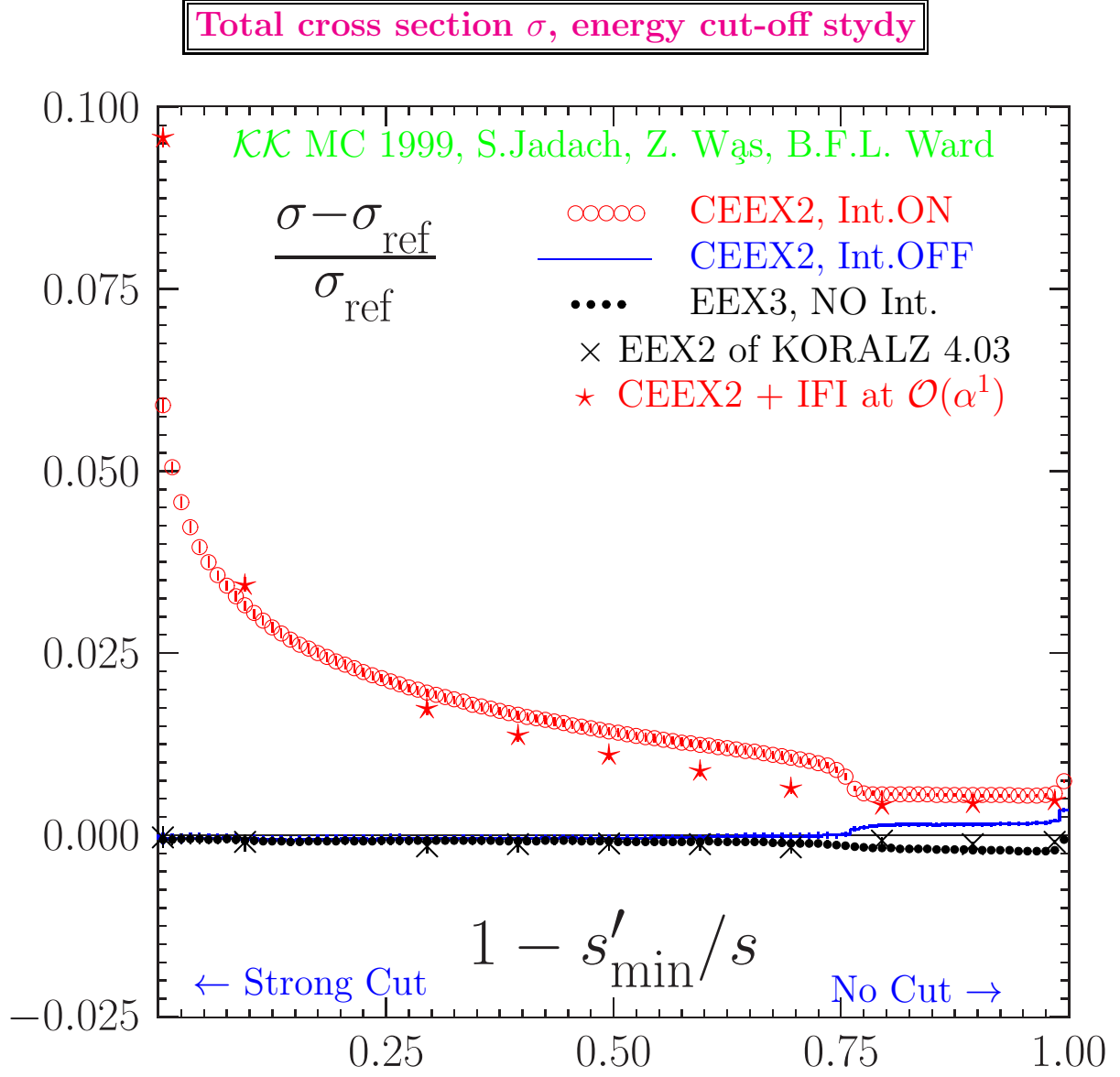


**CEEX  $\sigma$  and  $A_{\text{FB}}$ , energy cut-off study**

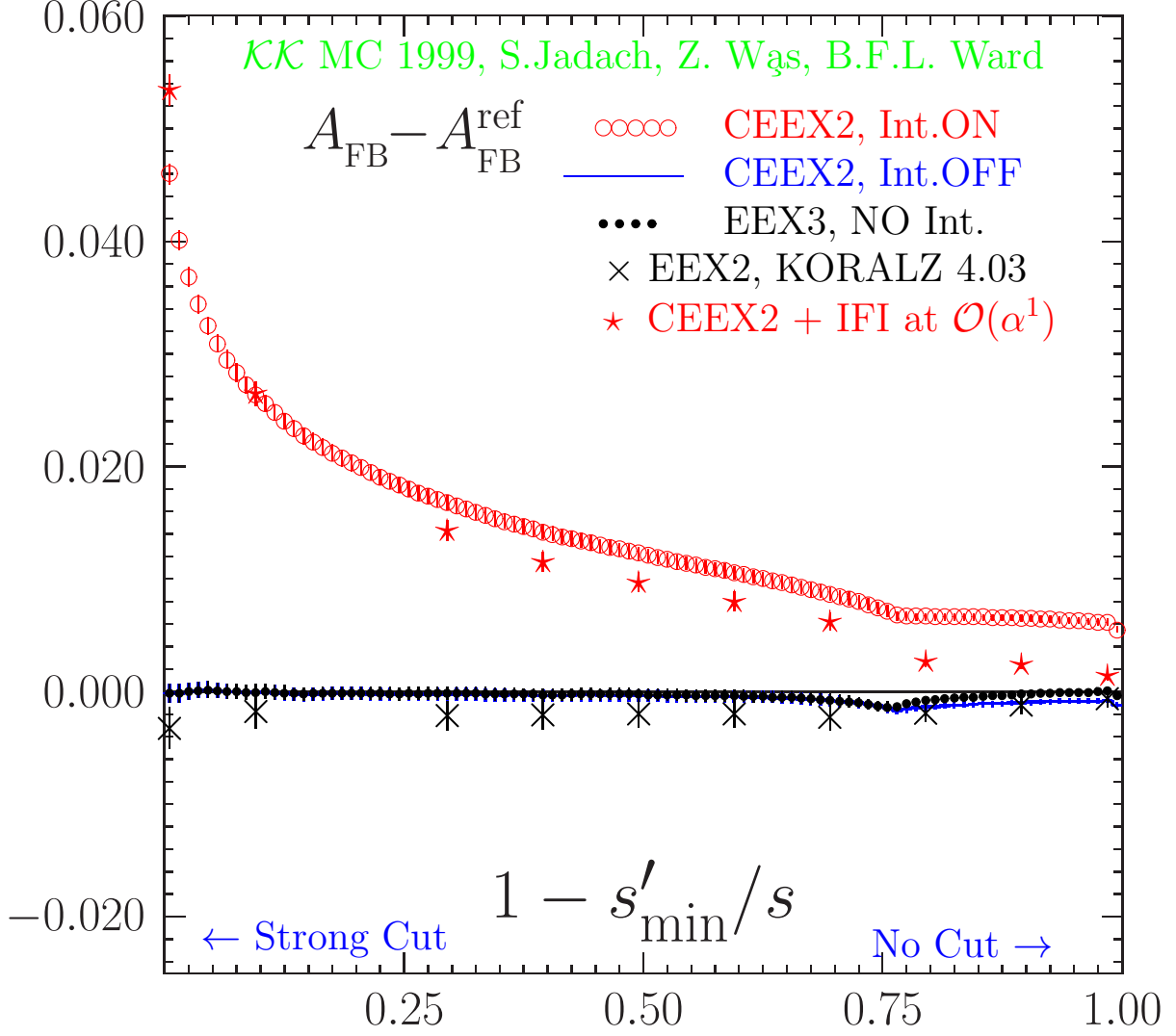
$v_{\text{max}}$	$\mathcal{KK}\text{sem}$ Refer.	$\mathcal{O}(\alpha^3)_{\text{EEX3}}$	$\mathcal{O}(\alpha^2)_{\text{CEEX}}$ intOFF	$\mathcal{O}(\alpha^2)_{\text{CEEX}}$	KORALZ	KORALZ Interf.
	$\sigma(v_{\text{max}})$ [pb]					
0.01	$1.6712 \pm 0.0000$	$1.6701 \pm 0.0012$	$1.6704 \pm 0.0012$	$1.7699 \pm 0.0014$	$0.9639 \pm 0.0009$	$0.1610 \pm 0.0000$
0.10	$2.5198 \pm 0.0000$	$2.5180 \pm 0.0013$	$2.5185 \pm 0.0013$	$2.5992 \pm 0.0016$	$2.1919 \pm 0.0010$	$0.0880 \pm 0.0000$
0.30	$3.0616 \pm 0.0000$	$3.0594 \pm 0.0014$	$3.0603 \pm 0.0014$	$3.1217 \pm 0.0017$	$2.7690 \pm 0.0010$	$0.0545 \pm 0.0000$
