

# **Artificial Intelligence Lab Report**



*Submitted by*

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**BACHELOR OF ENGINEERING**  
*in*  
**COMPUTER SCIENCE AND ENGINEERING**



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## Table of contents

<b>Program Number</b>	<b>Program Title</b>	<b>Page Number</b>
<b>1</b>	<b>Tic-Tac-Toe Game</b>	<b>1-9</b>
<b>2</b>	<b>8 Puzzle BFS and DFS</b>	<b>10-23</b>
<b>3</b>	<b>Iterative Deepening Search</b>	<b>24-28</b>
<b>4</b>	<b>Vacuum Cleaner Agent</b>	<b>29-34</b>
<b>5</b>	<b>A* Search Algorithm Hill Climbing Algorithm</b>	<b>35-58</b>
<b>6</b>	<b>Simulated Annealing</b>	<b>59-66</b>
<b>7</b>	<b>Knowledge Base using propositional logic</b>	<b>67-69</b>
<b>8</b>	<b>Knowledge Base - Resolution</b>	<b>70-76</b>
<b>9</b>	<b>Unification in FOL</b>	<b>77-82</b>
<b>10</b>	<b>FOL to CNF</b>	<b>83-86</b>
<b>11</b>	<b>Forward Reasoning</b>	<b>87-90</b>
<b>12</b>	<b>Alpha Beta Pruning</b>	<b>91-94</b>

## Program 1 - Tic Tac toe

### Algorithm

Date → 04/10/2024

Week-1

Q. → Implement a tic tac toe game using python.

Ans →

Algorithm / Pseudo code :

```
function minimax (node, depth, isMaximisingPlayer)
    if node is a terminal state:
        return evaluate (node)

    if isMaximisingPlayer:
        bestValue = -infinity
        for each child in node:
            value = minimax (child, depth+1, false)
            bestValue = max (bestValue, value)
        return bestValue

    else:
        bestValue = +infinity
        for each child in node:
            value = minimax (child, depth+1, true)
            bestValue = min (bestValue, value)
        return bestValue
```

## Code

```
import random
```

```
import math
```

```
def print_board(board):
```

```
    for row in board:
```

```
        print(" | ".join(row))
```

```
        print("-" * 9)
```

```
def check_winner(board, mark):
```

```
    # Check rows, columns, and diagonals for a win
```

```
    for row in board:
```

```
        if all(cell == mark for cell in row):
```

```
            return True
```

```
    for col in range(3):
```

```
        if all(board[row][col] == mark for row in range(3)):
```

```
            return True
```

```
if all(board[i][i] == mark for i in range(3)) or all(board[i][2 - i] == mark for i in range(3)):
```

```
    return True
```

```
return False
```

```
def get_available_moves(board):
```

```
    return [(r, c) for r in range(3) for c in range(3) if board[r][c] == " "]
```

```
def minimax(board, depth, is_maximizing):
```

```
    if check_winner(board, "O"):
```

```
        return 10 - depth
```

```
    if check_winner(board, "X"):
```

```
        return depth - 10
```

```
    if not get_available_moves(board):
```

```
        return 0
```

```
    if is_maximizing:
```

```
        best_score = -math.inf
```

```
        for (row, col) in get_available_moves(board):
```

```

        board[row][col] = "O"

        score = minimax(board, depth + 1, False)

        board[row][col] = " "

        best_score = max(best_score, score)

    return best_score

else:

    best_score = math.inf

    for (row, col) in get_available_moves(board):

        board[row][col] = "X"

        score = minimax(board, depth + 1, True)

        board[row][col] = " "

        best_score = min(best_score, score)

    return best_score


def computer_move(board):

    best_score = -math.inf

    best_move = None

    for (row, col) in get_available_moves(board):

        board[row][col] = "O"

```

```

    score = minimax(board, 0, False)

    board[row][col] = " "

    if score > best_score:

        best_score = score

        best_move = (row, col)

    return best_move


def main():

    print("Vyom Gupta (1BM22CS333)")

    print("Welcome to Tic Tac Toe!")

    board = [[" " for _ in range(3)] for _ in range(3)]

    print_board(board)

    for turn in range(9):

        if turn % 2 == 0:

            # Player's turn

            while True:

                try:

```

```

row = int(input("Enter the row (0, 1, 2): "))

col = int(input("Enter the column (0, 1, 2): "))

if (row, col) not in get_available_moves(board):

    print("This spot is already taken or invalid. Try again.")

else:

    board[row][col] = "X"

    break

except ValueError:

    print("Invalid input. Please enter numbers 0, 1, or 2.")

else:

    # Computer's turn

    row, col = computer_move(board)

    board[row][col] = "O"

    print(f"Computer chose: ({row}, {col})")

print_board(board)

# Check for a winner

```



```
if check_winner(board, "X"):

    print("Congratulations! You win!")

    return

elif check_winner(board, "O"):

    print("Computer wins! Better luck next time.")

    return

print("It's a tie!")


if __name__ == "__main__":

    main()
```

## Output

```
Vyom Gupta (1BM22CS333)
Welcome to Tic Tac Toe!

| | |
| | |
| | |
-----
Enter the row (0, 1, 2): 0
Enter the column (0, 1, 2): 0
X | | |
| | |
| | |
-----
Computer chose: (1, 1)
X | | |
| O | |
| | |
-----
Enter the row (0, 1, 2): 1
Enter the column (0, 1, 2): 2
X | | |
| O | X
| | |
-----
Computer chose: (0, 1)
X | O | |
| O | X
| | |
-----
Enter the row (0, 1, 2): 2
Enter the column (0, 1, 2): 1
X | O | |
| O | X
| X | |
```

```
Enter the row (0, 1, 2): 1
Enter the column (0, 1, 2): 1
This spot is already taken or invalid. Try again.
Enter the row (0, 1, 2): 2
Enter the column (0, 1, 2): 2
X | O | 
  | O | X
O | X | X
-----
Computer chose: (0, 2)
X | O | O
  | O | X
O | X | X
-----
Computer wins! Better luck next time.

...Program finished with exit code 0
Press ENTER to exit console.
```

## Program 2 - 8 Puzzle BFS and DFS

### Algorithm

Print "Goal state", goal\_state  
Print "cost: ", cost  
End Function

Q.) Implement 8 Puzzle problem using BFS and DFS.

