

Model Question Paper-I with effect from 2022 (CBCS Scheme)

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First Semester B.E Degree Examination

Mathematics-I for Mechanical Engineering Stream (BMATM101)

TIME: 03 Hours

Max. Marks: 100

Note:

1. Answer any **FIVE** full questions, choosing atleast **ONE** question from each **MODULE**
2. VTU Formula Hand Book is Permitted
3. M: Marks, L: RBT levels, C: Course outcomes.

| | | Module - 1 | M | L | C |
|------------|---|---|---|----|-----|
| Q.1 | a | Find the angle of intersection of the curves $r = \sin \theta + \cos \theta, r = 2 \sin \theta$. | 6 | L2 | CO1 |
| | b | Find the pedal equation of the curve $r^2 = a^2 \sec 2\theta$. | 7 | L2 | CO1 |
| | c | Find the radius of curvature of the curve $x^4 + y^4 = 2$ at (1, 1). | 7 | L2 | CO1 |
| OR | | | | | |
| Q.2 | a | Derive the radius of curvature for polar curve $r = f(\theta)$ in the form $\rho = \frac{(r^2 + r_1^2)^{3/2}}{(r^2 + 2r_1^2 - r r_2)}$. | 7 | L2 | CO1 |
| | b | Find the angle between the radius vector and the tangent and also find the slope of the tangent $r = a(1 + \cos \theta)$ at $\theta = \frac{\pi}{3}$. | 8 | L2 | CO1 |
| | c | Using modern mathematical tool write a program/code to plot the sine and cosine curve. | 5 | L3 | CO5 |
| Module - 2 | | | | | |
| Q.3 | a | Expand $\log(\cos x)$ by Maclaurin's series up to the term containing x^6 | 6 | L2 | CO2 |
| | b | If $z = \frac{x^2 + y^2}{x + y}$, show that $\left(\frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}\right)^2 = 4\left(1 - \frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}\right)$. | 7 | L2 | CO2 |
| | c | If $x + y + z = u, y + z = uv, z = uvw$ find $\frac{\partial(x, y, z)}{\partial(u, v, w)}$. | 7 | L3 | CO2 |
| OR | | | | | |
| Q.4 | a | If $u = f(ax - by, by - cz, cz - ax)$ Prove that $\frac{1}{a} \frac{\partial u}{\partial x} + \frac{1}{b} \frac{\partial u}{\partial y} + \frac{1}{c} \frac{\partial u}{\partial z} = 0$. | 7 | L2 | CO2 |

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|-------------------|----------|--|----------|-----------|------------|
| | b | Find the extreme values of $f(x, y) = x^3 + 3x^2 + 4xy + y^2$. | 8 | L3 | CO2 |
| | c | Using modern mathematical tool write a program/code to evaluate $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x$. | 5 | L3 | CO5 |
| Module – 3 | | | | | |
| Q.5 | a | Solve $\frac{dy}{dx} - y \tan x = y^2 \sec x$. | 6 | L2 | CO3 |
| | b | Water at temperature 10°C takes 5 minutes to warm up to 20°C at room temperature of 40° . Find the temperature of the water after 20 minutes. | 7 | L3 | CO3 |
| | c | Solve $\frac{dy}{dx} - \frac{dx}{dy} = \frac{x}{y} - \frac{y}{x}$. | 7 | L2 | CO3 |
| OR | | | | | |
| Q.6 | a | Solve $(y \log y)dx + (x - \log y)dy = 0$ | 6 | L2 | CO3 |
| | b | Find the orthogonal trajectories of the family curve $r = 2a(\cos \theta + \sin \theta)$ | 7 | L3 | CO3 |
| | c | Find the general and singular solutions of $xp^2 + xp - yp + 1 - y = 0$. | 7 | L2 | CO3 |
| Module – 4 | | | | | |
| Q.7 | a | Solve $(D^3 - 6D^2 + 11D - 6)y = e^{2x}$ | 6 | L2 | CO3 |
| | b | Solve $(D^2 - 4)y = \cos 2x$. | 7 | L2 | CO3 |
| | c | Solve by variation of parameters $(D^2 + 1)y = \sec x$. | 7 | L2 | CO3 |
| OR | | | | | |
| Q.8 | a | Solve $(D^2 + D + 1)y = x^2 + 1$. | 6 | L2 | CO3 |
| | b | Solve by variation of parameters $(D - 2)^2 y = 8(x^2 + \sin 2x + e^{2x})$. | 7 | L2 | CO3 |
| | c | Solve $x^2 \frac{d^2 y}{dx^2} + 4x \frac{dy}{dx} + 2y = \log x$. | 7 | L2 | CO3 |
| Module – 5 | | | | | |
| Q.9 | a | Find the rank of the matrix $\begin{bmatrix} 1 & 2 & 3 & 1 \\ 2 & 1 & -1 & 0 \\ 3 & 3 & 2 & 1 \\ 2 & 4 & 6 & 2 \end{bmatrix}$. | 6 | L2 | CO4 |
| | b | Solve the system of equations by Gauss-Elimination method $3x + y + 2z = 3$, $2x - 3y - z = -3$, $x + 2y + z = 4$. | 7 | L3 | CO4 |
| | c | Using the Gauss-Seidel iteration method, solve the equations | 7 | L3 | CO4 |