0.50	$3.3747 \pm 0.0000$	$3.3717 \pm 0.0014$	$3.3734 \pm 0.0014$	$3.4228 \pm 0.0017$	$3.0565 \pm 0.0010$	$0.0385 \pm 0.0000$
0.70	$3.7223 \pm 0.0000$	$3.7182 \pm 0.0015$	$3.7217 \pm 0.0015$	$3.7618 \pm 0.0018$	$3.3649 \pm 0.0010$	$0.0246 \pm 0.0000$
0.90	$7.1430 \pm 0.0000$	$7.1285 \pm 0.0014$	$7.1533 \pm 0.0014$	$7.1822 \pm 0.0017$	$6.3558 \pm 0.0010$	$0.0210 \pm 0.0000$
0.99	$7.6135 \pm 0.0000$	$7.5979 \pm 0.0014$	$7.6285 \pm 0.0014$	$7.6570 \pm 0.0017$	$6.7004 \pm 0.0010$	$0.0213 \pm 0.0000$
	$A_{\text{FB}}(v_{\text{max}})$					
0.01	$0.5654 \pm 0.0000$	$0.5653 \pm 0.0008$	$0.5653 \pm 0.0008$	$0.6115 \pm 0.0009$	$0.5765 \pm 0.0013$	$0.1201 \pm 0.0000$
