

Intelligence Program 2017

Code Test (HCMC)

1> Generate 100 samples in class 0 (blue color) and 360 samples in class 1 (red color) as figure 1.

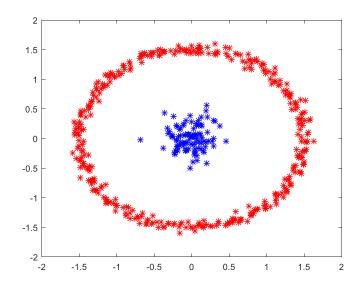


Figure 1: Simulation data

2> Denote x_i is the ith sample that we have generated; compute the matrix W as:

$$W_{ij} = exp\left(-\frac{\|x_i - x_j\|^2}{\sigma^2}\right), \sigma = 0.3$$

- 3> Compute a diagonal matrix D that $D_{ii} = \sum_{j} W_{ij}$
- 4> Compute matrix L = D W;
- 5> Compute matrix $L_{rw} = D^{-1}L = I D^{-1}W$ where I is identity matrix
- 6> Compute eigenvalue and eigenvector of L_{rw}
- 7> Sorts the elements of eigenvalue in ascending order
- 8> Create a matrix Y_{460*3} that :
 - a. First column of Y is the eigenvector with the smallest eigenvalue
 - b. Second column of Y is the eigenvector with the second eigenvalue
 - c. Third column of Y is the eigenvector with the third eigenvalue

- 9> Display the second and the third column of Y on a 2D plane. Each row presents one point.
- 10> Explain the purpose of the code? In your opinion, how the code helps with machine learning problems?

Solution:

HCM test:

