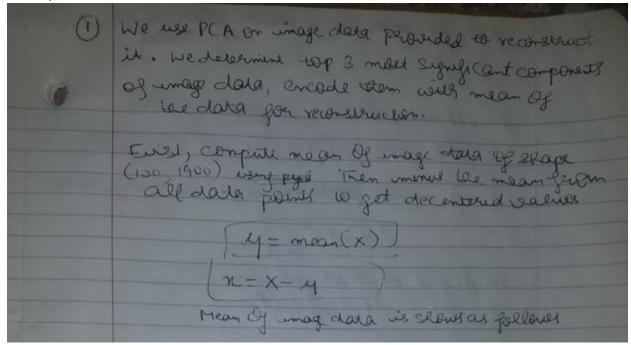
## **Ans 1:** MATLAB Code:

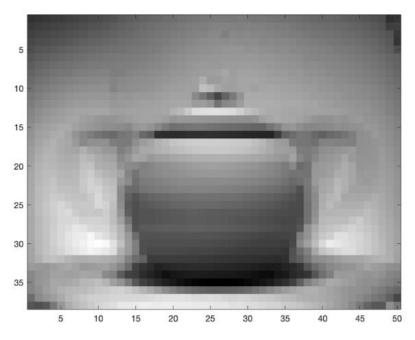
```
load('teapots.mat')
teapot_data = teapotImages;
m = mean(teapot data);
X = teapot data - m;
C = cov(X);
[V, D] = eig(C);
[d, ind] = sort(diag(D), 'descend');
d = d(1:3,:);
v = V(:,ind(1:3));
c = X*v;
X hat = m+c*v';
%10 images
for i = 11:20
    figure(i);
    colormap gray;
    subplot(1,2,1);
    imagesc(reshape(teapot_data(i,:),38,50));
    title('Before Recon');
    axis image;
    subplot(1,2,2)
    imagesc(reshape(X_hat(i,:),38,50));
    title('After Recon');
    axis image;
end
norm(teapot_data-X_hat)
load('teapots.mat')
X = teapotImages;
[coefficient_of_3, score3] = pca(X,'Algorithm','eig','Rows','all','NumComponents',3);
Xhat3 = mean(X)+score3*coefficient_of_3';
[coefficient_of_6, score6] = pca(X,'Algorithm','eig','Rows','all','NumComponents',6);
Xhat6 = mean(X)+score6*coefficient of 6';
[coefficient_of_32, score32] =
pca(X,'Algorithm','eig','Rows','all','NumComponents',32);
Xhat32 = mean(X)+score32*coefficient_of_32';
figure(1);
colormap gray;
subplot(2,2,1);
imagesc(reshape(data(10,:),38,50));
title('Before');
axis image;
subplot(2,2,2)
imagesc(reshape(Xhat3(10,:),38,50));
title('TOP3');
axis image;
subplot(2,2,3)
imagesc(reshape(Xhat6(10,:),38,50));
```

```
title('TOP6');
axis image;
subplot(2,2,4)
imagesc(reshape(Xhat32(10,:),38,50));
title('TOP32');
axis image;
Python code for determining Eigenvalues:
import numpy as np
import matplotlib.pyplot as plt
from numpy.linalg import eig
from scipy.io import loadmat
if __name__=='__main__':
    data = loadmat('teapots.mat')
    X = data['teapotImages']
    u = np.mean(X, axis=0).reshape(1,1900)
    x = X - np.repeat(u, 100, axis=0)
    C = x.T.dot(x)/(x.shape[0]-1)
    D, V = eig(C)
    print(x.shape)
    print(C)
    print(D[:3])
    print(V[:,:3])
```

-----

Writeup:





Then, find cosavance motion of data of stape (100,1900).

C = cos(n) = x<sup>T</sup>n which los downt (1900,1900).

