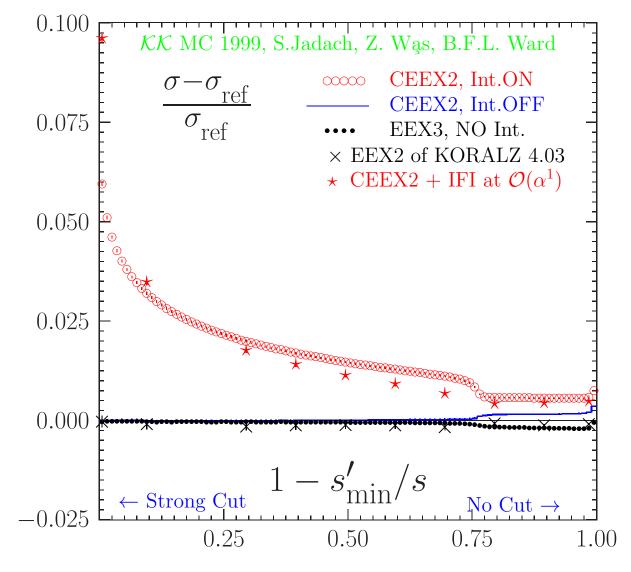
#### CEEX $\sigma$ and $A_{\rm FB}$ , energy cut-off study

$v_{ m max}$	$\mathcal{KK}$ sem Refer.	$\mathcal{O}(lpha^3)_{ ext{EEX}3}$	$\mathcal{O}(\alpha^2)_{\text{CEEX}}$ intOFF	$\mathcal{O}(lpha^2)_{ ext{CEEX}}$	KORALZ	KORALZ Interf.
	$\sigma(v_{ m max})~{ m [pb]}$					
0.01	$1.6712 \pm 0.0000$	$1.6708 \pm 0.0006$	$1.6710 \pm 0.0006$	$1.7707 \pm 0.0007$	$0.9639 \pm 0.0009$	$0.1610 \pm 0.0000$
0.10	$2.5198 \pm 0.0000$	$2.5191 \pm 0.0006$	$2.5196 \pm 0.0006$	$2.6004 \pm 0.0008$	$2.1919 \pm 0.0010$	$0.0880 \pm 0.0000$
0.30	$3.0616 \pm 0.0000$	$3.0605 \pm 0.0007$	$3.0613 \pm 0.0007$	$3.1226 \pm 0.0008$	$2.7690 \pm 0.0010$	$0.0545 \pm 0.0000$
0.50	$3.3747 \pm 0.0000$	$3.3731 \pm 0.0007$	$3.3747 \pm 0.0007$	$3.4242 \pm 0.0008$	$3.0565 \pm 0.0010$	$0.0385 \pm 0.0000$
0.70	$3.7223 \pm 0.0000$	$3.7198 \pm 0.0007$	$3.7232 \pm 0.0007$	$3.7637 \pm 0.0008$	$3.3649 \pm 0.0010$	$0.0246 \pm 0.0000$
0.90	$7.1430 \pm 0.0000$	$7.1294 \pm 0.0007$	$7.1542 \pm 0.0007$	$7.1833 \pm 0.0008$	$6.3558 \pm 0.0010$	$0.0210 \pm 0.0000$
0.99	$7.6135 \pm 0.0000$	$7.5986 \pm 0.0007$	$7.6292 \pm 0.0007$	$7.6579 \pm 0.0008$	$6.7004 \pm 0.0010$	$0.0213 \pm 0.0000$
	$A_{ m FB}(v_{ m max})$					
0.01	$0.5654 \pm 0.0000$	$0.5654 \pm 0.0004$	$0.5654 \pm 0.0004$	$0.6118 \pm 0.0004$	$0.5765 \pm 0.0013$	$0.1201 \pm 0.0000$
0.10	$0.5664 \pm 0.0000$	$0.5666 \pm 0.0003$	$0.5666 \pm 0.0003$	$0.5930 \pm 0.0003$	$0.5784 \pm 0.0006$	$0.0324 \pm 0.0000$
0.30	$0.5692 \pm 0.0000$	$0.5693 \pm 0.0003$	$0.5692 \pm 0.0003$	$0.5863 \pm 0.0003$	$0.5818 \pm 0.0005$	$0.0164 \pm 0.0000$
0.50	$0.5744 \pm 0.0000$	$0.5743 \pm 0.0002$	$0.5742 \pm 0.0002$	$0.5870 \pm 0.0003$	$0.5868 \pm 0.0005$	$0.0112 \pm 0.0000$
0.70	$0.5863 \pm 0.0000$	$0.5857 \pm 0.0002$	$0.5857 \pm 0.0002$	$0.5953 \pm 0.0003$	$0.5972 \pm 0.0004$	$0.0078 \pm 0.0000$
0.90	$0.3105 \pm 0.0000$	$0.3105 \pm 0.0001$	$0.3098 \pm 0.0001$	$0.3174 \pm 0.0001$	$0.3260 \pm 0.0002$	$0.0037 \pm 0.0000$
0.99	$0.2851 \pm 0.0000$	$0.2855 \pm 0.0001$	$0.2846 \pm 0.0001$	$0.2917 \pm 0.0001$	$0.3039 \pm 0.0002$	$0.0024 \pm 0.0000$

