



FINAL REPORT

**Project name: Using seasonal model and missing data estimation
to forecast Ceramic Store Revenue in Time series analysis**

Group: 9

Class: A01E

Instructor: MsC. Ngo Thuan Du

Ho Chi Minh city, Thursday 30th October 2025

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I. INTRODUCTION

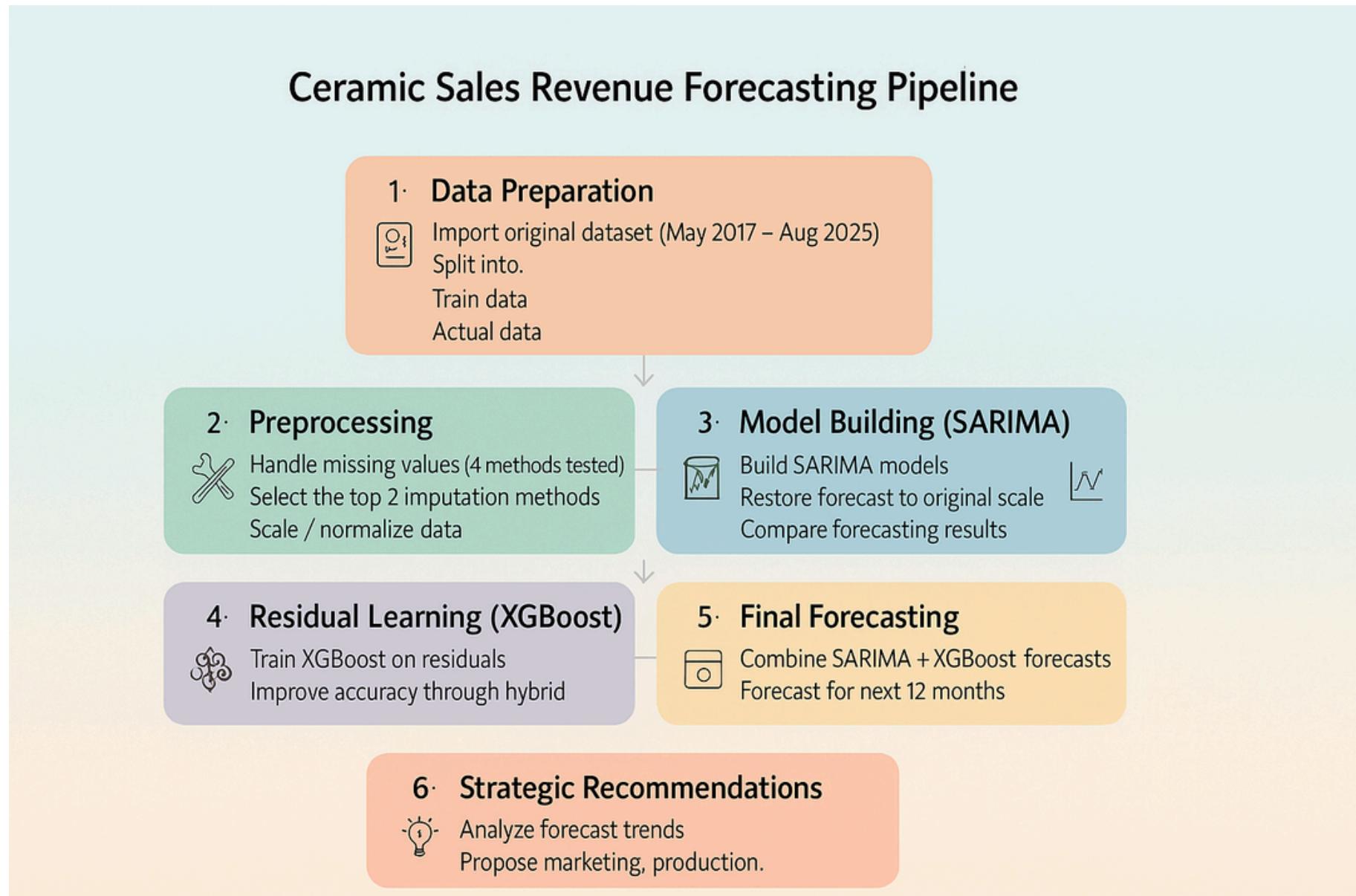
1. Reason for Topic Selection: The ceramics industry is characterized by strong seasonality and significant fluctuations throughout the year. This necessitates that businesses accurately forecast revenue to proactively manage production and business operations.

2. Research Objectives:

- Develop and evaluate various ceramic revenue forecasting models to identify the model with the highest accuracy.
- Apply the forecasting results to support businesses in planning production, distribution, and business strategies according to seasonal cycles.

3. Tool Used: R

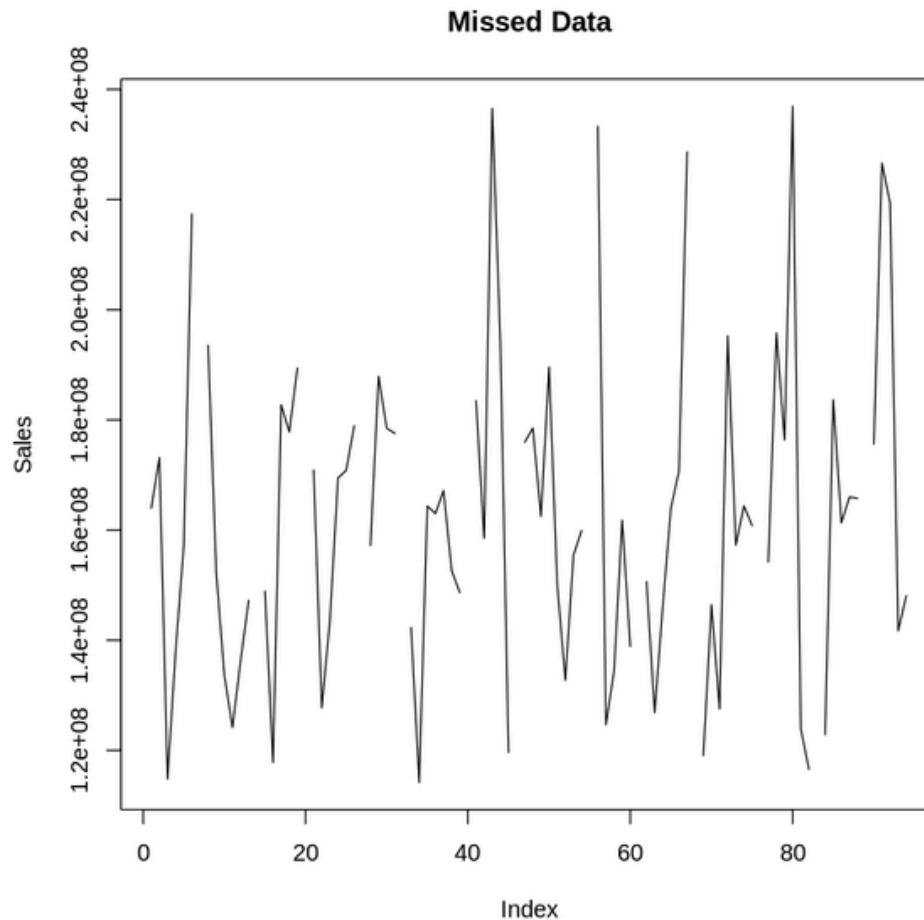
IMPLEMENTATION PROCESS:



Pipeline diagram showing the steps in order

II. IMPLEMENTATION PROCESS:

1. Handle missing values

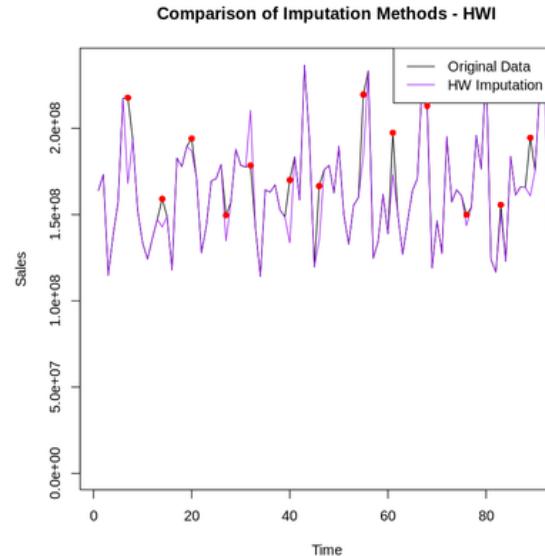
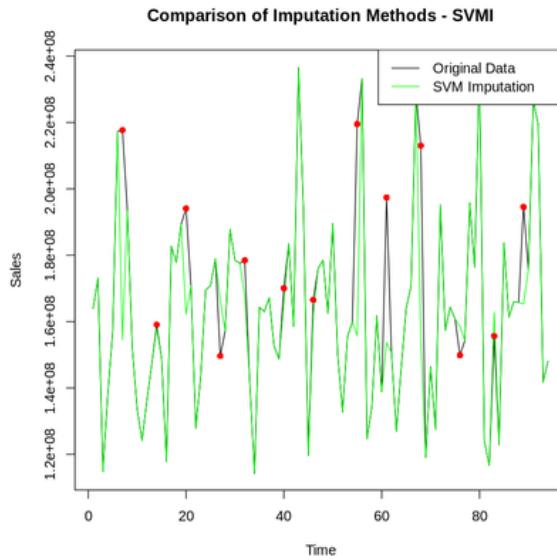
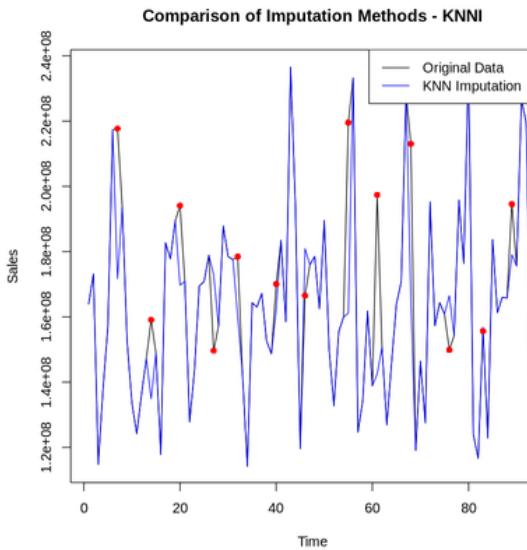
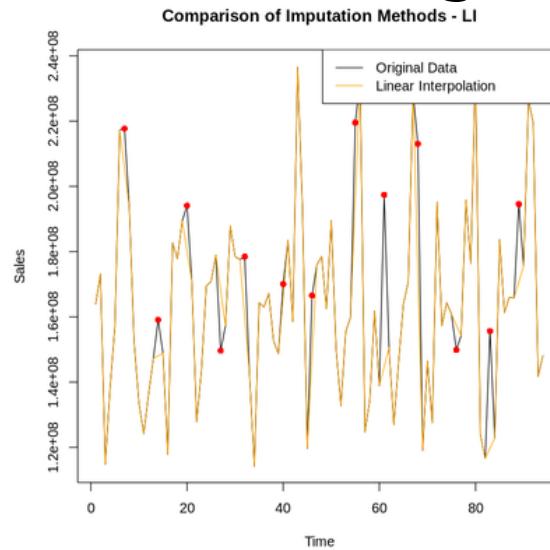


“Missed Data” Chart

- Gaps show missing (NA) values in Sales.
- Missing points appear uneven and periodic.
- Continuous data needed for ARIMA/ETS/Prophet.
- Visualization aids imputation and forecast stability.
- With missing percentage is 13.83%

II. IMPLEMENTATION PROCESS:

1. Handle missing values



SVMI and KNNI create excessive volatility, significantly distorting the original trend.

III. RESEARCH RESULT

```
[1] "Comparison of Imputation Methods (RMSE)
      Method      RMSE
1   Linear Interpolation 25211067
2   KNN Imputation 32357125
3   SVM Imputation 34911481
4 Holt-Winters Based Imputation 26813983
```

Linear Interpolation (LI) and Holt-Winters (HW) are the two most effective imputation methods, achieving significantly lower error metrics compared to KNN Imputation (32.36M) and SVM Imputation (34.91M).

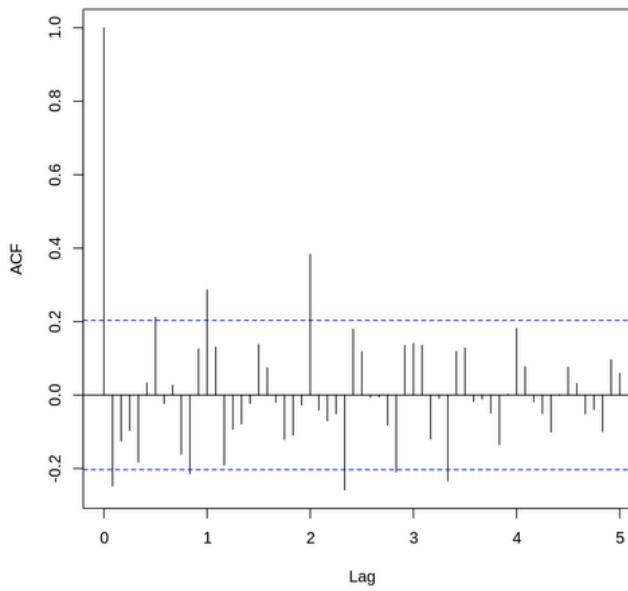
$$Z = \frac{x - \text{mean}}{\text{sd}}$$

```
[1] "Scaled LI Imputed Data (first 10):"
[1,] 0.04816805
[2,] 0.36892683
[3,] -1.66806523
[4,] -0.85670943
[5,] -0.19317029
[6,] 1.91156707
[7,] 1.49556575
[8,] 1.07956443
[9,] -0.35925208
[10,] -1.00904240
[1] "Scaled HW Imputed Data (first 10):"
Jan      Feb Mar Apr      May      Jun      Jul
2017          0.04857962 0.36347055 -1.63625750
2018 -0.35138731 -0.98929060
Aug      Sep Oct      Nov      Dec
2017 -0.83974436 -0.18834377 1.87789027 0.18725752 1.06110800
2018
```