Apply Expensible Decomptitude to covariance making to find with mallier mallier and product with expensable on the chappened A

C = V NV-1

Delevant with expension of the chappened A

Re cost matrix is expensable and 120state definite expensables are all non-negative and 120state definite expensables are all non-negative are.

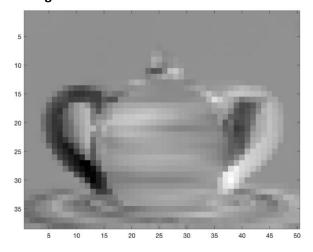
Top 3 most expension expensable are.

[4.2150, 3.0168, 2.0493]

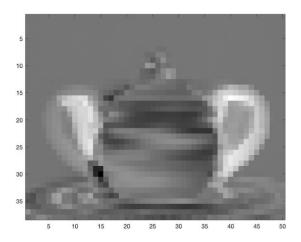
cach with corresponding expensable are.

Each eigenistelle can be shown as an emigh, depicted below

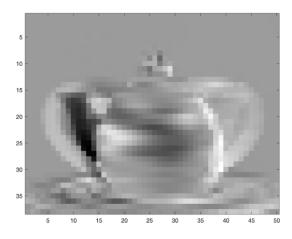
Eigen Value=4.2150

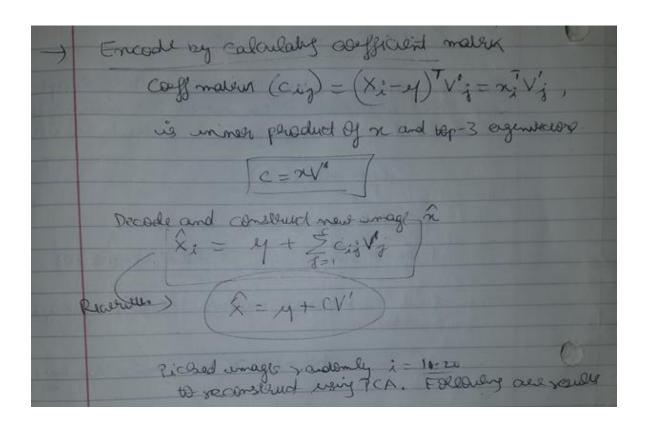


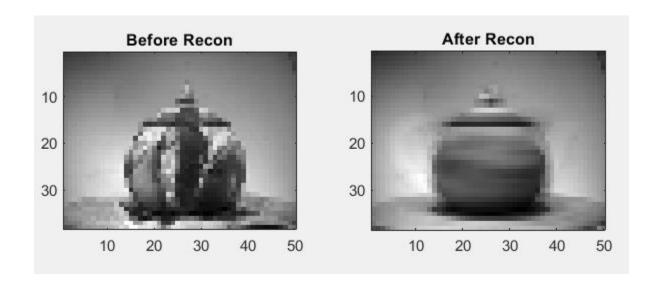
Eigen Value: 3.0168

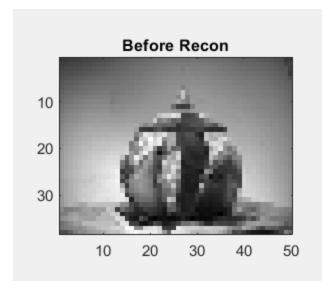


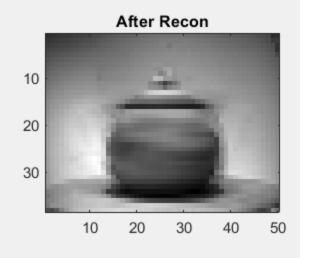
Eigen Value: 2.0993

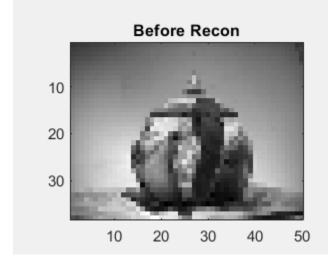


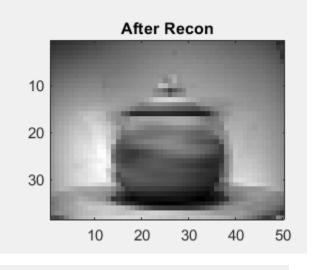


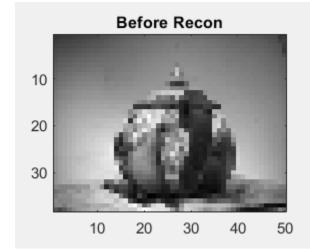


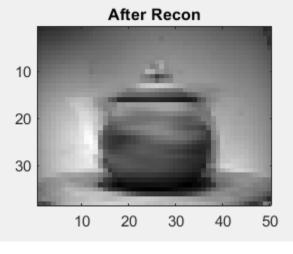


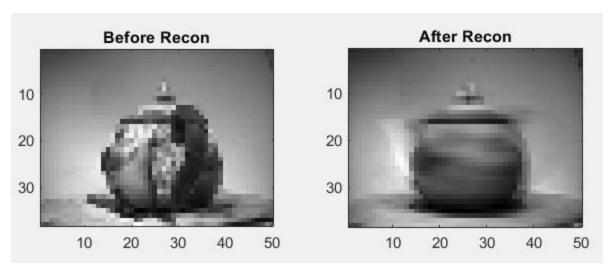


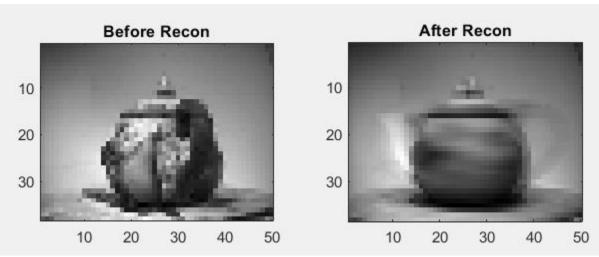


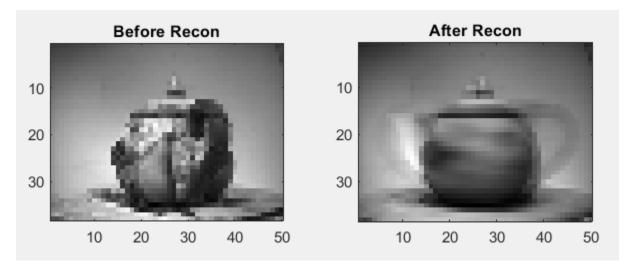


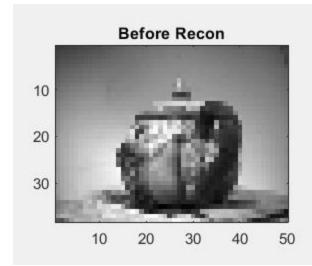


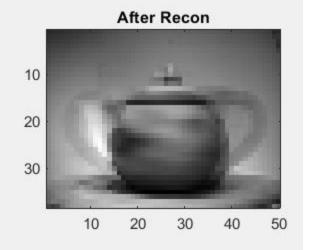


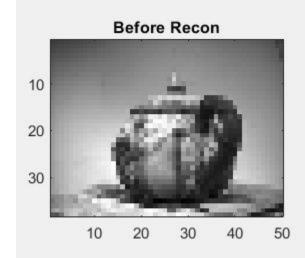


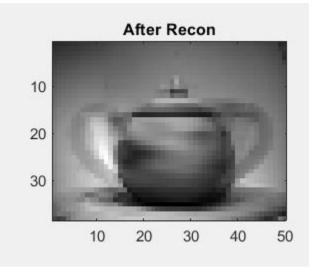


