

Causal diagrams

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WTMC method track – Computational methods & modelling

11 February 2021

① Observing \neq doing

② d -separation simplified

Observing \neq doing

- Predict future citations

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 - ▶ Tweets predict future citations

Predicting

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- Predict accept/reject decisions

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- Predict future career paths

Predicting

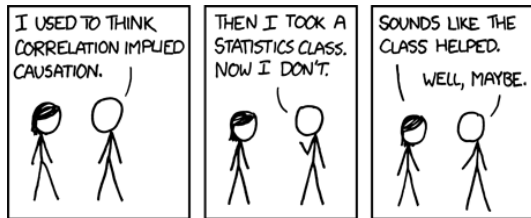
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Observations → prediction



Prediction

Observing x may make y more likely to be observed.

Observing vs doing

Prediction

Observing x may make y more likely to be observed.

Intervention

Doing x may make y more likely to be observed.

Observation vs doing

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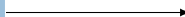
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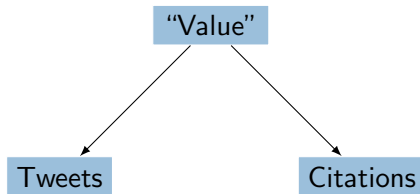
Tweets



Citations

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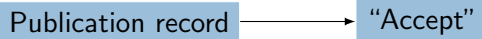
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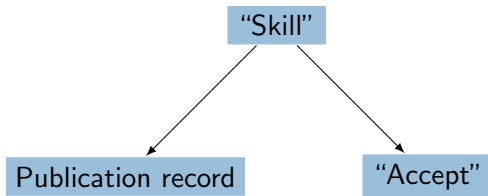
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Causality

- Causality is about *doing* something, about (hypothetical) interventions.
- Important for policy implications:
 - ▶ If you observe x and y are associated, but they are *not* causally related, then *doing* x does not change y , and x should not be advocated as a policy to achieve a change in y .

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- ① Assume a causal model (background knowledge, earlier research, ...).
- ② Given causal model, under some conditions associations may reveal *causal* effects.
 - ▶ Key to this is understanding d -separation.
- ③ Test whether implications of causal model hold in observations.
 - ▶ Different causal models may have same observational implications.

d-separation simplified

Two variables x and y are associated if between them there is an open undirected path

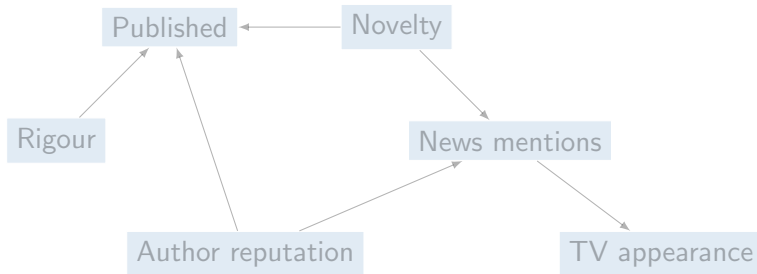
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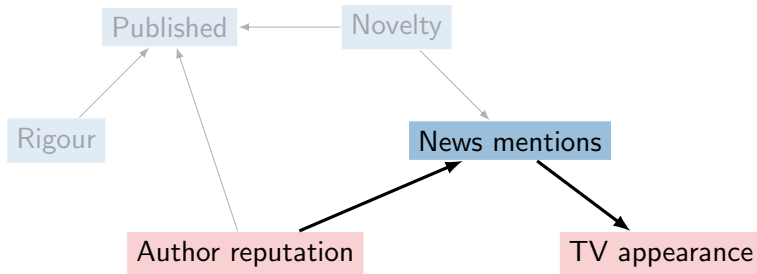
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Technical term	Meaning	Implication
d -connected	there is an open undirected path	x and y are associated
d -separated	there is no open undirected path	x and y are not associated

