

Q2. There are three major manufacturing companies that make a product: Manufacturers A, B, and C. Manufacture A has a 50% market share, and Manufacture B has a 30% market share. 5% of A's products are defective, 6% of B's products are defective, and 8% of C's products are defective.

- What is the probability that a randomly selected product is defective? $P(\text{Defective})$?
- What is the probability that a randomly selected product is defective and that it came from A? $P(A \text{ and Defective})$?
- What is the probability that a defective product came from B? $P(B/\text{Defective})$?
- Are these events (being defective and coming from B) independent? Why?

Answer-

	Good	Defective
A	$0.50 - 0.025 = 0.475$	$0.05(0.50) = 0.025$
B	$0.30 - 0.018 = 0.282$	$0.06(0.30) = 0.018$
C	$0.20 - 0.016 = 0.184$	$0.08(0.20) = 0.016$
Total		$0.059 = 5.9\%$

A.

$P(\text{Defective}) = 0.059$ or 5.9% (Calculated in table)

B.

$P(A \text{ and Defective}) = 0.025 = 2.5\%$ (from the table)

C.

$P(B/\text{Defective}) = 0.018/0.059 = 0.305 = 30.5\%$

D.

No.

If they were,

$P(B|D) = 0.305$ would have to be equal to the $P(B) = 0.30$ but it doesn't

Hence, the given events are not independent