0.10	$0.5664 \pm 0.0000$	$0.5664 \pm 0.0006$	$0.5663 \pm 0.0006$	$0.5928 \pm 0.0007$	$0.5784 \pm 0.0006$	$0.0324 \pm 0.0000$
0.30	$0.5692 \pm 0.0000$	$0.5691 \pm 0.0005$	$0.5690 \pm 0.0005$	$0.5860 \pm 0.0006$	$0.5818 \pm 0.0005$	$0.0164 \pm 0.0000$
0.50	$0.5744 \pm 0.0000$	$0.5742 \pm 0.0005$	$0.5741 \pm 0.0005$	$0.5867 \pm 0.0006$	$0.5868 \pm 0.0005$	$0.0112 \pm 0.0000$
0.70	$0.5863 \pm 0.0000$	$0.5856 \pm 0.0005$	$0.5855 \pm 0.0005$	$0.5950 \pm 0.0006$	$0.5972 \pm 0.0004$	$0.0078 \pm 0.0000$
0.90	$0.3105 \pm 0.0000$	$0.3102 \pm 0.0002$	$0.3095 \pm 0.0002$	$0.3170 \pm 0.0003$	$0.3260 \pm 0.0002$	$0.0037 \pm 0.0000$
0.99	$0.2851 \pm 0.0000$	$0.2852 \pm 0.0002$	$0.2843 \pm 0.0002$	$0.2913 \pm 0.0003$	$0.3039 \pm 0.0002$	$0.0024 \pm 0.0000$