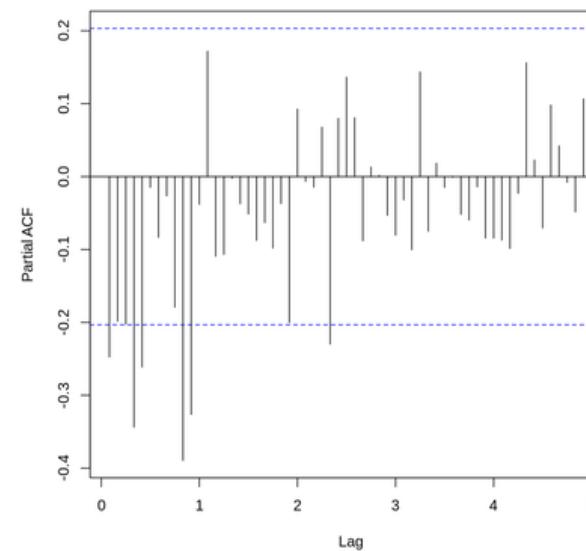
The values have been successfully scaled → suitable for proceeding with building and training the SARIMA forecasting model in the next step

RESEARCH RESULTS**Seasonal Data**

Graph of the ACF of D=1 IN LI

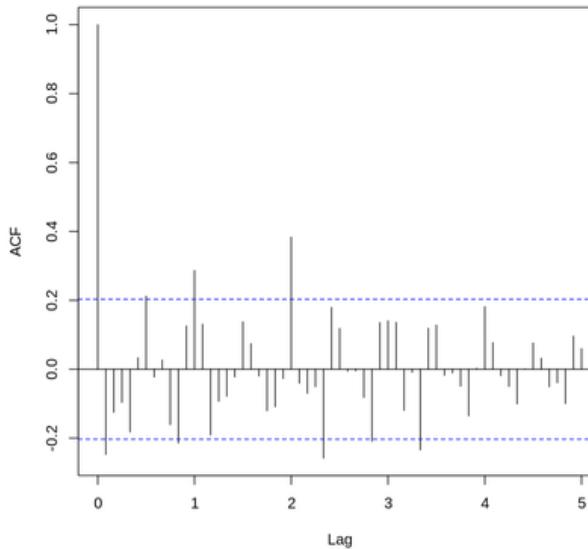


Graph of the PACF function at D=1 IN LI

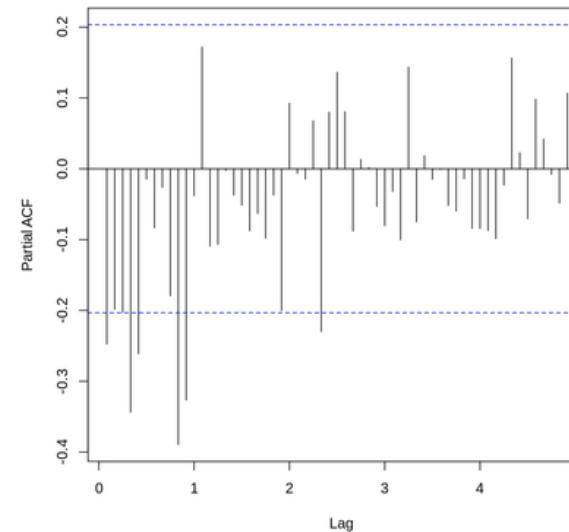


LI
Q = 1,2,3
P=1

Graph of the ACF of D=1 IN HWI



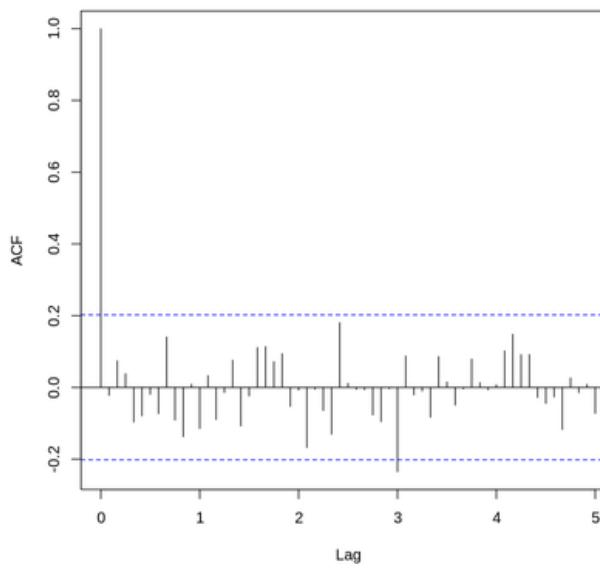
Graph of the PACF of D=1 IN HWI



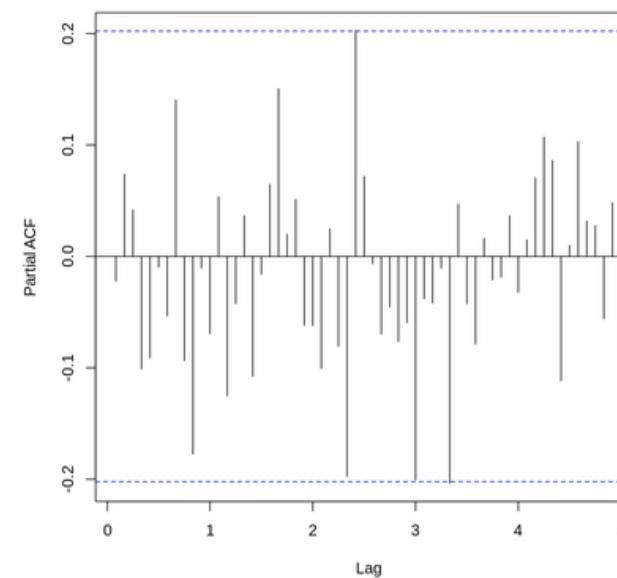
HWI
Q = 1,2,3,4
P = 1

RESEARCH RESULTS**Non-Seasonal Data**

Graph of the ACF function at d=0 IN LI

