

9.  $\delta(A, x) = B$  iff  $w$  has an odd # of '1's because

- Reason: The induction hyp. states that if  $x$  has an odd # of '1', we're in  $B$
- (A)

10.  $\delta(A, w) = B$  iff  $w$  has an odd # of '1' because

- Reason: Given  $\delta(A, x) = B \wedge w = x0$ , the transition function keeps us in  $B$  on input '0'
- (B)

4. (a) Start with a DFA for regular language since every regular language can be represented by a DFA

2. Transform the DFA  $\rightarrow \epsilon$ -NFA by

- Adding new start state with a single  $\epsilon$ -transition to the original start state
- for each state, ensure that for each input symbol, there is only 1 transition out of that state. If a state has  $> 1$  transitions for the same input, introduce intermediate states w/  $\epsilon$ -transitions to separate these transitions
- If there are multiple accept states, add  $\epsilon$ -transitions from each to a new, single acceptor

(b) 1. from a DFA of regular lang., create a chain of states in the  $\epsilon$ -NFA where each state has an  $\epsilon$ -tran. to the next state

2. At each state, include 1 non- $\epsilon$ -tran that corresponds to the transition in the DFA for the current input symbol

3. When the DFA would transition to a new state on an input symbol, the  $\epsilon$ -NFA transitions on that symbol to a new state in the chain, which then  $\epsilon$ -transitions to the next state in the sequence, simulating DFA's computation

4. The accept states of the DFA correspond to states in the  $\epsilon$ -NFA chain that will  $\epsilon$ -tran to a new accepting state

5. b.  $(011)^* 1 (011)^* \{g\} \$$

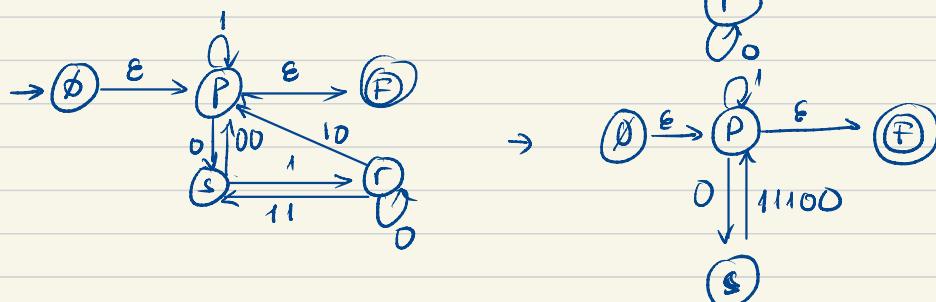
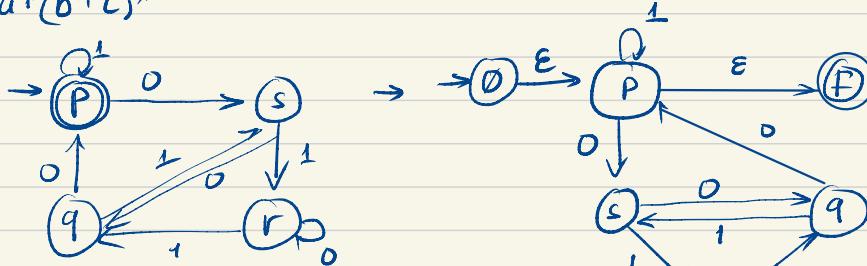
c.  $^*(0^* 1 0^* 1)^* 0^* \$$

6. a.  $^* 0^* 1 0^* 1 0^* 1^* \$$

b.  $^*(1^* 0 1^* 0 1^* 0 1^* 0 1^*)^* \$$

f.  $a^* (b+c)^*$

8.



$1 + 0((0+10^* 1)1)^* (0+10^* 1)0$   
answer