Fundamentals of Artificial Neural Networks

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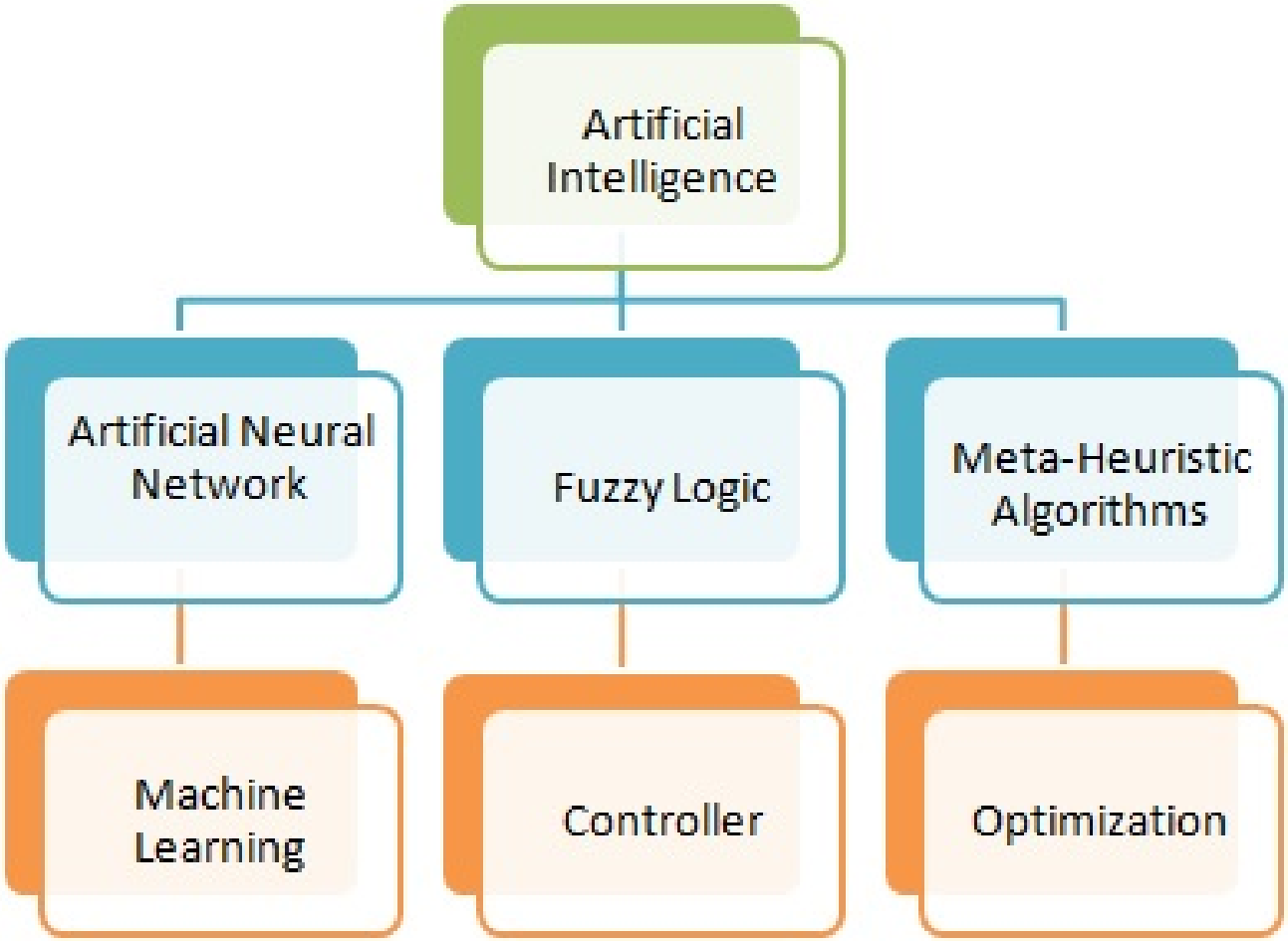
September 15, 2020

AI - Artificial Intelligence



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What is an artificial neural network?

- Artificial neural networks are one of the main tools used in machine learning. As the "neural" part of their name suggests, they are brain-inspired systems which are intended to replicate the way that we humans learn.
- Like our human brain has millions of neurons in a hierarchy and Network of neurons which are interconnected with each other via Axons and passes Electrical signals from one layer to another called synapses.

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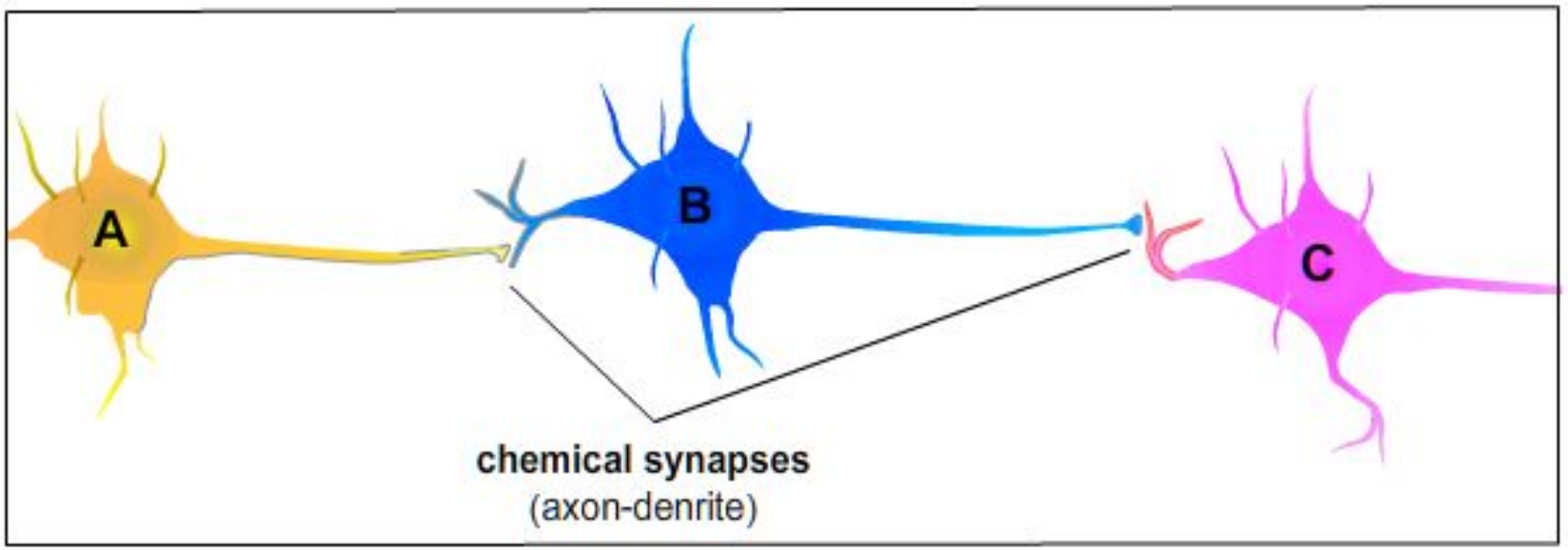

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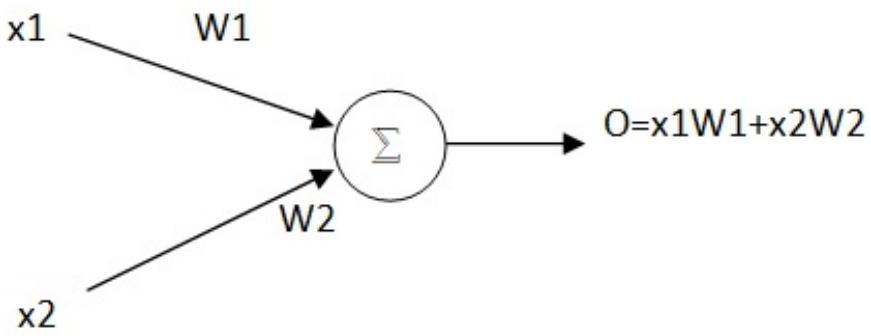
Neuron Modeling

- It is linear neuron, but most of the problems are non linear



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ANN Classification

- ✓ Feed Forward Neural Network
  - Single Layer Feed Forward Neural Network
  - Multi-layer Feed Forward Neural Network
- ✓ Feed Back Neural Network (Or) Recurrent Neural Network
  - Single Layer Feed Back Neural Network
  - Multi-layer Feed Back Neural Network

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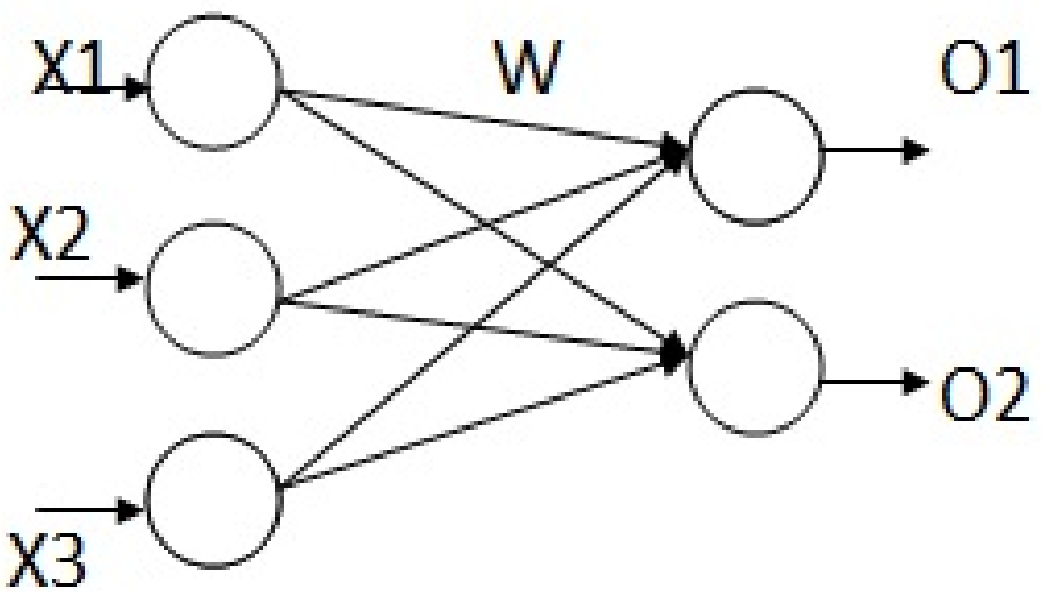
Single Layer Feed Forward Neural Network



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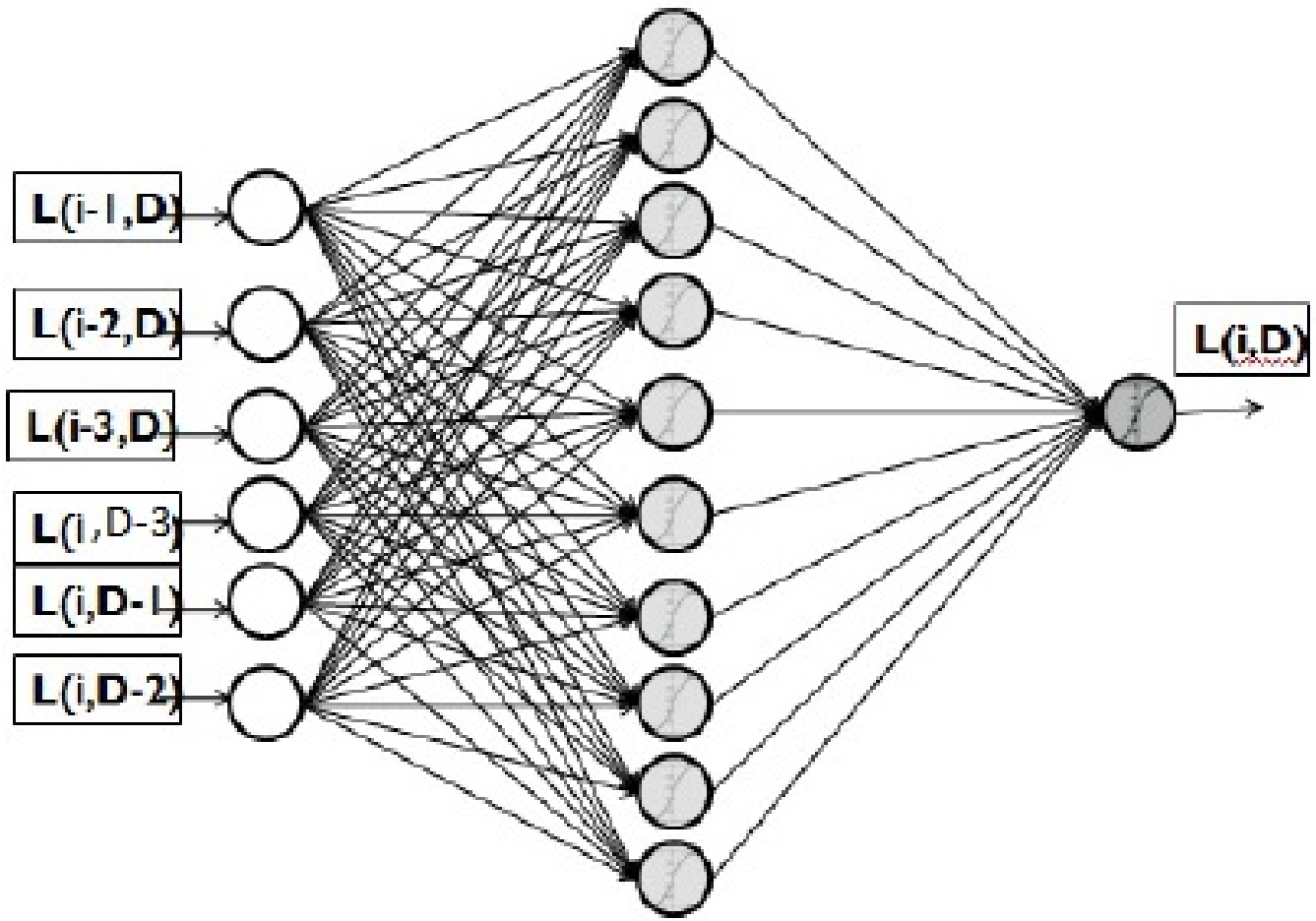
Multi-Layer Feed Forward Neural Network



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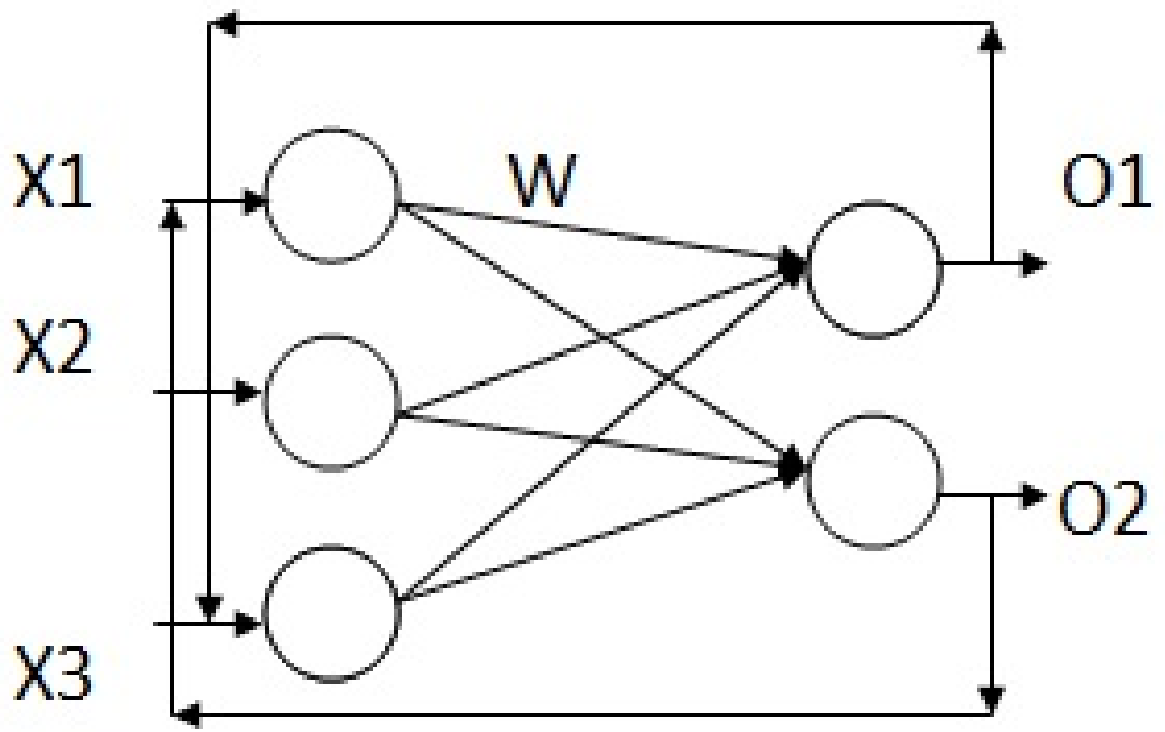
Single Layer Feed Back Neural Network



