

---

**CS771 : Introduction to Machine Learning**  
**Assignment - 1**  
**Team: Syntax Killer**

---

**Dhruv Varshney**

220366

Dept. of Electrical Engineering  
IIT Kanpur  
vdhruv22@iitk.ac.in

**Sarthak Paswan**

220976

Dept. of Computer Science and Engineering  
IIT Kanpur  
sarthakp22@iitk.ac.in

**Ansh Jain**

220166

Dept. of Civil Engineering  
IIT Kanpur  
anshjain22@iitk.ac.in

**Shyam Sundar**

221049

Dept. of Mathematics and Scientific Computing  
IIT Kanpur  
shyams22@iitk.ac.in

**Rudraksh Pal Singh**

220920

Dept. of Mechanical Engineering  
IIT Kanpur  
rudrakshps22@iitk.ac.in

**Daniel Siwakoti**

231040127

Dept. of Electrical Engineering  
IIT Kanpur  
daniels23@iitk.ac.in

**Abstract**

This is our solution to the first Assignment of the course CS771. We are required to show (mathematical derivation) how for a simple arbiter PUF, a linear model can predict the time it takes for the upper signal to reach the finish line. Then using that derivation to derive how a linear model can predict Response0 and Response1 for a COCO-PUF. Finally, we have to report the outcomes of experiments with both the `sklearn.svm.LinearSVC` and `sklearn.linear model.LogisticRegression` methods when used to learn the linear model for the COCO-PUF, how various hyperparameters affected training time and test accuracy.

# 1 Linear model to predict the time it takes for the upper signal to reach the finish line for Arbiter PUF

## 1.1 Arbiter PUFs – A Brief Introduction

Arbiter Physically Unclonable Functions are hardware systems that capitalise on unpredictable differences in data transmission speed in different iterations of the same design to implement security.

They consist of a series of multiplexers (mux'es, hereafter) each having a selection bit. A particular set of selection bits is said to form a "question/challenge", and depending on these selection bits, the signal that reaches the end of the PUF first is said to be the "answer". The answer to a particular challenge is therefore unique to the hardware of that particular PUF.

## 1.2 Using ML to find the time taken by upper signal to reach the finish line

It has been found that knowing time taken by a relatively small number of challenges, a model can be trained to predict the time taken by any other challenge for a particular arbiter PUF, the analysis for which is shown below:

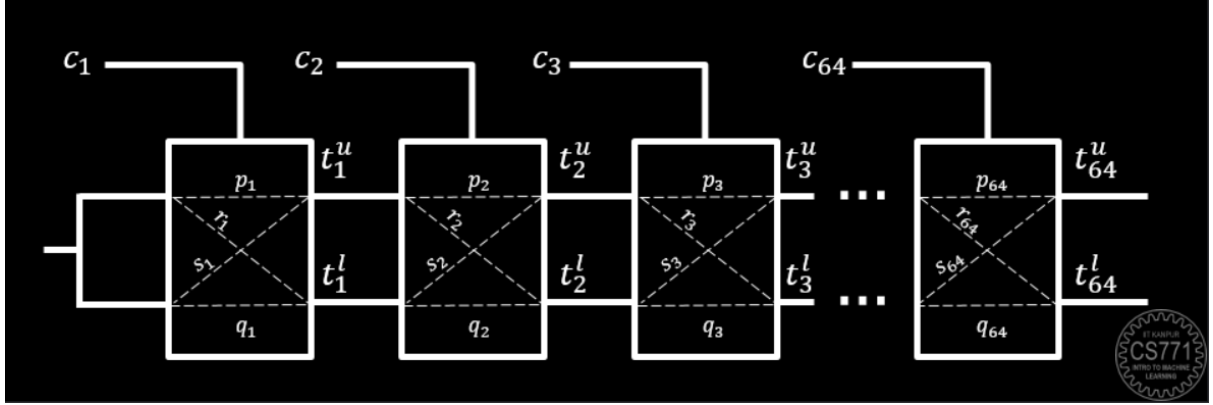


Figure 1: A simple arbiter PUF with 64 multiplexers

$t_i^u$  is the (unknown) time at which the upper signal leaves the i-th PUF.

$t_i^l$  is the time at which the lower signal leaves the i-th PUF.

All PUFs are different so that  $p_i$ ,  $r_i$ ,  $s_i$ , and  $q_i$  are distinct.

Therefore, the answer is 0 if  $t_{31}^u < t_{31}^l$  and 1 otherwise.

(Here, we have assumed zero based indexing which implies  $t_{-1}^u = t_{-1}^l = 0$ )

Now, as given in the lecture slides -

$$t_n^u = (1 - c_n) \cdot (t_{n-1}^u + p_n) + c_n \cdot (t_{n-1}^l + s_n) \quad (1)$$

$$t_n^l = (1 - c_n) \cdot (t_{n-1}^l + q_n) + c_n \cdot (t_{n-1}^u + r_n) \quad (2)$$

Adding equations (1) and (2), we get -

$$t_n^u + t_n^l = t_{n-1}^u + t_{n-1}^l + (1 - c_n) \cdot (p_n + q_n) + c_n \cdot (r_n + s_n)$$

For  $n = 0$ ,

$$t_0^u + t_0^l = (1 - c_0) \cdot (p_0 + q_0) + c_0 \cdot (r_0 + s_0) \quad (\text{Since, } t_{-1}^u = 0 \text{ \& } t_{-1}^l = 0)$$

For  $n = 1$ ,

$$t_1^u + t_1^l = (1 - c_0).(p_0 + q_0) + c_0.(r_0 + s_0) + (1 - c_1).(p_1 + q_1) + c_1.(r_1 + s_1)$$