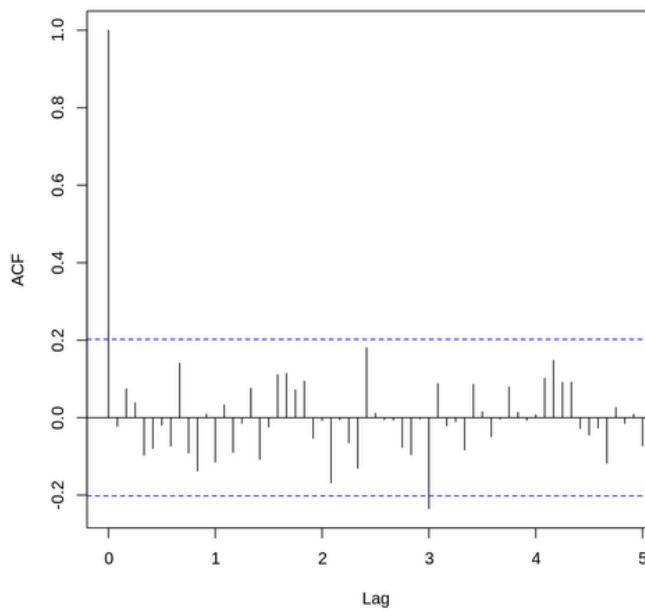


Graph of the PACF function at d=0 IN LI

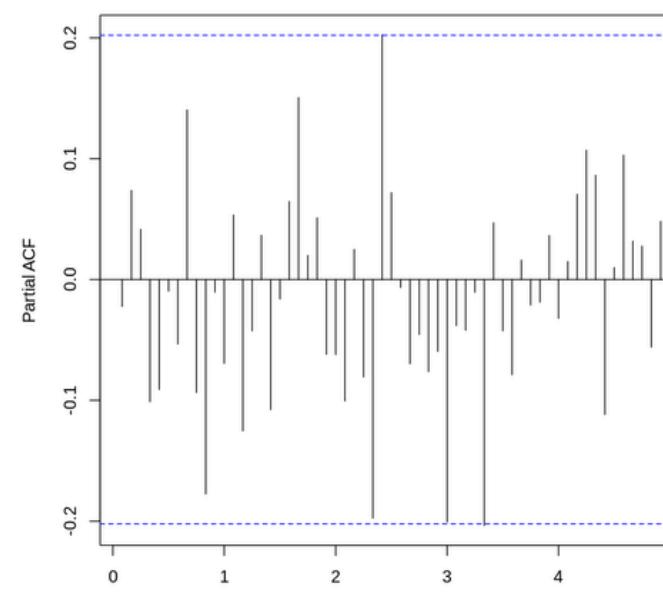


LI
 $q=3$
 $p=4$

Graph of the ACF function at d=0 IN HWI



Graph of the PACF function at d=0 IN HWI



HWI
 $q=3$
 $p=4$

RESEARCH RESULTS

L1 TIME

A data.frame: 6 × 2

	df	AIC
	<dbl>	<dbl>
MH1	10	201.5680
MH2	11	200.7935
MH3	12	198.9715
MH4	12	201.3156
MH5	13	203.2724
MH6	14	204.6986

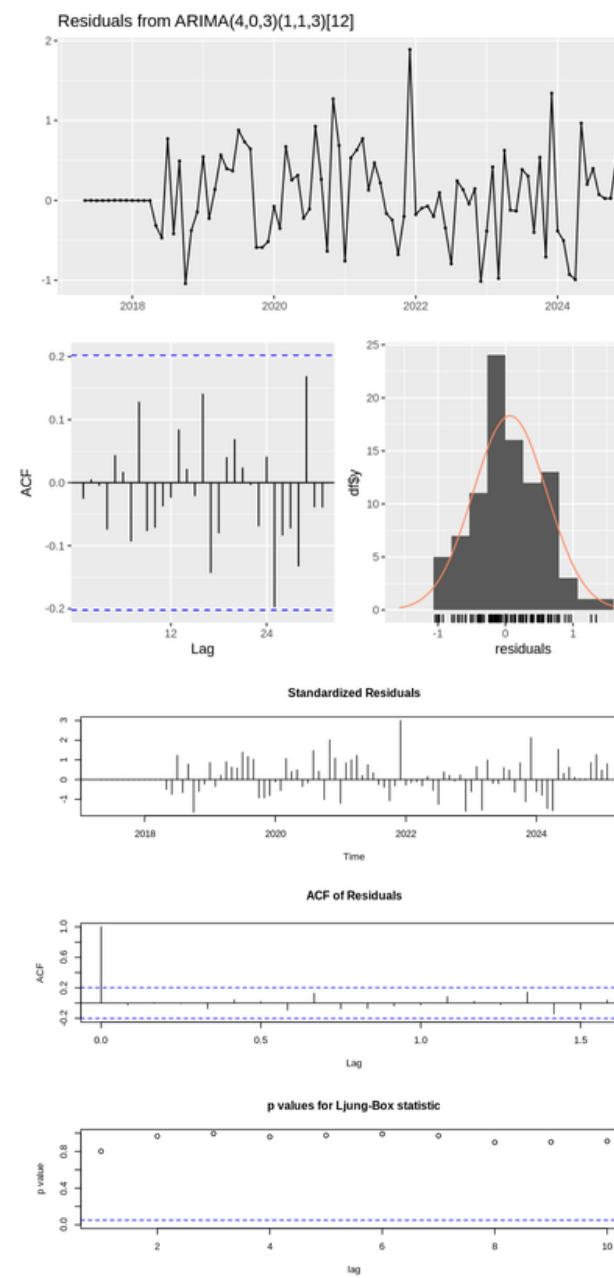
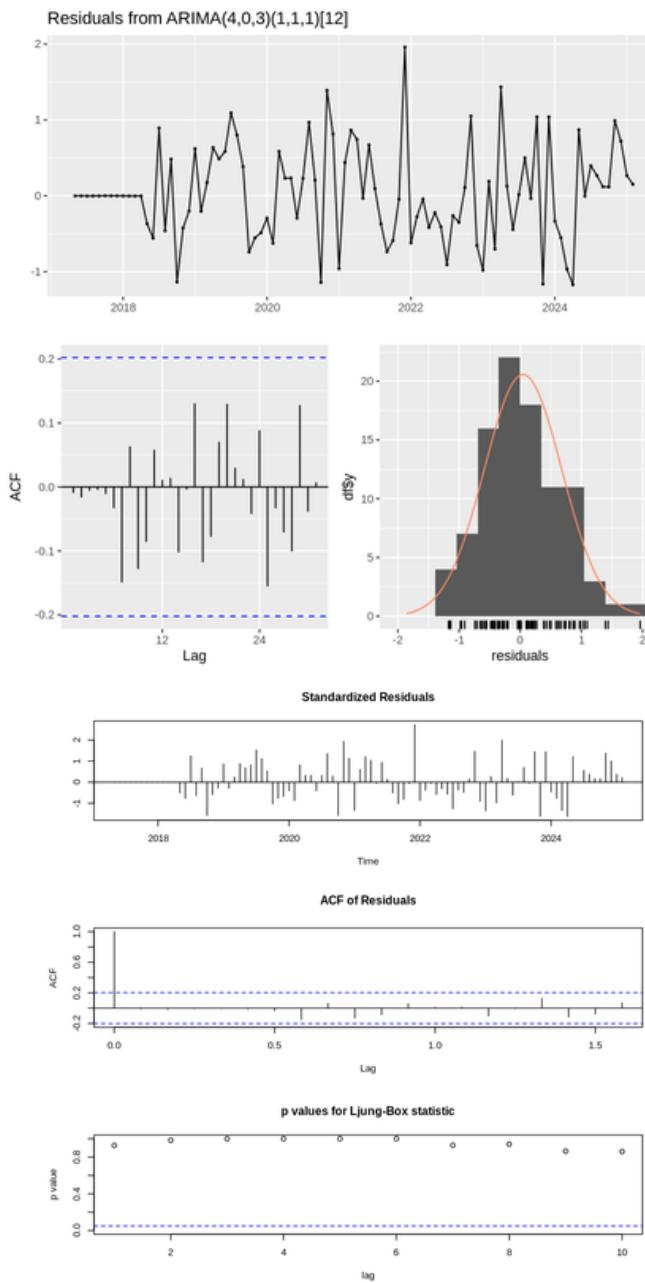
AIC: MH3
BIC: MH1

A data.frame: 6 × 2

	df	BIC
	<dbl>	<dbl>
MH1	10	225.6352
MH2	11	227.2674
MH3	12	227.8521
MH4	12	230.1962
MH5	13	234.5598
MH6	14	238.3927