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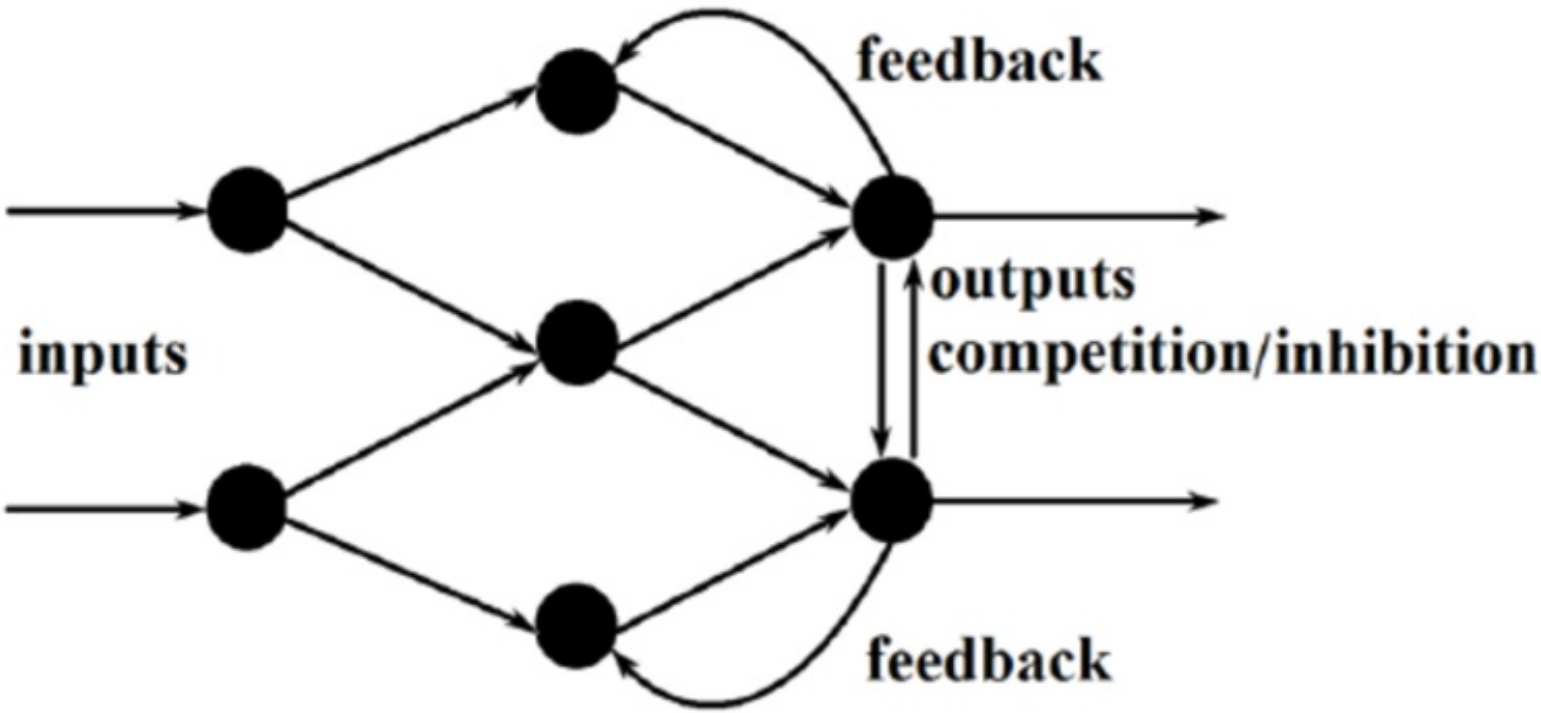
Multi-Layer Feed Back Neural Network



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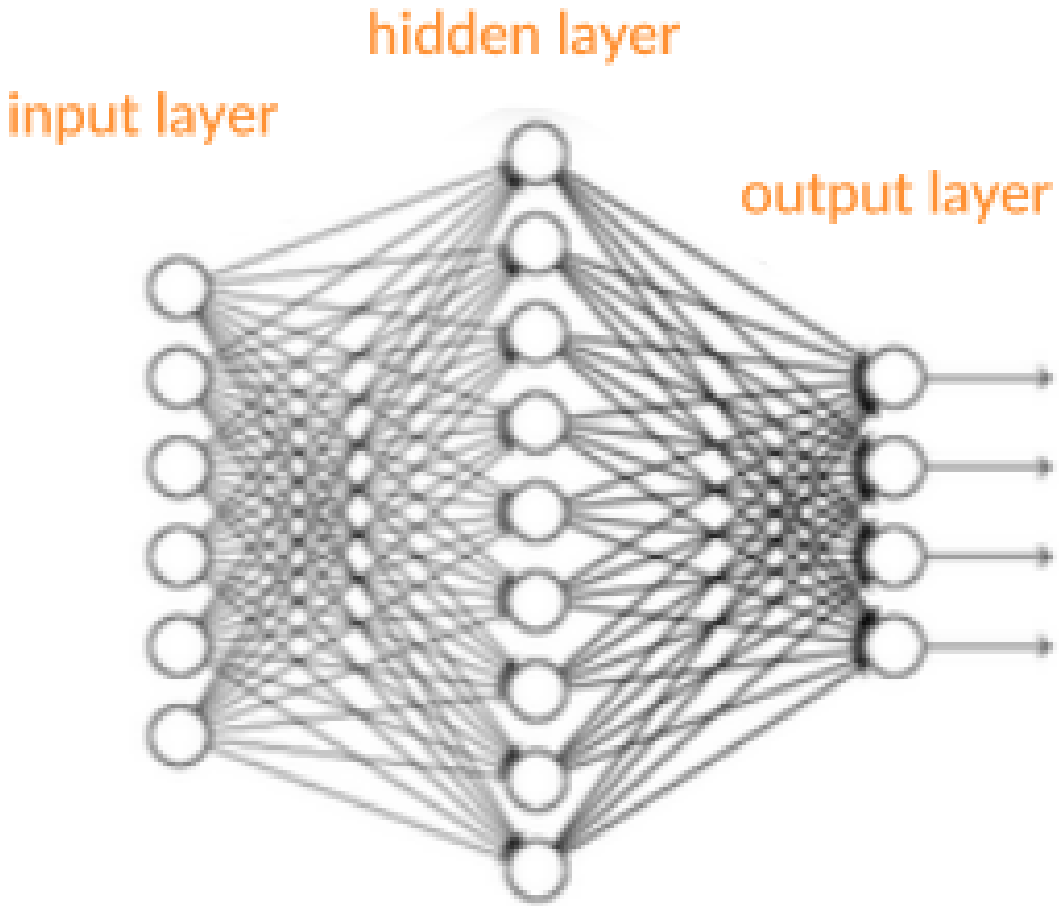
Shallow Neural Network

- Input layer:1, Hidden layer: 1, Output layer: 1



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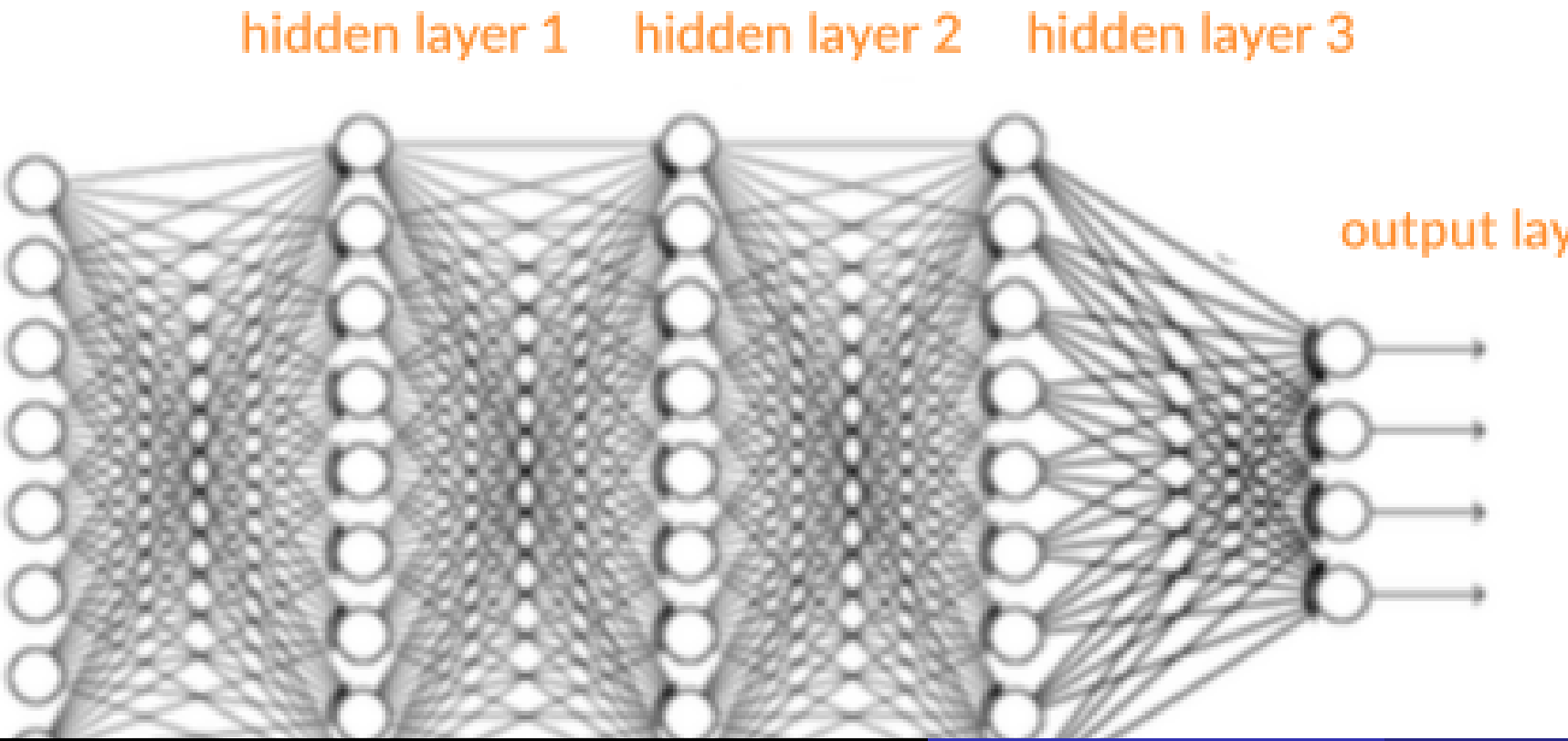
Deep Neural Network

- Input layer:1, Hidden layer: 3-10, Output layer: 1
- Beyond 10 predictive power may starts to decline



Neural Network Activation Function

Neural network activation functions are crucial components in deep learning. Activation functions determine

- Output of deep learning model
- Accuracy
- Computational efficiency

Activation functions also have impact on neural network's ability to converge and the convergence speed

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- Activation functions are mathematical equations that determine the output of a neural network.
- The function is attached to each neuron in the network, and determines whether it should be activated ("fired") or not, based on whether each neuron's input
- Activation functions also help normalize the output of each neuron to a range between 1 and 0 or between -1 and 1.

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What is need of Activation Function in ANN

- Activation functions are required for ANN in order learn non linear functional mapping between input and output
- A Neural Network without Activation function would simply be a Linear regression Model, which has limited power and does not performs good most of the times
- Without activation function our Neural network would not be able to learn and model other complicated kinds of data such as images, videos , audio , speech etc.

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- Important feature of a Activation function is that it should be differentiable to perform back propagation optimization strategy while propagation backwards in the network to compute gradients of Error(loss) with respect to Weights and then accordingly optimize weights using Gradient descend or any other Optimization technique to reduce Error

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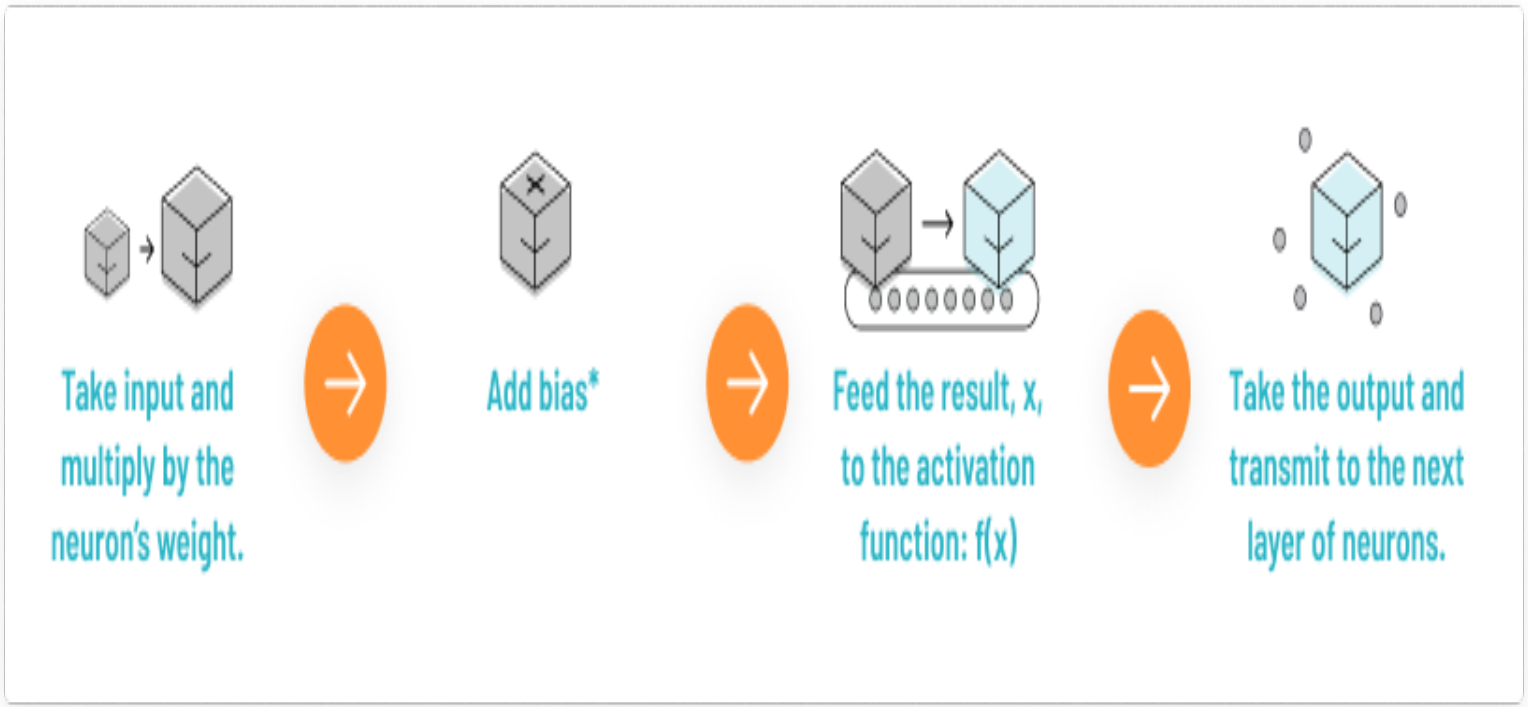
What activation function do in NN



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Activation Functions

- Sigmoid
- Tan Hyperbolic
- ReLU
- Leaky ReLU
- Softmax

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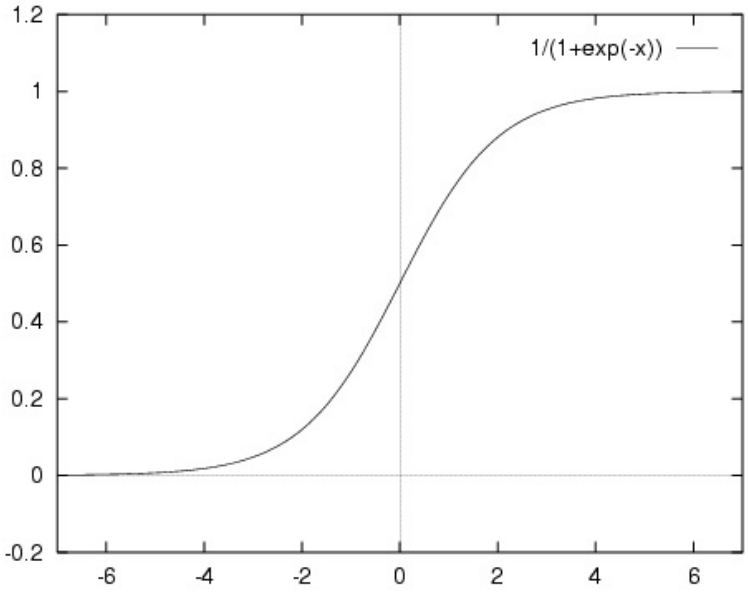
Sigmoid Activation function



$$f(x)=\frac{1}{1+e^{-x}}$$

Generally used in output layer for regression problems

Advantages	Disadvantages
Smooth gradient	Vanishing gradient problem
Clear prediction	Computationally burden
Bounded output values	Sigmoids have slow convergence

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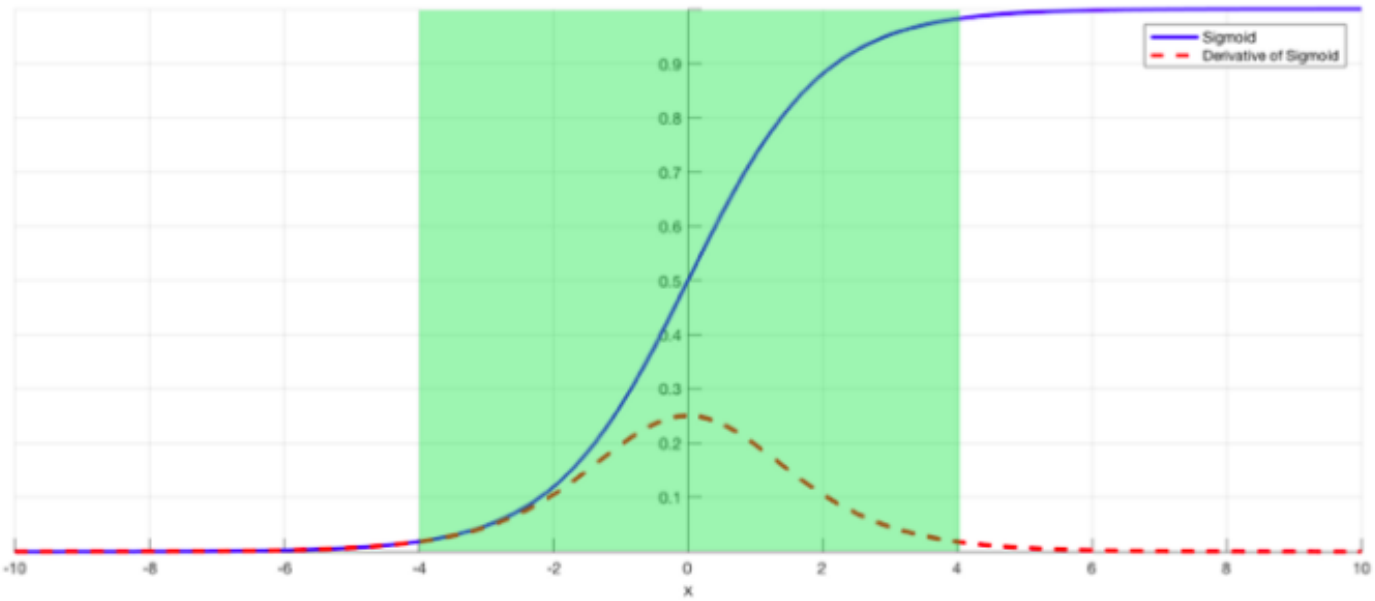
Vanishing Gradient Problem



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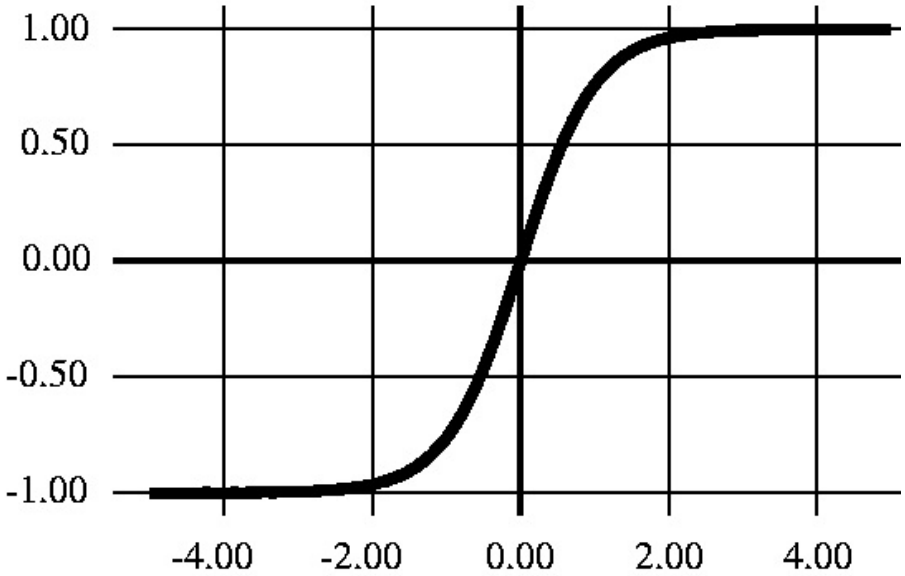
Hyperbolic Tangent function



$$f(x) = \frac{e^{x} - e^{-x}}{e^{x} + e^{-x}} \tag{1}$$

Advantages	Disadvantages
Zero centered	Vanishing gradient problem
	Computationally burden
	Sigmoids have slow convergence
Generally used in hidden layer	

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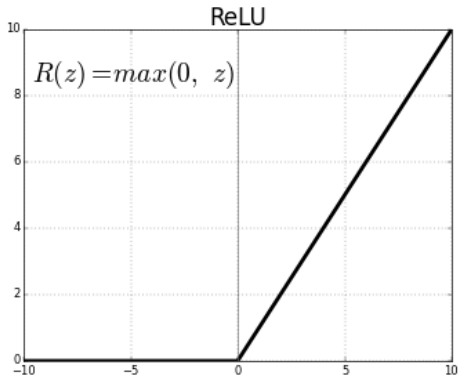
ReLu- Rectified Linear units



$$R(z) = max(0, z), if \quad z > 0 \tag{2}$$

$$R(z) = 0, if \quad z <= 0 \tag{3}$$

Advantages	Disadvantages
Computationally efficient	Dead neuron
Generally used in hidden layer	

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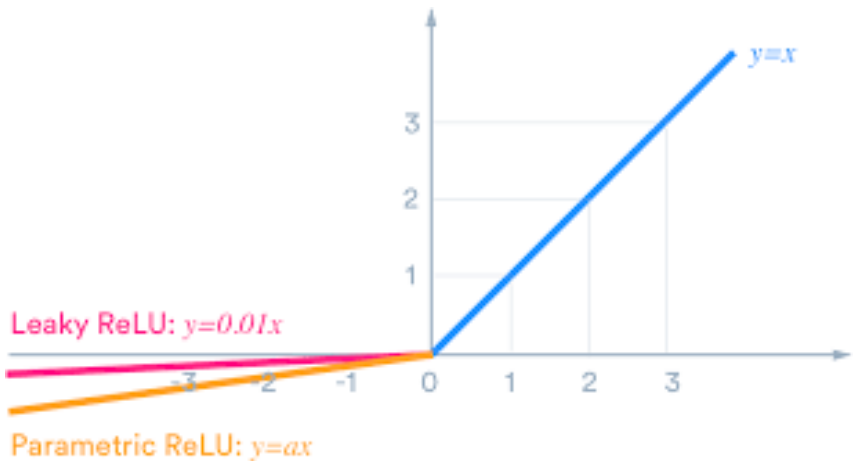
Leaky ReLU



for $\alpha = 100$ Leaky ReLu similar to ReLu. best $\alpha = 5.5$

$$f(z) = \begin{cases} z & z >= 0 \\ \frac{z}{\alpha} & z < 0 \end{cases} \quad \textit{where } \alpha \textit{ is a small value} \qquad (4)$$

Advantages	Disadvantages
Prevents Dead neuron	Results not consistent for negative inputs
Generally used in hidden layer	

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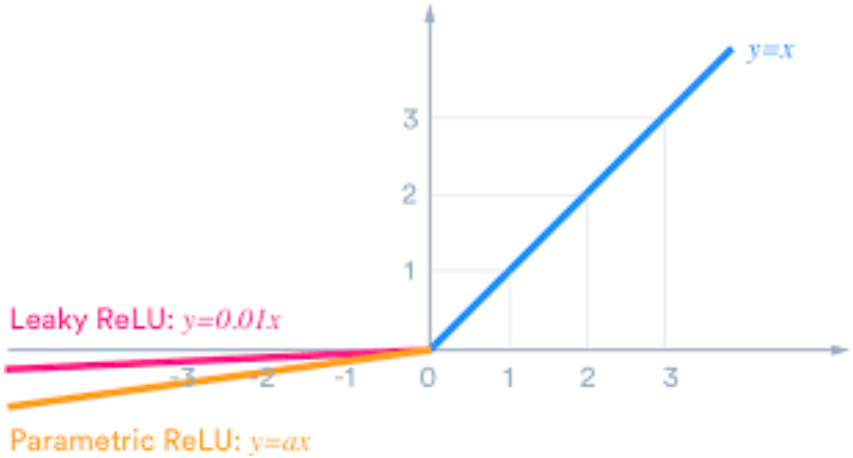
Randomized Leaky ReLU



$$f(z) = \begin{cases} z & z >= 0 \\ \alpha * z & z < 0 \end{cases} \tag{5}$$

$$\alpha = \frac{l + u}{2} :: l, u \epsilon 0, 1 \tag{6}$$

- Prevents Dead neuron
- Combats over fitting problem

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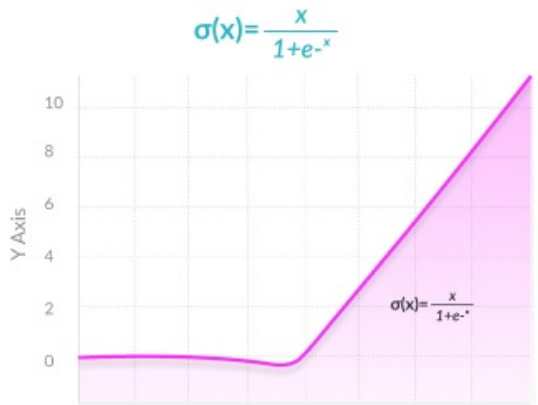
Swish

- Swish is a new, self-gated activation function discovered by researchers at Google
- Performing well over ReLU for computer vision problems



$$R(z) = \frac{z}{1 + e^{-z}} \tag{7}$$

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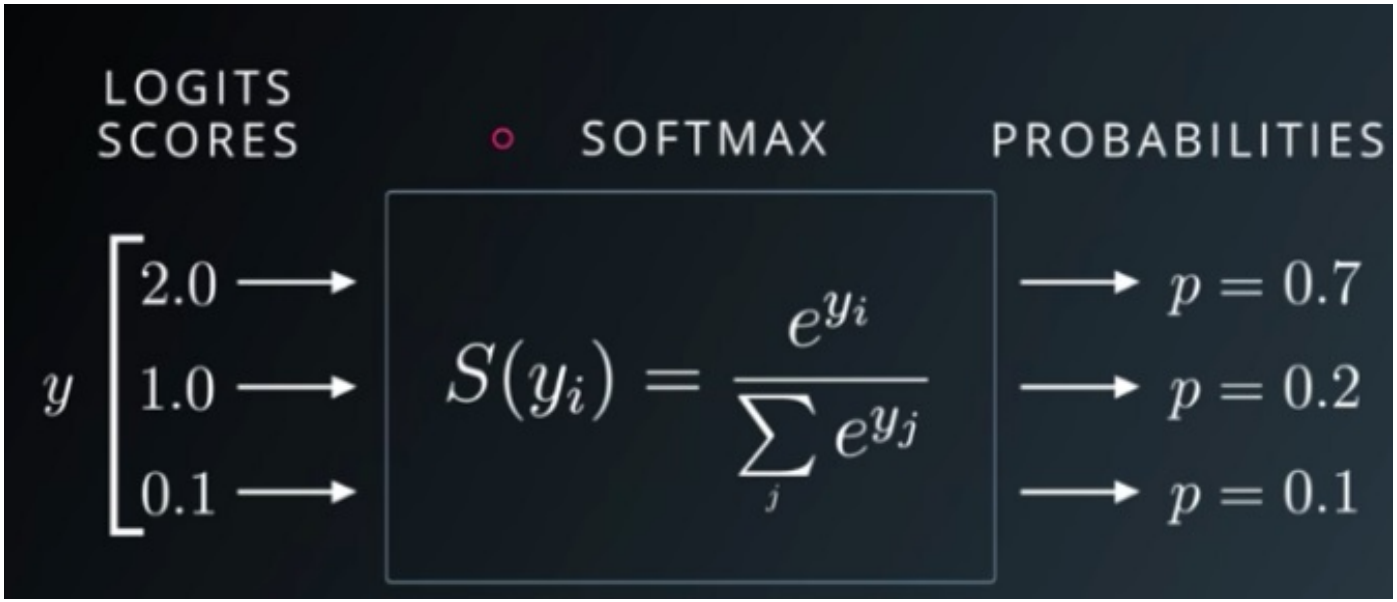
Softmax

- Softmax function outputs a vector that represents the probability distributions of a list of potential outcomes



