

## ADTs on Parade

ADT	When to use	Array-based?	Linked list-based?	Time complexity: Insertion <i>Avg case</i> <b>Worst case</b>		Time complexity: Deletion <i>Avg case</i> <b>Worst case</b>		Time complexity: Search <i>Avg case</i> <b>Worst case</b>	
Array (not an ADT; built-in data structure)	Collection of homogeneous elements.	Yes	No	$O(n)$	<b><math>O(n)</math></b>	$O(n)$	<b><math>O(n)</math></b>	$O(n)$	<b><math>O(n)</math></b> ( $O(1)$ to find elmt $i$ )
Linked List	Collection of homogeneous elements.	No	Yes	$O(1)$	<b><math>O(1)</math></b>	$O(1)$	<b><math>O(1)</math></b>	$O(n)$	<b><math>O(n)</math></b> ( $O(n)$ to find node $i$ )
Bag	Growable container. Unordered. Unindexed.	Yes	Yes	$O(n)^4$	<b><math>O(n)</math></b>	$O(n)^4$	<b><math>O(n)</math></b>	$O(n)$	<b><math>O(n)</math></b>
Sequence	Growable container. Ordered. Unindexed. Has a current element.	Yes	Yes	$O(n)^4$	<b><math>O(n)</math></b>	$O(n)^4$	<b><math>O(n)</math></b>	$O(n)$	<b><math>O(n)</math></b>
Stack	Growable container. Use for LIFO behavior, backtracking, and iterative solutions to recursive problems	Yes	Yes	$O(1)$	<b><math>O(1)</math></b>	$O(1)$	<b><math>O(1)</math></b>	$O(n)^0$	<b><math>O(n)</math></b>
Queue	Growable container. Use for FIFO behavior, first-come-first-serve simulations	Yes	Yes	$O(1)$	<b><math>O(1)</math></b> <sup>1</sup>	$O(1)$	<b><math>O(1)</math></b> <sup>1</sup>	$O(n)^0$	<b><math>O(n)</math></b>
Priority queue	Container for retrieving elements in order of priority. Good for scheduling, sorting	Yes	Yes	Depends on how elmts are stored. Usually array or heap-based. See stats for <b>Array</b> or <b>Heap</b> , respectively.					
Binary search tree	Tree for organizing by a key. Great for all around performance.	Yes <sup>2</sup>	Yes	$O(\log n)$	<b><math>O(n)</math></b>	$O(\log n)$	<b><math>O(n)</math></b>	$O(\log n)$	<b><math>O(n)</math></b>
2-3 tree	Dynamic search tree that maintains balance via node splitting. Better performance than BST at a cost of higher coding complexity. Use to guarantee $O(\log n)$ performance at all times.	No	Yes	$O(\log n)$	<b><math>O(\log n)</math></b>	$O(\log n)$	<b><math>O(\log n)</math></b>	$O(\log n)$	<b><math>O(\log n)</math></b>
Heap	Tree where smallest (minheap) or largest (maxheap) item can be obtained in $O(1)$ time. Great for sorting, PQs	Yes	No <sup>3</sup>	$O(\log n)$	<b><math>O(\log n)</math></b>	$O(\log n)$	<b><math>O(\log n)</math></b>	$O(n)$	<b><math>O(n)</math></b>
Hash Table	Implementation of the table ADT. A BST-tree-based table or sorted-array-based table are other options.	Yes	No	$O(1)$	<b><math>O(n)</math></b>	$O(1)$	<b><math>O(n)</math></b>	$O(1)$	<b><math>O(n)</math></b>
Graph	Use to establish arbitrary relationships between nodes of data. Good for networks, factories, databases, and many more.	Yes = adjacency matrix	Yes = adjacency list	$O(1)^5$	<b><math>O(1)</math></b>	Matrix $O( V ^2)$ <b><math>O( V ^2)</math></b>	Adj List <sup>6</sup> $O( E )$ <b><math>O( E )</math></b>	Matrix <sup>7</sup> $O(1)$ <b><math>O(1)</math></b>	Adj List $O( V )$ <b><math>O( V )</math></b>

<sup>0</sup> This operation isn't really supported by this ADT.

<sup>1</sup> Assumes wrap around for array-based implementation and firstNode and lastNode pointers for LL-based implementation.

<sup>2</sup> While do-able, an array-based implementation would have poor space complexity if tree not complete.

<sup>3</sup> Well, you could. But no one does. An array provides better performance without the complexity.

<sup>4</sup> These are for the array-based version. The LL-based version would have time complexities listed for LL.

<sup>5</sup> Insertion means inserting a new vertex into the graph (without its edges).  $|V|$  is the number of vertices.

<sup>6</sup> Deletion means deleting a vertex (along with its edges).  $|E|$  = number of edges, which at worst will be  $|V|^2$  if every vertex is adjacent to every other vertex

<sup>7</sup> Here, search refers to searching to see if edge  $(x, y)$  exists