RESEARCH RESULTS

LI TIME

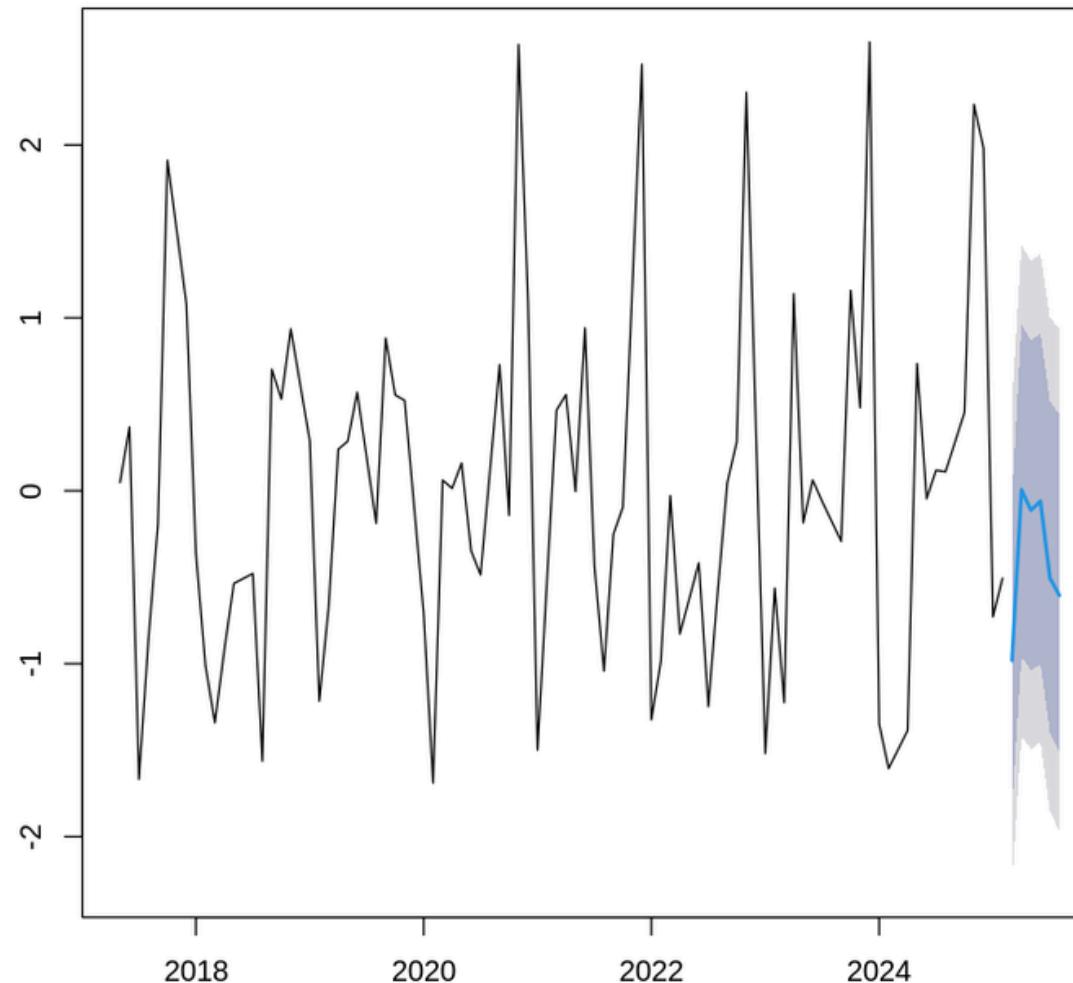


The SARIMA(4,0,3)
(1,1,1)[12] model
shows a slight
superiority

RESEARCH RESULTS

LI TIME

Forecasts from ARIMA(4,0,3)(1,1,3)[12]



The forecasting model is capable of capturing the variability and seasonality of the time series.

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RESEARCH RESULTS

HWI

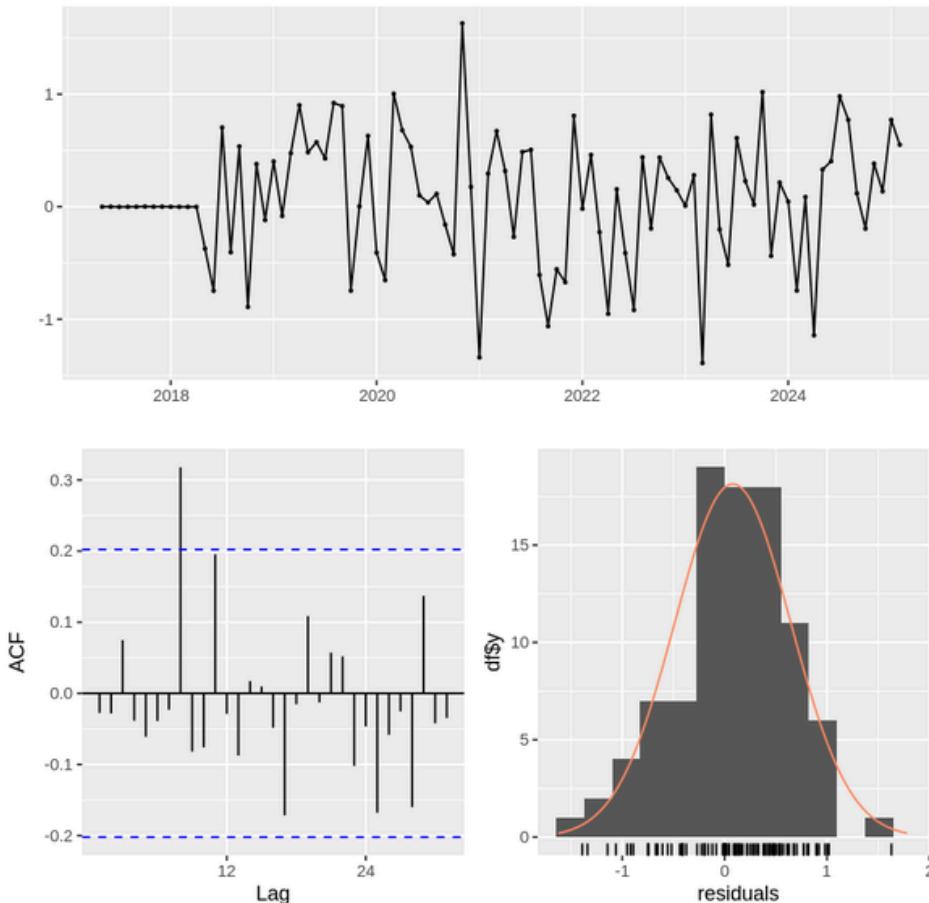
A data.frame: 20 × 2			A data.frame: 20 × 2		
	df	AIC		df	BIC
	<dbl>	<dbl>		<dbl>	<dbl>
HW1	5	170.3287	HW1	5	182.3623
HW2	6	171.5360	HW2	6	185.9763
HW3	7	171.0658	HW3	7	187.9129
HW4	8	172.7788	HW4	8	192.0326
HW5	6	172.1463	HW5	6	186.5866
HW6	7	171.9909	HW6	7	188.8380
HW7	8	173.0185	HW7	8	192.2723
HW8	9	174.3972	HW8	9	196.0576
HW9	7	173.8208	HW9	7	190.6679
HW10	8	174.8631	HW10	8	194.1169
HW11	9	173.2805	HW11	9	194.9410
HW12	10	174.6266	HW12	10	198.6938
HW17	7	173.7520	HW17	7	190.5990
HW18	8	174.9037	HW18	8	194.1574
HW19	9	174.5669	HW19	9	196.2274
HW20	10	175.9248	HW20	10	199.9920
HW25	9	174.4158	HW25	9	196.0763
HW26	10	175.1079	HW26	10	199.1751
HW27	11	172.8686	HW27	11	199.3425
HW28	12	175.9321	HW28	12	204.8128