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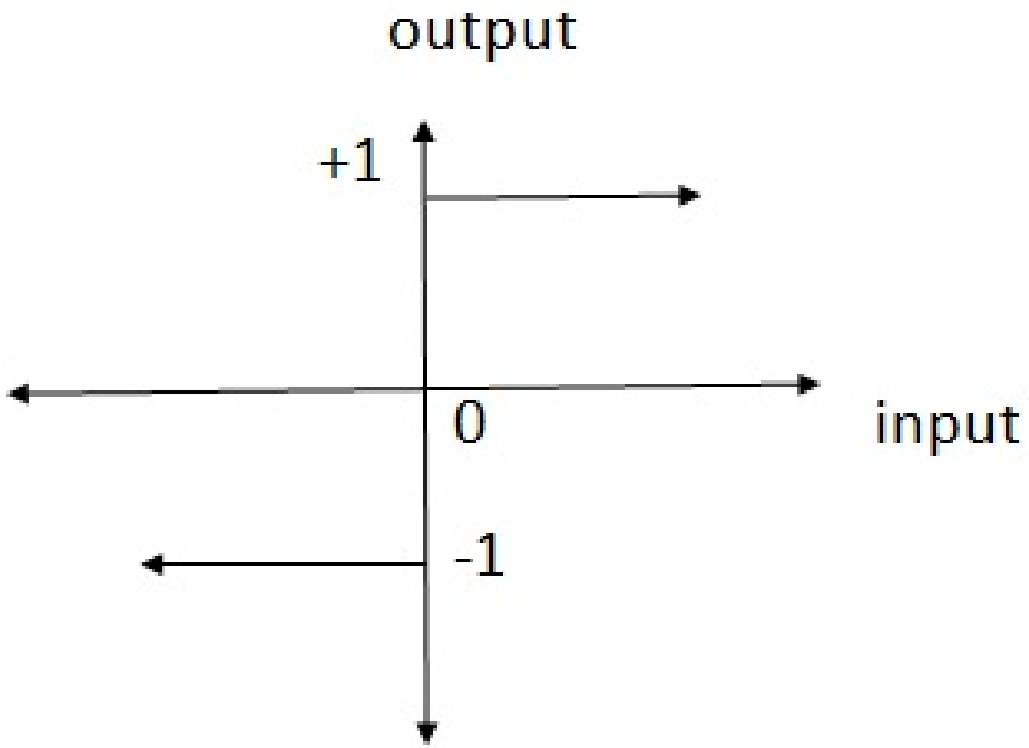
Bipolar activation function



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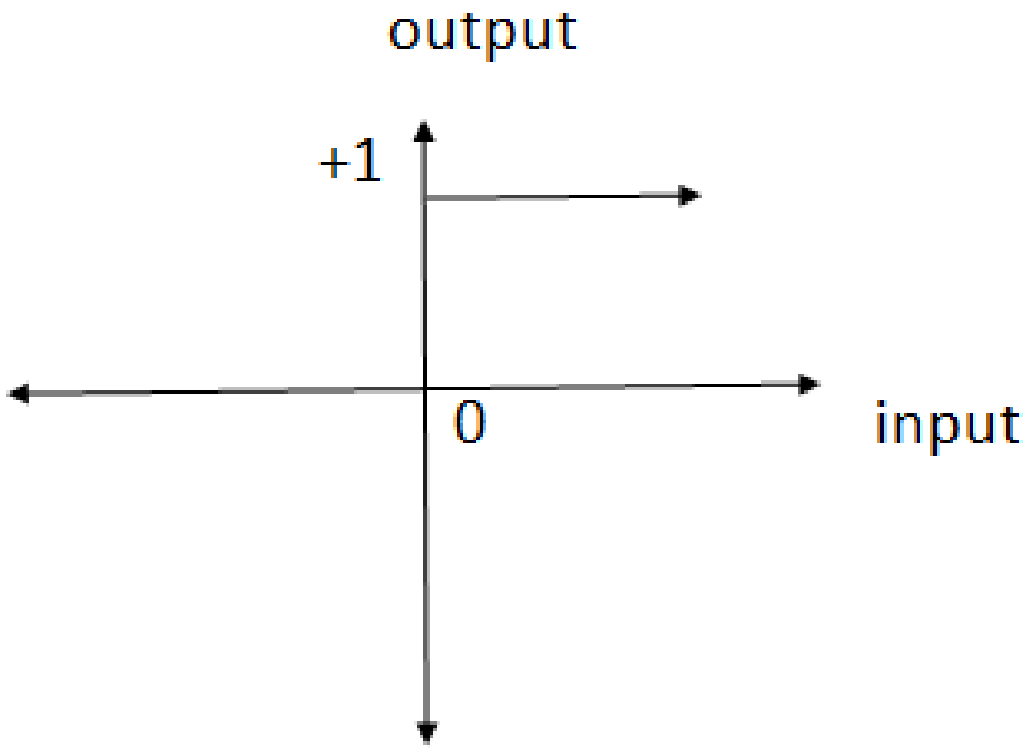
Binary activation function



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- The problem with a this function is that it does not allow multi-value outputs

Research Problem

- Optimal activation function for a certain neural network and to even automatically combine activation functions to achieve the highest accuracy. This is a very promising field of research because it attempts to discover an optimal activation function configuration automatically, whereas today, this parameter is manually tuned.

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Neural Network Learning Rules

- ✓ Supervised Learning
  - Delta learning rule
  - Perceptron learning rule
  - Widro-hoff learning rule
- ✓ Unsupervised Learning
  - Competitive learning rule

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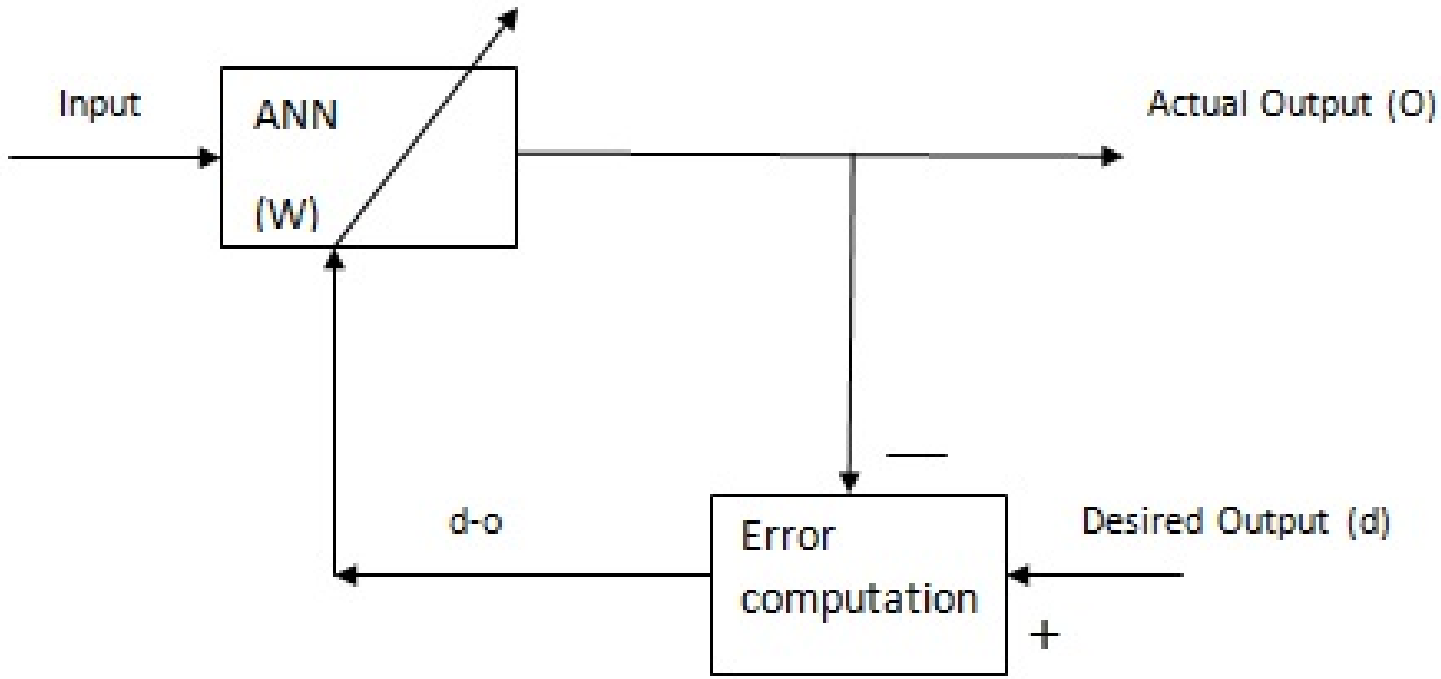
Supervised Learning



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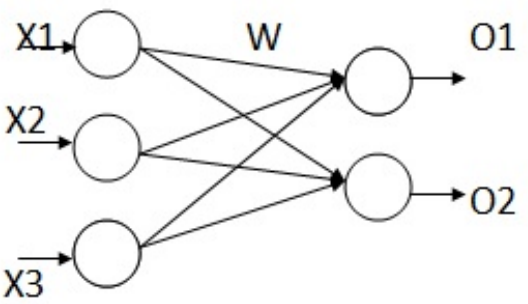
Delta learning rule



- Use Sigmoid Activation function

$$net = X * W^T \tag{8}$$

$$O = \frac{1}{1 + exp(-net)} \tag{9}$$

$$\Delta W = \eta * (d - O) * O(1 - O) * X \tag{10}$$

$$W = W + \Delta W \tag{11}$$

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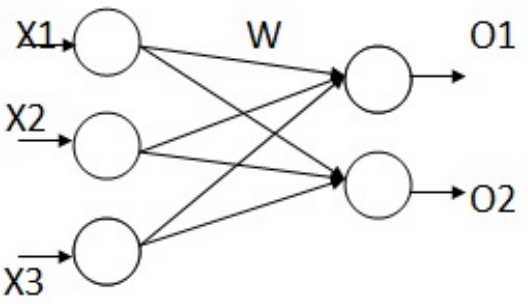
Perceptron learning rule



$$net = X * W^T \tag{12}$$

- Use Linear Activation function like bi-polar or binary activation functions

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For Bipolar activation function

$$O = -1 \ \ if \ \ net < 0 \ \ and \ \ O = 1 \ \ if \ \ net > 0 \quad (13)$$

$$\Delta W = \eta * (d - O)) * X \quad (14)$$

For Binary activation function

$$O = 0 \ \ if \ \ net < 0 \ \ and \ \ O = 1 \ \ if \ \ net > 0 \quad (15)$$

$$\Delta W = \eta * (d - O) * X \quad (16)$$

$$W = W + \Delta W \quad (17)$$

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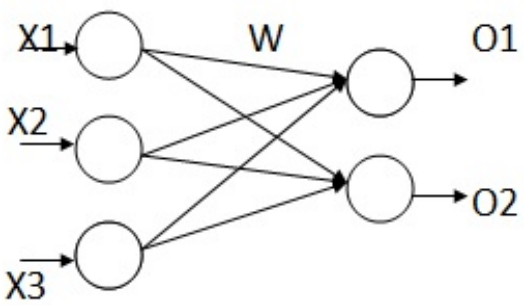
Widro-hoff learning rule



- Independent of activation function

$$O = X * W^T \tag{18}$$

$$\Delta W = \eta * (d - O) * X \tag{19}$$

$$W = W + \Delta W \tag{20}$$

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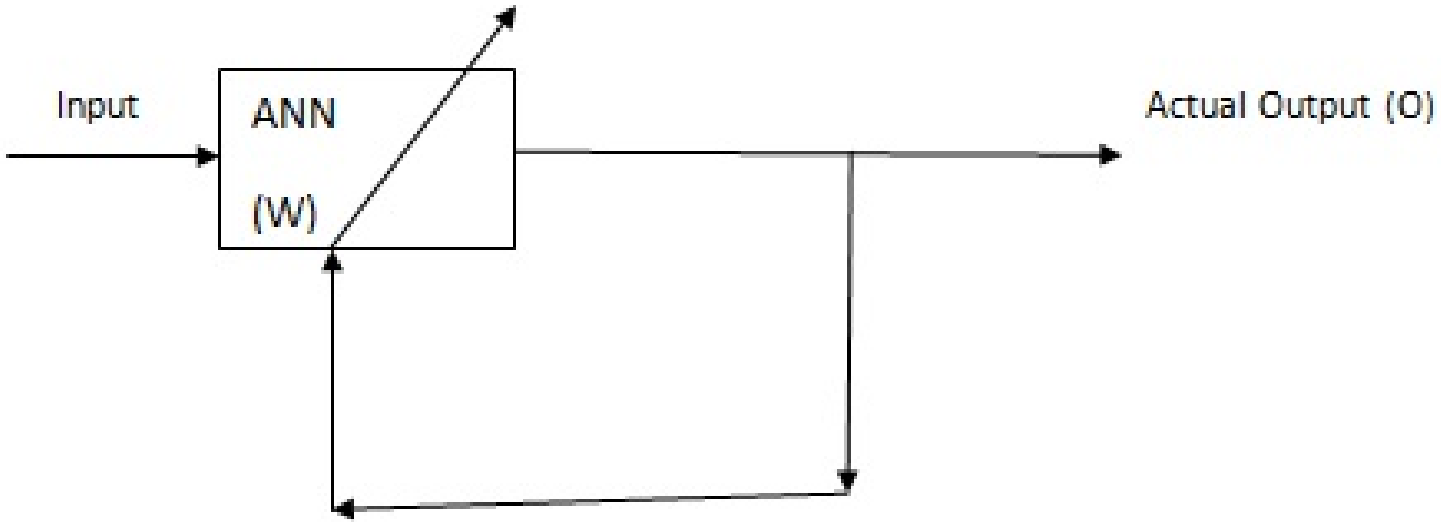
Unsupervised Learning



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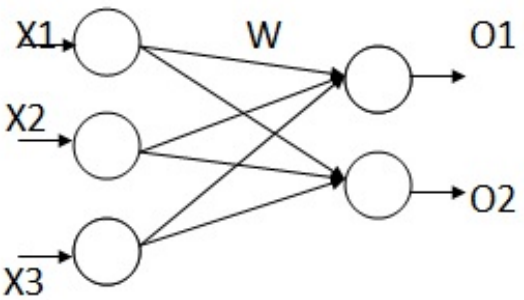
Competitive Learning



- Weights connected to winning output neuron will be updated

$$\Delta W = \eta * (X - W^{WinningNeuron}) \tag{21}$$

$$W = W + \Delta W \tag{22}$$

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Steps to follow to solve problem with AI

Step-1: Prepare data based on how you want to solve the problem

Step-2: Split the data as training and testing with 95% and 5% respectively. or 70%, 15% and 15% if validation is considered (Numbers not mandatory). **This can be done randomly**.

Step-3: Design architecture based on how you want to solve the problem

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Steps to follow to solve problem with AI

Step-4: Train the network with training data and proper algorithm. Training the network means updating the weights based on error

Step-5: If validation data is available then use it during training to identify the network performance. Validating the network means testing the network while training

Step-6: Test the performance of the network with test data.

Step-6: If training, validation and testing accuracy are good then we can use the network for prediction in real time

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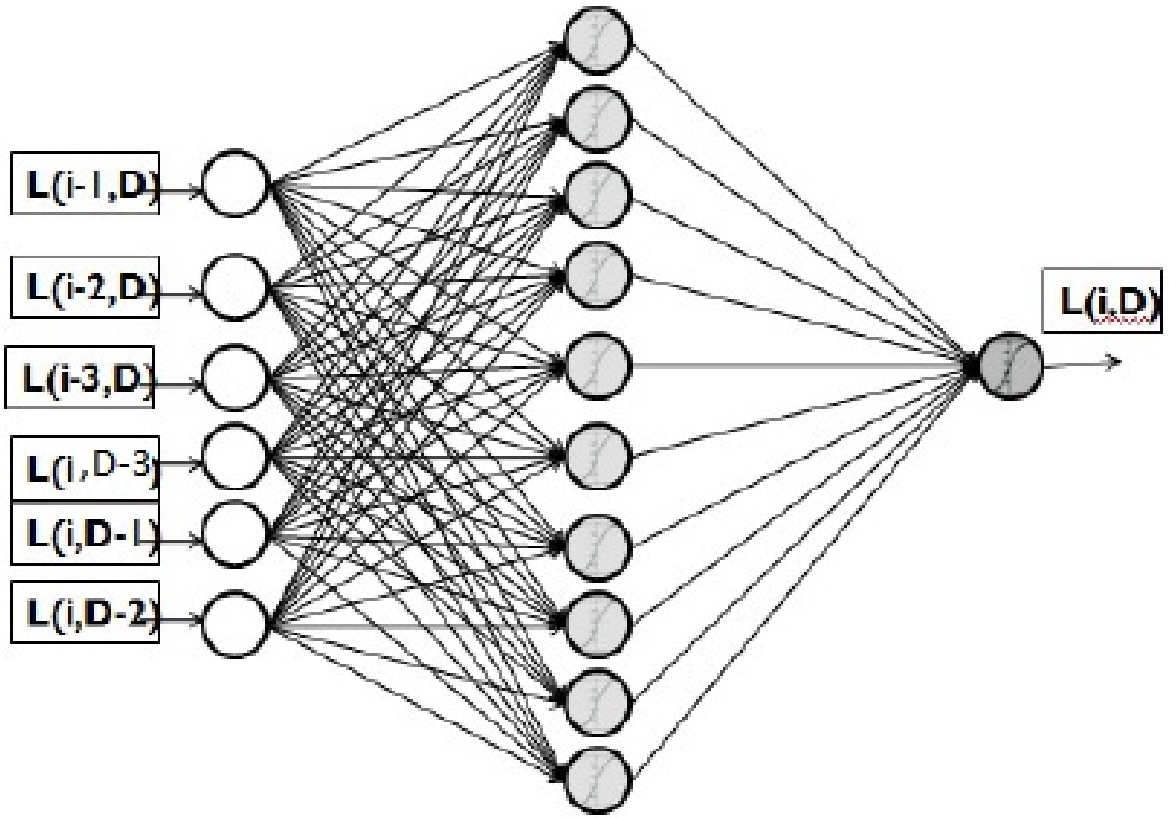
Back Propagation Algorithm



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Back Propagation Algorithm Cont.

