

Numerical Linear Algebra



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Pseudocode for LU Decomposition Method

Step – 1:

`n = size(A)`

`L = create_identity_matrix(n)`

`U = create_empty_matrix(n, n)`

Step – 2: Apply Decomposition on Matrix A :

for k from 1 to n:

$U[k][k] = A[k][k]$

for i from k+1 to n:

$L[i][k] = A[i][k] / U[k][k]$

$U[k][i] = A[k][i]$

end

for i from k+1 to n:

for j from k+1 to n:

$A[i][j] = A[i][j] - L[i][k] * U[k][j]$

end

end

end

return L, U

Step – 3:

`n = size(L)`

`y = create_empty_vector(n)`

`x = create_empty_vector(n)`

Step – 4: Forward Substitution to Solve $Ly = b$

for i from 1 to n:

$$y[i] = b[i]$$

for j from 1 to i-1:

$$y[i] = y[i] - L[i][j] * y[j]$$

end

$$y[i] = y[i] / L[i][i]$$

end

Step – 5: Backward Substitution to Solve $Ux = y$:

for i from n to 1 step -1:

$$x[i] = y[i]$$

for j from i+1 to n:

$$x[i] = x[i] - U[i][j] * x[j]$$

end

$$x[i] = x[i] / U[i][i]$$

end

Step – 6: Stop

Assignment – 2:

Q1. What is the worst-case running time of the LU Decomposition Method for an n -by- n matrix in terms of computational complexity notation?

Q2. Compare the running time between Gauss Elimination and LU Decomposition Methods.

Q3. Which method is better? Why?

Solving $Ax = b$ Using LU Decomposition in Julia

Import the LinearAlgebra library

Command: using LinearAlgebra

Define the coefficient matrix A and the right-hand side vector b

Command: A = [2.0 1.0 -1.0;
 -3.0 -1.0 2.0;
 -2.0 1.0 2.0]

Command: b = [8.0, -11.0, -3.0]

Perform LU decomposition

Command: `lu_result = lu(A)`

Extract the L and U matrices from the result

Command: `L = lu_result.L`

Command: `U = lu_result.U`

Solve for y in $Ly = b$ using forward substitution

Command: $y = L \setminus b$

Solve for x in $Ux = y$ using backward substitution

Command: $x = U \setminus y$

Display the solution

Command: `println("Solution x:")`

Command: `println(x)`

Thank You