

a:
 $T(n) = 9T(n/3) + n^2$ so $a = 9$, $b = 3$ and $f(n) = n^2$
 Is $n^2 = \Theta(n^{\log_3(9)})$? [Rule 2]
 Is $n^2 = \Theta(n^2)$? True.
 $\therefore T(n) = \Theta(n^2 \log n)$

b:
 $T(n) = 4T(n/2) + 100n$ so $a = 4$, $b = 2$ and $f(n) = 100n$
 Is $100n = O(n^{\log_2(4)-\epsilon})$? [Rule 1]
 Is $100n = O(n^{2-\epsilon})$? True.
 $\therefore T(n) = \Theta(n^2)$

c:
 $T(n) = 2^n T(n/2) + n^3$ so $a = 2^n$, $b = 2$ and $f(n) = n^3$
 a is not constant \therefore Master Theorem cannot be applied.

d:
 $T(n) = 3T(n/3) + cn$ so $a = 3$, $b = 3$ and $f(n) = cn$
 Assuming c is constant term then Master Theorem can be applied.
 Is $cn = \Theta(n^{\log_3(3)})$? [Rule 2]
 Is $cn = \Theta(n)$? True.
 $\therefore T(n) = \Theta(n \log n)$

e:
 $T(n) = 0.99T(n/7) + 1/(n^2)$ so $a = 0.99$, $b = 7$ and $f(n) = 1/(n^2) = n^{-2}$
 Master Theorem can be applied if $a \geq 1$.
 $a = 0.99 \therefore$ Master Theorem cannot be applied.