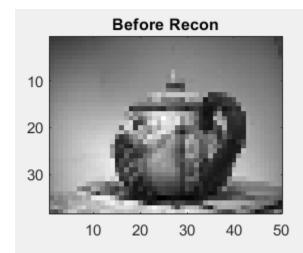


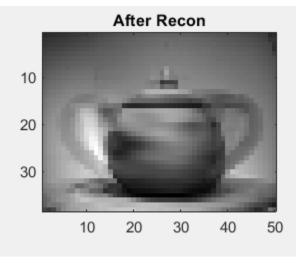










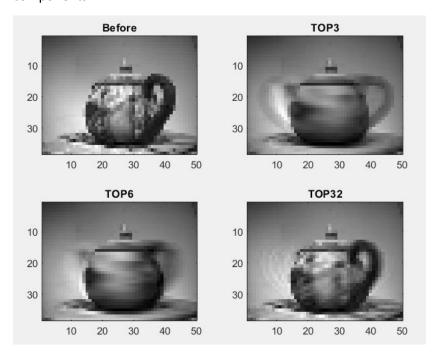


As observed, some images are well reconstructed and distinguishable but many others appear to be not that well reconstructed. Only top 3 components are sharp/aggressive. As per Eigenvalue decomposition, 32 values are more than 0.1, and 6 values are higher than 1. Decoding with more components could get a better reconstruction.

Performance of PCA encoder is determined by computing L-2 norm of X and X hat. The outcome number is 13.6262.

By picking top-6 components, norm value goes down to 9.8303; by picking top 6 component, norm reduces to 3.1382.

Following are snips of image data encode/decode with top 3, top 6 and top 32 most significant components.



Encoding more components into reconstruction gives better outcome with detailing. Deciding on how many most significant components we pick comes down to the requirements of the problem, item in question and how main feature is defined.

Ans 2:

VBZ182 HWY  BOX 1 8 applies, 4 oranges 10 applies, 2 oranges  Applies soluted =, Protability of sollicing a Sidx  P(E,) = P(Ez) = 1/2
Apple solated - Procability of solecting a Sux
Apple soluted = Probability of sollicing a Sidx $P(E) = P(E_Z) = V_Z$
A. Solerin Apple form por