- Let assume W_{ij} is a weight matrix between input layer (i) and hidden layer (j) and W_{jk} is a weight matrix between hidden layer (j) and output layer (k)
- X represents input to the network, d represents target output and O represents actual output given by ANN
- Sigmoid activation function is used to map non linear relation between input and output

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Back Propagation Algorithm Cont.

Step-1: Calculate net_j for hidden layer by using equation (23)

$$net_j = X * W_{ij}^T \tag{23}$$

Step-2: Calculate output of hidden layer using equation (52)

$$O_j = \frac{1}{1 + e^{-net_j}} \tag{24}$$

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Back Propagation Algorithm Cont.

Step-3: Calculate net_0 for output layer by using equation (60)

$$net_0 = O_j * W_{jk}^T \tag{25}$$

Step-4: Calculate output of output layer using equation (34)

$$O_k = \frac{1}{1 + e^{-net_o}} \tag{26}$$

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Back Propagation Algorithm Cont.

Step-5: Update the weights between hidden layer and output layer using equation (35)

$$W_{jk} = W_{jk} + \Delta W_{jk} \tag{27}$$

where

$$\Delta W_{jk} = \eta * (d_k - O_k) * O_k * (1 - O_k) * O_j \tag{28}$$

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Back Propagation Algorithm Cont.

Step-6: Update the weights between hidden layer and input layer using equation (39)

$$W_{ij} = W_{ij} + \Delta W_{ij} \tag{29}$$

where

$$\Delta W_{ij} = \eta * \sum_{k=1}^{n_o} (d_k - O_k) * O_k * (1 - O_k) * W_{jk} * O_j * (1 - O_j) * X \tag{30}$$

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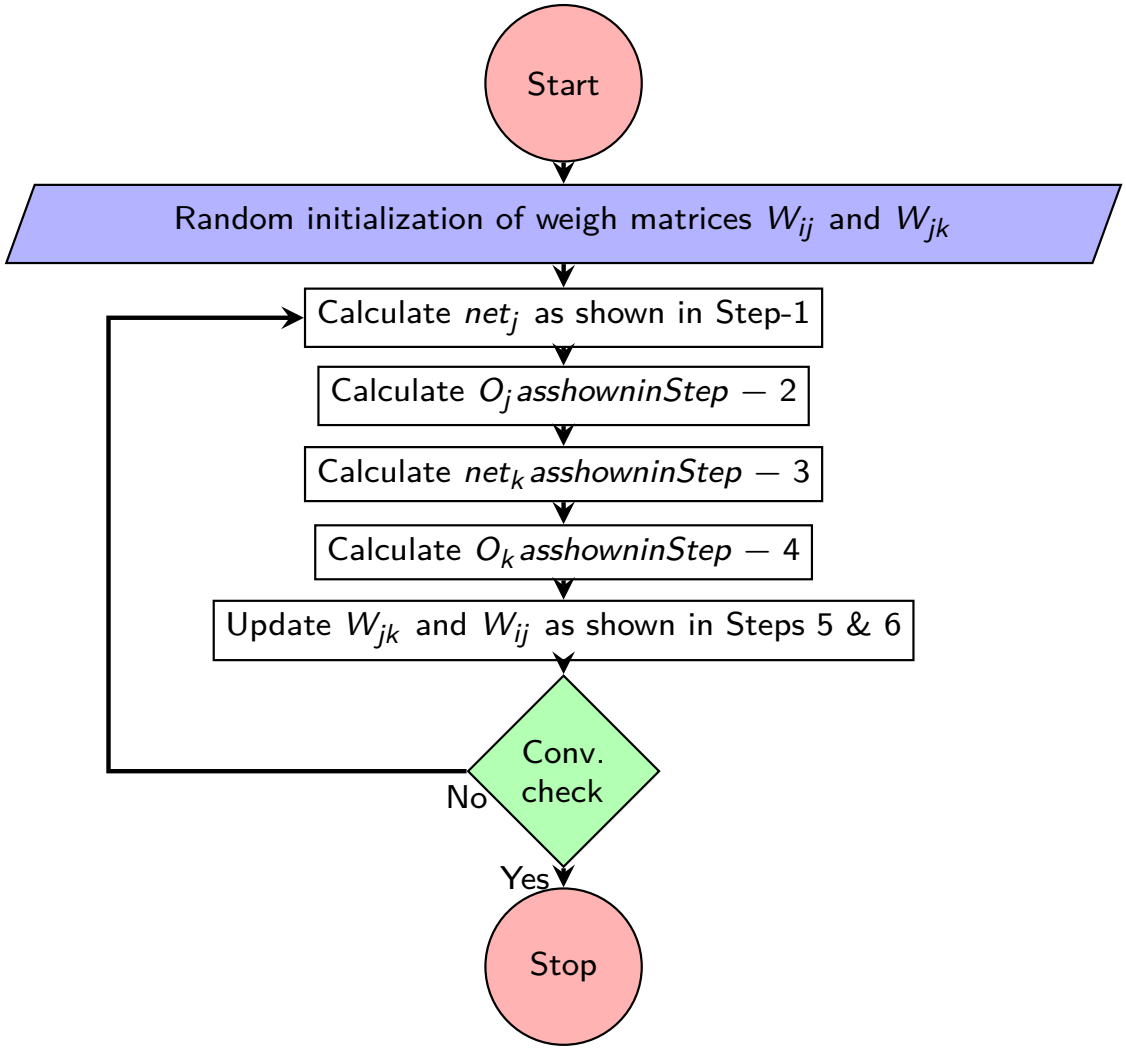
Back Propagation Algorithm Cont.



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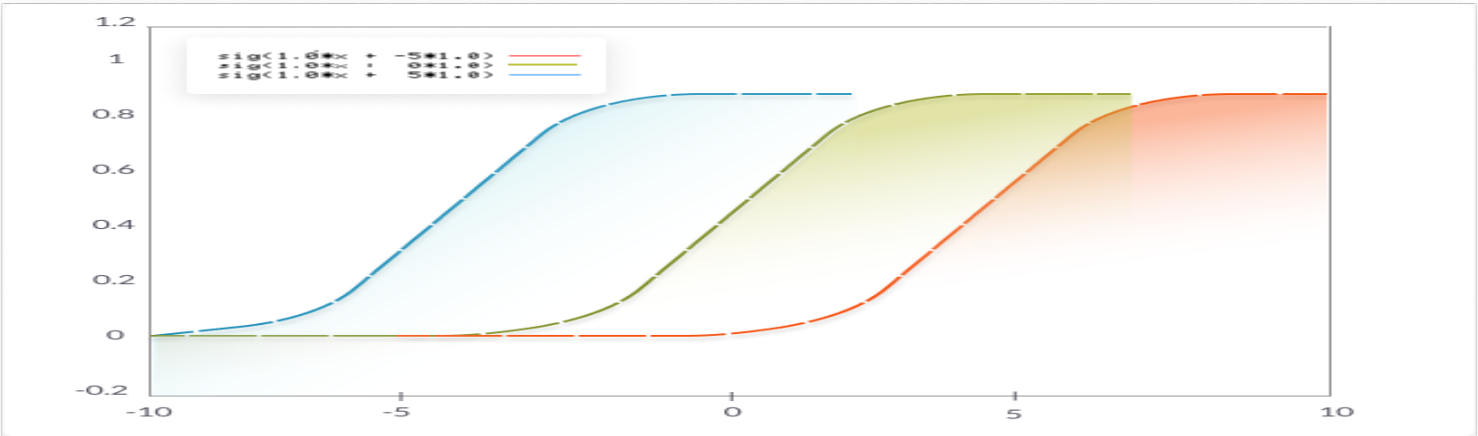
Conv. check is $\max(\Delta W_{ij}, \Delta W_{jk}) < 0.0001$

What is bias neuron?

- Bias is one of the neuron which always feed a constant value(is generally 1, some times a random value) to each hidden and output layers
- It helps the activation function to shift in right or left or up or down direction



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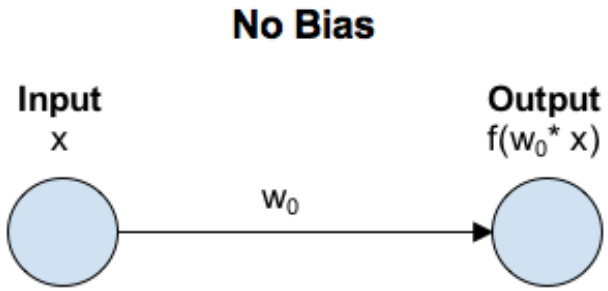
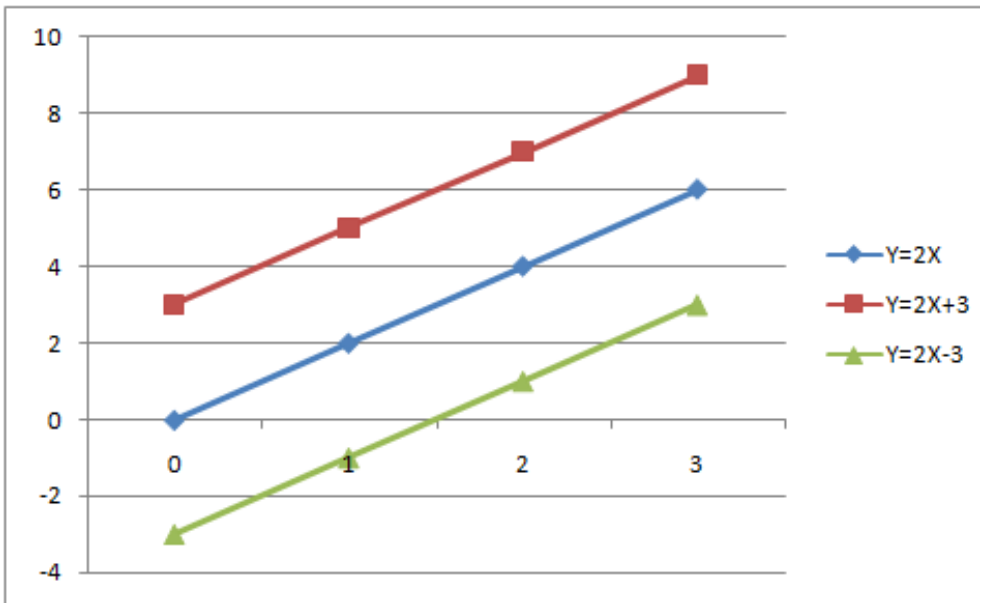
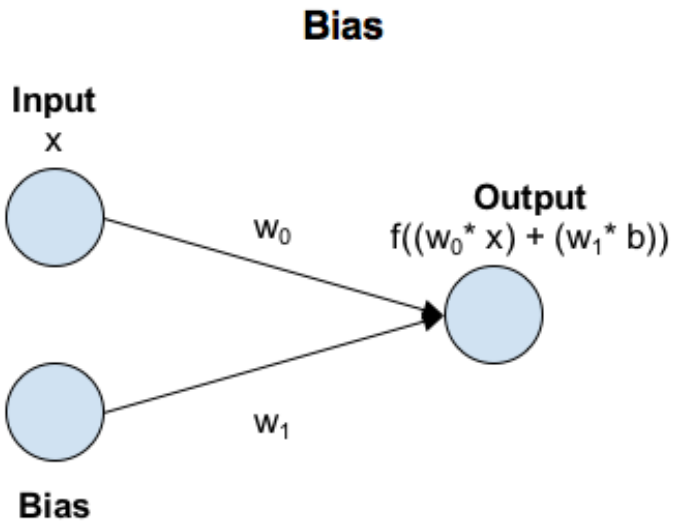

No Bias
Input
x
Output
f(w0* x)
w0


10
8
6
4
2
0
-2
-4
0
1
2
3
Y=2X
Y=2X+3
Y=2X-3


Bias
Input
x
w0
Output
f((w0* x) + (w1* b))
w1
Bias

Back Propagation Algorithm with bias neuron

Step-1: Calculate net_j for hidden layer by using equation (31)

$$net_j = X * W_{ij}^T + b_j \tag{31}$$

Step-2: Calculate output of hidden layer using equation (52)

$$O_j = \frac{1}{1 + e^{-net_j}} \tag{32}$$

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Back Propagation Algorithm with bias Cont.

Step-3: Calculate net_0 for output layer by using equation (33)

$$net_0 = O_j * W_{jk}^T + b_o \tag{33}$$

Step-4: Calculate output of output layer using equation (34)

$$O_k = \frac{1}{1 + e^{-net_o}} \tag{34}$$

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Back Propagation Algorithm with bias Cont.

Step-5: Update the weights between hidden layer and output layer using equation (35)

$$W_{jk} = W_{jk} + \Delta W_{jk} \tag{35}$$

where

$$\Delta W_{jk} = \eta * (d_k - O_k) * O_k * (1 - O_k) * O_j \tag{36}$$

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Step-6: Update the bias parameter between hidden layer and output layer using equation (37)

$$b_o = b_o + \Delta b_o \tag{37}$$

where

$$\Delta b_o = \eta * (d_k - O_k) * O_k * (1 - O_k) \tag{38}$$

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Back Propagation Algorithm with bias Cont.