For  $n = 2$ ,

$$t_2^u + t_2^l = (1 - c_0).(p_0 + q_0) + c_0.(r_0 + s_0) + (1 - c_1).(p_1 + q_1) + c_1.(r_1 + s_1) + (1 - c_2).(p_2 + q_2) + c_2.(r_2 + s_2)$$

By induction-

$$t_{31}^u + t_{31}^l = \sum_{i=0}^{31} [(1 - c_i).(p_i + q_i) + c_i.(r_i + s_i)] \quad (3)$$

From the lecture slides we have expression for the difference of the equation (1) and (2),

$$\Delta_i = d_i \cdot \Delta_{i-1} + \alpha_i \cdot d_i + \beta_i$$

where,

$$\begin{aligned} \Delta_i &= t_i^u - t_i^l \\ d_i &= (1 - 2c_i) \\ \alpha_i &= (p_i - q_i + r_i - s_i)/2 \\ \beta_i &= (p_i - q_i - r_i + s_i)/2 \end{aligned}$$

For  $i = 0$ ,

$$\Delta_0 = \alpha_0.d_0 + \beta_0 \quad (\text{Since, } \Delta_{-1} = 0)$$

Let us take -

$$A_i = \alpha_i.d_i + \beta_i$$

Then,

$$\Delta_0 = A_0$$

For  $i = 1$ ,

$$\Delta_1 = d_1.\Delta_0 + \alpha_1.d_1 + \beta_1$$

$$\Delta_1 = d_1.A_0 + A_1$$

For  $i = 2$ ,

$$\Delta_2 = d_2.d_1.A_0 + d_2.A_1 + A_2$$

Similarly,

$$\Delta_{31} = \sum_{i=0}^{31} A_i \cdot \prod_{j=i+1}^{31} d_j$$

So,

$$t_{31}^u - t_{31}^l = \sum_{i=0}^{31} [(p_i - q_i)(1 - c_i) + c_i.(s_i - r_i)] \prod_{j=i+1}^{31} (1 - 2c_j) \quad (4)$$

$$(5)$$

Adding equation (3) and (4), we get,

$$t_{31}^u = t^u = \frac{1}{2} \cdot \sum_{i=0}^{31} (1 - c_i)(p_i + q_i) + c_i \cdot (r_i + s_i) + \frac{1}{2} \cdot \sum_{i=0}^{31} [(1 - c_i) \cdot (p_i - q_i) + c_i \cdot (s_i - r_i)] \prod_{j=i+1}^{31} (1 - 2c_j) \quad (6)$$

If we take,

$$\begin{aligned} d_i &= (1 - 2 \cdot c_i) \\ \alpha_i &= \frac{(p_i + q_i + r_i + s_i)}{4} \\ \beta_i &= \frac{(p_i + q_i - r_i - s_i)}{4} \\ \gamma_i &= \frac{(p_i - q_i + s_i - r_i)}{4} \\ \delta_i &= \frac{(p_i - q_i + r_i - s_i)}{4} \end{aligned}$$

And simplyfying equation (5), we get -

$$t^u = \sum_{i=0}^{31} \alpha_i + \gamma_{31} + \sum_{i=0}^{31} d_i \cdot \beta_i + \sum_{i=0}^{31} (\delta_i + \gamma_{i-1})(d_i \cdot d_{i+1} \cdot d_{i+2} \dots d_{31}) \quad (\text{Here, } \gamma_{-1} = 0)$$

$$\text{Take } b = \sum_{i=0}^{31} \alpha_i + \gamma_{31}$$

Now, converting this to matrix form, we get -

$$t^u(c) = W^T \phi(c) + b$$

where,

$$W = \begin{pmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_{30} \\ \delta_0 \\ (\delta_1 + \gamma_0) \\ \vdots \\ (\delta_{31} + \gamma_{30} + \beta_{31}) \end{pmatrix}$$

and,

$$\phi(c) = \begin{pmatrix} d_0 \\ d_1 \\ \vdots \\ d_{30} \\ d_0 d_1 d_2 \dots d_{31} \\ d_1 d_2 d_3 \dots d_{31} \\ \vdots \\ d_{31} \end{pmatrix}$$

## 2 Dimensionality of the model $\mathbf{W}$

From previous part,

$$W = \begin{pmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_{30} \\ \delta_0 \\ (\delta_1 + \gamma_0) \\ \vdots \\ (\delta_{31} + \gamma_{30} + \beta_{31}) \end{pmatrix}$$

Clearly, it is **63 x 1** matrix.

Hence, dimension of the  $\mathbf{W}(\text{model})$  is **63 x 1**.

## 3 Linear models to predict Response0 and Response1

### 1.3 Another type of PUF — COCO-PUF

A COCO-PUF uses 2 arbiter PUFs, say PUF0 and PUF1 – each PUF has its own set of multiplexers with possibly different delays. Given a challenge, it is fed into both the PUFs. Instead of the lower and upper signals of PUF0 competing with each other, the lower signal from PUF0 compete with the lower signal from PUF1 using an arbiter called Arbiter0 to generate a response called Response0. Also, the upper signal from PUF0 compete with the upper signal from PUF1 using a second arbiter called Arbiter1 to generate a response called Response1.