| | | | | | |
|-------------|----------|---|----------|-----------|------------|
| | | $27x + 6y - z = 85,$ $6x + 15y + 2z = 72,$ $x + y + 54z = 110$ Carryout four iterations starting with the initial approximations (0, 0, 0). | | | |
| OR | | | | | |
| Q.10 | a | Using Rayleigh's power method find the dominant eigenvalue and the corresponding eigenvector of $\begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$ by taking $[1 \ 0 \ 0]^T$ as the initial eigenvector [carry out 6 iterations]. | 8 | L3 | CO4 |
| | b | Using Gauss-Jordan method, solve $x + y + z = 11, 3x - y + 2z = 12, 2x + y - z = 3.$ | 7 | L3 | CO4 |
| | c | Using modern mathematical tool write a program/code to test the consistency of the equations, $x+2y-z=1, 2x+y+4z=2, 3x+3y+4z=1.$ | 5 | L3 | CO5 |

Model Question Paper-II with effect from 2022 (CBCS Scheme)

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First Semester B.E Degree Examination

Mathematics-I for Mechanical Engineering Stream (BMATM101)

TIME: 03 Hours

Max. Marks: 100

Note:

1. Answer any **FIVE** full questions, choosing atleast **ONE** question from each **MODULE**
2. VTU Formula Hand Book is Permitted
3. M: Marks, L: RBT levels, C: Course outcomes.

| Module – 1 | | | M | L | C |
|------------|---|---|---|----|-----|
| Q.1 | a | Find the angle of intersection of the curves $r = \sin \theta + \cos \theta$, $r = 2 \sin \theta$. | 6 | L2 | CO1 |
| | b | With usual notations prove that for the curve $r = f(\theta)$, $\frac{1}{p^2} = \frac{1}{r^2} + \frac{1}{r^4} \left(\frac{dr}{d\theta} \right)^2$ | 7 | L2 | CO1 |
| | c | Find the radius of curvature for the curve $y = ax^2 + bx + c$ at $x = \frac{1}{2a} \left(\sqrt{a^2 - 1} - b \right)$. | 7 | L3 | CO1 |
| OR | | | | | |
| Q.2 | a | Show that the pedal equation for the curve $r^m = a^m \cos m\theta$ is $pa^m = r^{m+1}$. | 8 | L2 | CO1 |
| | b | Derive the radius of curvature in Cartesian form. | 7 | L2 | CO1 |
| | c | Using modern mathematical tool write a program/code to plot the curve $r = 2 \cos 2\theta $. | 5 | L3 | CO5 |
| Module – 2 | | | | | |
| Q.3 | a | Expand $e^{\cos x}$ by Maclaurin's series up to the term containing x^6 . | 6 | L2 | CO2 |
| | b | If $u = f(x - y, y - z, z - x)$, show that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$. | 7 | L2 | CO2 |
| | c | Examine the function $f(x, y) = x^3 + 3xy^2 + 15x^2 - 15y^2 + 72x$ for extreme values. | 7 | L3 | CO2 |
| OR | | | | | |
| Q.4 | a | Evaluate $\lim_{x \rightarrow 0} \left(\frac{a^x + b^x + c^x + d^x}{4} \right)^{\frac{1}{x}}$. | 7 | L2 | CO2 |
| | b | If $u = x^2 + y^2 + z^2$, $v = xy + yz + zx$, $w = x + y + z$ find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$. | 8 | L3 | CO2 |
| | c | Using modern mathematical tool write a program/code to show that $u_{xx} + u_{yy} = 0$ given $u = e^x(x \cos y - y \sin y)$. | 5 | L3 | CO5 |

