

Q1

$$(a) \quad a^n b^m \quad n \geq 4, m \leq 3$$

$$(aaaa)a^*(\lambda + b + bb + bbb)$$

$$(b) \quad a^n b^m \quad (n+m) \text{ is even}$$

$$(aa)^*a(bb)^*b + (aa)^*(bb)^*$$

$$(c) \quad a^n b^m, n \geq 3, m \text{ is even}$$

$$(aaaa)a^*(bb)^*$$

$$(d) \quad a^n b^m \quad n < 4, m \leq 3$$

$$(\lambda + a + aa + aaa)(\lambda + b + bb + bbb)$$

$$(e) \quad ab^nw : n \geq 3, w \in \{a, b\}^+$$

$$a(bbb)b^*(a+b)(a+b)^*$$

$$(f) \quad vwv : v, w \in \{a, b\}^*, |v| \geq 2$$

$$(a+b)^*$$

$$(g) \quad w \in (0, 1)^*$$

~~$$(01)^* (011)^*$$~~

~~$$1^* (011)^* 00 (110)^* 1^*$$~~

$$(1+01)^* 00 (1+10)^*$$

(h) Complement of $a^{2n} b^{2m+1}$, $n \geq 0, m \geq 0$

~~$$a^2 b, a^4 b, a^6 b, \dots, b, b^3, b^5, \dots$$~~

~~$$a^2 b, a^4 b, a^6 b$$~~

even powers of a and odd powers of b
complement \rightarrow ~~odd powers of a & even powers of b~~

$$a^{2n} b^{2m}, m \geq 0, n \geq 0 \cup a^{2n+1} b^{2m}, m \geq 0, n \geq 0$$

$$\epsilon, a^2, a^4, a^6, \dots, b^2, b^4, b^6, \dots, a^2 b^2 \cup a, a^3, a^5, \dots, a b^2$$

~~$$a^n b^{2m}$$~~
$$n \geq 0, m \geq 0$$

$$(a)^* (bb)^*$$

(i) Complement of $L = a^n b^m$ $n \geq 4$ $m \leq 3$

$\hookrightarrow L = a^n b^m$ ~~$n \leq 4$~~ $m > 3$

$(\epsilon + a + aa + aaa) (bbbb) b^*$

(j) Complement of $L = a^n b^m$ $n < 4$ $m \leq 3$

$\hookrightarrow L = a^n b^m$ $n \geq 4$ $m > 3$

$(aaaa) a^* (bbbb) b^*$

Q2 $\Sigma = \{a, b, c\}$

(a) $(b+c)^* a (b+c)^*$

(b) $(b+c)^* (a+\epsilon) (b+c)^* (a+\epsilon) (b+c)^* (a+\epsilon) (b+c)^*$

(c)

(d) $(b+c)^* + (b+c)^* ((a+aa)(b+c)^+)^* (a+aa)$
 $(b+c)^*$

$$(e) \quad (b+c)^* ((aaa)(b+c)^*)^*$$

(c) possible orders

$$abc + acb + bac + bca + cab + cba$$

$$X = (a+b+c)^*$$

ans \Rightarrow

$$XaXbXcX + XaXcXbX + XbXaXcX + XbXcXaX + XcXaXbX + XcXbXaX$$

$$(d) \quad (b+c)^* (a+aa)(b+c)^*$$

$$(b+c)(b+c)^* (a+aa)(b+c)^*$$

$$(e) \quad (aaa+b+c)^*$$

$$\mathbb{Q}_2 \leq = \{0, 1\}$$

$$(a) \quad (0+1)^* 01$$

$$(b) \quad (0+1)^* 0 + (0+1)^* 11 + \cancel{10} + 1$$

$$(c) \quad 1^* + (1^* 01^* 0)^* 1^*$$

$$(d) (1+b)^* 00(1+b)^* 00(1+b)^* + (1+b)^* 000(1+b)^*$$

(e) 3 cases
 \rightarrow 0 occurrence, 1 occurrence, 2 occurrence

$$(1+b)^*(1+00+000+0011^*00)(1+b)^*$$

$$(f) 0^*(1^*000^*)^*1^*0^*$$

$$\underline{Q4} \leq \{a, b\}$$

$$(a) w: |w| \bmod 3 = 0$$

$$((a+b)(a+b)(a+b))^*$$

$$(b) w: h_a(w) \bmod 3 = 0$$

$$b^* + (ab^*ab^*ab^*)^*$$

$$(c) w: h_a(w) \bmod 5 > 0$$

$$\left[(b^* a b^*) + (b^* a b^* a b^*) + (b^* a b^* a b^* a b^*) + (b^* a b^* a b^* a b^* a b^*) \right]^* + \text{}$$

$$[b + (a b^* a b^* a b^* a b^* a)]^*$$

$$\Sigma = (a, b, c)$$

$$(a) ((a+b+c)(a+b+c)(a+b+c))^*$$

$$(b) (b+c)^* + (a(b+c)^* a(b+c)^* a(b+c)^*)^*$$

$$(c) \left[((b+c)^* a (b+c)^*) + ((b+c)^* a (b+c)^* a (b+c)^*) + ((b+c)^* a (b+c)^* a (b+c)^* a (b+c)^*) + ((b+c)^* a (b+c)^* a (b+c)^* a (b+c)^* a (b+c)^*) \right]^* +$$

$$[(b+c) + (a(b+c)^* a(b+c)^* a(b+c)^* a(b+c)^* a)]^*$$