Ans → Using BFS Algorithm:

Let fringe be a list containing the initial state

Loop

if fringe is empty return failure  
Node ← remove-first (fringe)  
if Node is a goal  
then return the path from initial state to Node  
else  
generate all successors of Node  
and add generated nodes to the back of fringe.

End loop.

→ Using DFS Algorithm:

Let fringe be a list containing the state

loop

if fringe is empty return failure  
Node ← remove first (fringe)  
if Node is a goal  
then return the path from  
Initial state to Node

else

generate all successors of Node and  
add generated nodes to the front  
of the fringe.

State space tree: Using BFS?

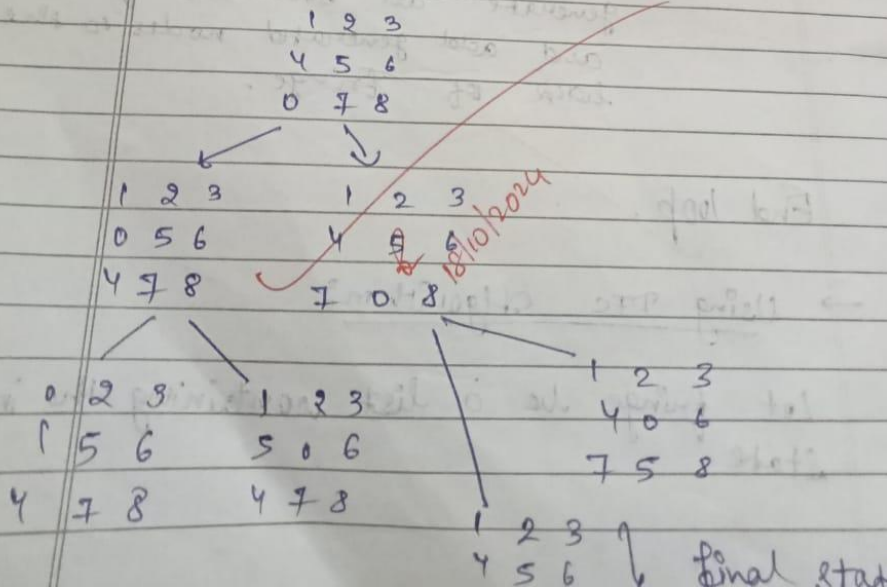
Consider Initial state and final state

Initial

1 2 3  
4 5 6  
0 7 8

Final

1 2 3  
4 5 6  
7 8 0



## **Code (BFS)**

```
from collections import deque
```

```
def is_solvable(state):
```

```
    inversions = 0
```

```
    flattened = [num for row in state for num in row if num != 0]
```

```
    for i in range(len(flattened)):
```

```
        for j in range(i + 1, len(flattened)):
```

```
            if flattened[i] > flattened[j]:
```

```
                inversions += 1
```

```
    return inversions % 2 == 0
```

```
def print_state(state, label=None):
```

```
    if label:
```

```
        print(label)
```

```
    for row in state:
```

```
        print(" ".join(str(num) if num != 0 else " " for num in row))
```

```
    print()
```

```

def get_neighbors(state):

    rows, cols = len(state), len(state[0])

    for r in range(rows):

        for c in range(cols):

            if state[r][c] == 0:

                zero_pos = (r, c)

                break

    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)]

    neighbors = []

    for dr, dc in directions:

        nr, nc = zero_pos[0] + dr, zero_pos[1] + dc

        if 0 <= nr < rows and 0 <= nc < cols:

            new_state = [row[:] for row in state]

            new_state[zero_pos[0]][zero_pos[1]], new_state[nr][nc] = new_state[nr][nc],
            new_state[zero_pos[0]][zero_pos[1]]

            neighbors.append(new_state)

    return neighbors


def bfs(initial, goal):

    queue = deque([(initial, [])])

```

```
visited = set()
```

```
visited.add(tuple(tuple(row) for row in initial))
```

```
while queue:
```

```
    current, path = queue.popleft()
```

```
    if current == goal:
```

```
        return path + [current]
```

```
    for neighbor in get_neighbors(current):
```

```
        neighbor_tuple = tuple(tuple(row) for row in neighbor)
```

```
        if neighbor_tuple not in visited:
```

```
            visited.add(neighbor_tuple)
```

```
            queue.append((neighbor, path + [current]))
```

```
return None
```

```
def main():
```

```
    print("Vyom Gupta(1BM22CS333)")
```

```
    print("8-Puzzle Solver Using BFS")
```

```
    initial_state = [[1, 2, 3], [4, 0, 5], [7, 8, 6]] # Example initial state
```



```
goal_state = [[1, 2, 3], [4, 5, 6], [7, 8, 0]]    # Goal state
```

```
print_state(initial_state, label="Initial State:")
```

```
print_state(goal_state, label="Goal State:")
```

```
if not is_solvable(initial_state):
```

```
    print("This puzzle is not solvable.")
```

```
    return
```

```
solution = bfs(initial_state, goal_state)
```

```
if solution:
```

```
    print("Solution found in {} steps:\n".format(len(solution) - 1))
```

```
    for i, step in enumerate(solution):
```

```
        if i == 0:
```

```
            print_state(step, label="Initial State:")
```

```
        elif i == len(solution) - 1:
```

```
            print_state(step, label="Final State:")
```

```
        else:
```

```
            print_state(step, label=f"Step {i}:")
```

else:

print("No solution exists.")

if \_\_name\_\_ == "\_\_main\_\_":

main()