| Module – 3 | | | | | |
|------------|----------|---|----------|-----------|------------|
| Q.5 | a | Solve $\frac{dy}{dx} + x \sin 2y = x^2 \cos^2 y$. | 6 | L2 | CO3 |
| | b | Solve $(x^3 + y^3 + 6x)dx + (xy^2)dy = 0$. | 7 | L2 | CO3 |
| | c | Find the orthogonal trajectories of cardioid $r = a(1 - \cos \theta)$. | 7 | L3 | CO3 |
| OR | | | | | |
| Q.6 | a | Solve $\frac{dy}{dx} + \frac{y \cos x + \sin y + y}{\sin x + x \cos y + x} = 0$ | 6 | L2 | CO3 |
| | b | A body is heated to 110°C and placed in air at 10°C . After an hour its temperature becomes 60°C . How much additional time is required for it to cool 30°C . | 7 | L3 | CO3 |
| | c | Find the general and singular solution of the equation $x^2(y - px) = p^2y$ reducing into Clairaut's form, using the substitution $X = x^2, Y = y^2$. | 7 | L2 | CO3 |
| Module – 4 | | | | | |
| Q.7 | a | Solve $(D^4 - 4D^3 + 8D^2 - 8D + 4)y = 0$ | 6 | L2 | CO3 |
| | b | Solve $(D^2 - 6D + 9)y = 6e^{3x} + 7e^{-2x} - \log 2$. | 7 | L3 | CO3 |
| | c | Solve by variation of parameters $(D^2 - 1)y = \frac{2}{1 + e^x}$ | 7 | L2 | CO3 |
| OR | | | | | |
| Q.8 | a | Solve $(D^3 - 3D^2 + 3D - 1)y = 0$. | 6 | L2 | CO3 |
| | b | Solve $(D^3 + 2D^2 + D)y = \sin 2x$. | 7 | L2 | CO3 |
| | c | Solve $(2x + 3)^2 \frac{d^2y}{dx^2} - (2x + 3) \frac{dy}{dx} - 12y = 6x$. | 7 | L2 | CO3 |
| Module – 5 | | | | | |
| Q.9 | a | Find the rank of the matrix $\begin{bmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$. | 6 | L2 | CO4 |
| | b | Solve the system of equations by Gauss-Jordan method $x + y + z = 8, -x - y + 2z = -4, 3x + 5y - 7z = 14$. | 7 | L3 | CO4 |
| | c | Solve the system of equations using Gauss-Seidel method by taking $(0, 0, 0)$ as an initial approximate root $5x + 2y + z = 12, x + 4y + 2z = 15, x + 2y + 5z = 20$ | 7 | L3 | CO4 |

| OR | | | | | |
|------|----------|---|---|----|-----|
| Q.10 | a | Find the rank of the matrix $\begin{bmatrix} 1 & 2 & 4 & 3 \\ 2 & 4 & 6 & 8 \\ 4 & 8 & 12 & 16 \\ 1 & 2 & 3 & 4 \end{bmatrix}$. | 7 | L2 | CO4 |
| | b | For what values λ and μ the system of equations $2x + 3y + 5z = 9$, $7x + 3y - 2z = 8$, $2x + 3y + \lambda z = \mu$, has (i) no solution (ii) a unique solution and (iii) infinite number of solutions. | 8 | L2 | CO4 |
| | c | Using modern mathematical tool write a program/code to find the largest eigen value of $A = \begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$ by power method. | 5 | L3 | CO5 |