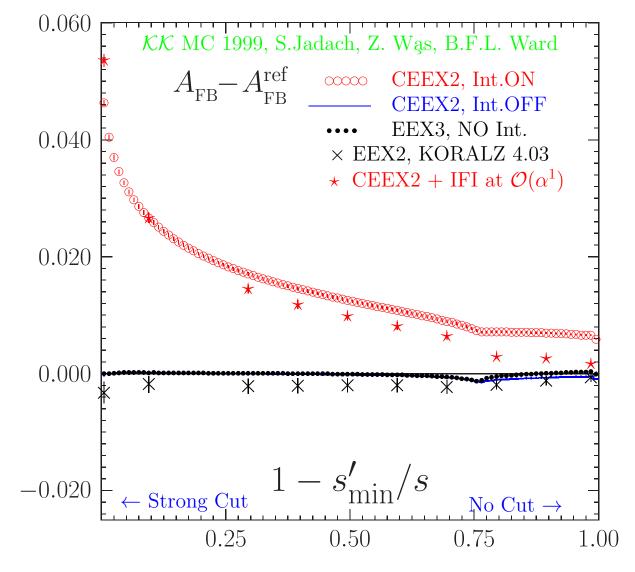
Process:  $e^-e^+ \to f\bar{f}$ ,  $f = \mu^-$ , at 189GeV. Energy cut:  $v < v_{\rm max}$ , where  $v = 1 - M_{f\bar{f}}^2/s$ . Scattering angle for  $A_{\rm FB}$  is  $\theta = \theta^{\bullet}$ . No cut in  $\theta^{\bullet}$ . E-W corr. in  $\mathcal{KK}$  according to DIZET 6.x.  $\mathcal{O}(\alpha^3)_{\rm LL}$  EEX3 matrix element in  $\mathcal{KK}$  (without ISR\*FSR interf.)  $\mathcal{KK}$ sem is semianalytical part of  $\mathcal{KK}$ . (Angle  $\theta^{\bullet}$  is from Phys. Rev. **D41**, 1425 (1990).)

# Total cross section $\sigma$ , energy cut-off stydy



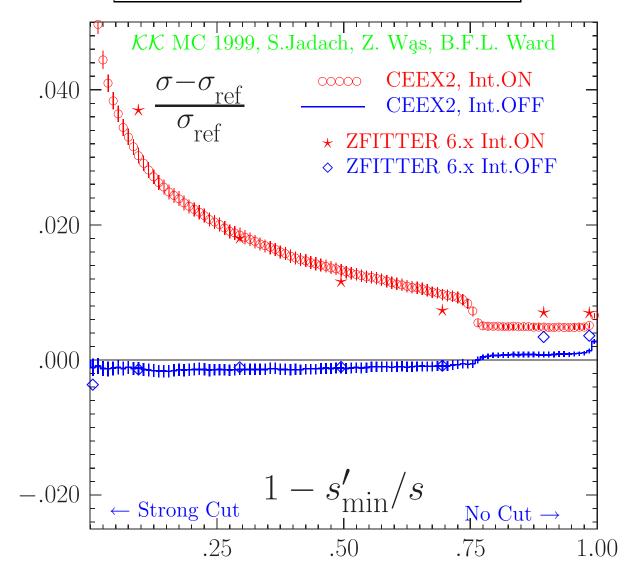
The same as in the table. The ISR $\otimes$ FSR interf. switched on/off wherever possible. No cut in  $\theta^{\bullet}$ . Reference  $\sigma_{\text{ref}} = \text{semianalytical of } \mathcal{KK}\text{sem}$ , (no ISR $\otimes$ FSR, up to  $\mathcal{O}(\alpha^3)_{\text{LL}}$ , JSW exponentiation). EEX2 data points from KORALZ/YFS3 version 4.03 (QED up to  $\mathcal{O}(\alpha^2)_{\text{LL}}$ , ISR $\otimes$ FSR off).

