16 | 11.7 | 104 | 54.0 | -2.1          | 13507 | 0.0  | 0.636 |
| 2 | 0 Wisconsin    | 1.20 | 11.8 | 148 | 59.9 | 3.5           | 7287  | 41.1 | 0.702 |
| 2 | 1 United       | 1.04 | 8.6  | 204 | 61.0 | 3.5           | 6650  | 0.0  | 2.116 |
| 2 | 2 Virginia     | 1.07 | 9.3  | 174 | 54.3 | 5.9           | 10093 | 26.6 | 1.306 |
|   | -              |      |      |     |      |               |       |      |       |
|   |                |      |      |     |      |               |       |      |       |

#### Data on public utilities (Shmueli, Patel, and Bruce, 2007):

|    | Company      | Fixed.charge | RoR  | Cost | Load.factor | Dema |
|----|--------------|--------------|------|------|-------------|------|
| 1  | Arizona      | 1.06         | 9.2  | 151  | 54.4        |      |
| 2  | Boston       | 0.89         | 10.3 | 202  | 57.9        |      |
| 3  | Central      | 1.43         | 15.4 | 113  | 53.0        |      |
| 4  | Commonwealth | 1.02         | 11.2 | 168  | 56.0        |      |
| 5  | NY           | 1.49         | 8.8  | 192  | 51.2        |      |
| 6  | Florida      | 1.32         | 13.5 | 111  | 60.0        |      |
| 7  | Hawaiian     | 1.22         | 12.2 | 175  | 67.6        |      |
| 8  | Idaho        | 1.10         | 9.2  | 245  | 57.0        |      |
| 9  | Kentucky     | 1.34         | 13.0 | 168  | 60.4        |      |
| 10 | Madison      | 1.12         | 12.4 | 197  | 53.0        |      |
| 11 | Nevada       | 0.75         | 7.5  | 173  | 51.5        |      |
| 12 | New England  | 1.13         | 10.9 | 178  | 62.0        |      |
| 13 | Northern     | 1.15         | 12.7 | 199  | 53.7        |      |
| 14 | Oklahoma     | 1.09         | 12.0 | 96   | 49.8        |      |
| 15 | Pacific      | 0.96         | 7.6  | 164  | 62.2        |      |
| 16 | Puget        | 1.16         | 9.9  | 252  | 56.0        |      |
| 17 | San Diego    | 0.76         | 6.4  | 136  | 61.9        |      |
| 18 | Southern     | 1.05         | 12.6 | 150  | 56.7        | 9    |

#### 8 operational variables:

Fixed.charge: Fixed-charge covering ratio (income/debt)

RoR: rate of return on capital Cost: cost per kilowatt capacity

Load.factor Demand.growth

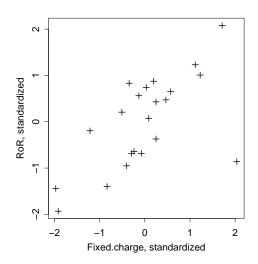
Sales: Kilowatthour use per year

Nuclear: % nuclear

Fuel.cost: Total fuel costs

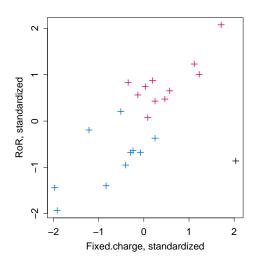
- Let's first cluster based just on the first two variables (Fixed.charge and RoR), so we can visualize the results
- What do you notice about the variance of Fixed.charge relative to that of RoR?
- What effect could that have on the cluster assignments?
- We probably need to standardize the variables

#### Plot the resulting variables:

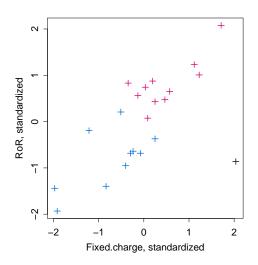


- What type of relationship do the variables Fixed.charge and RoR appear to have overall?
- Are there any utilities that do not fit this overall trend?
- Are there clear clusters?
- If you had to divide into 3 clusters, what clusters would you use?

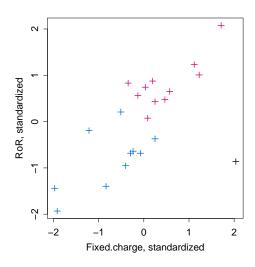
Applying k-means using one random initialization we obtain the clusters:



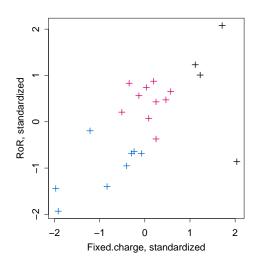
Here the points are the utilities in the data set



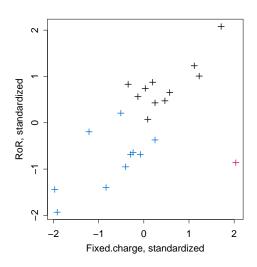
#### The colors correspond to the clusters



Using a different random initialization we obtain:



#### Using a third random initialization we obtain:



- How are the first and third cluster assignments related?
- Which cluster assignment do you think is most appropriate?

- The within-cluster variation W(C) for the first and third cluster assignments is 15.62
- That for the second cluster assignment is 13.77
- Which would you choose based on this information?

- I then applied k-means with K = 3 using all 8 of the variables (standardized)
- I ran it several times using randomly generated cluster means  $\{m_k : k = 1, ..., K\}$
- I chose the cluster assignment that gave the smallest W(C)

- The cluster assignments are:
  - Arizona, Central, Florida, Kentucky, Oklahoma, Southern, Texas
  - Boston, NY, Hawaiian, New England, Pacific, San Diego, United
  - Commonwealth, Idaho, Madison, Nevada, Northern, Puget, Wisconsin, Virginia