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First Semester B.E Degree Examination

Mathematics-I for Mechanical Engineering stream (22MATM11)

TIME: 03 Hours

Max. Marks: 100

Note: Answer any **FIVE** full questions, choosing at least **ONE** question from each module.

| Module -1 | | | Marks |
|-----------|---|---|-------|
| Q.01 | a | Find the angle of intersection of the curves $r = \sin \theta + \cos \theta$ and $r = 2 \sin \theta$ | 06 |
| | b | Find the pedal equation of the curve $r^2 = a^2 \sec 2\theta$. | 07 |
| | c | Find the radius of curvature of the curve $x^4 + y^4 = 2$ at the point (1, 1) | 07 |
| OR | | | |
| Q.02 | a | Derive the radius of curvature for polar curve $r = f(\theta)$ in the form $\rho = \frac{(r^2 + r_1^2)^{3/2}}{r^2 + 2r_1^2 - rr_2}$ | 06 |
| | b | Find the angle between the radius vector and the tangent and also find the slope of the tangent $r = a(1 + \cos \theta)$ at $\theta = \pi/3$. | 07 |
| | c | Find that the radius of curvature of $a^2 y = x^3 - a^3$ at the point where the curves cut the X-axis. | 07 |
| Module-2 | | | |
| Q. 03 | a | Expand $\log \cos x$ by Maclaurin's series up to the term containing x^6 | 06 |
| | b | If $z = \frac{x^2 + y^2}{x + y}$, show that $\left(\frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}\right)^2 = 4\left(1 - \frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}\right)$ | 07 |
| | c | If $u = x + y + z$, $uv = y + z$, $uvw = z$, evaluate $\frac{\partial(x,y,z)}{\partial(u,v,w)}$ | 07 |
| OR | | | |
| Q.04 | a | Evaluate (i) $\lim_{x \rightarrow 0} \left(\frac{\sin x}{x}\right)^{1/x^2}$ (ii) $\lim_{x \rightarrow 0} (\tan x)^{\tan x}$ | 6 |
| | b | If $u = f(ax - by, by - cz, cz - ax)$, show that $\frac{1}{a} \frac{\partial u}{\partial x} + \frac{1}{b} \frac{\partial u}{\partial y} + \frac{1}{c} \frac{\partial u}{\partial z} = 0$ | 07 |
| | c | Find the extreme values of $f(x, y) = x^3 + 3x^2 + 4xy + y^2$ | 07 |
| Module-3 | | | |
| Q. 05 | a | Solve $\frac{dy}{dx} - y \tan x = y^2 \sec x$ | 06 |
| | b | Water at temperature 10°C takes 5 minutes to warm up to 20°C at room temperature of 40° . Find the temperature of the water after 20 minutes. | 07 |
| | c | Solve $\frac{dy}{dx} - \frac{dx}{dy} = \frac{x}{y} - \frac{y}{x}$ | 07 |
| OR | | | |