Step-7: Update the weights between hidden layer and input layer using equation (39)

$$W_{ij} = W_{ij} + \Delta W_{ij} \tag{39}$$

where

$$\Delta W_{ij} = \eta * \sum_{k=1}^{n_o} (d_k - O_k) * O_k * (1 - O_k) * W_{jk} * O_j * (1 - O_j) * X \tag{40}$$

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Step-8: Update the bias parameter between hidden layer and input layer using equation (41)

$$b_j = b_j + \Delta b_j \tag{41}$$

where

$$\Delta b_j = \eta * \sum_{k=1}^{n_o} (d_k - O_k) * O_k * (1 - O_k) * O_j * (1 - O_j) \tag{42}$$

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ANN for binary classification problem

- Cannot use MSE for binary classification problem as it will be a non-convex function so we are going with binary cross entropy loss function instead of MSE

✓ **Binary Cross Entropy Loss :**

$$L = -y * log(p) - (1 - y) * log(1 - p) \qquad (43)$$

To calculate probability p we can use sigmoid activation in output layer

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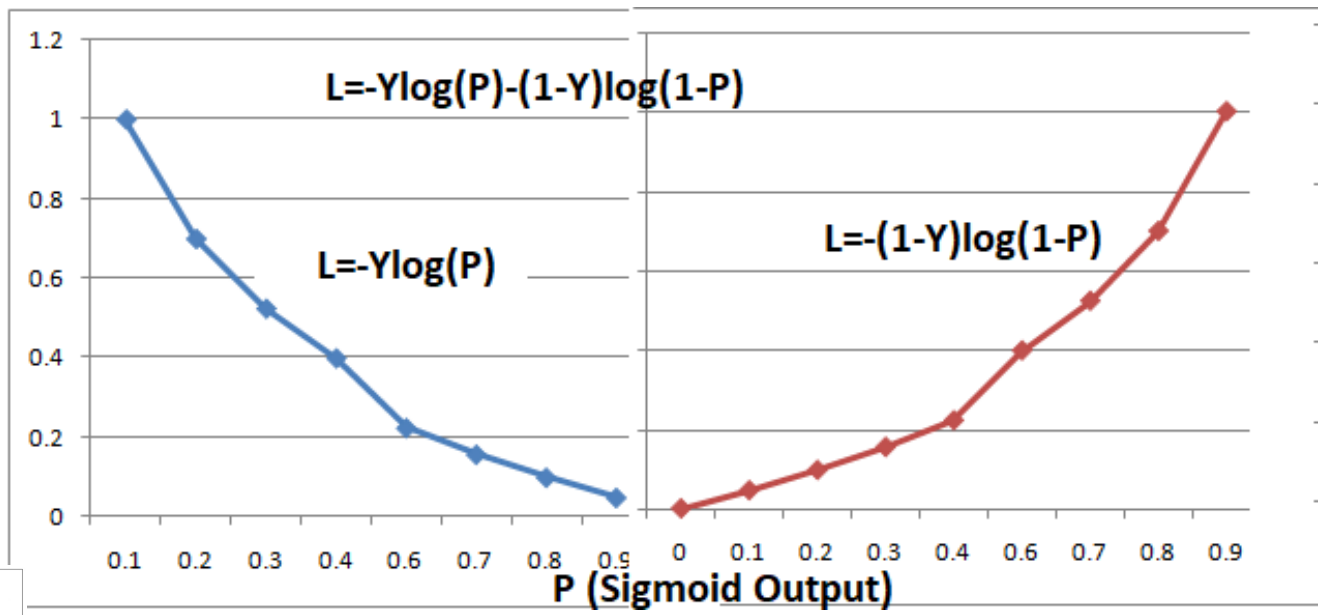
Predicted output ($\hat{Y}$)	$L\|_{Y=1}$=-log($\hat{Y}$)	$L\|_{Y=0}$=-log(1-$\hat{Y}$)
0	∞	0
0.1	1	0.045757
0.2	0.69897	0.09691
0.3	0.522879	0.154902
0.4	0.39794	0.221849
0.6	0.221849	0.39794
0.7	0.154902	0.522879
0.8	0.09691	0.69897
0.9	0.045757	1
1	0	∞



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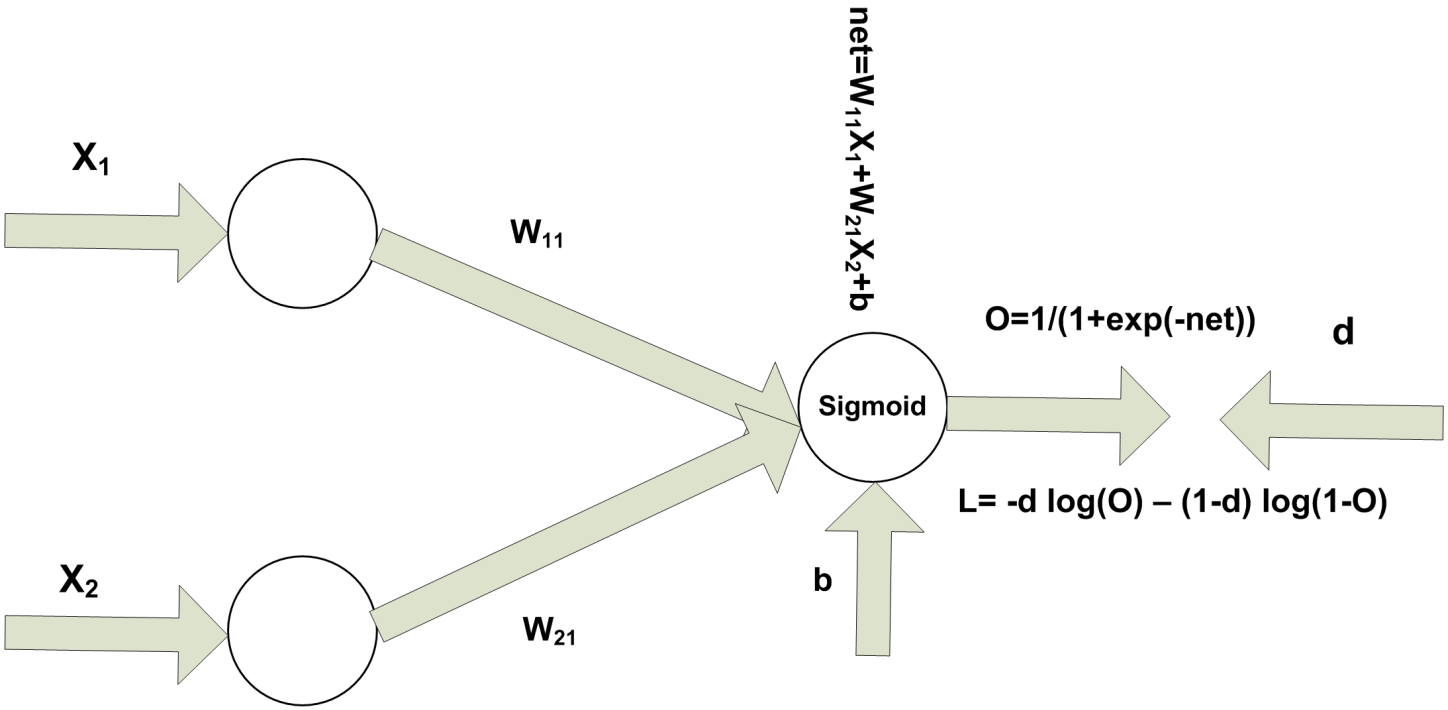
Single Layer ANN for binary Classification



Email ID: (vvr.nitw@ieee.org)

Step1: Read dataset $X=\begin{pmatrix} X_1 \\ X_2 \end{pmatrix}$, $Y=(d)$, η. Initialize

weights $W=\begin{pmatrix} W_{11} \\ W_{21} \end{pmatrix}$ and bias "b"

Step2: Compute net input to output neuron using equation (44)

$$net = W_{11}X_1 + W_{21}X_2 + b = W^T X + b = \sum_{i=1}^{n_i} W_{i1}X_i + b \tag{44}$$

Step3: Compute output (O) using equation (65)

$$O = \frac{1}{1 + e^{-net}} \tag{45}$$

Step4: Compute binary cross entropy loss using equation (66)

$$L = -dlog(O) - (1 - d)log(1 - O) \tag{46}$$

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Step5: Compute change in weight (ΔW) using equation (67)

$$\Delta W = \begin{pmatrix} \Delta W_{11} \\ \Delta W_{21} \end{pmatrix} = -\eta(d - O) \begin{pmatrix} X_1 \\ X_2 \end{pmatrix} \quad (47)$$

Step6: Compute change in bias (Δb) using equation (68)

$$\Delta b = -\eta(d - O) \quad (48)$$

Step7: Update weight matrix using equation (69) and bias using equation (70)

$$W = W + \Delta W \quad (49)$$

$$b = b + \Delta b \quad (50)$$

p8: Repeat steps 2,3,4,5,6,7 till convergence check

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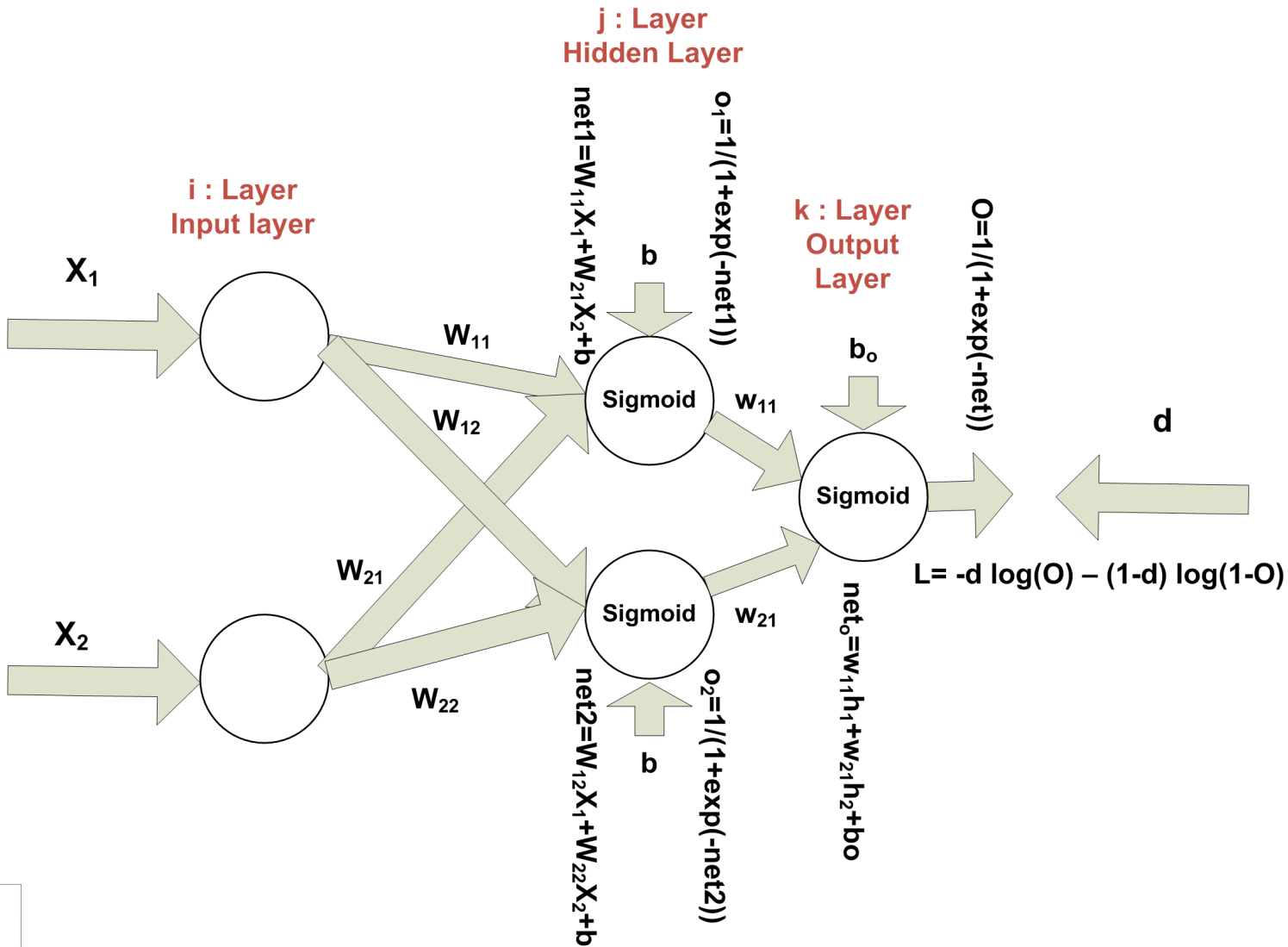
Multiple layer ANN for classification



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Back Propagation Algorithm for binary classification

Step-1: Calculate net_j for hidden layer by using equation (51)

$$net_j = W_{ij}^T * X + b_j \tag{51}$$

Step-2: Calculate output of hidden layer using equation (??)

$$O_j = \frac{1}{1 + e^{-net_j}} \tag{52}$$

refer to hidden neuron

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Back Propagation Algorithm for binary classification Cont.

Step-3: Calculate net_0 for output layer by using equation (53)

$$net_0 = w_{jk}^T * O_j + b_o \tag{53}$$

Step-4: Calculate output of output layer using equation (54)

$$O = \frac{1}{1 + e^{-net_o}} \tag{54}$$

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Back Propagation Algorithm for binary classification Cont.

Step-5: Update the weights between hidden layer and output layer using equation (55)

$$W_{jk} = W_{jk} + \Delta W_{jk} \tag{55}$$

where

$$\Delta W_{jk} = -\eta * (d - O) * O_j \tag{56}$$

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Step-6: Update the bias parameter between hidden layer and output layer using equation (57)

$$b_o = b_o + \Delta b_o \tag{57}$$

where

$$\Delta b_o = -\eta * (d_k - O_k) \tag{58}$$

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Back Propagation Algorithm for binary classification Cont.

Step-7: Update the weights between hidden layer and input layer using equation (59)

$$W_{ij} = W_{ij} + \Delta W_{ij} \tag{59}$$

where

$$\Delta W_{ij} = -\eta * (d - O) * W_{jk} * O_j * (1 - O_j) * X \tag{60}$$

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Step-8: Update the bias parameter between hidden layer and input layer using equation (61)

$$b_j = b_j + \Delta b_j \tag{61}$$

where

$$\Delta b_j = -\eta * (d - O) * O_j * (1 - O_j) \tag{62}$$

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Single layer ANN for Multiple Classification

For multiple classifications, categorical cross entropy is used

- ✓ **Categorical Cross Entropy Loss :**

$$L(X_i, Y_i) = -\sum_{j=1}^{n} Y_{ij} log(p_{ij}) \tag{63}$$

where p_{ij} calculated using softmax activation function

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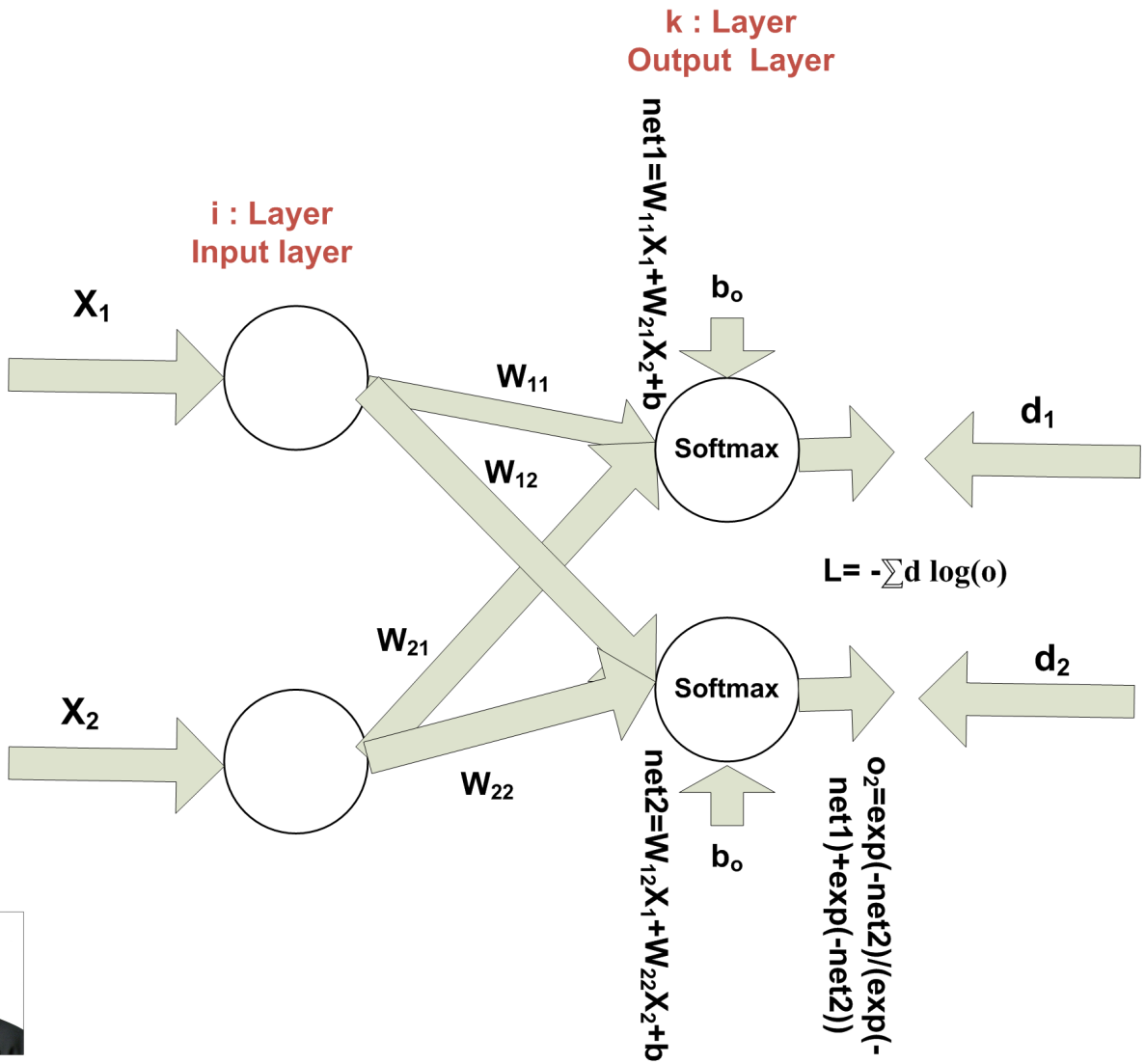
Single layer ANN for Multiple Classification