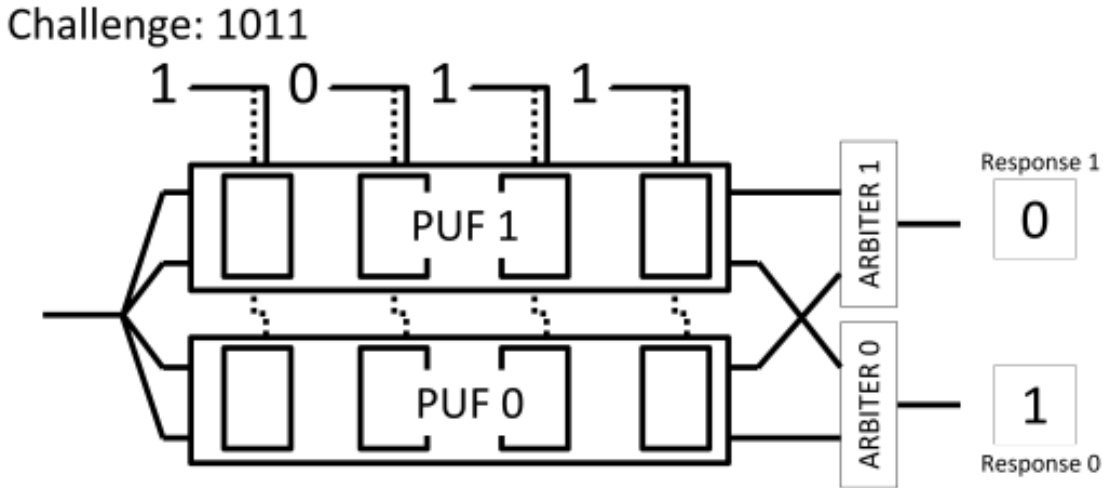


Figure 2: A COCO-PUF with 4-bit challenges and 2-bit responses

### 1.4 Using ML to crack COCO-PUF

From the previous part, the expression for  $t_{31}^u$  is:

$$t_{31}^u = \frac{1}{2} \cdot \sum_{i=0}^{31} (1 - c_i)(p_i + q_i) + c_i \cdot (r_i + s_i) + \frac{1}{2} \cdot \sum_{i=0}^{31} [(1 - c_i) \cdot (p_i - q_i) + c_i \cdot (s_i - r_i)] \prod_{j=i+1}^{31} (1 - 2c_j)$$

Similar expression for  $t_{31}^l$  can be derived by subtracting equation (4) from (3),

$$t_{31}^l = \frac{1}{2} \cdot \sum_{i=0}^{31} (1 - c_i)(p_i + q_i) + c_i \cdot (r_i + s_i) - \frac{1}{2} \cdot \sum_{i=0}^{31} [(1 - c_i) \cdot (p_i - q_i) + c_i \cdot (s_i - r_i)] \prod_{j=i+1}^{31} (1 - 2c_j)$$

$$2t_{31}^{l_1} = \sum_{i=0}^{31} (1 - c_i)(p_i^1 + q_i^1) + c_i(s_i^1 + r_i^1) - \sum_{i=0}^{31} ((1 - c_i)(p_i^1 - q_i^1) + c_i(s_i^1 - r_i^1)) \left( \prod_{j=i+1}^{31} (1 - 2c_j) \right) \dots\dots(7)$$

$$2t_{31}^{l_0} = \sum_{i=0}^{31} (1 - c_i)(p_i^0 + q_i^0) + c_i(s_i^0 + r_i^0) - \sum_{i=0}^{31} ((1 - c_i)(p_i^0 - q_i^0) + c_i(s_i^0 - r_i^0)) \left( \prod_{j=i+1}^{31} (1 - 2c_j) \right) \dots\dots(8)$$

Subtracting equation (8) from (7),

$$\begin{aligned} 2(t_{31}^{l_0} - t_{31}^{l_1}) &= \sum_{i=0}^{31} (1 - c_i) (p_i^0 + q_i^0 - p_i^1 - q_i^1) + c_i (s_i^0 + r_i^0 - s_i^1 - r_i^1) \\ &\quad + \sum_{i=0}^{31} ((1 - c_i) (p_i^1 - q_i^1 - p_i^0 + q_i^0) + c_i (s_i^1 - r_i^1 - s_i^0 + r_i^0)) \left( \prod_{j=i+1}^{31} (1 - 2c_j) \right) \end{aligned}$$

$$\text{let, } (1 - 2c_i) = d_i$$

$$\begin{aligned} 2(t_{31}^{l_0} - t_{31}^{l_1}) &= \sum_{i=0}^{31} \left( \frac{1}{2} + \frac{d_i}{2} \right) (p_i^0 + q_i^0 - p_i^1 - q_i^1) + \left( \frac{1 - d_i}{2} \right) (s_i^0 + r_i^0 - s_i^1 - r_i^1) \\ &\quad + \sum_{i=0}^{31} \left( \frac{1}{2} + \frac{d_i}{2} \right) (d_{i+1} \dots d_{31}) (p_i^1 - q_i^1 - p_i^0 + q_i^0) + \left( \frac{1 - d_i}{2} \right) (d_{i+1} \dots d_{31}) (s_i^1 - r_i^1 - s_i^0 + r_i^0) \end{aligned}$$

$$\begin{aligned} t_{31}^{l_0} - t_{31}^{l_1} &= \sum_{i=0}^{31} \left( \frac{p_i^0 + q_i^0 + s_i^0 + r_i^0 - p_i^1 - q_i^1 - s_i^1 - r_i^1}{4} \right) + d_i \left( \frac{p_i^0 + q_i^0 - s_i^0 - r_i^0 - p_i^1 - q_i^1 + s_i^1 + r_i^1}{4} \right) \\ &\quad + (d_{i+1} \dots d_{31}) \left( \frac{p_i^1 - q_i^1 - p_i^0 + q_i^0 + s_i^1 - r_i^1 - s_i^0 + r_i^0}{4} \right) \\ &\quad + (d_i \dots d_{31}) \left( \frac{p_i^1 - q_i^1 - p_i^0 + q_i^0 - s_i^1 + r_i^1 + s_i^0 - r_i^0}{4} \right) \end{aligned}$$