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|-----------------|---|--|----|
| Q. 06 | a | Solve $(y \log y)dx + (x - \log y)dy = 0$ | 06 |
| | b | Find the orthogonal trajectories of the family curve $r = 2a(\cos\theta + \sin\theta)$. | 07 |
| | c | Find the general and singular solutions of $x^2p^2 + xp - yp + 1 - y = 0$ | 07 |
| Module-4 | | | |
| Q. 07 | a | Solve $(D^3 - 6D^2 + 11D - 6)y = e^{2x}$ | 06 |
| | b | Solve $\frac{d^2y}{dx^2} - 4y = \cos 2x$ | 07 |
| | c | Solve by variation of parameters method $(D^2 + 1)y = \sec x$ | 07 |
| OR | | | |
| Q. 08 | a | Solve $(D^2 + D + 1)y = x^2 + 1$ | 06 |
| | b | Solve $(D - 2)^2y = 8(x^2 + \sin 2x + e^{2x})$ | 07 |
| | c | Solve $x^2 \frac{d^2y}{dx^2} + 4x \frac{dy}{dx} + 2y = \log x$ | 07 |
| Module-5 | | | |
| Q. 09 | a | Find the rank of the matrix $\begin{bmatrix} 1 & 2 & 3 & 1 \\ 2 & 1 & -1 & 0 \\ 3 & 3 & 2 & 1 \\ 2 & 4 & 6 & 2 \end{bmatrix}$ | 06 |
| | b | Solve the system of equations by using the Gauss elimination method $3x + y + 2z = 3,$ $2x - 3y - z = -3,$ $x + 2y + z = 4.$ | 07 |
| | c | Using the Gauss-Seidel iteration method, solve the equations $27x + 6y - z = 85,$ $6x + 15y + 2z = 72,$ $x + y + 54z = 110.$ Carryout four iterations starting with the initial approximations (0, 0, 0) | 07 |
| OR | | | |
| Q. 10 | a | Test for consistency and solve $5x + 3y + 7z = 4,$ $3x + 26y + 2z = 9,$ $7x + 2y + 10z = 5$ | 06 |
| | b | Using Gauss-Jordan method, solve $x + y + z = 11,$ $3x - y + 2z = 12,$ $2x + y - z = 3$ | 07 |
| | c | Find the largest eigenvalue and the corresponding eigenvector of $\begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$ with the initial approximate eigenvector $[1 \ 0 \ 0]^T$. Carry out 4 iterations. | 07 |

| Table showing the Bloom's Taxonomy Level, Course Outcome and Program Outcome | | | | |
|--|---|---------------------------------|---|--|
| Question | | Bloom's Taxonomy Level attached | Course Outcome | Program Outcome |
| Q.1 | (a) | L1 | CO 01 | PO 01 |
| | (b) | L2 | CO 01 | PO 01 |
| | (c) | L3 | CO 01 | PO 02 |
| Q.2 | (a) | L1 | CO 01 | PO 01 |
| | (b) | L2 | CO 01 | PO 01 |
| | (c) | L3 | CO 01 | PO 02 |
| Q.3 | (a) | L2 | CO 02 | PO 01 |
| | (b) | L2 | CO 02 | PO 01 |
| | (c) | L3 | CO 02 | PO 02 |
| Q.4 | (a) | L2 | CO 02 | PO 01 |
| | (b) | L2 | CO 02 | PO 01 |
| | (c) | L3 | CO 02 | PO 03 |
| Q.5 | (a) | L2 | CO 03 | PO 02 |
| | (b) | L3 | CO 03 | PO 03 |
| | (c) | L2 | CO 03 | PO 01 |
| Q.6 | (a) | L2 | CO 03 | PO 02 |
| | (b) | L3 | CO 03 | PO 03 |
| | (c) | L2 | CO 03 | PO 01 |
| Q.7 | (a) | L2 | CO 04 | PO 02 |
| | (b) | L2 | CO 04 | PO 02 |
| | (c) | L2 | CO 04 | PO 02 |
| Q.8 | (a) | L2 | CO 04 | PO 02 |
| | (b) | L2 | CO 04 | PO 02 |
| | (c) | L2 | CO 04 | PO 02 |
| Q.9 | (a) | L2 | CO 05 | PO 01 |
| | (b) | L3 | CO 05 | PO 01 |
| | (c) | L3 | CO 05 | PO 02 |
| Q.10 | (a) | L2 | CO 05 | PO 01 |
| | (b) | L3 | CO 05 | PO 01 |
| | (c) | L3 | CO 05 | PO 02 |
| | | | | |
| Bloom's Taxonomy Levels | Lower order thinking skills | | | |
| | Remembering (Knowledge): L ₁ | | Understanding (Comprehension): L ₂ | Applying (Application): L ₃ |
| | Higher-order thinking skills | | | |
| | Analyzing (Analysis): L ₄ | | Valuating (Evaluation): L ₅ | Creating (Synthesis): L ₆ |