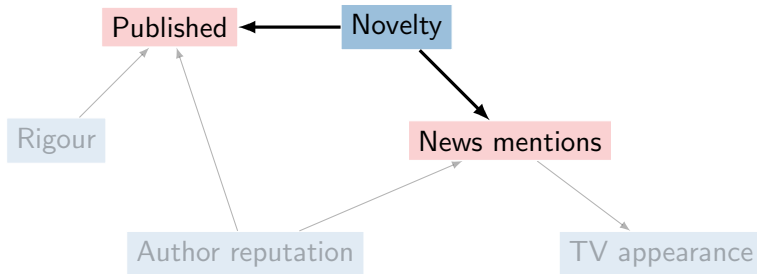
d -separation – Undirected paths



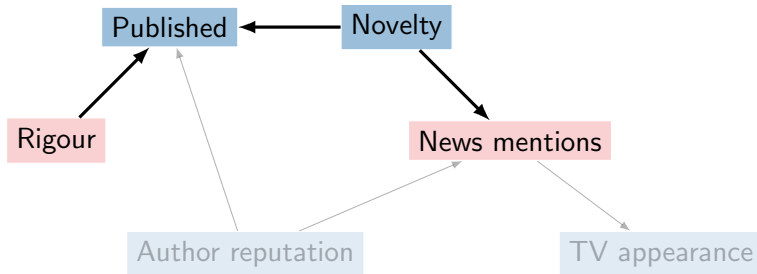
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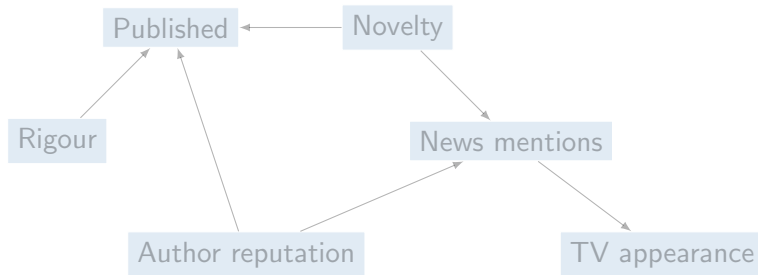
d -separation – Undirected paths



An undirected path is open if *all* nodes on the path are open .

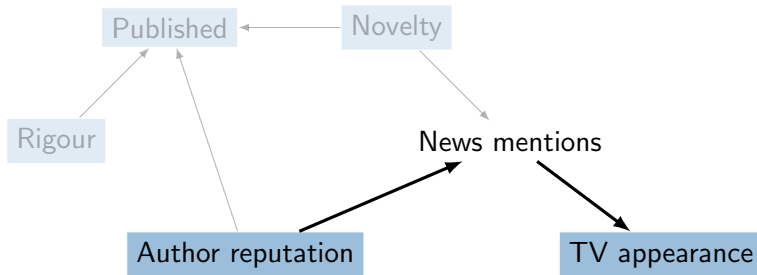
An undirected path is open if *all* nodes on the path are open.

d-separation – Mediators, confounders & colliders



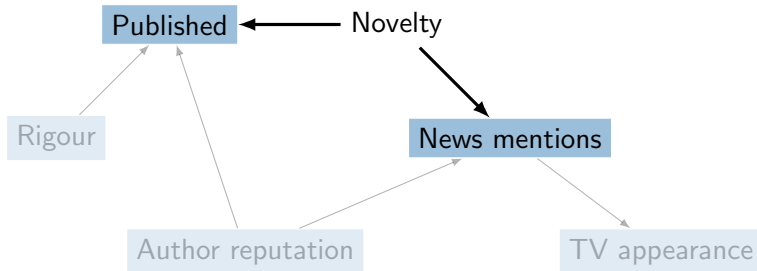
Mediator (causation) – Open

... \longrightarrow Z \longrightarrow ...



