

discrete dist.

① Bernoulli dist.

② Binomial dist

n sequential Bernoulli dist

prob (K success) is

①  $\binom{n}{k}$

②  $p^k \cdot (1-p)^{n-k}$

$\rightarrow \binom{n}{k} \cdot p^k (1-p)^{n-k}$

③ Geometric distribution

k trials in total

k-1 trials failure

k<sup>th</sup> trial success

k-1 trials  
1-p

k<sup>th</sup> success

Q.  $E(X)$ ,  $Var(X)$   $(1-p)^{k-1} \cdot p$



Def:  $E(X) = \sum_i x_i \cdot P_{X_i}$

$$Var(X) = E[(X - E(X))^2]$$

$$= \sum_i (x_i - E(X))^2 \cdot P_{X_i}(x_i)$$

$(x=k)$   
 $P_X = (1-p)^{k-1} \cdot p$

$$E(X) = \frac{1}{p}$$

$$Var(X) = \frac{1-p}{p^2} \quad \square$$

Q: What is the prob of . . . . . based on distribution.

Note X

$$P(X \leq 3) = P(X=0) + P(X=1) + P(X=2) + P(X=3)$$

$$P(X \leq 3) = 1 - \underline{P(X > 3)}$$

$$\underline{P(X > 3)} = P(X=4) + P(X=5) + \dots$$

the prob of number of trials needed



for the first time success  
is greater than 3.

~~Prob~~

that is, the first 3 trials are all failures.

$$\begin{aligned}\text{prob} &= (1-p)^3 \\ &= P(X > 3) \quad \square\end{aligned}$$

△ Po's dist

Def. # of events occurred in a certain time period or space.

0, 1, 2, ...

pmf  $\therefore p(x) = \frac{e^{-\lambda} \cdot \lambda^x}{x!}, \quad x=0, 1, 2, \dots$

$\lambda$  : the rate parameter.

Notes

- ① the count data.
- ② each occurrence is independent.
- ③ the rate of occurrence in a time period / space.
- ④ it's counting how many events have occurred, not the events that have not occurred.
- ⑤

Q  $E(x)$  ?  $Var(x)$

$$E(x) = \lambda$$

$$Var(x) = \lambda \quad \text{①}$$

Q: this prob.  $p(x) = \frac{e^{-\lambda} \cdot \lambda^x}{x!}$  the pmf?

①  $[0, 1]$

②  $\sum_{k=0}^{\infty} p(x) = 1$  ~~Wan~~



( $x=k$ ).

$$\sum_{k=0}^{\infty} P(x) = \sum_{k=0}^{\infty} \frac{e^{-\lambda} \cdot \lambda^k}{k!}$$

$$= e^{-\lambda} \cdot \sum_{k=0}^{\infty} \frac{\lambda^k}{k!}$$

Fact:

$$e^x = \sum_{k=0}^{\infty} \frac{x^k}{k!}$$

trick.

$$= e^{-\lambda} \cdot e^{\lambda}$$

$$= e^0$$

$$= 1$$