Let,

$$\begin{aligned} \alpha_i &= \frac{p_i^0 + q_i^0 + s_i^0 + r_i^0 - p_i^1 - q_i^1 - s_i^1 - r_i^1}{4} \\ \beta_i &= \frac{p_i^0 + q_i^0 - s_i^0 - r_i^0 - p_i^1 - q_i^1 + s_i^1 + r_i^1}{4} \\ \gamma_i &= \frac{p_i^1 - q_i^1 - p_i^0 + q_i^0 + s_i^1 - r_i^1 - s_i^0 + r_i^0}{4} \\ \delta_i &= \frac{p_i^1 - q_i^1 - p_i^0 + q_i^0 - s_i^1 + r_i^1 + s_i^0 - r_i^0}{4} \end{aligned}$$

$$t_{31}^{l_0} - t_{31}^{l_1} = \sum_{i=0}^{31} \alpha_i + \sum_{i=0}^{31} d_i \beta_i + \sum_{i=0}^{31} (d_{i+1} \dots d_{31}) \gamma_i + \sum_{i=0}^{31} (d_i \dots d_{31}) \delta_i$$

$$t_{31}^{l_0} - t_{31}^{l_1} = \left( \sum_{i=0}^{31} \alpha_i + \gamma_{31} \right) + \left( \sum_{i=0}^{30} d_i \beta_i \right) + \delta_1(d_1 \dots d_{31}) + (\delta_2 + \gamma_1)(d_2 \dots d_{31}) + \dots + (\delta_{31} + \gamma_{30} + \beta_{31})d_{31}$$

$$\text{Let, } \tilde{b} = \sum_{i=0}^{31} \alpha_i + \gamma_{31}$$

$$t_{31}^{l_0} - t_{31}^{l_1} = \tilde{b} + [\beta_0 \quad \beta_1 \quad \dots \quad \beta_{30} \quad \delta_1 \quad (\delta_2 + \gamma_1) \quad \dots \quad (\delta_{31} + \gamma_{30} + \beta_{31})] \begin{bmatrix} d_0 \\ d_1 \\ \vdots \\ d_{30} \\ d_0 d_1 \dots d_{31} \\ d_1 d_2 \dots d_{31} \\ \vdots \\ d_{30} d_{31} \\ d_{31} \end{bmatrix}$$

$$t_{31}^{l_0} - t_{31}^{l_1} = \tilde{b} + \tilde{W}_0^T \phi_0(C) \quad , \text{ where}$$

$$\tilde{W}_0 = \begin{bmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_{30} \\ \delta_1 \\ \delta_2 + \gamma_1 \\ \vdots \\ \delta_{31} + \gamma_{30} + \beta_{31} \end{bmatrix} \quad \text{and} \quad \phi_0(C) = \begin{bmatrix} d_0 \\ d_1 \\ \vdots \\ d_{30} \\ d_0 d_1 \dots d_{31} \\ d_1 d_2 \dots d_{31} \\ \vdots \\ d_{31} \end{bmatrix}$$

Hence the Response0 can predicted using this linear model as -

$$\frac{1 + \text{sign}(\tilde{\mathbf{W}}_0^T \phi_0(\mathbf{c}) + \tilde{\mathbf{b}})}{2} = r^0(\mathbf{c})$$

Similar to the Response0, we can predict Responel by using the expression of  $t_{31}^{u_0}$  and  $t_{31}^{u_1}$  in equation (7) and (8) respectively, we get-

$$t_{31}^{u_0} - t_{31}^{u_1} = \sum_{i=0}^{31} \alpha_i + \sum_{i=0}^{31} d_i \beta_i + \sum_{i=0}^{31} (d_{i+1} \dots d_{31}) \gamma_i + \sum_{i=0}^{31} (d_i \dots d_{31}) \delta_i$$

Here,

$$\alpha_i = \frac{p_i^0 + q_i^0 + s_i^0 + r_i^0 - p_i^1 - q_i^1 - s_i^1 - r_i^1}{4}$$

$$\beta_i = \frac{p_i^0 + q_i^0 - s_i^0 - r_i^0 - p_i^1 - q_i^1 + s_i^1 + r_i^1}{4}$$

$$\gamma_i = \frac{p_i^0 - q_i^0 - p_i^1 + q_i^1 + s_i^0 - r_i^0 - s_i^1 + r_i^1}{4}$$

$$\delta_i = \frac{p_i^0 - q_i^0 - p_i^1 + q_i^1 - s_i^0 + r_i^0 + s_i^1 - r_i^1}{4}$$

**Note:** Here the value for the  $\gamma_i$  and  $\delta_i$  in Response0 and Response1 are slightly different. So finally the Resposnel can similarly be predicted as -

$$\frac{1 + \text{sign}(\tilde{\mathbf{W}}_1^T \phi_1(\mathbf{c}) + \tilde{\mathbf{b}})}{2} = r^1(\mathbf{c})$$

Here,

$$\widetilde{W}_1 = \begin{bmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_{30} \\ \delta_1 \\ \delta_2 + \gamma_1 \\ \vdots \\ \delta_{31} + \gamma_{30} + \beta_{31} \end{bmatrix} \quad \text{and} \quad \phi_1(\widetilde{C}) = \begin{bmatrix} d_0 \\ d_1 \\ \vdots \\ d_{30} \\ d_0 d_1 \dots d_{31} \\ d_1 d_2 \dots d_{31} \\ \vdots \\ d_{31} \end{bmatrix}$$