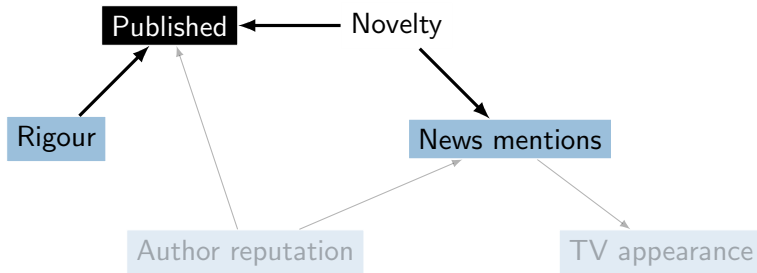
Confounder – Open

... \longleftrightarrow Z \longrightarrow ...



d-separation – Mediators, confounders & colliders

Collider – Closed

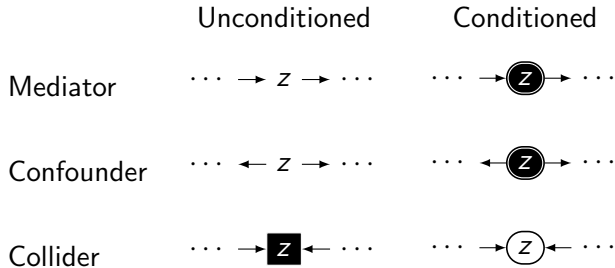


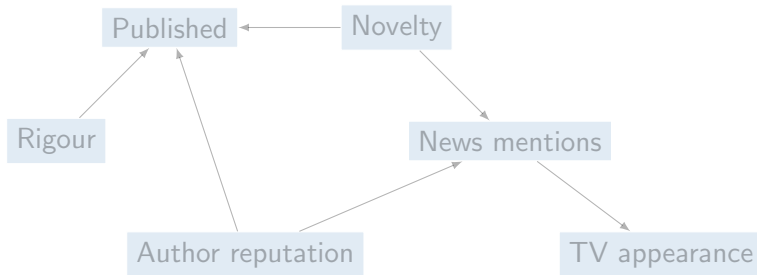
Many possible ways to “condition” on a variable:

- Include only subset of cases in analysis.
- Perform analyses separately on different subsets of data.
- “Normalise” indicators (e.g field-normalise).
- Include variable in regression.

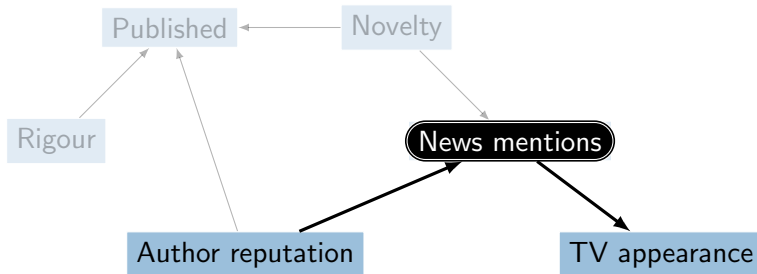
d-separation – Open nodes & conditioning

Conditioning on a variable “flips” the node on a path from open \square to closed \blacksquare and vice-versa.