P(NE) = 8/12 = 2/3; P(A/E2) = 10/12 = 5/6
Applying Bayes' Orebram.
P(E/A)- P(E) D(A/E)
$\frac{P(\varepsilon_1) \times P(A/\varepsilon_1) + P(\varepsilon_2) \times P(A/\varepsilon_2)}{V(\times 2/3)} = \frac{1}{2} - \frac{1}{2} - \frac{1}{2}$
$= \frac{1}{2} \times \frac{2}{3} + \frac{1}{2} \times \frac{5}{3} + \frac{1}{2} \times \frac{5}{3} + \frac{5}{2} \times \frac{1}{3} + $

## Ans 3:

Each close is Gaussian  0 = 20, 11, 21, 12, 22 }  close probability sin Boundall' distribute  P(y/0) = 0 of (1-0) of  Posability of detap((x/y,0) = N(x/4,2y).  Use man absorbed for x, 11's and 2's.  HMG = augmax N(  Lebourhood forcest L = p(x/y,0) = N(x/4,2y).
For, MLE of Grandlan model, we would to find good estimated of y & E  MMIE = argmax N(x   My, Zy)  ZMIE = argmax N(n   My, Zy)
we need to got best parameter of for a go Caucia  Once organist log (Monty, o  - organ log (Norty, o))
Seg (N(n/y,0)) = \$\gamma\left(\sigma\left(\maximu\) \\ \n=1 \[ \left(\sigma\left(\maximu\) \\ \n=1 \]  \[ \left(\maximu\) \\ \n=1 \]  \[ \left(\sigma\left(\maximu\) \\ \n=1 \]  \[ \left(\sigma\left(\maximu\) \\ \n=1 \]  \[ \left(\maximu\) \\ \n=1 \]  \[ \left(\sigma\left(\maximu\) \\ \n=1 \]  \[ \left(\maximu\)
es full observance makin & god replaced by a diagonal placemance vector of the (N(xky, Eg)) = Slog (N(xky, Eg))