## **Code (DFS)**

```
def is_solvable(state):

    inversions = 0

    flattened = [num for row in state for num in row if num != 0]

    for i in range(len(flattened)):

        for j in range(i + 1, len(flattened)):

            if flattened[i] > flattened[j]:

                inversions += 1

    return inversions % 2 == 0


def print_state(state, label=None):

    if label:

        print(label)

    for row in state:

        print(" ".join(str(num) if num != 0 else " " for num in row))

    print()


def get_neighbors(state):

    rows, cols = len(state), len(state[0])
```

```

for r in range(rows):

    for c in range(cols):

        if state[r][c] == 0:

            zero_pos = (r, c)

            break

directions = [(-1, 0), (1, 0), (0, -1), (0, 1)]

neighbors = []

for dr, dc in directions:

    nr, nc = zero_pos[0] + dr, zero_pos[1] + dc

    if 0 <= nr < rows and 0 <= nc < cols:

        new_state = [row[:] for row in state]

        new_state[zero_pos[0]][zero_pos[1]], new_state[nr][nc] = new_state[nr][nc],
new_state[zero_pos[0]][zero_pos[1]]

        neighbors.append(new_state)

return neighbors


def dfs(initial, goal):

    stack = [(initial, [])]

    visited = set()

    visited.add(tuple(tuple(row) for row in initial))

```

```
while stack:
```

```
    current, path = stack.pop()
```

```
    if current == goal:
```

```
        return path + [current]
```

```
    for neighbor in get_neighbors(current):
```

```
        neighbor_tuple = tuple(tuple(row) for row in neighbor)
```

```
        if neighbor_tuple not in visited:
```

```
            visited.add(neighbor_tuple)
```

```
            stack.append((neighbor, path + [current]))
```

```
return None
```

```
def main()
```

```
    print("Vyom Gupta (1BM22CS333)")
```

```
    print("8-Puzzle Solver Using DFS")
```

```
    initial_state = [[1, 2, 3], [4, 0, 5], [7, 8, 6]] # Example initial state
```

```
    goal_state = [[1, 2, 3], [4, 5, 6], [7, 8, 0]]    # Goal state
```

```

print_state(initial_state, label="Initial State:")

print_state(goal_state, label="Goal State:")


if not is_solvable(initial_state):

    print("This puzzle is not solvable.")

    return


solution = dfs(initial_state, goal_state)

if solution:

    print("Solution found in {} steps:\n".format(len(solution) - 1))

    for i, step in enumerate(solution):

        if i == 0:

            print_state(step, label="Initial State:")

        elif i == len(solution) - 1:

            print_state(step, label="Final State:")

        else:

            print_state(step, label=f"Step {i}:")

    else:

        print("No solution exists.")

```

```
if __name__ == "__main__":
```

```
    main()
```

## Output (BFS)

```
Vyom Gupta (1BM22CS333)
8-Puzzle Solver Using BFS
Initial State:
1 2 3
4   5
7 8 6

Goal State:
1 2 3
4 5 6
7 8

Solution found in 2 steps:

Initial State:
1 2 3
4   5
7 8 6

Step 1:
1 2 3
4 5
7 8 6

Final State:
1 2 3
4 5 6
7 8

...Program finished with exit code 0
Press ENTER to exit console.
```



## Output (DFS)

```
Vyom Gupta (1BM22CS333)
8-Puzzle Solver Using DFS
Initial State:
1 2 3
4   5
7 8 6

Goal State:
1 2 3
4 5 6
7 8

Solution found in 2 steps:

Initial State:
1 2 3
4   5
7 8 6

Step 1:
1 2 3
4 5
7 8 6

Final State:
1 2 3
4 5 6
7 8

...Program finished with exit code 0
Press ENTER to exit console.
```

## Program 3 - Iterative Deepening Search

### Algorithm

\* Iterative Deepening Search

Pseudocode:

function IDSC(problem) returns a solution  
inputs : problem, a problem

for depth  $\leftarrow 0$  to  $\infty$  do  
    result  $\leftarrow$  Depth.Limited Search (problem, depth)  
    if result  $\neq$  cutoff then return result  
end.

*✓ solution*

## Code

```
print("Vyom Gupta (1BM22CS333)")

def is_solvable(state):
    inversions = 0
    flattened = [num for row in state for num in row if num != 0]
    for i in range(len(flattened)):
        for j in range(i + 1, len(flattened)):
            if flattened[i] > flattened[j]:
                inversions += 1
    return inversions % 2 == 0

def print_state(state, label=None):
    if label:
        print(label)
    for row in state:
        print(" ".join(str(num) if num != 0 else " " for num in row))
    print()

def get_neighbors(state):
    rows, cols = len(state), len(state[0])
    for r in range(rows):
        for c in range(cols):
            if state[r][c] == 0:
                zero_pos = (r, c)
                break
    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)]
    neighbors = []
    for dr, dc in directions:
        nr, nc = zero_pos[0] + dr, zero_pos[1] + dc
        if 0 <= nr < rows and 0 <= nc < cols:
            new_state = [row[:] for row in state]
            new_state[zero_pos[0]][zero_pos[1]], new_state[nr][nc] = new_state[nr][nc],
            new_state[zero_pos[0]][zero_pos[1]]
            neighbors.append(new_state)
    return neighbors

def ids(initial, goal, depth_limit):
    def dls(state, path, depth):
        if state == goal:
            return path
```

```

        return path + [state]
    if depth == 0:
        return None
    for neighbor in get_neighbors(state):
        if tuple(tuple(row) for row in neighbor) not in visited:
            visited.add(tuple(tuple(row) for row in neighbor))
            result = dls(neighbor, path + [state], depth - 1)
            if result:
                return result
    return None

for depth in range(depth_limit):
    visited = set()
    visited.add(tuple(tuple(row) for row in initial))
    result = dls(initial, [], depth)
    if result:
        return result
return None

def main():
    print("8-Puzzle Solver Using Iterative Deepening Search")
    initial_state = [[1, 2, 3], [4, 0, 5], [7, 8, 6]] # Example initial state
    goal_state = [[1, 2, 3], [4, 5, 6], [7, 8, 0]]    # Goal state

    print_state(initial_state, label="Initial State:")
    print_state(goal_state, label="Goal State:")

    if not is_solvable(initial_state):
        print("This puzzle is not solvable.")
        return

    depth_limit = 20
    solution = ids(initial_state, goal_state, depth_limit)
    if solution:
        print("Solution found in {} steps:\n".format(len(solution) - 1))
        for i, step in enumerate(solution):
            if i == 0:
                print_state(step, label="Initial State:")
            elif i == len(solution) - 1:
                print_state(step, label="Final State:")
            else:

```

```
        print_state(step, label=f"Step {i}:")
    else:
        print("No solution exists within depth limit {}".format(depth_limit))

if __name__ == "__main__":
    main()
```

## Output

Vyom Gupta (1BM22CS333)

8-Puzzle Solver Using Iterative Deepening Search

Initial State:

```
1 2 3
  4 5
7 8 6
```

Goal State:

```
1 2 3
4 5 6
7 8
```

Solution found in 3 steps:

Initial State:

```
1 2 3
  4 5
7 8 6
```

Step 1:

```
1 2 3
4   5
7 8 6
```

Step 2:

```
1 2 3
4 5
7 8 6
```

Final State:

```
1 2 3
4 5 6
7 8
```

## Program 4 - Vacuum Cleaner Agent

### Algorithm

Q.2) Implement a vacuum cleaner agent using python.

Ans →

```
function vacuum_world():  
    goal_state = ['A', '0', '0', '0']  
    cost = 0  
    Input location_input, status_input  
    , status_input_complement  
    print "Initial condition:", goal_state  
    if location_input == 'A' Then  
        if status_input == '1' Then  
            goal_state['A'] = '0'  
            cost += 1  
        if status_input_complement == '1'  
            Then  
                goal_state['B'] = '0'  
                cost += 2  
        Else  
            if status_input == '1' Then  
                goal_state['B'] = '0'  
                cost += 1  
            if status_input_complement == '1' Then  
                goal_state['A'] = '0'
```

## **Code**

```
print("Vyom Gupta (1BM22CS333)")

def vacuum_cleaner(initial_state):

    # Initial states of rooms A and B

    room_A, room_B = initial_state

    # Trace of actions

    actions = []

    # Start in Room A

    actions.append("Starting in Room A.")

    # Check room A

    if room_A == 1:

        actions.append("Room A is dirty. Cleaning Room A.")

        room_A = 0

    else:

        actions.append("Room A is already clean.")
```



```
# Move to Room B

actions.append("Moving to Room B.")


# Check room B

if room_B == 1:

    actions.append("Room B is dirty. Cleaning Room B.")

    room_B = 0

else:

    actions.append("Room B is already clean.")


# Move back to Room A

actions.append("Returning to Room A.")


# Final state

final_state = (room_A, room_B)

actions.append("Both rooms are now clean.")


return final_state, actions
```

```

def main():

    print("Vacuum Cleaner AI")

    # Input initial states of Room A and Room B

    room_A = int(input("Enter the state of Room A (0 for clean, 1 for dirty): "))

    room_B = int(input("Enter the state of Room B (0 for clean, 1 for dirty): "))

    # Validate input

    if room_A not in (0, 1) or room_B not in (0, 1):

        print("Invalid input. Please enter 0 or 1.")

        return

    # Solve using vacuum cleaner AI

    final_state, actions = vacuum_cleaner((room_A, room_B))

    # Output actions and final state

    print("\nActions:")

    for action in actions:

```

```
print(action)
```

```
print("\nFinal State:")
```

```
print(f"Room A: {'Clean' if final_state[0] == 0 else 'Dirty'}")
```

```
print(f"Room B: {'Clean' if final_state[1] == 0 else 'Dirty'}")
```

```
if __name__ == "__main__":
```

```
    main()
```

## Output

```
Vyom Gupta (1BM22CS333)
Vacuum Cleaner AI
Enter the state of Room A (0 for clean, 1 for dirty): 1
Enter the state of Room B (0 for clean, 1 for dirty): 1

Actions:
Starting in Room A.
Room A is dirty. Cleaning Room A.
Moving to Room B.
Room B is dirty. Cleaning Room B.
Returning to Room A.
Both rooms are now clean.

Final State:
Room A: Clean
Room B: Clean

...Program finished with exit code 0
Press ENTER to exit console.
```

## Program 5 - A\* Search Algorithm and Hill Climbing Algorithm

### Algorithm

Date → 25/10/24

Lab-5

Q) Implement A\* algorithm using python.

Ans →

```
function A*search (problem) return a solution or failure
    node ← a node n with n.state = problem.initial_state, neg = 0
    frontier ← a priority queue ordered by ascending g+h, only element 'n'
    loop do
        if empty? (frontier) then return failure
        n ← pop (frontier)
        if problem.goalTest (n.state) then return solution
        for each action a in problem.actions (n.state) do
            n' ← childNode (problem, n, a)
            fcost ← (n'.g (n') + h (n'))
            insert (n', fcost) into frontier
```

Output:

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 0 & 5 \\ 7 & 8 & 6 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 0 \\ 7 & 8 & 6 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 0 \end{bmatrix}$$

Using Manhattan Distance:

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 0 & 5 \\ 7 & 8 & 6 \end{bmatrix}$$

Manh. dist → 1 + 3 = 4

Initial distance

$f(h) = 0 + 3 = 3$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 0 & 5 \\ 7 & 8 & 6 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 0 \\ 7 & 8 & 6 \end{bmatrix}$$

Manhattan dist  $\Rightarrow 1+1=2$   
 $f(n) = 2+2=4$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 0 \end{bmatrix}$$