AIC/BIC: HW1

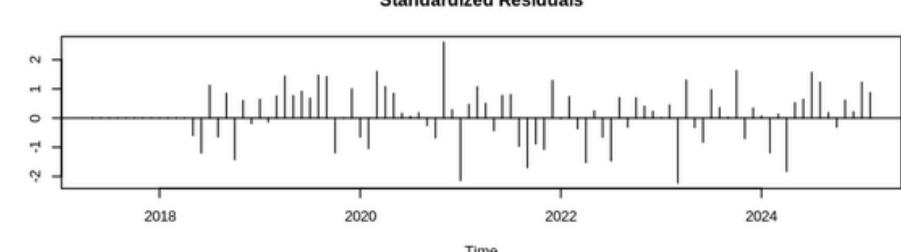
RESEARCH RESULTS

HWI

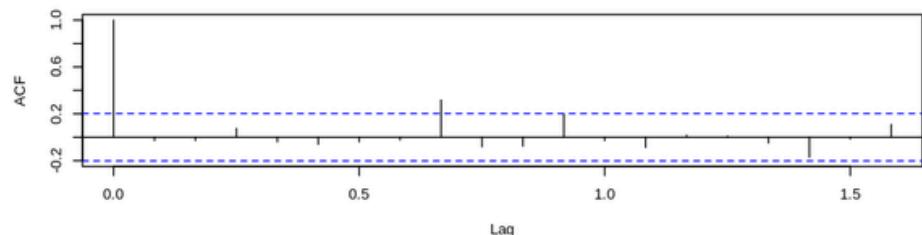
Residuals from ARIMA(1,0,1)(1,1,1)[12]



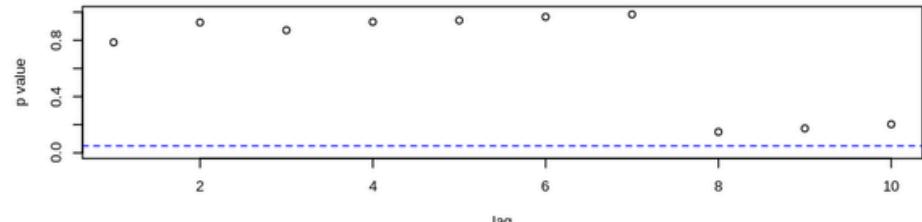
Standardized Residuals



ACF of Residuals



p values for Ljung-Box statistic

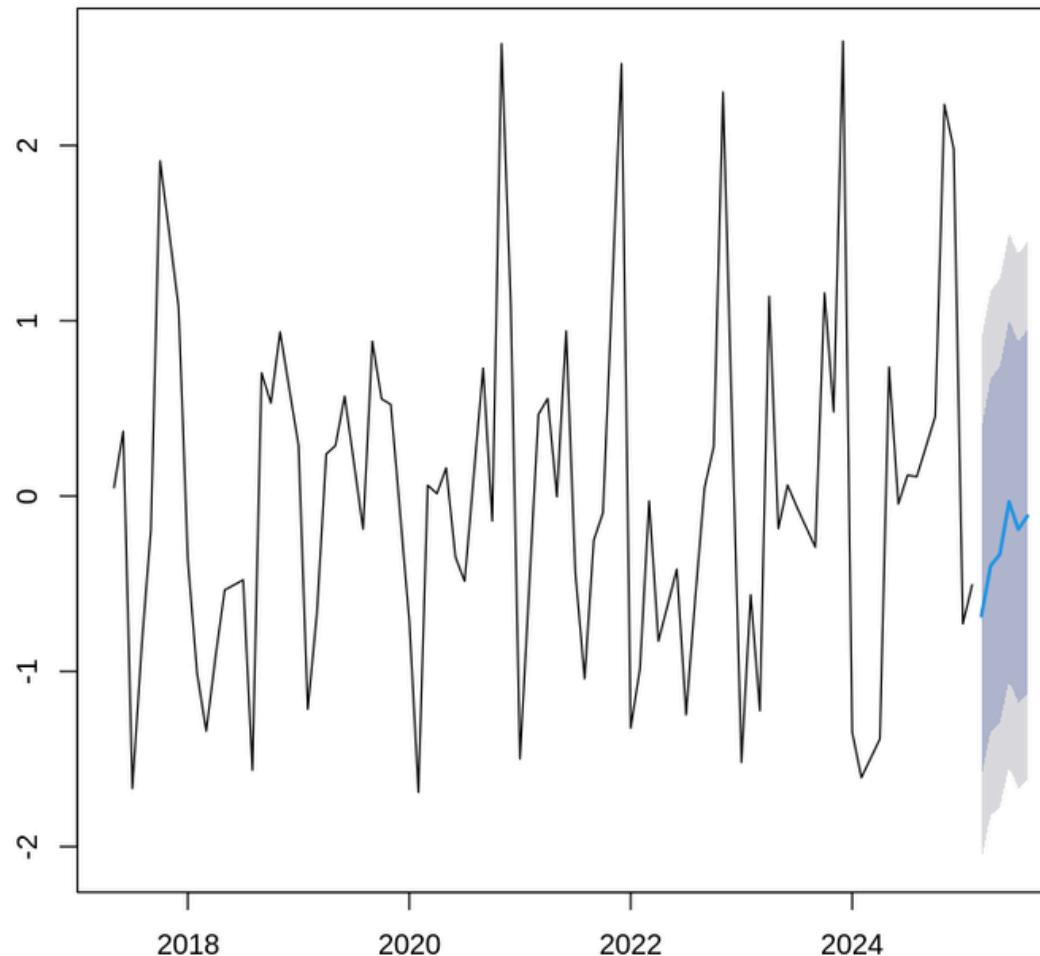


The SARIMA(1,0,1)(1,1,1)[12] model is appropriate and adequate for describing the time series, as the residuals are nearly white noise, indicating that the model has captured most of the data structure.

RESEARCH RESULTS

HWI

Forecasts from ARIMA(4,0,3)(1,1,1)[12]



The SARIMA(1,0,1)(1,1,1)[12] model provides good short-term forecasts, but the uncertainty increases rapidly.

RESEARCH RESULTS

[1] "Comparison of Actual and Forecast Values (starting March 2025):"				
	Datetime	Actual_Values	Forecast_LI	Forecast_HWI
1	2025-03-01	145399492	143001507	130103418
2	2025-04-01	157758923	151196176	173517020
3	2025-05-01	176006666	153055016	166310141
4	2025-06-01	182082611	161647008	166728412
5	2025-07-01	205509243	157160697	168849748
6	2025-08-01	236514347	159345408	151897607

- Both models failed to track the strong, accelerating growth in Actual_Values (especially May-Aug).
- Forecast_LI was too conservative (underestimated the trend).
- Forecast_HWI was volatile, with large errors (overestimated in April, failed at the August peak).