Process:  $e^-e^+ \rightarrow f\bar{f}$ ,  $f = \mu^-$ , at 189GeV. Energy cut:  $v < v_{\text{max}}$ , where  $v = 1 - M_{f\bar{f}}^2/s$ . Scattering angle for  $A_{\text{FB}}$  is  $\theta = \theta^\bullet$ . No cut in  $\theta^\bullet$ . E-W corr. in  $\mathcal{KK}$  according to DIZET 6.x.  $\mathcal{O}(\alpha^3)_{\text{LL}}$  EEX3 matrix element in  $\mathcal{KK}$  (without ISR\*FSR interf.)  $\mathcal{KK}\text{sem}$  is semianalytical part of  $\mathcal{KK}$ . (Angle  $\theta^\bullet$  is from Phys. Rev. **D41**, 1425 (1990).)

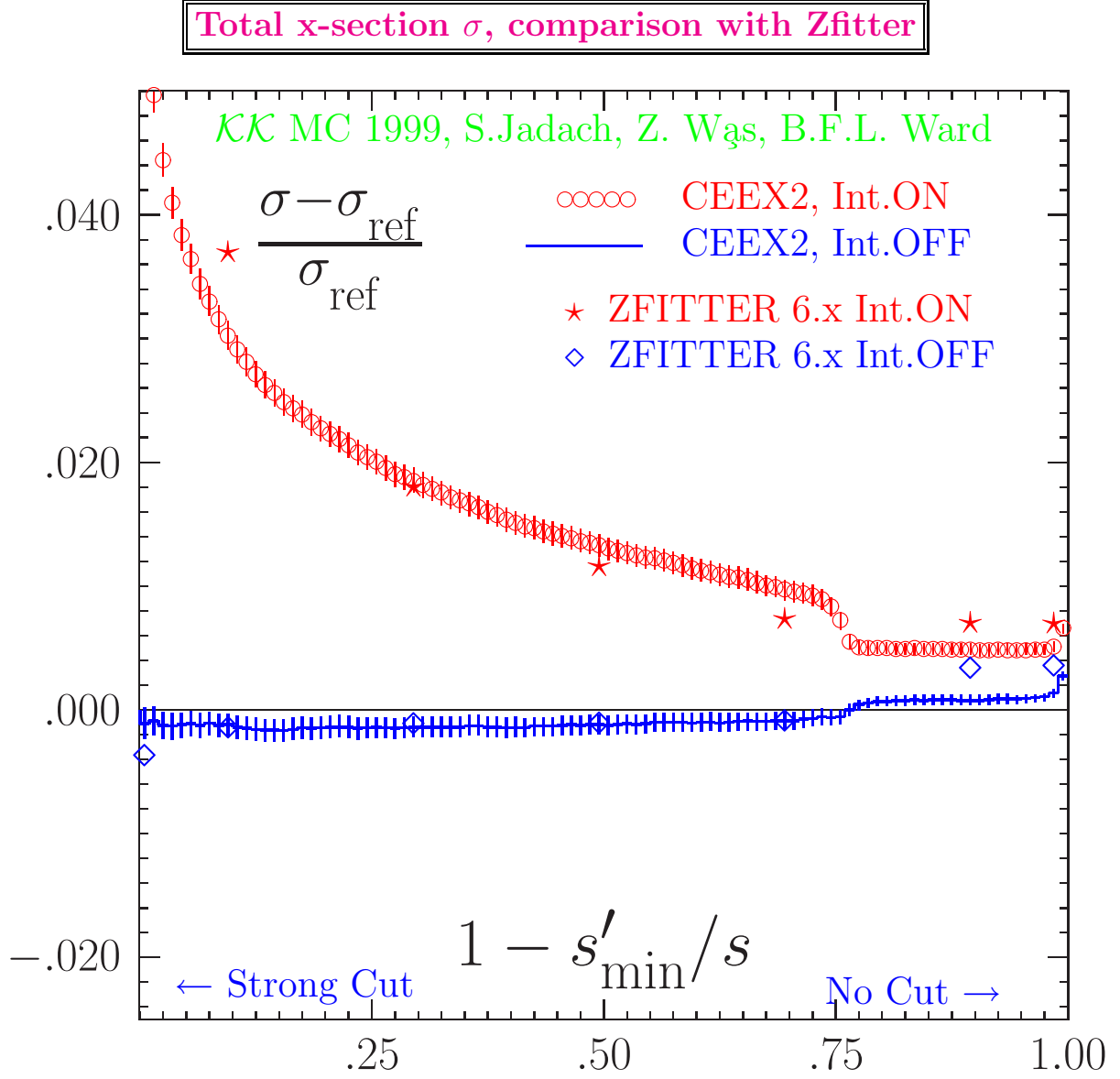


The same as in the table. The ISR $\otimes$ FSR interf. switched on/off whenever possible. No cut in  $\theta^\bullet$ . Reference  $\sigma_{\text{ref}}$  = semianalytical of  $\mathcal{K}\mathcal{K}\text{sem}$ , (no ISR $\otimes$ FSR, up to  $\mathcal{O}(\alpha^3)_{\text{LL}}$ , JSW exponentiation). EEX2 data points from KORALZ/YFS3 version 4.03 (QED up to  $\mathcal{O}(\alpha^2)_{\text{LL}}$ , ISR $\otimes$ FSR off).