Manh-dist  $= 0$   
 $f(n) = 3+0=3$

$f(n) = 3$

$24/10$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 0 \end{bmatrix}$$

Date: 8/11/21 Lab: 4

Q1 Hill climbing search Algorithm

function hill-climbing (problem) returns a state that is a local maxima

```

current ← make-node (problem.initial-state)
loop do
    neighbours ← highest valued successors of current
    if neighbour.value < current.value then
        return current.state
    current ← neighbour

```

N Queens using Hill climbing:

Function N-Queens (problem) returns the state that is a local minimum

```

while (not True)
    if calculateHeuristic (board) = 0
        return board
    for each row in board:
        for position in row:
            neighbour = makeNode (board, r, pos)

```

heuristic = calculate (neighbour)

if heuristic < bestneighbour

if lowest heuristic = 0 calculate Heuristic (board)

return "total minimum value", board

board = bestneighbour

Cost Calculation:

	Q <sub>0</sub>	Q <sub>1</sub>	Q <sub>2</sub>	Q <sub>3</sub>
3	1	2	0	
1	3	2	0	Q <sub>0</sub> , Q <sub>1</sub>
2	1	3	0	Q <sub>1</sub> , Q <sub>2</sub>
0	1	2	3	Q <sub>0</sub> , Q <sub>3</sub>
3	0	2	1	Q <sub>1</sub> , Q <sub>2</sub>
3	2	1	0	Q <sub>1</sub> , Q <sub>2</sub>
3	1	0	2	Q <sub>2</sub> , Q <sub>3</sub>

			Q <sub>3</sub>
Q <sub>0</sub>			
		Q <sub>2</sub>	
	Q <sub>1</sub>		

Q<sub>0</sub> - Q<sub>3</sub> cost = 1

Date \_\_\_\_\_  
 Page \_\_\_\_\_

			Q <sub>3</sub>
Q <sub>0</sub>	Q <sub>1</sub>		
		Q <sub>2</sub>	

Q<sub>0</sub> - Q<sub>1</sub>  
 Q<sub>1</sub> - Q<sub>2</sub>    cost = 1  
 Q<sub>2</sub> -  
 Q<sub>3</sub> -

Q <sub>0</sub>			
	Q <sub>1</sub>		
		Q <sub>2</sub>	
			Q <sub>3</sub>

Q<sub>0</sub> - Q<sub>1</sub> - Q<sub>2</sub> - Q<sub>3</sub>  
 Q<sub>1</sub> - Q<sub>0</sub> - Q<sub>1</sub> - Q<sub>3</sub>  
 Q<sub>2</sub> - Q<sub>0</sub> - Q<sub>1</sub> - Q<sub>3</sub>    cost = 3  
 Q<sub>3</sub> - Q<sub>0</sub> - Q<sub>1</sub> - Q<sub>2</sub>

	Q <sub>0</sub>		
		Q <sub>2</sub>	
Q <sub>3</sub>			

Q<sub>0</sub> -  
 Q<sub>1</sub> -  
 Q<sub>2</sub> - Q<sub>3</sub>  
 Q<sub>3</sub> - Q<sub>2</sub>    cost = 1

consider - 1320

Q <sub>0</sub>	Q <sub>1</sub>	Q <sub>2</sub>	Q <sub>3</sub>
1	3	2	0
3	1	2	0
2	3	1	0
0	3	2	1
1	2	3	0
1	0	3	2
1	3	0	2

		Q <sub>1</sub>	
Q <sub>0</sub>			
			Q <sub>3</sub>
	Q <sub>2</sub>		

Output:    Queen = 1, Empty = 0

0	0	0	0	0	1	0	0
0	0	1	0	0	0	0	0
1	0	0	0	0	0	0	0
0	0	0	0	0	0	1	0
0	0	0	0	1	0	0	0
0	0	0	0	0	0	0	1
0	1	0	0	0	0	0	0
0	0	0	1	0	0	0	0



### **Code (A\* algorithm using N – displaced Tiles)**

```
import heapq

# Goal state

goal_state = (

    (1, 2, 3),

    (4, 5, 6),

    (7, 8, 0)

)


# Function to compute the heuristic (misplaced tiles)

def misplaced_tiles(state):

    misplaced = 0

    for i in range(3):

        for j in range(3):

            if state[i][j] != goal_state[i][j] and state[i][j] != 0:

                misplaced += 1

    return misplaced


# Function to get possible moves (neighbors)
```

```

def get_neighbors(state):

    neighbors = []

    zero_pos = [(i, j) for i in range(3) for j in range(3) if state[i][j] == 0][0]

    i, j = zero_pos

    # Possible moves: up, down, left, right

    moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]

    for move in moves:

        new_i, new_j = i + move[0], j + move[1]

        if 0 <= new_i < 3 and 0 <= new_j < 3:

            new_state = list(list(row) for row in state) # Create a copy of the state

            new_state[i][j], new_state[new_i][new_j] = new_state[new_i][new_j], new_state[i][j]

            neighbors.append(tuple(tuple(row) for row in new_state)) # Convert back to tuple

    return neighbors

# Function to count the number of inversions in the puzzle

def count_inversions(state):

    one_d_state = [tile for row in state for tile in row if tile != 0]

    inversions = 0

```

```

for i in range(len(one_d_state)):

    for j in range(i + 1, len(one_d_state)):

        if one_d_state[i] > one_d_state[j]:

            inversions += 1

return inversions

```

# Check if the puzzle is solvable

```

def is_solvable(state):

    inversions = count_inversions(state)

    return inversions % 2 == 0

```

# A\* Algorithm

```

def a_star(initial_state):

    if not is_solvable(initial_state):

        print("This puzzle is not solvable.")

        return None

```

```

open_list = []

```

```

    heapq.heappush(open_list, (0 + misplaced_tiles(initial_state), 0, initial_state, [])) # (f(n), g(n),
state, path)