## 4 Dimensionality of the linear models $W_0$ and $W_1$

From previous part -

$$\widetilde{W}_0 = \begin{bmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_{30} \\ \delta_1 \\ \delta_2 + \gamma_1 \\ \vdots \\ \delta_{31} + \gamma_{30} + \beta_{31} \end{bmatrix} \quad \text{and} \quad \widetilde{W}_1 = \begin{bmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_{30} \\ \delta_1 \\ \delta_2 + \gamma_1 \\ \vdots \\ \delta_{31} + \gamma_{30} + \beta_{31} \end{bmatrix}$$

**Note:** Here the  $\gamma_i$  and  $\delta_i$  for these two models are slightly different.

Clearly, both  $\widetilde{W}_0$  and  $\widetilde{W}_1$  are **63 x 1** matrices.

Hence, the dimensionality for both the  $\widetilde{W}_0$  and  $\widetilde{W}_1$  is **63 x 1**.

## 5 Code for the two linear models $W_0$ , $b_0$ , $W_1$ , $b_1$

Code Submitted



## 6 Outcomes of the Experiments

### 6.1 Training Set

The model is trained on `public.trn.txt` and tested on `public.tst.txt` with the different set of hyperparameters and their accuracy and training time is recorded.

#### a) Effect of changing the loss hyperparameter in LinearSVC

The *loss function* characterizes how well the model performs on a given dataset. `sklearn.svm.LinearSVC` provides two loss functions, namely: *hinge* and *squared hinge*.

We made the observations that are mentioned below using the hyperparameters  $C = 1$ , `tolerance = 1e-3`, `penalty = L2` and `dual = True` for `LinearSVC`.

Table 1: Loss Hyperparameters

Loss	Training Time (in seconds)	Accuracy y0	Accuracy y1
Hinge	1.87	0.9841	0.9961
Squared Hinge	5.66	0.9800	0.9979

#### b) Effect of changing the $C$ hyperparameter in LinearSVC and Logistic Regression model

Regularization is a technique used to prevent overfitting by penalizing large coefficients in the model. The  $C$  parameter represents the inverse of regularization strength, where smaller values of  $C$  correspond to stronger regularization.

In both Logistic Regression and Linear SVC, adjusting  $C$  influences how closely the model fits the training data. Increasing  $C$  tightens the fit, potentially leading to overfitting, while decreasing  $C$  encourages simpler decision boundaries, helping generalization but risking underfitting.

We made the observations that are mentioned below using the hyperparameters `loss = Squared Hinge`, `tolerance = 1e-3`, `penalty = L2` and `dual = False` for `LinearSVC` and `tolerance = 1e-3`, `penalty = L2` and `dual = False` for `Logistic Regression`:

Table 2: C Hyperparameters in LinearSVC

C value	Training Time (in seconds)	Accuracy y0	Accuracy y1
0.01	1.43	0.9799	0.9948
0.1	1.41	0.9803	0.9964
1	1.51	0.9800	0.9980
10	1.57	0.9800	0.9987
100	1.52	0.9800	0.9989

Table 3: C Hyperparameters in Logistic Regression

C value	Training Time (in seconds)	Accuracy y0	Accuracy y1
0.01	0.90	0.9800	0.9931
0.1	1.02	0.9805	0.9956
1	1.01	0.9806	0.9970
10	1.03	0.9808	0.9981
100	1.02	0.9808	0.9990