# Charge asymmetry $A_{\text{FB}}$ , energy cut-off study

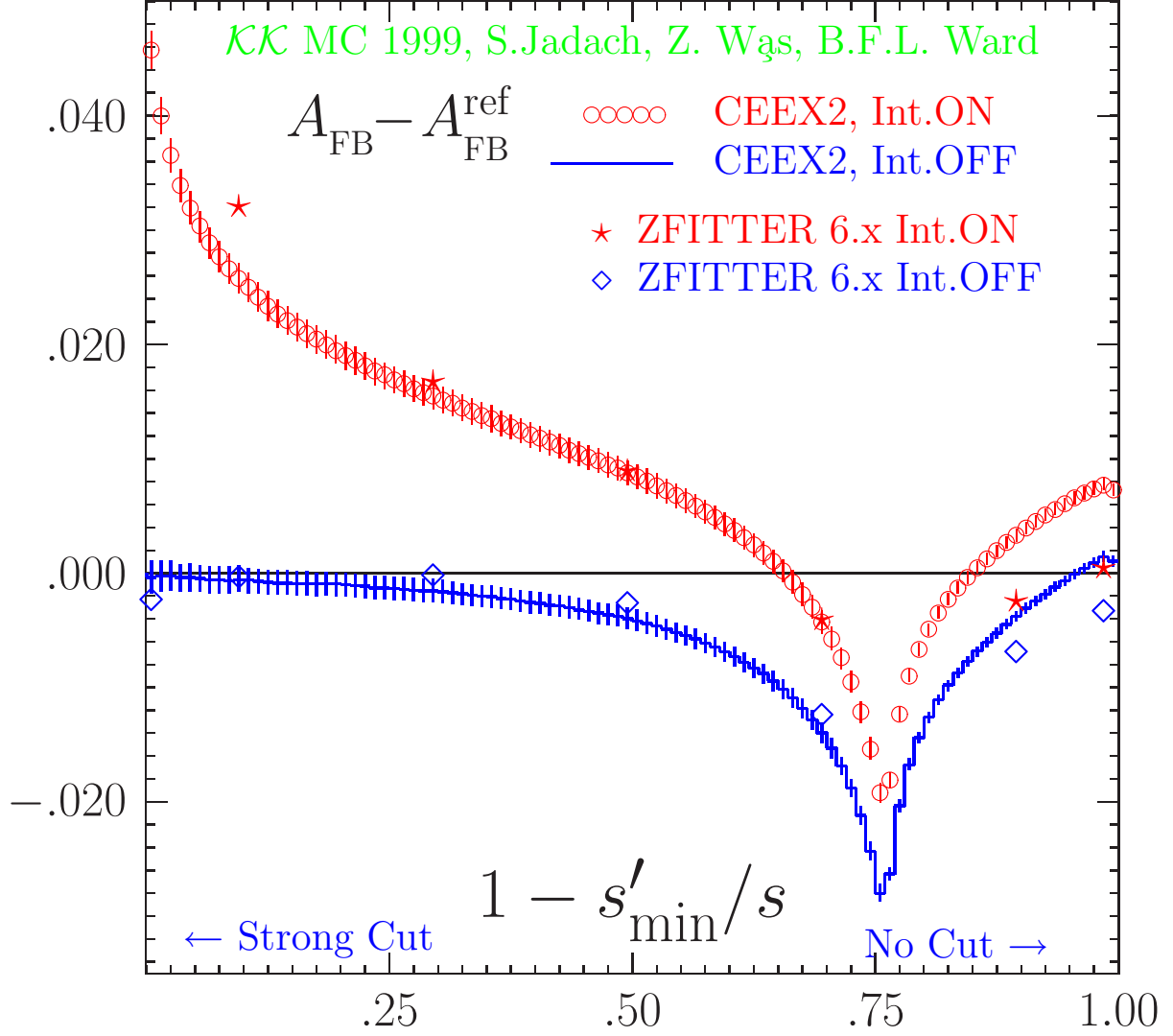


The same as in the table. The **ISR $\otimes$ FSR interf.** switched on/off whenever possible. No cut in  $\theta^\bullet$ . Reference  $A_{\text{FB}}^{\text{ref}}$  = semianalytical  $\mathcal{K}\mathcal{K}$ sem, (no ISR $\otimes$ FSR, up to  $\mathcal{O}(\alpha^3)_{\text{LL}}$ , JSW exponentiation). EEX2 data points are from KORALZ/YFS3 version 4.03 (QED up to  $\mathcal{O}(\alpha^2)_{\text{LL}}$ , ISR $\otimes$ FSR off.).