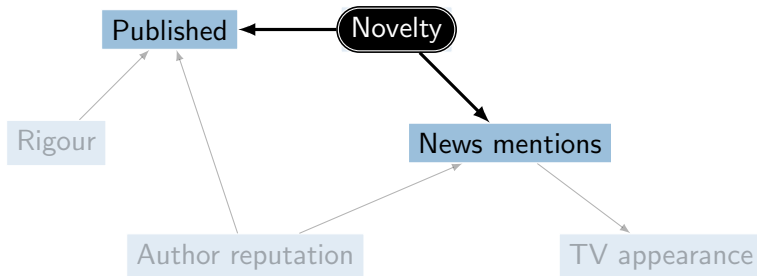




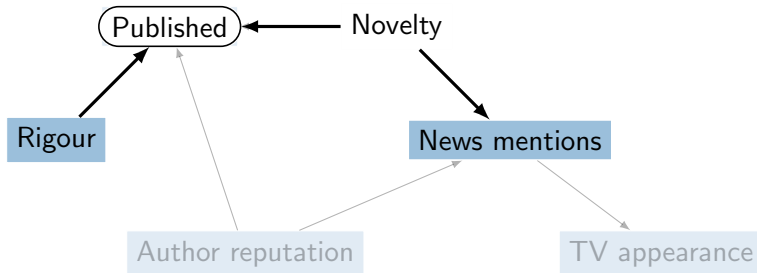
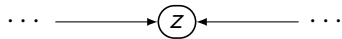
Condition on mediator – Closed

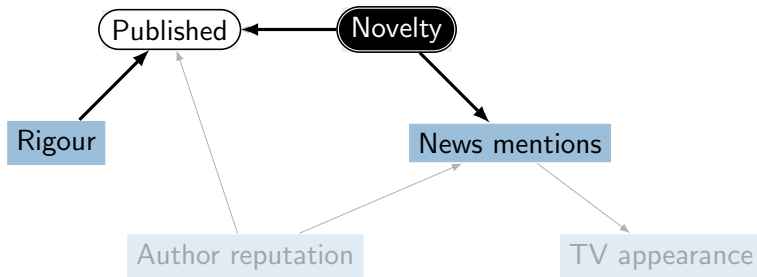


Condition on confounder – Closed



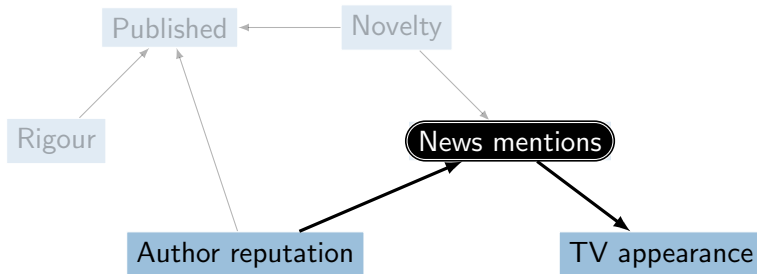
Condition on collider – Open





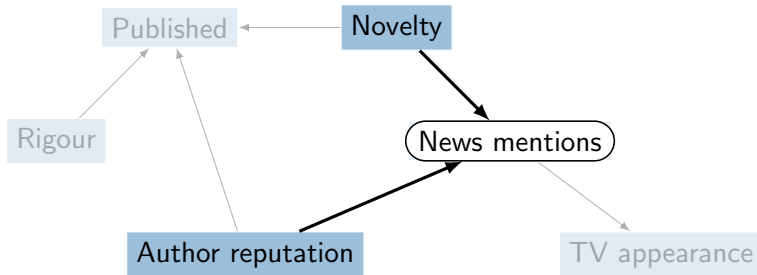
d -separation – Conditioning

Conditioning may close one path but open another.



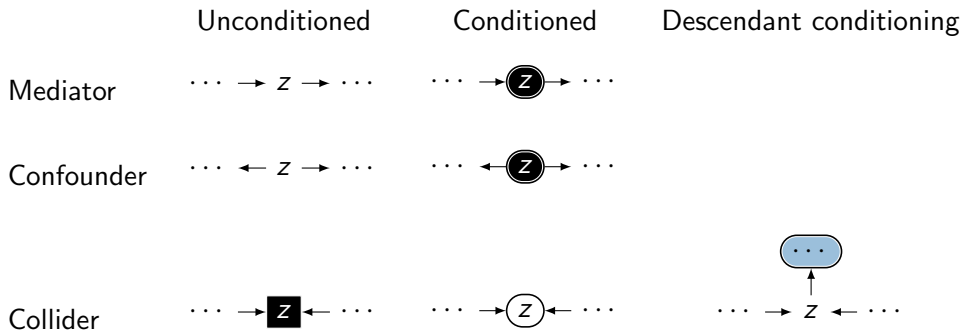
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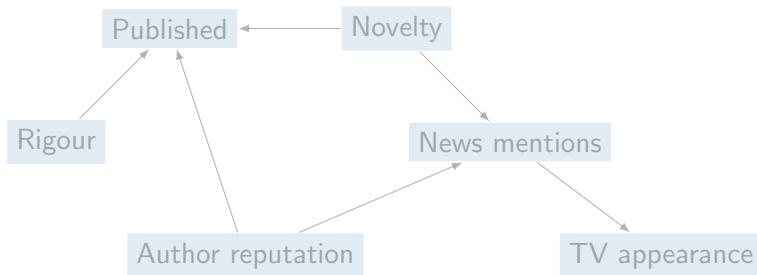