Model Question Paper-2 with effect from 2022 (CBCS Scheme)

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First Semester B.E Degree Examination

Mathematics-I for Mechanical Engineering Stream (22MATM11)

TIME: 03 Hours

Max. Marks: 100

Note: Answer any **FIVE** full questions, choosing at least **ONE** question from each **MODULE**.

| Module -1 | | | Marks |
|-----------|---|---|-------|
| Q.01 | a | Find the angle between the polar curves $r = a(1 + \cos \theta)$ and $r^2 = a^2 \cos 2\theta$ | 06 |
| | b | Prove with usual notations $\frac{1}{p^2} = \frac{1}{r^2} + \frac{1}{r^4} \left(\frac{dr}{d\theta} \right)^2$ | 07 |
| | c | Find the radius of curvature for the curve $y = ax^2 + bx + c$ at $x = \frac{1}{2a}(\sqrt{a^2 - 1} - b)$. | 07 |
| OR | | | |
| Q.02 | a | Show that the pedal equation for the curve $r^m = a^m \cos m\theta$ is $pa^m = r^{m+1}$ | 06 |
| | b | Derive the radius of curvature in Cartesian form. | 07 |
| | c | Show that for the curve $r = a(1 - \cos \theta)$ is $\frac{\rho^2}{r} = \text{constant}$. | 07 |
| Module-2 | | | |
| Q. 03 | a | Expand $e^{\cos x}$ up to the terms containing fourth degree using Maclaurin's series. | 06 |
| | b | If $u = f(x - y, y - z, z - x)$ show that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$ | 07 |
| | c | Find the extreme values of the function $f(x, y) = x^3 + 3xy^2 + 15x^2 - 15y^2 + 72x$ | 07 |
| OR | | | |
| Q.04 | a | Evaluate $\lim_{x \rightarrow 0} \left(\frac{a^x + b^x + c^x + d^x}{4} \right)^{\frac{1}{x}}$ | 06 |
| | b | Find the total derivative $\frac{du}{dx}$ for $u = xy^2 + x^2y$; $x = at$; $y = 2at$ | 07 |
| | c | If $u = x^2 + y^2 + z^2$, $v = xy + yz + zx$, $w = x + y + z$ find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$ | 07 |
| Module-3 | | | |
| Q. 05 | a | Solve $\frac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$ | 06 |

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|-----------------|---|--|----|
| | b | Solve $(x^3 + y^3 + 6x) dx + (xy^2) dy = 0$ | 07 |
| | c | Find the orthogonal trajectories of cardioid $r = a(1 - \cos \theta)$ | 07 |
| OR | | | |
| Q. 06 | a | Solve $\frac{dy}{dx} + \frac{y \cos x + \sin y + y}{\sin x + x \cos y + x} = 0$ | 06 |
| | b | A body is heated to 110°C and placed in air at 10°C . After an hour its temperature becomes 60°C . How much additional time is required for it to cool to 30°C . | 07 |
| | c | Find the general solution of $x^2(y - px) = p^2 y$ by reducing it to Clairaut's form using the substitution $X = x^2, Y = y^2$. | 07 |
| Module-4 | | | |
| Q. 07 | a | Solve $[D^4 - 4D^3 + 8D^2 - 8D + 4]y = 0$. | 06 |
| | b | Solve $[D^2 - 6D + 9]y = 6e^{3x} + 7e^{-2x} - \log 2$ | 07 |
| | c | Solve by the method of variation of parameter $\frac{d^2 y}{dx^2} - y = \frac{2}{1+e^x}$ | 07 |
| OR | | | |
| Q. 08 | a | Solve $(D^3 - 3D^2 + 3D - 1)y = 0$ | 06 |
| | b | Solve $[D^3 + 2D^2 + D]y = \sin 2x$ | 07 |
| | c | Solve $(2x + 3)^2 \frac{d^2 y}{dx^2} - (2x + 3) \frac{dy}{dx} - 12y = 6x$ | 07 |
| Module-5 | | | |
| Q. 09 | a | Find the rank of the matrix $A = \begin{bmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$ | 06 |
| | b | Solve the system of equations by Gauss-Jordan method $x + y + z = 8; -x - y + 2z = -4; 3x + 5y + -7 = 14$ | 07 |
| | c | Using Rayleigh's power method find the dominant eigenvalue and the corresponding eigenvector of $A = \begin{bmatrix} 25 & 1 & 2 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{bmatrix}$ by taking $(1, 0, 0)^T$ as initial eigenvector by carrying out 6 iterations. | 07 |
| OR | | | |