```

```

closed_list = set()

while open_list:

    f, g, current_state, path = heapq.heappop(open_list)

    closed_list.add(current_state)

    # If goal state is reached

    if current_state == goal_state:

        return path + [current_state]

    # Generate neighbors

    for neighbor in get_neighbors(current_state):

        if neighbor not in closed_list:

            heapq.heappush(open_list, (

                g + 1 + misplaced_tiles(neighbor), #  $f(n) = g(n) + h(n)$ 

                g + 1, # Increment  $g(n)$  by 1 for each move

                neighbor,

                path + [current_state]

            ))

```

```

    return None # No solution found

# Function to display the puzzle state

def display_state(state, label):

    print(f"{label} state:")

    for row in state:

        print(" ".join(str(x) for x in row))

    print()

# Example initial state (this one is solvable)

initial_state = (

    (1, 2, 3),

    (5, 6, 4),

    (7, 8, 0)

)

# Solving the puzzle

solution = a_star(initial_state)

```

```
# Displaying the result

if solution:

    # Print Vyom's information

    print("Vyom Gupta (1BM22CS333)\n")


    # Print the initial state

    display_state(initial_state, "Initial")


    # Print the final state

    display_state(goal_state, "Goal")


    # Displaying the solution path

    print("Solution path:")

    for step in solution:

        display_state(step, "Step")

else:

    print("No solution found.")
```

### **Code (A\* algorithm using Manhattan distance)**

```
import heapq

# Goal state

goal_state = (

    (1, 2, 3),

    (4, 5, 6),

    (7, 8, 0)

)


# Function to compute the Manhattan distance heuristic

def manhattan_distance(state):

    distance = 0

    for i in range(3):

        for j in range(3):

            tile = state[i][j]

            if tile != 0:

                goal_i, goal_j = divmod(tile - 1, 3)

                distance += abs(goal_i - i) + abs(goal_j - j)
```

```
return distance
```

```
# Function to get possible moves (neighbors)
```

```
def get_neighbors(state):
```

```
    neighbors = []
```

```
    zero_pos = [(i, j) for i in range(3) for j in range(3) if state[i][j] == 0][0]
```

```
    i, j = zero_pos
```

```
    # Possible moves: up, down, left, right
```

```
    moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]
```

```
    for move in moves:
```

```
        new_i, new_j = i + move[0], j + move[1]
```

```
        if 0 <= new_i < 3 and 0 <= new_j < 3:
```

```
            new_state = list(list(row) for row in state) # Create a copy of the state
```

```
            new_state[i][j], new_state[new_i][new_j] = new_state[new_i][new_j], new_state[i][j]
```

```
            neighbors.append(tuple(tuple(row) for row in new_state)) # Convert back to tuple
```

```
    return neighbors
```

```
# Function to count the number of inversions in the puzzle
```



```

def count_inversions(state):

    one_d_state = [tile for row in state for tile in row if tile != 0]

    inversions = 0

    for i in range(len(one_d_state)):

        for j in range(i + 1, len(one_d_state)):

            if one_d_state[i] > one_d_state[j]:

                inversions += 1

    return inversions

```

# Check if the puzzle is solvable

```

def is_solvable(state):

    inversions = count_inversions(state)

    return inversions % 2 == 0

```

# A\* Algorithm

```

def a_star(initial_state):

    if not is_solvable(initial_state):

        print("This puzzle is not solvable.")

    return None

```

```

open_list = []

heapq.heappush(open_list, (0 + manhattan_distance(initial_state), 0, initial_state, [])) # (f(n),
g(n), state, path)

closed_list = set()

while open_list:

    f, g, current_state, path = heapq.heappop(open_list)

    closed_list.add(current_state)

    # Print the current state and its f(n) value

    print(f"State: {current_state}")

    print(f"f(n) = g(n) + h(n) = {g} + {manhattan_distance(current_state)} = {f}")

    print()

    # If goal state is reached

    if current_state == goal_state:

        return path + [current_state]

    # Generate neighbors

```

```

for neighbor in get_neighbors(current_state):

    if neighbor not in closed_list:

        heapq.heappush(open_list, (

            g + 1 + manhattan_distance(neighbor), #  $f(n) = g(n) + h(n)$ 

            g + 1, # Increment  $g(n)$  by 1 for each move

            neighbor,

            path + [current_state]

        ))

return None # No solution found


# Function to display the puzzle state

def display_state(state, label):

    print(f"{label} state:")

    for row in state:

        print(" ".join(str(x) for x in row))

    print()


# Example initial state (this one is solvable)

```

```
initial_state = (
```

```
    (1, 2, 3),
```

```
    (5, 6, 4),
```

```
    (7, 8, 0)
```

```
)
```

```
# Solving the puzzle
```

```
solution = a_star(initial_state)
```

```
# Displaying the result
```

```
if solution:
```

```
    print("Vyom Gupta(1BM22CS333)\n")
```

```
# Print the initial state
```

```
display_state(initial_state, "Initial")
```

```
# Print the final state
```

```
display_state(goal_state, "Goal")
```

```

# Displaying the solution path

print("Solution path:")

for step in solution:

    display_state(step, "Step")

else:

    print("No solution found.")