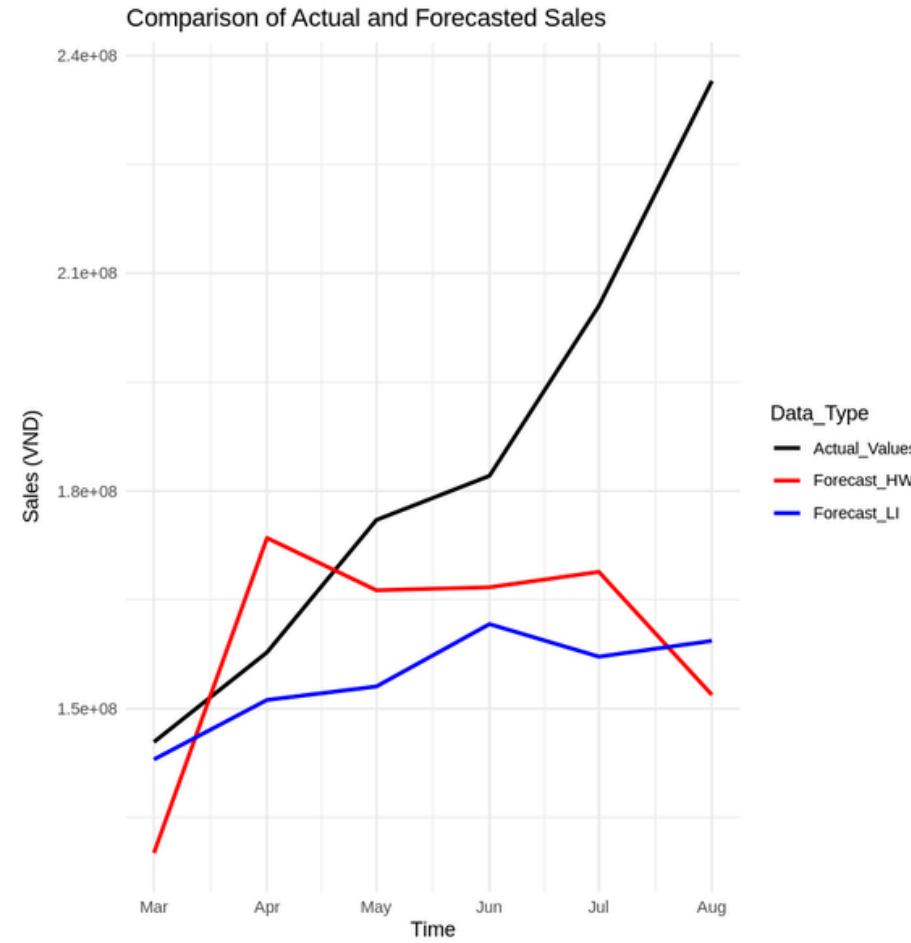
RESEARCH RESULTS

Table: Comparative Analysis of Revenue Forecasting Models

Models	MAE	RMSE	MAPE (%)
Linear Interpolation Forecast	39340054	29644245	14.37108
Holt-Winters Based Imputation Forecast	39403834	29563522	14.67757

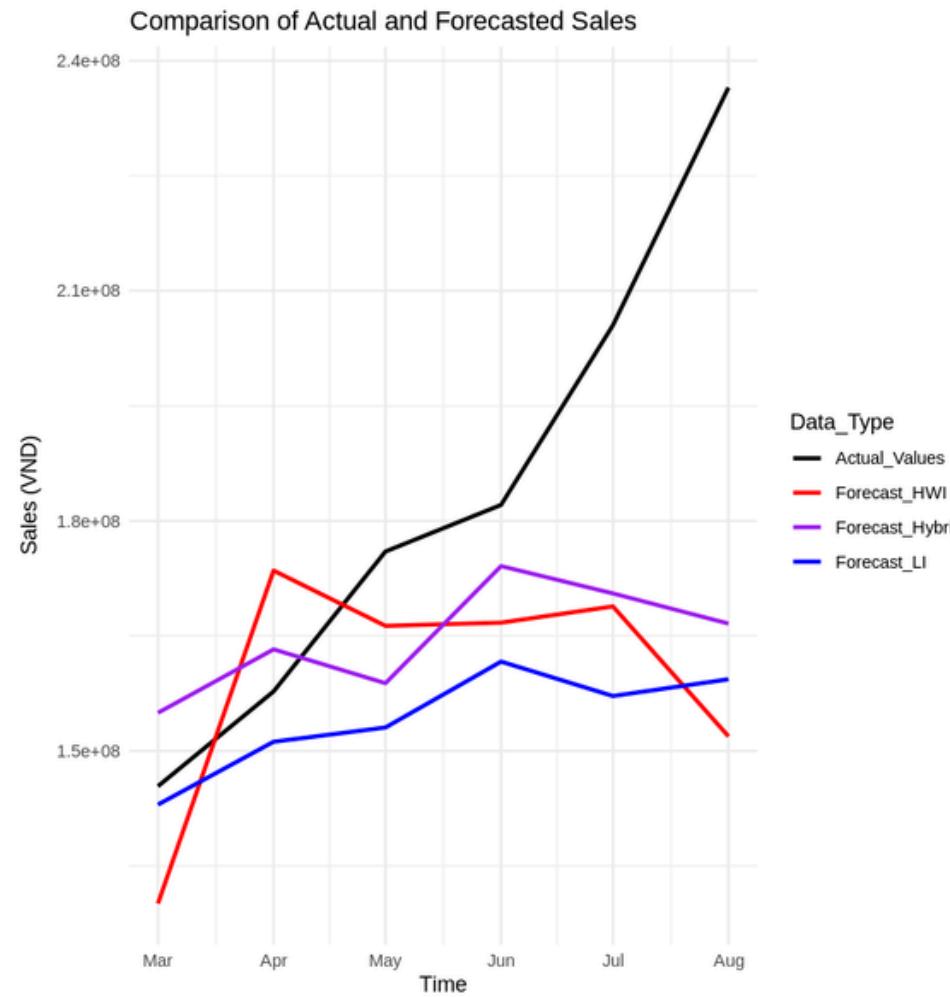
- Performance Comparison: The Linear Interpolation (LI) method demonstrated superior forecasting performance compared to Holt-Winters (HWI).
 - Error Metrics: LI achieved a lower RMSE and MAPE (14.37%) compared to HWI.
- Based on the error metrics, LI is the most suitable method for imputing missing values, ensuring the continuity of the revenue time series data.

RESEARCH RESULTS



- Both the LI and HWI forecast models significantly underestimate this growth rate, but LI exhibits a smoother and more stable trend.
- Based on the stability of the trend and associated error metrics, LI is the more optimal model compared to HWI for initial estimation.