| | | | |
|-------|---|---|----|
| Q. 10 | a | Find the rank of the matrix $A = \begin{bmatrix} 1 & 2 & 4 & 3 \\ 2 & 4 & 6 & 8 \\ 4 & 8 & 12 & 16 \\ 1 & 2 & 3 & 4 \end{bmatrix}$ | 06 |
| | b | Investigate the value of λ and μ so that the equations $2x + 3y + 5z = 9$, $7x + 3y - 2z = 8$, $2x + 3y + \lambda z = \mu$ may have i) unique solution ii) many solution iii) no solution. | 07 |
| | c | Solve the system of equations using Gauss-Seidel method by taking (0, 0, 0) as an initial approximate root. $\begin{aligned} 5x + 2y + z &= 12 \\ x + 4y + 2z &= 15 \\ x + 2y + 5z &= 20 \end{aligned}$ | 07 |

| Table showing the Bloom's Taxonomy Level, Course Outcome and Program Outcome | | | | |
|--|-----|---------------------------------|----------------|-----------------|
| | | | | |
| Question | | Bloom's Taxonomy Level attached | Course Outcome | Program Outcome |
| Q.1 | (a) | L1 | CO 01 | PO 01 |
| | (b) | L2 | CO 01 | PO 01 |
| | (c) | L3 | CO 01 | PO 02 |
| Q.2 | (a) | L1 | CO 01 | PO 01 |
| | (b) | L2 | CO 01 | PO 01 |
| | (c) | L3 | CO 01 | PO 02 |
| Q.3 | (a) | L2 | CO 02 | PO 01 |
| | (b) | L2 | CO 02 | PO 01 |
| | (c) | L3 | CO 02 | PO 02 |
| Q.4 | (a) | L2 | CO 02 | PO 01 |
| | (b) | L2 | CO 02 | PO 01 |
| | (c) | L3 | CO 02 | PO 03 |
| Q.5 | (a) | L2 | CO 03 | PO 01 |
| | (b) | L3 | CO 03 | PO 02 |
| | (c) | L2 | CO 03 | PO 01 |
| Q.6 | (a) | L2 | CO 03 | PO 01 |
| | (b) | L3 | CO 03 | PO 02 |
| | (c) | L2 | CO 03 | PO 01 |
| Q.7 | (a) | L2 | CO 04 | PO 01 |
| | (b) | L2 | CO 04 | PO 01 |
| | (c) | L2 | CO 04 | PO 02 |
| Q.8 | (a) | L2 | CO 04 | PO 01 |
| | (b) | L2 | CO 04 | PO 01 |
| | (c) | L2 | CO 04 | PO 02 |
| Q.9 | (a) | L2 | CO 05 | PO 01 |
| | (b) | L3 | CO 05 | PO 01 |
| | (c) | L3 | CO 05 | PO 02 |

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|--------------------------------|---|--|-------|---|
| Q.10 | (a) | L2 | CO 05 | PO 01 |
| | (b) | L3 | CO 05 | PO 01 |
| | (c) | L3 | CO 05 | PO 02 |
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| Bloom's Taxonom y Levels | Lower order thinking skills | | | |
| | Remembering (knowledge):L ₁ | Understanding (Comprehension): L ₂ | | Applying (Application): L ₃ |
| | Higher order thinking skills | | | |
| | Analyzing (Analysis):L ₄ | Valuating (Evaluation): L ₅ | | Creating (Synthesis): L ₆ |
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