## Charge asymmetry $A_{FB}$ , energy cut-off study



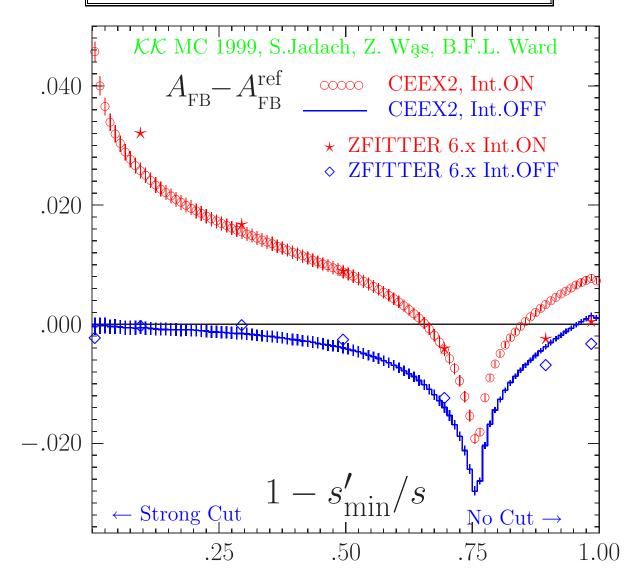
The same as in the table. The ISR $\otimes$ FSR interf. switched on/off wherever possible. No cut in  $\theta^{\bullet}$ . Reference  $A_{\rm FB}^{\rm ref}$  = semianalytical  $\mathcal{KK}$ sem, (no ISR $\otimes$ FSR, up to  $\mathcal{O}(\alpha^3)_{\rm LL}$ , JSW exponentiation). EEX2 data points are from KORALZ/YFS3 version 4.03 (QED up to  $\mathcal{O}(\alpha^2)_{\rm LL}$ , ISR $\otimes$ FSR off.).

#### Total x-section $\sigma$ , comparison with Zfitter



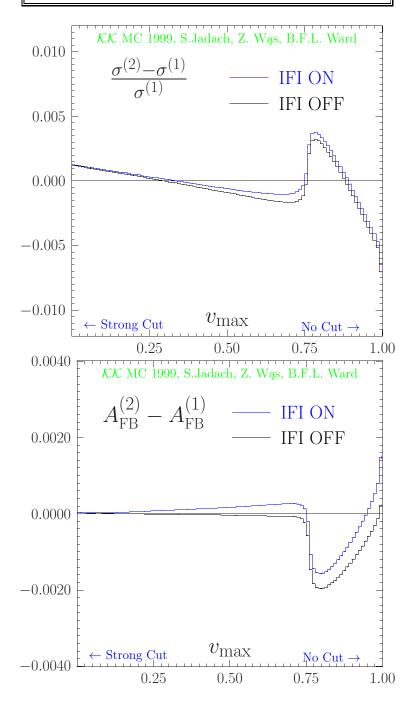
Comparison with Zfitter 6.xx. The ISR $\otimes$ FSR interf. switched on/off. No cut in  $\theta_1$ . Reference  $\sigma_{ref}$  = semianalytical of  $\mathcal{KK}$ sem, (no ISR $\otimes$ FSR, up to  $\mathcal{O}(\alpha^3)_{LL}$ , JSW exponentiation).

#### Charge asymmetry $A_{\rm FB}$ , comparison with Zfitter



Comparison with Zfitter 6.xx. The ISR $\otimes$ FSR interf. switched on/off. No cut in  $\theta_1$ . Reference  $A_{\rm FB}^{\rm ref}$  = semianalytical  $\mathcal{KK}$ sem, (no ISR $\otimes$ FSR, up to  $\mathcal{O}(\alpha^3)_{\rm LL}$ , JSW exponentiation).

### Physical Precision of CEEX, NEW!!!



The difference between second and first order CEEX results for at 189GeV. The energy cut is on s'/s, where  $s'=m_{f\bar{f}}^2$ .

Scattering angle is  $\theta = \theta^{\bullet}$ . [Angle  $\theta^{\bullet}$  is defined in Phys. Rev. **D41**, 1425 (1990)]