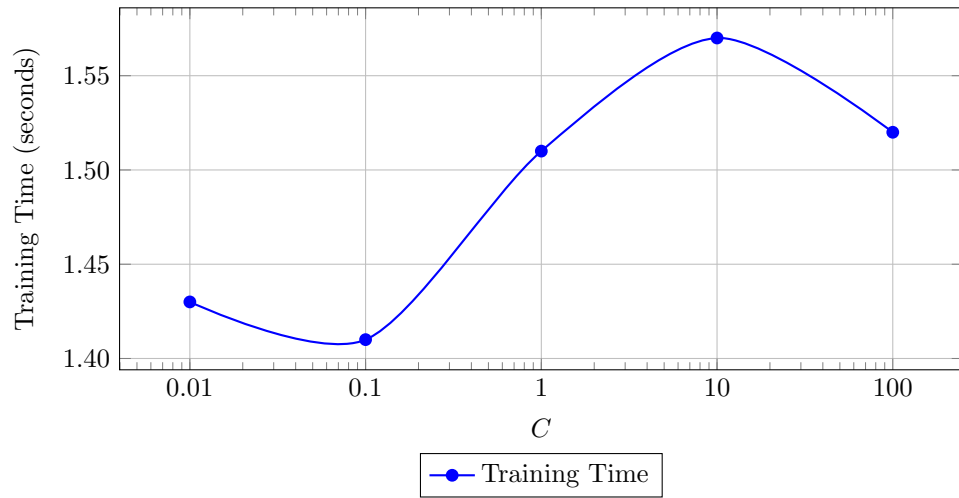


Figure 3: Training Time vs  $C$  for LinearSVC

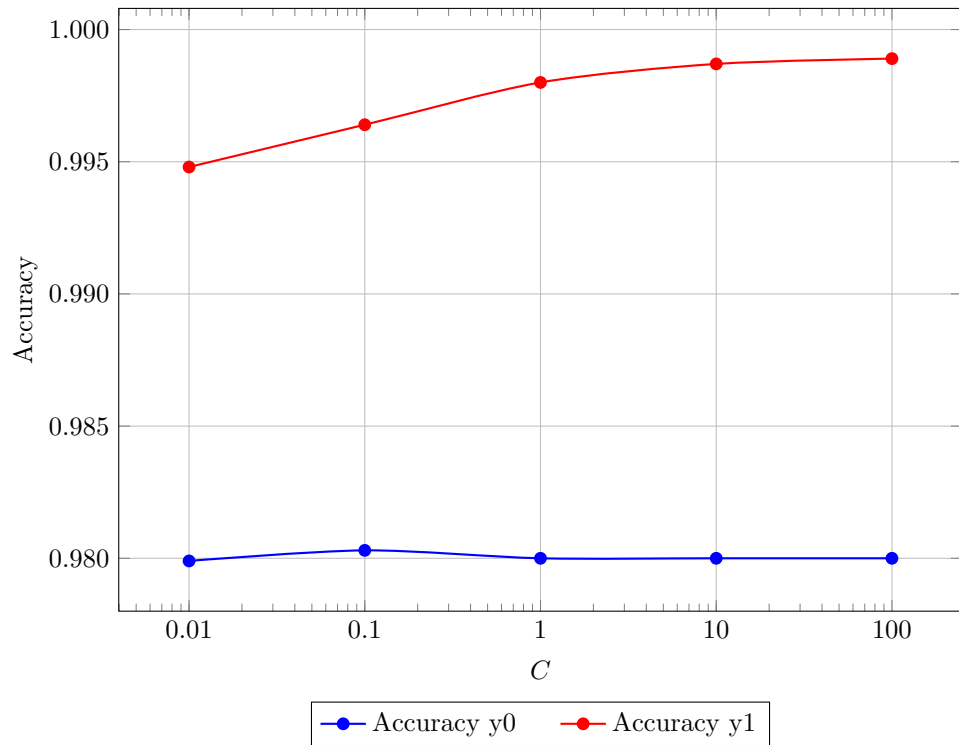


Figure 4: Accuracy vs  $C$  for LinearSVC

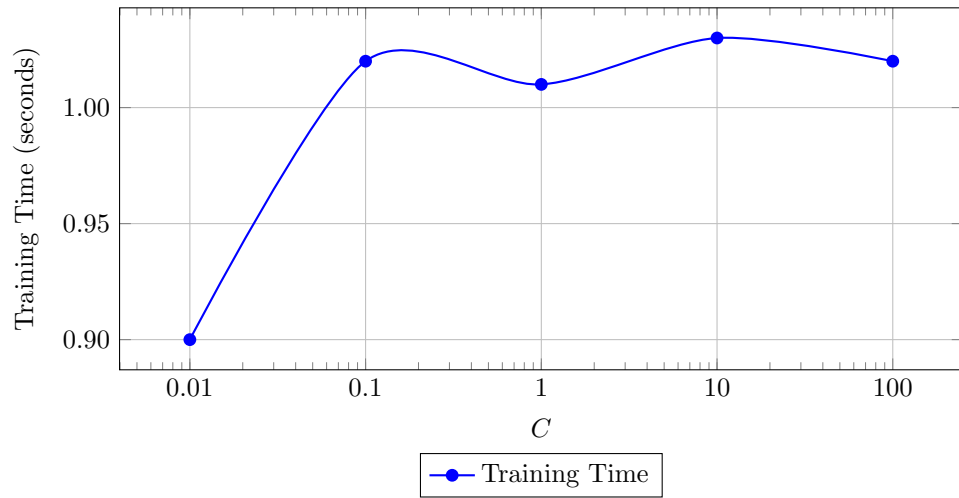


Figure 5: Training Time vs  $C$  for Logistic Regression

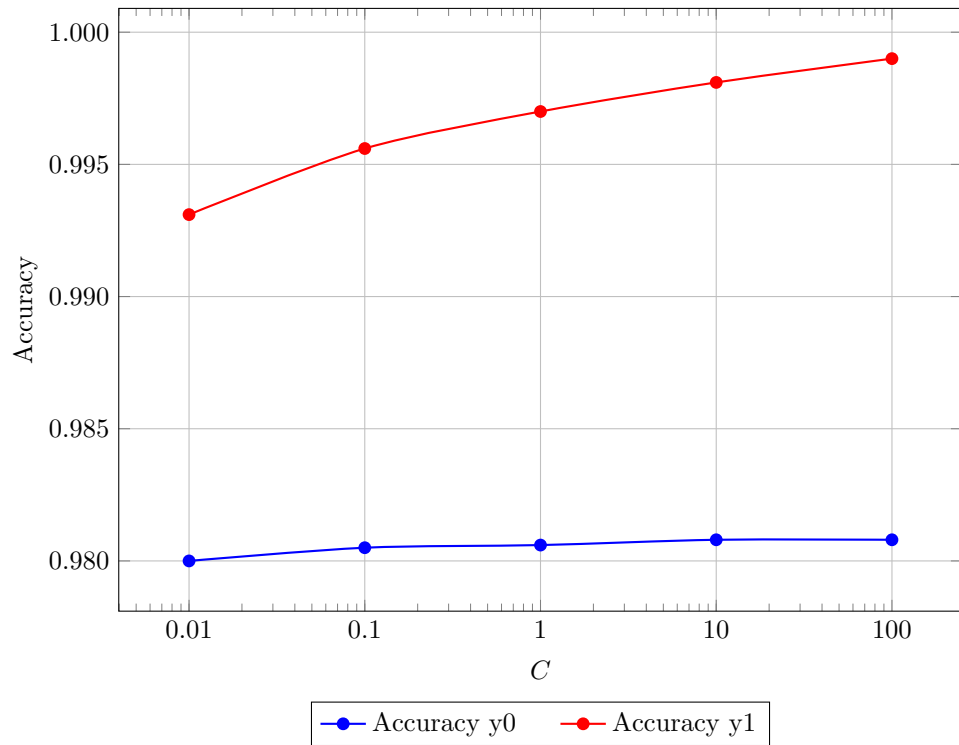


Figure 6: Accuracy vs  $C$  for Logistic Regression

### c) Effect of changing the *tol* hyperparameter in LinearSVC and Logistic Regression model

The *tol* hyperparameter, representing tolerance, sets the convergence threshold for optimization algorithms in *LinearSVC* and *LogisticRegression*. It determines when the iterative optimization process stops by measuring the change in the objective function or coefficients between iterations. A smaller *tol* implies stricter convergence criteria, prolonging training but potentially improving accuracy. Conversely, a larger *tol* speeds up training but might compromise precision. Balancing computational efficiency and model accuracy hinges on selecting an appropriate *tol* value.

We made the observations that are mentioned below using the hyperparameters `loss = Squared Hinge`, `C=10`, `penalty = L2` and `dual = False` for **LinearSVC** and `C=100`, `penalty = L2`, `solver = 'lbfgs'` and `dual = False` for **Logistic Regression**:

Table 4: *tol* Hyperparameters in LinearSVC

tol value	Training Time (in seconds)	Accuracy y0	Accuracy y1
$10^{-1}$	1.28	0.9800	0.9923
$10^{-2}$	1.45	0.9800	0.9961
$10^{-3}$	1.34	0.9800	0.9987
$10^{-4}$	1.49	0.9800	0.9987
$10^{-5}$	1.51	0.9800	0.9989

Table 5: *tol* Hyperparameters in Logistic Regression

C value	Training Time (in seconds)	Accuracy y0	Accuracy y1
$10^{-1}$	1.39	0.9808	0.9990
$10^{-2}$	1.20	0.9808	0.9990
$10^{-3}$	1.18	0.9808	0.9990
$10^{-4}$	0.99	0.9808	0.9990
$10^{-5}$	1.01	0.9808	0.9990