Conditioning on descendants and d -separation

Conditioning on descendant of collider opens it.

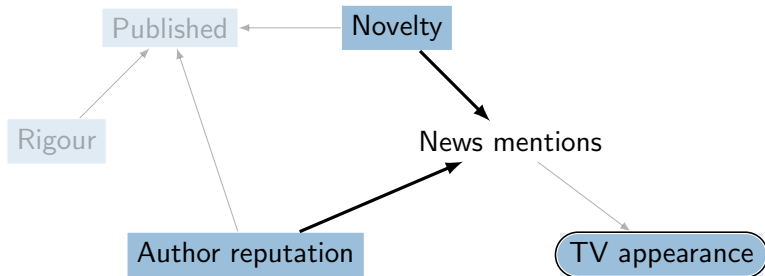
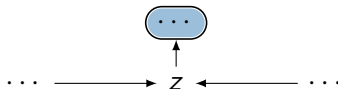


d -separation – Conditioning on descendants



d-separation – Conditioning on descendants

Condition on descendant of collider – Opens collider



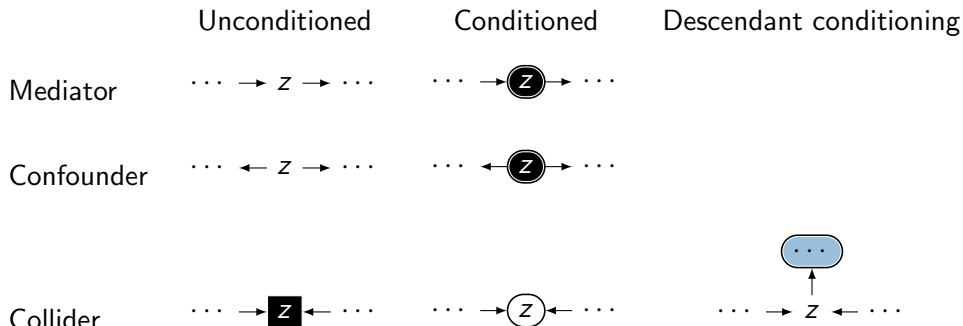
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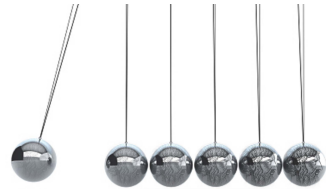
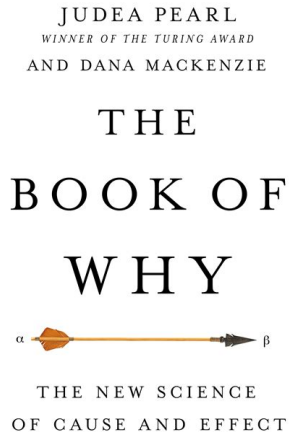
d -separation summary

- ① x and y are associated if there is an open undirected path between them.
- ② An undirected path is open if all nodes are open.

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- ② An undirected path is open if all nodes are open.
- ③ A node on a path is open \square or closed \blacksquare in the following situations
 - Conditioning on a variable “flips” nodes from open to closed and vice-versa.





CAUSAL INFERENCE IN STATISTICS

A Primer

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Madelyn Glymour
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WILEY

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