Email ID: (vvr.nitw@ieee.org)

Step1: Read dataset X=$\begin{pmatrix} X_1 \\ X_2 \end{pmatrix}$, Y=$(d)$, η. Initialize weights W=$\begin{pmatrix} W_{11} & W_{12} \\ W_{21} & W_{22} \end{pmatrix}$ and bias "b"

Step2: Compute net input to each output neuron

$$\begin{pmatrix} net_1 \\ net_2 \end{pmatrix} = W^T X + b \tag{64}$$

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Step3: Compute output (O_k) for each output neuron

$$O_k = \frac{e^{net_k}}{\sum_{i=1}^{n_o} e^{net_i}} \tag{65}$$

Step4: Compute categorical cross entropy loss

$$L = -\sum_{i=1}^{n_o} d_i log(O_i) \tag{66}$$

[Weights which are connected to output neuron corresponding to class will be updated]

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Step5: Compute change in weight (ΔW) using equation (67)

$$\Delta W = \begin{pmatrix} \Delta W_{11} \\ \Delta W_{21} \end{pmatrix} = -\eta(d - O) \begin{pmatrix} X_1 \\ X_2 \end{pmatrix} \quad (67)$$

Step6: Compute change in bias (Δb) using equation (68)

$$\Delta b = -\eta(d - O) \quad (68)$$

Step7: Update weight matrix using equation (69) and bias using equation (70)

$$W = W + \Delta W \quad (69)$$

$$b = b + \Delta b \quad (70)$$

p8: Repeat steps 2,3,4,5,6,7 till convergence check

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- **Training Set:** A training set is a group of sample inputs feed into the neural network in order to train the model. The neural network learns from inputs and finds weights for the neurons that can result in an accurate prediction.
- **Training Error:** The error is the difference between the known correct output for the inputs and the actual output of the neural network. During the course of training, the training error is reduced until the model produces an accurate prediction for the training set.
- **Validation Set:** A validation set is another group of sample inputs which were not included in training and preferably are different from the samples in the training set.
- **Validation Error:** The difference between correct prediction for the validation set with the actual model prediction is the validation error.

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Bias Vs. Variance

- √ High Bias:: High training loss
- √ Low Bias:: Low training loss
- √ High Variance:: High Validation loss
- √ Low Variance:: Low Validation loss

Model with low bias and low variance is good for real time application

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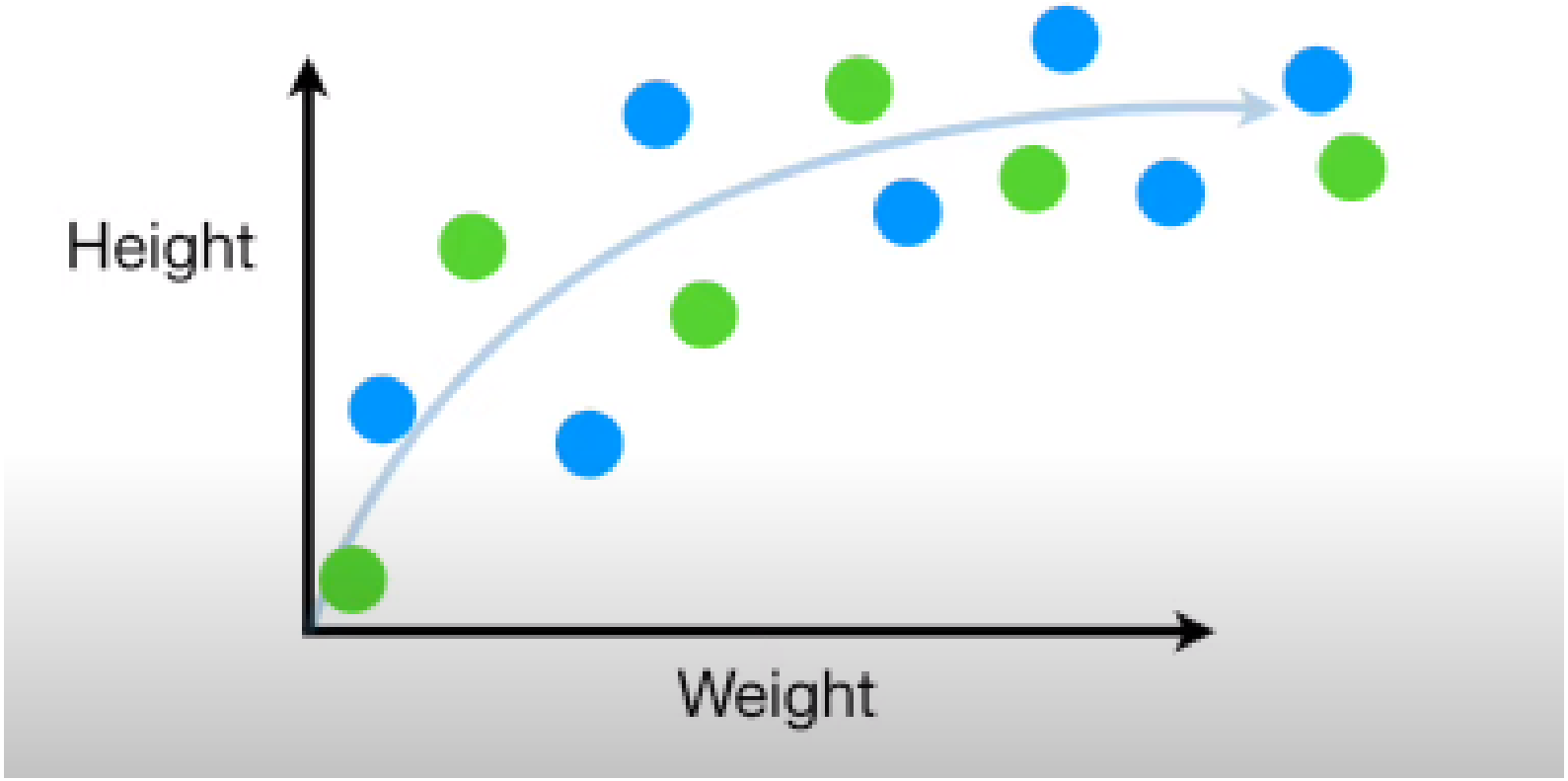
Let consider a model to predict height based on weight.



Blue dots: Training Set

Green dots: Testing/Validation Set

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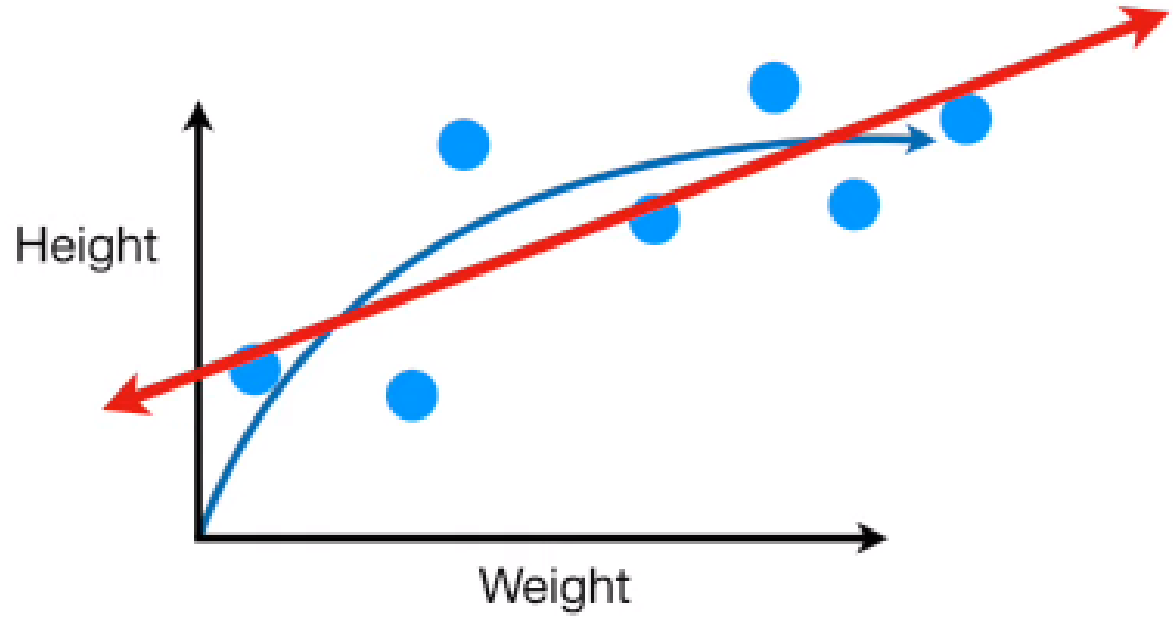
If we consider a linear regression model, it may not find the true relation between weight and height leads high training loss. This is called **high bias**.

Inability of model to find the true relation between input and output based on training data is called High



Bias

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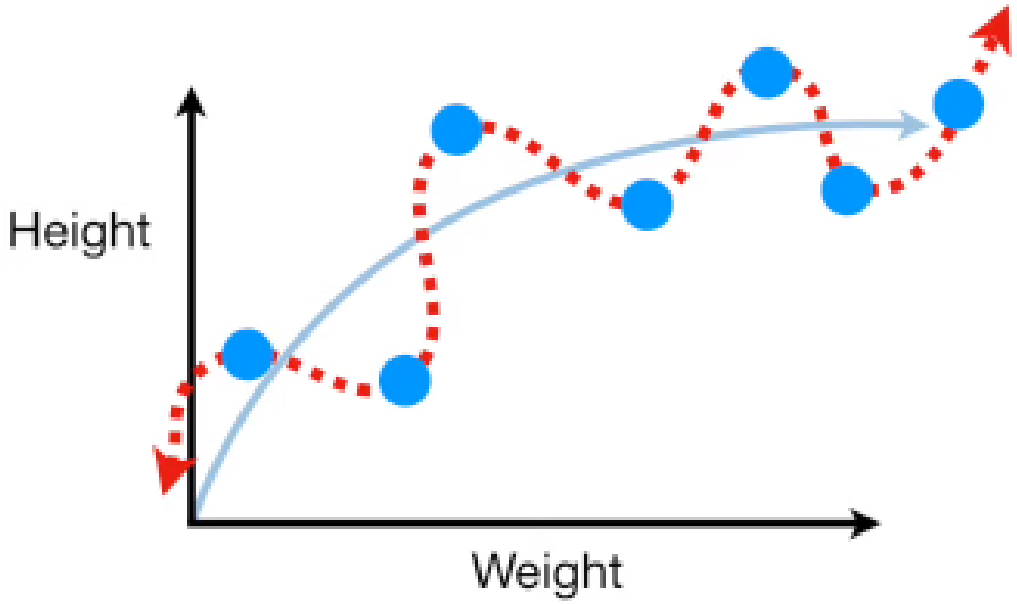
If we consider a polynomial regression model, which fits almost all samples in dataset that leads low training loss. This is called **low bias**. Ability of model to find the exact relation between input and output based on training data is called Low Bias



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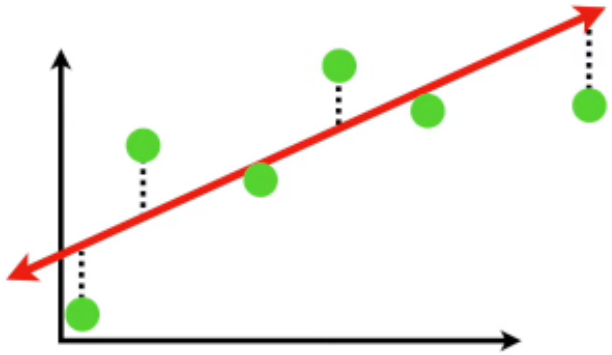
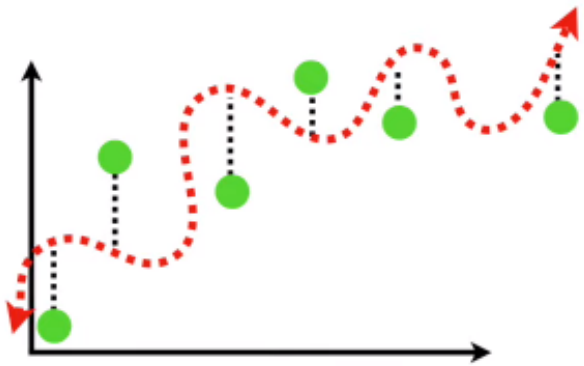
Model performance on validation dataset

- Low testing loss with linear regression model. It is called low variance



- High testing loss with polynomial regression model. It is called high variance



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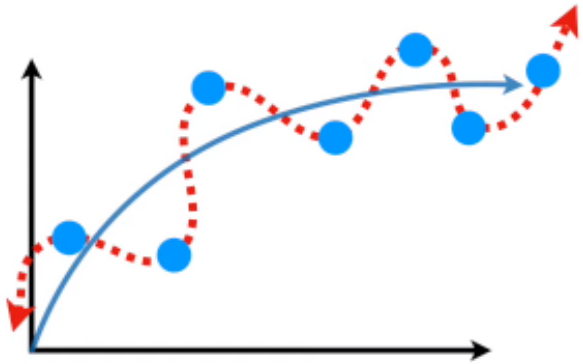
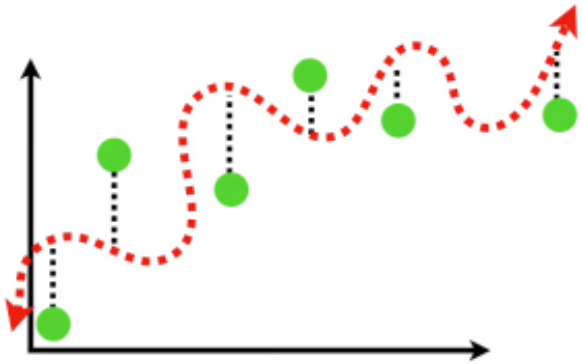
Polynomial regression model fits really well for training dataset but not for the testing dataset. This issue is called **over fitting**[Low Bias and High Variance].