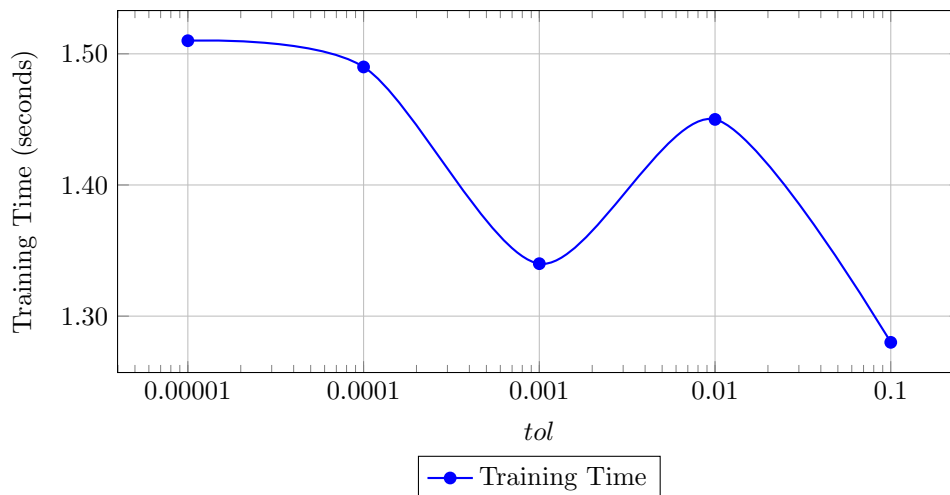


Figure 7: Training Time vs *tol* for LinearSVC

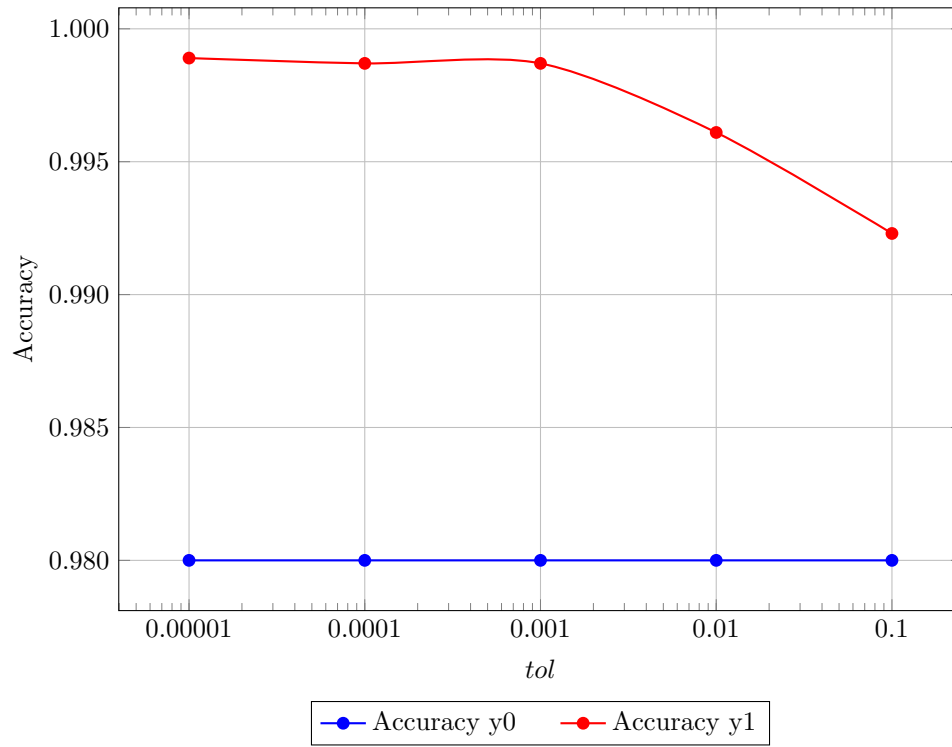


Figure 8: Accuracy vs  $tol$  for LinearSVC

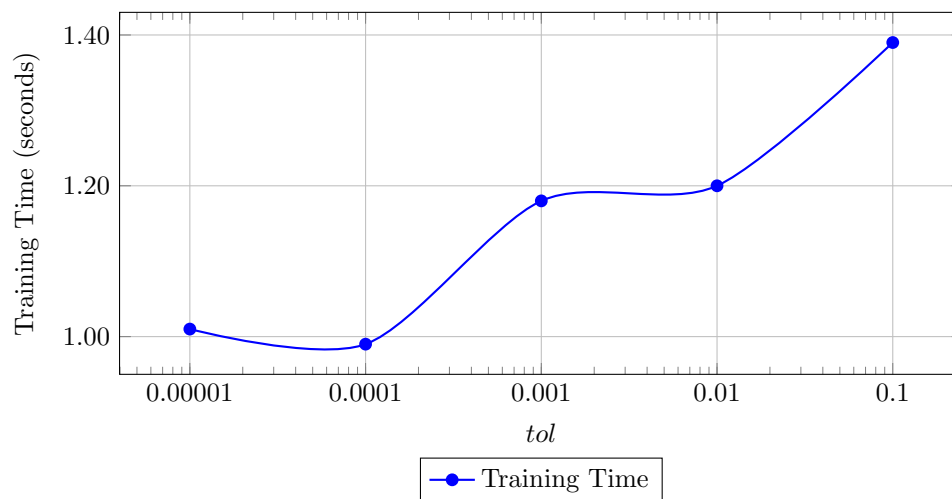


Figure 9: Training Time vs  $tol$  for Logistic Regression

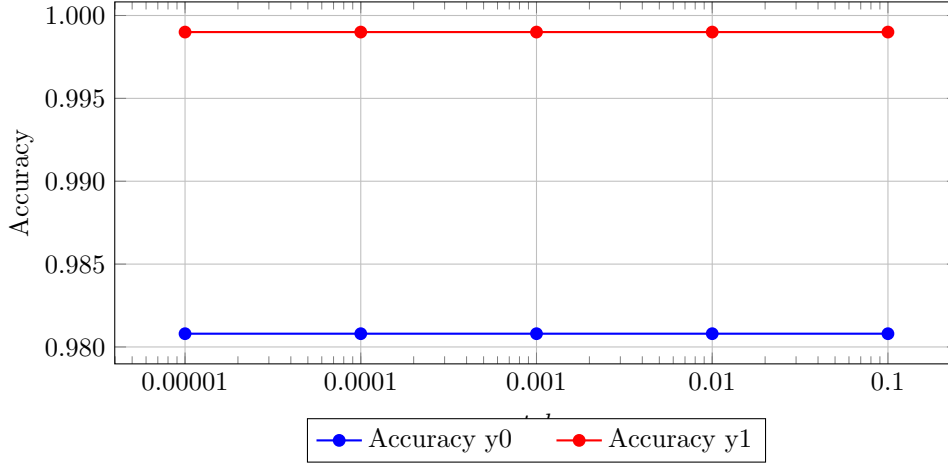


Figure 10: Accuracy vs  $tol$  for Logistic Regression

#### d) Effect of changing the *penalty* hyperparameter in LinearSVC and Logistic Regression model

In **Logistic regression**, the *penalty* hyperparameter determines regularization type ('l1' or 'l2'). 'l1' penalizes absolute coefficient values, promoting sparsity, while 'l2' penalizes squared coefficients, leading to smoother boundaries. Adjusting this hyperparameter controls overfitting, fostering simpler models for improved generalization.

In **LinearSVC**, the *penalty* hyperparameter controls regularization ('l1' or 'l2'). 'l1' induces sparsity by penalizing absolute coefficients, resulting in sparse solutions. 'l2' penalizes squared coefficients, promoting smaller values and smoother boundaries. Adjusting this hyperparameter regulates model complexity, mitigating overfitting and enhancing generalization to new data.

We made the observations that are mentioned below using the hyperparameters `loss = Squared Hinge`, `C=1`, `tolerance = 1e-3` and `dual = False` for **LinearSVC** and `C=100`, `tolerance = 1e-3`, `dual = False` for **Logistic Regression**:

Table 6: Penalty Hyperparameters in LinearSVC

Penalty	Training Time (in seconds)	Accuracy y0	Accuracy y1
L1	17.68	0.9801	0.9979
L2	1.53	0.9800	0.9980

Table 7: Penalty Hyperparameters in Logistic Regression

Solver	Penalty	Training Time (in seconds)	Accuracy y0	Accuracy y1
liblinear	L1	18.12	0.9808	0.9982
lbfgs	L2	1.25	0.9808	0.9990

The **liblinear** solver was used with the L1 penalty. For the L2 penalty, **lbfgs**, the default solver was used. Since in L1 penalty does not allow using **lbfgs** solver.