```

### Code (Hill Climbing algorithm)

```

import random

print("Vyom Gupta (1BM22CS333)")

# Function to calculate the number of attacking pairs of queens

def calculate_attacks(board):

    attacks = 0

    n = len(board)

    for i in range(n):

        for j in range(i + 1, n):

            if board[i] == board[j] or abs(board[i] - board[j]) == j - i:

```

```

        attacks += 1

    return attacks

# Function to generate a random initial state

def generate_initial_state(n):

    return [random.randint(0, n - 1) for _ in range(n)]

# Function to generate neighbors by moving one queen to a different row

def generate_neighbors(board):

    neighbors = []

    n = len(board)

    for col in range(n):

        for row in range(n):

            if row != board[col]: # Make sure we are not moving the queen to its current row

                neighbor = board[:]

                neighbor[col] = row

                neighbors.append(neighbor)

    return neighbors

```

```

# Hill Climbing algorithm with random restarts

def hill_climbing(n, max_restarts=100):

    for restart in range(max_restarts):

        current_state = generate_initial_state(n)

        current_attacks = calculate_attacks(current_state)


    while True:

        # Generate all neighbors

        neighbors = generate_neighbors(current_state)


        # Find the neighbor with the minimum number of attacks

        next_state = None

        next_attacks = current_attacks


        for neighbor in neighbors:

            attacks = calculate_attacks(neighbor)

            if attacks < next_attacks:

                next_state = neighbor

                next_attacks = attacks

```

```

# If no improvement, return the solution or terminate

if next_attacks == current_attacks:

    break

current_state = next_state

current_attacks = next_attacks


# If a solution is found, return the current state

if current_attacks == 0:

    return current_state


# If no solution found after max_restarts, return None

return None


# Function to display the board

def display_board(board):

    n = len(board)

    for i in range(n):

```



```

        row = ['Q' if i == board[col] else '.' for col in range(n)]

        print(' '.join(row))

    print()

# Set the size of the board (N)

N = 8

# Solve the N-Queens problem with random restarts

solution = hill_climbing(N)

# Display the result

if solution:

    print(f"Solution for {N}-Queens:")

    display_board(solution)

else:

    print(f"No solution found for {N}-Queens.")

```

## Output (N-displaced Tiles)

Vyom Gupta (1BM22CS333)

Initial state:

1 2 3  
5 6 4  
7 8 0

Goal state:

1 2 3  
4 5 6  
7 8 0

Solution path:

Step state:

1 2 3  
5 6 4  
7 8 0

Step state:

1 2 3  
5 6 0  
7 8 4

Step state:

1 2 3  
5 0 6  
7 8 4

Step state:

1 2 3  
0 5 6  
7 8 4

Step state:

1 2 3  
7 4 5  
0 8 6

Step state:

1 2 3  
0 4 5  
7 8 6

Step state:

1 2 3  
4 0 5  
7 8 6

Step state:

1 2 3  
4 5 0  
7 8 6

Step state:

1 2 3  
4 5 6  
7 8 0

Step state:

1 2 3  
7 4 5  
0 8 6

Step state:

1 2 3  
0 4 5  
7 8 6

Step state:

1 2 3  
4 0 5  
7 8 6

Step state:

1 2 3  
4 5 0  
7 8 6

Step state:

1 2 3  
4 5 6  
7 8 0

## Output (Manhattan Distance)

Vyom Gupta (1BM22CS333)

Initial state:

1 2 3  
5 6 4  
7 8 0

Goal state:

1 2 3  
4 5 6  
7 8 0

Solution path:

Step state:

1 2 3  
5 6 4  
7 8 0

Step state:

1 2 3  
5 6 0  
7 8 4

Step state:

1 2 3  
5 0 6  
7 8 4

Step state:

1 2 3  
0 5 6  
7 8 4

Step state:

1 2 3  
7 5 6  
0 8 4

Step state:

1 2 3  
7 5 6  
8 0 4

Step state:

1 2 3  
7 5 6  
8 4 0

Step state:

1 2 3  
7 5 0  
8 4 6

Step state:

1 2 3  
7 0 5  
8 4 6

Step state:

1 2 3  
7 4 5  
8 0 6

Step state:

1 2 3  
7 4 5  
0 8 6

Step state:

1 2 3  
0 4 5  
7 8 6

Step state:

1 2 3  
4 0 5  
7 8 6

Step state:

1 2 3  
4 5 0  
7 8 6

Step state:

1 2 3  
4 5 6  
7 8 0

Output (Hill Climbing)

Vyom Gupta (1BM22CS333)

Solution for 8-Queens:

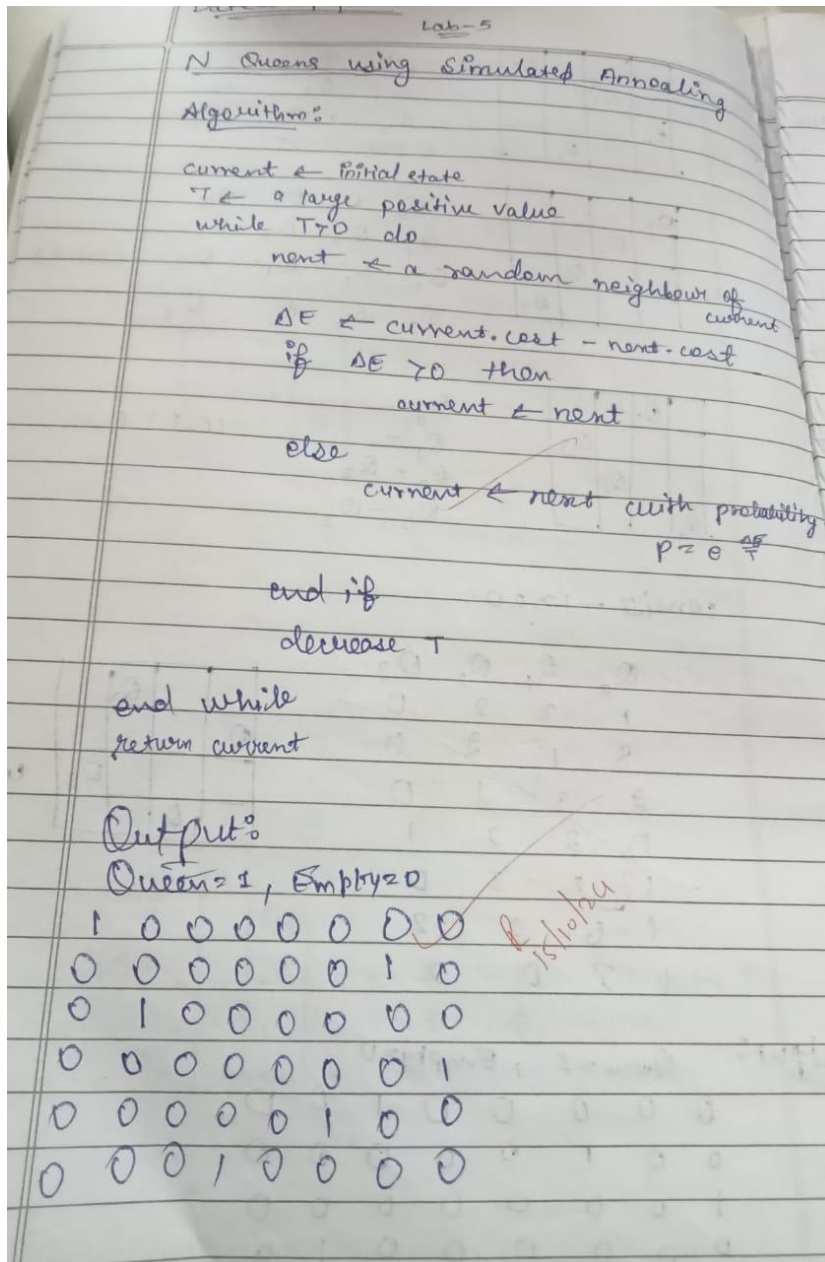
```
. . . Q . . . .  
. Q . . . . . .  
. . . . . . Q .  
. . . . Q . . .  
Q . . . . . . .  
. . . . . . . Q  
. . . . . Q . .  
. . Q . . . . .
```