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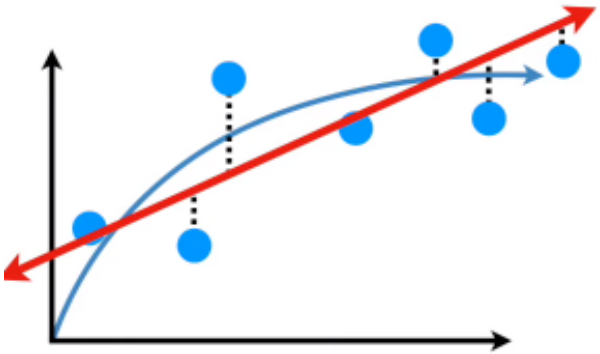
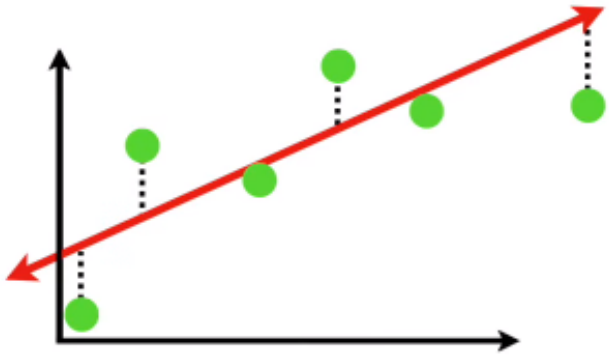
Linear regression model not fits well for training dataset but may be performing well on the testing dataset. This issue is called **under fitting**[High Bias and High Variance].





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Methods to Avoid Over fitting in Neural Networks

- ✓ Reduce complexity of neural network
  - Reduce number of hidden layers
  - Reduce number of hidden neurons (Dropout)
- ✓ Retraining Neural Networks
  - Running the same neural network model on the same training set, but each time with different initial weights.
- ✓ Multiple Neural Networks
  - Train several neural networks in parallel, with the same structure but each with different initial weights, and average their outputs.

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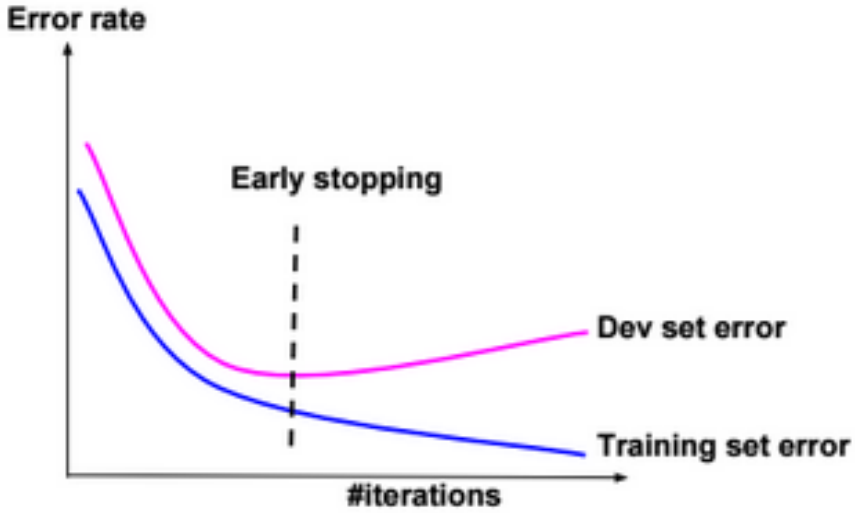

✓ Early Stopping

- The error on the validation set begins to rise
- If the training is unsuccessful, for example in a case where the error rate increases gradually over several iterations.
- If the training's improvement is insignificant, for example, the improvement rate is lower than a set threshold

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- ✓ Regularization
  - Involves slight modification in the error function
  - Add a term to the error function, which is intended to decrease the weights and biases, smoothing outputs and making the network less likely to overfit
  - Properly tune performance ration (γ) between 0 and 1,so that network will not overfit
  - Make self adaptive performance ration (γ), so that network will perform well
- ✓ Dropout
  - Kill some percentage of hidden neurons in each training iteration

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Methods to Avoid under fitting in Neural Networks

- ✓ Increase complexity of neural network
  - Increase number of hidden layers
  - Increase number of input neurons [Keep less or zero dropout]
- ✓ Improve training set
  - Increase number of samples
  - Increase variance in the training set
- ✓ Regularization
  - Keep low (zero or appox.zero) regularization performance ratio

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Kohonen Self Organizing Maps

- The Self-Organizing Map was developed by professor Kohonen. The SOM has been proven useful in many applications
- One of the most popular neural network models. It belongs to the category of competitive learning networks.
- Use the SOM for clustering data without knowing the class memberships of the input data. The SOM can be used to detect features inherent to the problem and thus has also been called SOFM, the Self-Organizing Feature Map.

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Kohonen Self Organizing Maps Cont.

- The weights are adjusted such that topology closed output nodes sense similar inputs. This is called as self organizing.

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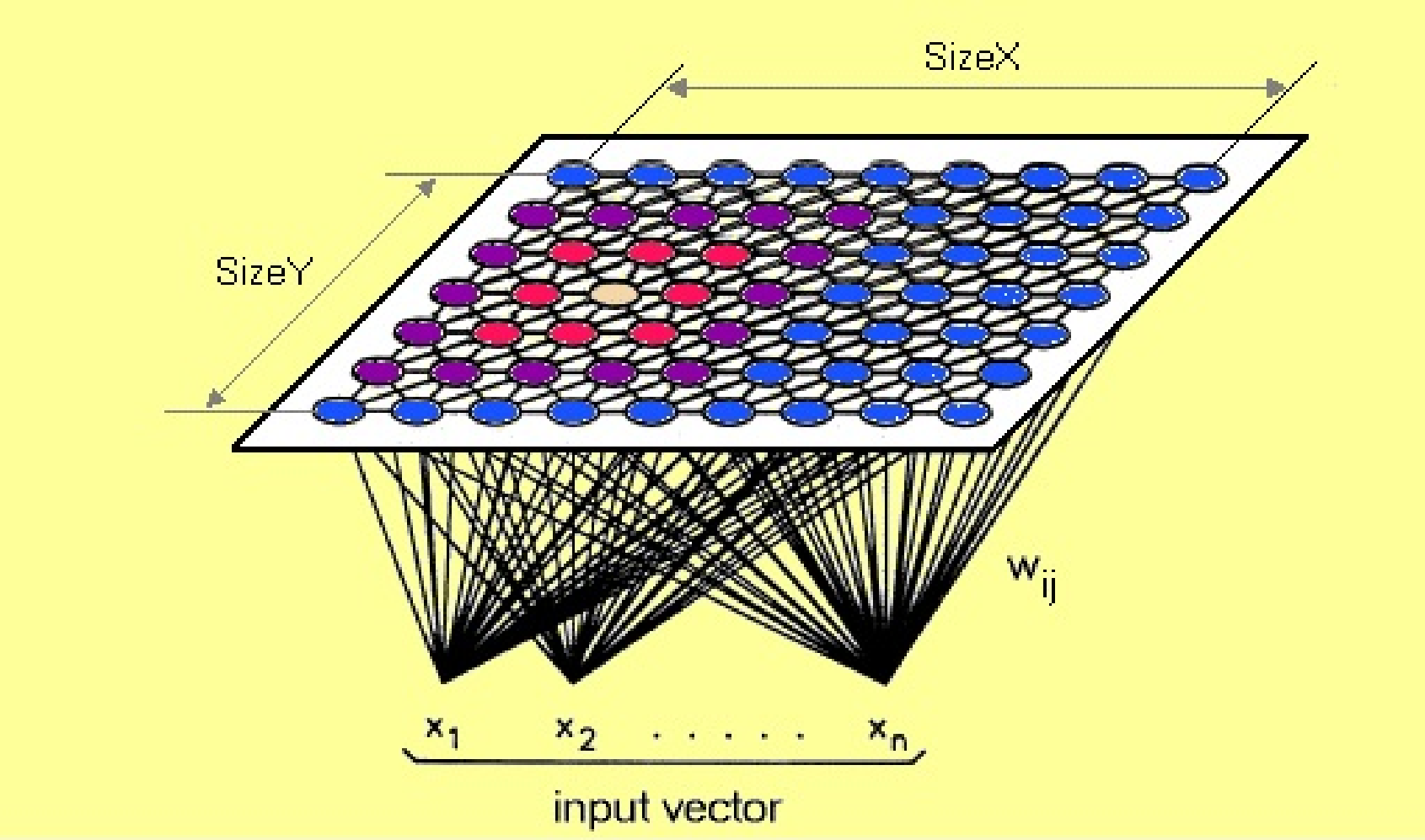

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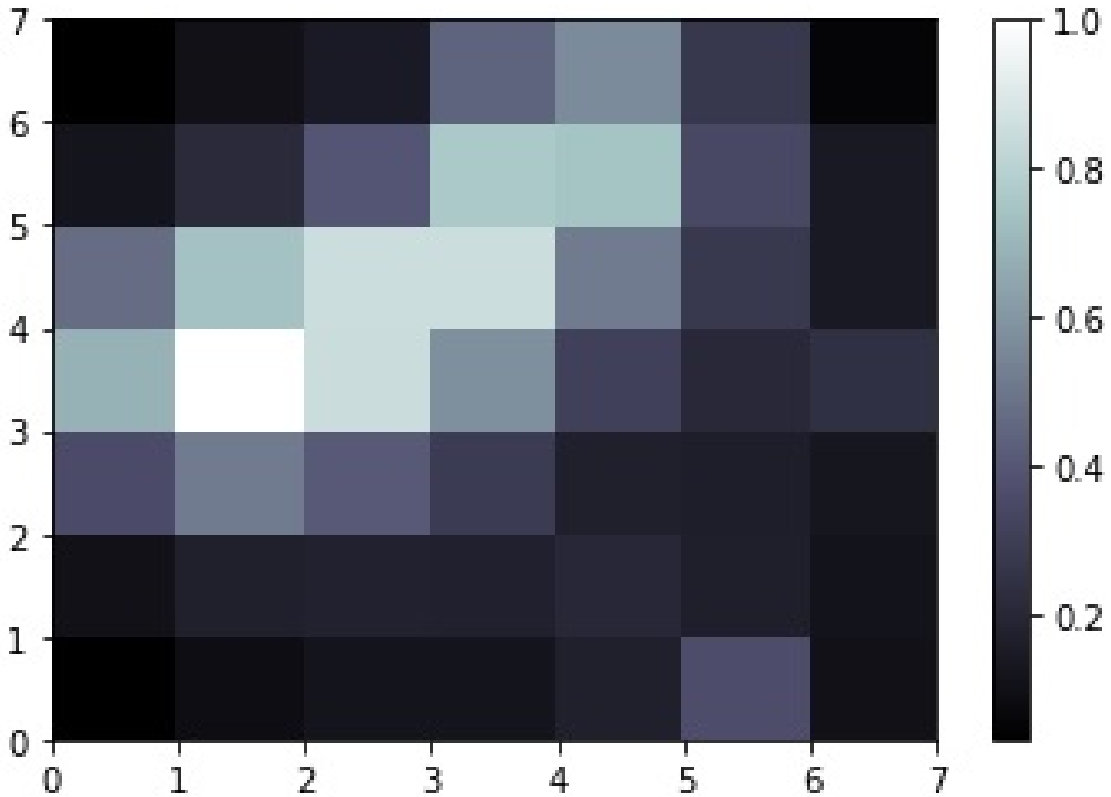
Clustering Data



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SOM Algorithm

Step-1 Initialize the weights between input and output layers W_{ij}

Step-2 Set input radius N_c and learning rate η

Step-3 Present input pattern to the network and calculate euclidean distance using equation (71)

$$ED_j = \sqrt{\sum_{i=1}^{n_f}(X_{pi} - Wji)} \qquad (71)$$

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Step-4 Update the weights connected to winning neuron using equations (72) and (73)

$$\Delta W_{ij} = \eta(X - W_{ij}^{WinningNeuron}) \quad (72)$$

$$W_{ij}^{WinningNeuron} = W_{ij}^{WinningNeuron} + \Delta W_{ij} \quad (73)$$

Winning neuron is the neuron which has minimum euclidean distance

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Step-5 Repeat Steps 3 and 4 for all patterns

Step-6 For every 10 iterations update radius **until** N_c **= 0** and learning rate using equations (74) and (75). and repeat steps 3 and 4

$$N_c = N_c - 1 \tag{74}$$

$$\eta = \eta - 0.02 \tag{75}$$

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Example for K-SOM

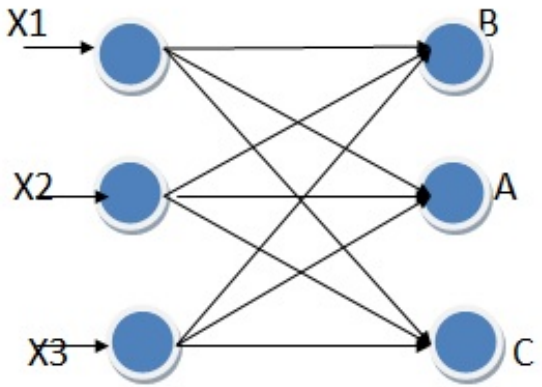

Table 1 : Input Patterns

Pattern	X1	X2	X3
1	1.1	1.7	1.8
2	0	0	0
3	0	0.5	1.5
4	1	0	0
5	0.5	0.5	0.5
6	1	1	1

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Random Weight Matrix

Table 2 : Random Weight Matrix

	1	2	3
W_a	0.2	0.7	0.3
W_b	0.1	0.1	0.9
W_c	1	1	1

Neighborhood Radius

Iteration=1 : D(t)=1

Iteration $>$ 1: D(t)=0

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Learning rate

Iteration 1, η=0.6
Iteration 2, η==0.25
Iteration>2 η=0.1

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Results

Iter	Pattern	ED_A	ED_B	ED_C	η	D(t)
1	1.1,1.7,1.8	2.01	2.09	**1.06**	0.6	1
1	0,0,0	1.91	**0.911**	2.308	0.6	1
1	0,0.5,1.5	**1.06**	1.22	1.403	0.6	1
1	1,0,0	1.48	**1.47**	1.819	0.6	1
1	0.5,0.5,0.5	**0.337**	0.397	1.06	0.6	1
1	1,1,1	0.927	0.957	**0.646**	0.6	1

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Results

Iter	Pattern	ED_A	ED_B	ED_C	η	D(t)
2	1.1,1.7,1.8	1.413	1.978	**1.231**	0.25	0
2	0,0,0	1.365	**0.795**	2.264	0.25	0
2	0,0.5,1.5	1.116	1.243	**1.077**	0.25	0
2	1,0,0	1.104	**0.737**	1.989	0.25	0
2	0.5,0.5,0.5	0.501	**0.39**	1.305	0.25	0
2	1,1,1	**0.37**	1.097	0.809	0.25	0

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Results

Iter	Pattern	ED_A	ED_B	ED_C	η	D(t)
2	1.1,1.7,1.8	1.326	2.13	**0.899**	0.1	0
2	0,0,0	1.456	**0.689**	2.118	0.1	0
2	0,0.5,1.5	1.133	1.33	**0.887**	0.1	0
2	1,0,0	1.177	**0.637**	1.992	0.1	0
2	0.5,0.5,0.5	0.591	**0.372**	1.296	0.1	0
2	1,1,1	**0.278**	1.139	0.804	0.1	0

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Loss Functions

- **Mean Absolute Error (MAE) :**

$$MAE = \frac{\sum_{i=1}^{n} |y^{actual,i} - y^{Predicted,i}|}{n} \tag{76}$$

- **Mean Square Error (MSE) :**

$$MSE = \frac{\sum_{i=1}^{n} (y^{actual,i} - y^{Predicted,i})^2}{n} \tag{77}$$

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Loss Functions

- **Mean Absolute Percentage Error (MAPE) :**

$$MAE = \frac{\sum_{i=1}^{n} |y^{actual,i} - y^{Predicted,i}|/y^{actual,i}}{n} * 100 \quad (78)$$

- **Root Mean Square Error (RMSE) :**

$$MSE = \sqrt{\frac{\sum_{i=1}^{n} (y^{actual,i} - y^{Predicted,i})^2}{n}} \quad (79)$$

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References

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