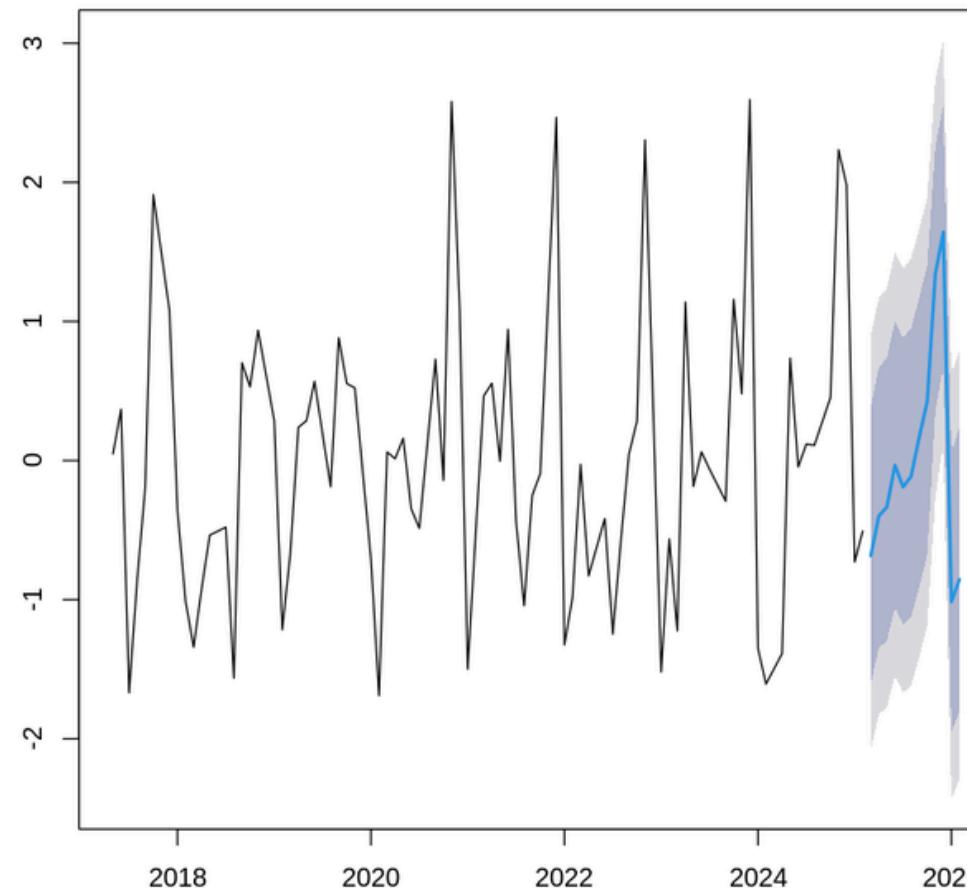
RESEARCH RESULTS



- Actual sales show a strong upward trend
- The Forecast_Hybrid model is the most accurate, closely tracking the general trend, significantly outperforming Forecast_HWI and Forecast_LI.

RESEARCH RESULTS

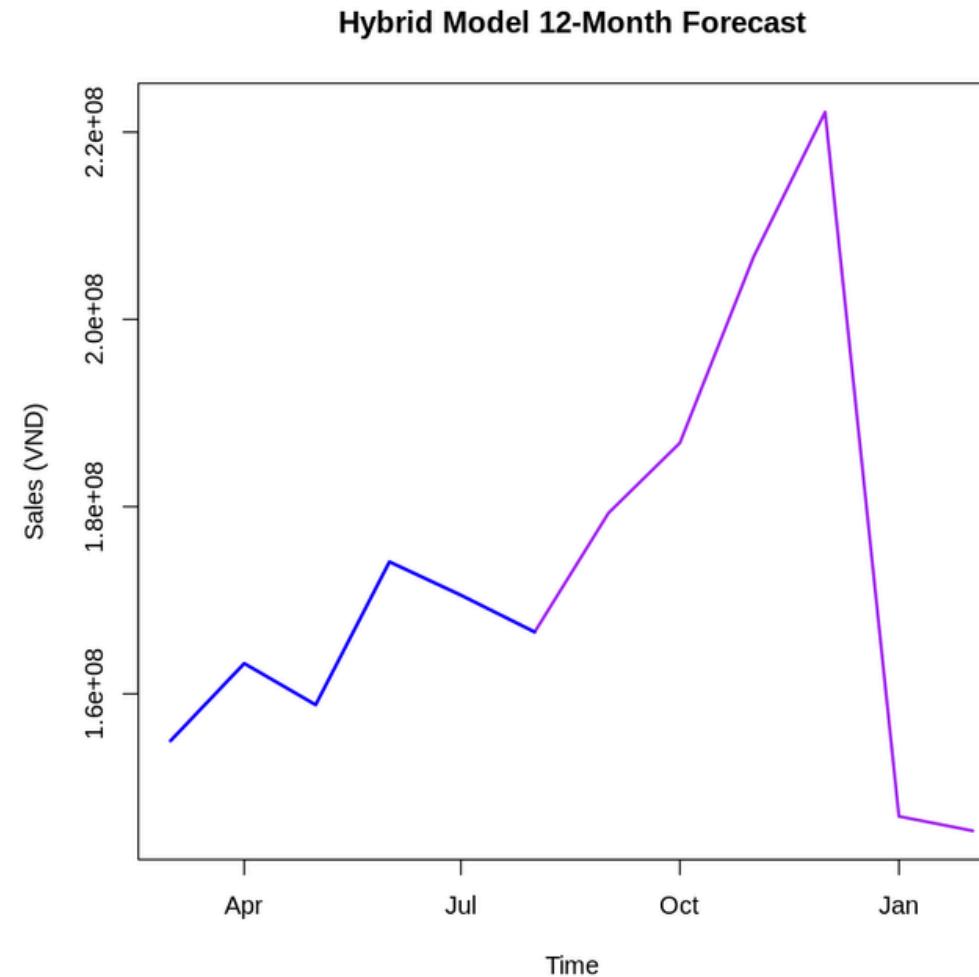
Forecasts from ARIMA(4,0,3)(1,1,1)[12]



- The SARIMA forecast chart clearly demonstrates the seasonality of the time series.
- The forecast reaches its growth peak at the end of 2025.

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RESEARCH RESULTS



The Hybrid Model's 12-month forecast shows revenue peaking highest in December, followed by a sharp drop in January, confirming the pronounced seasonality of the market.

CONCLUSION & STRATEGIC RECOMMENDATIONS:

Conclusion:

- Linear Interpolation (LI) is the most suitable method to fill missing data, ensuring the continuity and actual trend of the revenue time series.
- The Hybrid SARIMA–XGBoost model demonstrated high accuracy (low MAE, RMSE), precisely capturing the growth trend and seasonal characteristics of the ceramics revenue.
- Diagnostic tests confirmed that the residuals are random and show no autocorrelation, ensuring the reliability of the forecasts.
- The model serves as a direct support tool for ceramics shops in business decision-making (optimizing production, distribution, and inventory) based on seasonal cycles.

CONCLUSION & STRATEGIC RECOMMENDATIONS:

Strategy:

- 1. Production – Supply:** Sufficient stock and flexibility against market demand → Increase capacity by 20-30% and early inventory stocking of raw materials (before Q3)
- 2. Human Resources – Operations:** Maintain high productivity while minimizing labor costs during off-peak seasons → Seasonal labor recruitment and training, coupled with the application of automation, to limit human dependence.
- 3. Marketing – Sales:** Expand market share and capitalize on the year-end growth peak → Increase Marketing budget by 40% for Lunar New Year and year-end campaigns (Q3, Q4).
- 4. Financial – Risk:** Ensure stable cash flow and mitigate risks following the peak season → Increase cash reserves by 10-15% (pre-Dec) and establish short-term credit lines

THANKS FOR LISTENING!