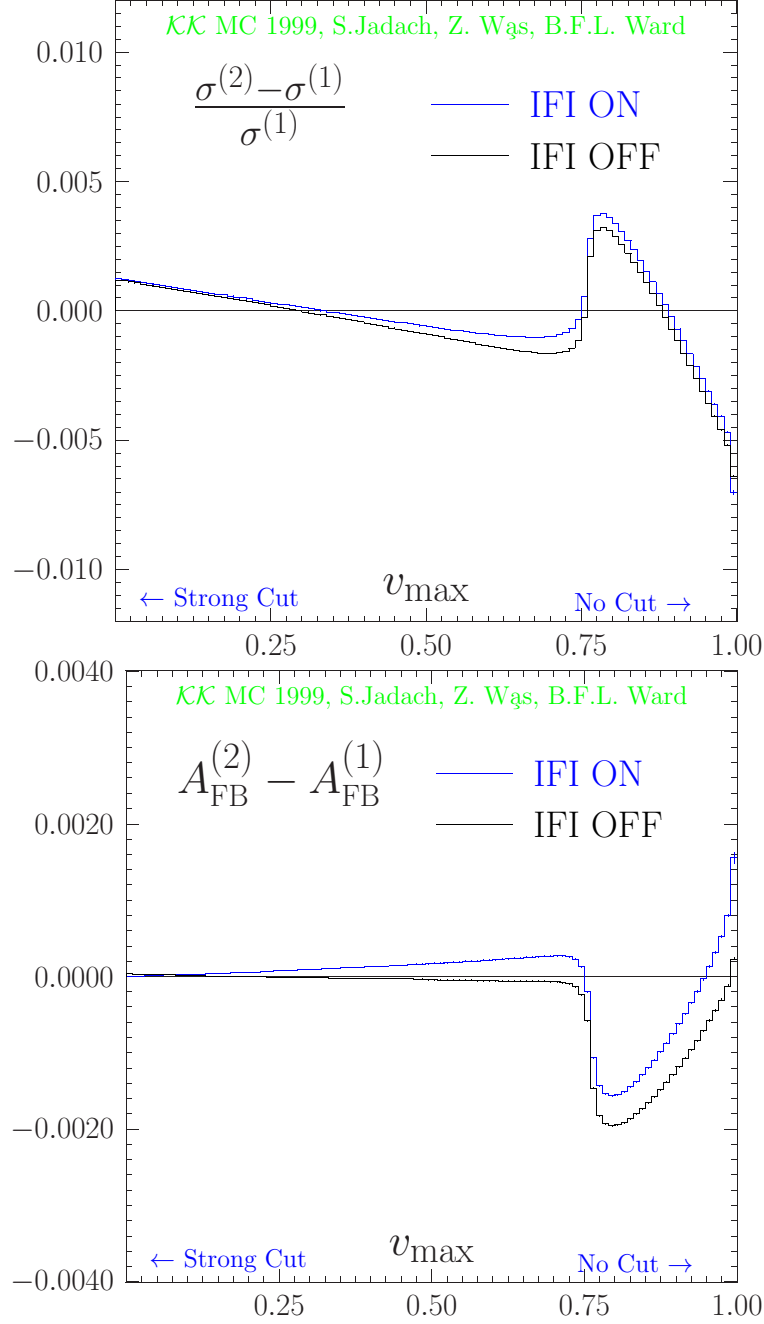
Comparison with Zfitter 6.xx. The ISR $\otimes$ FSR interf. switched on/off. No cut in  $\theta_1$ . Reference  $\sigma_{\text{ref}}$  = semianalytical of  $\mathcal{K}\mathcal{K}\text{sem}$ , (no ISR $\otimes$ FSR, up to  $\mathcal{O}(\alpha^3)_{\text{LL}}$ , JSW exponentiation).

# Charge asymmetry $A_{\text{FB}}$ , comparison with Zfitter



Comparison with Zfitter 6.xx. The **ISR $\otimes$ FSR interf.** switched on/off. No cut in  $\theta_1$ . Reference  $A_{\text{FB}}^{\text{ref}}$  = semianalytical  $K\bar{K}$ sem, (no ISR $\otimes$ FSR, up to  $\mathcal{O}(\alpha^3)_{\text{LL}}$ , JSW exponentiation).

# Physical Precision of CEEEX, NEW!!!



The difference between second and first order CEEEX results for at 189GeV. The energy cut is on  $s'/s$ , where  $s' = m_{f\bar{f}}^2$ .

Scattering angle is  $\theta = \theta^\bullet$ . [Angle  $\theta^\bullet$  is defined in Phys. Rev. **D41**, 1425 (1990)]