...Program finished with exit code 0

Press ENTER to exit console.

## Program 6 - Simulated Annealing

### Algorithm



## **Code**

```
import random
```

```
import math
```

```
print("Vyom Gupta (1BM22CS333)")
```

```
# Objective function: count the number of attacking pairs of queens
```

```

def calculate_attacks(board):

    attacks = 0

    n = len(board)

    for i in range(n):

        for j in range(i + 1, n):

            # Check if two queens are in the same row, column, or diagonal

            if board[i] == board[j] or abs(board[i] - board[j]) == j - i:

                attacks += 1

    return attacks


# Function to generate a random initial state (random queen positions in each column)

def generate_initial_state(n):

    return [random.randint(0, n - 1) for _ in range(n)]


# Function to generate a neighboring solution by moving one queen in a column

def generate_neighbor(board):

    neighbor = board[:]

    column = random.randint(0, len(board) - 1)

    # Randomly select a new row for the queen in the chosen column

```

```
neighbor[column] = random.randint(0, len(board) - 1)
```

```
return neighbor
```

```
# Simulated Annealing algorithm to solve the N-Queens problem
```

```
def simulated_annealing(n, max_iterations, initial_temperature, cooling_rate):
```

```
    current_state = generate_initial_state(n)
```

```
    current_attacks = calculate_attacks(current_state)
```

```
    temperature = initial_temperature
```

```
    best_state = current_state
```

```
    best_attacks = current_attacks
```

```
    for iteration in range(max_iterations):
```

```
        # Generate a neighbor solution
```

```
        neighbor = generate_neighbor(current_state)
```

```
        neighbor_attacks = calculate_attacks(neighbor)
```

```
        # Calculate the energy difference (how much worse the new state is)
```

```
        delta_attacks = neighbor_attacks - current_attacks
```



```

# Accept the neighbor if it has fewer attacks or with a probability if it's worse

if delta_attacks < 0 or random.random() < math.exp(-delta_attacks / temperature):

    current_state = neighbor

    current_attacks = neighbor_attacks


# Update the best solution if necessary

if current_attacks < best_attacks:

    best_state = current_state

    best_attacks = current_attacks


# Cool down the temperature

temperature *= cooling_rate


# If no attacks, we found the solution

if best_attacks == 0:

    break


return best_state, best_attacks

```

```
# Function to display the board (where 'Q' is a queen and '.' is an empty space)
```

```
def display_board(board):
```

```
    n = len(board)
```

```
    for i in range(n):
```

```
        row = ['Q' if i == board[col] else '.' for col in range(n)]
```

```
        print(' '.join(row))
```

```
    print()
```

```
# Parameters for Simulated Annealing
```

```
N = 8 # Set the size of the board (N x N)
```

```
max_iterations = 10000 # Higher number of iterations for better convergence
```

```
initial_temperature = 1000 # High initial temperature
```

```
cooling_rate = 0.995 # Cooling rate (temperature decreases by 0.5% every iteration)
```

```
# Solve the N-Queens problem using Simulated Annealing
```

```
solution, attacks = simulated_annealing(N, max_iterations, initial_temperature, cooling_rate)
```

```
# Output the result
```

```
print(f"Solution for {N}-Queens found:")  
  
display_board(solution)  
  
print(f"Total number of attacks: {attacks}")
```

## Output

```
Vyom Gupta (1BM22CS333)
Solution for 8-Queens found:
Q . . . . . . .
. . . . Q . . .
. . . . . . . Q
. . . . . Q . .
. . Q . . . . .
. . . . . . Q .
. Q . . . . . .
. . . Q . . . .

Total number of attacks: 0

...Program finished with exit code 0
Press ENTER to exit console.
```

## Program 7 - Knowledge base using propositional logic and show that the given query entails the knowledge base or not.

### Algorithm

```
Q.) Initialize knowledge base with propositional logic statements.  
Ans. Input Query:  
    if forward-chaining (knowledge base, query):  
        print("Query is entailed")  
    else:  
        print("Query is not entailed by the knowledge base")  
function Forward_chaining (Knowledge_base, query):  
    Initialize agenda with known facts from knowledge base  
    while agenda is not empty:  
        pop a fact from agenda  
        if fact matches query:  
            return True  
        for each rule in Knowledge:  
            if fact satisfies a rule's premise:  
                Add the rule's conclusion to agenda  
    return False
```

Output:  
For the knowledge base =  $\{A, B, A \wedge B \rightarrow C\}$   
Query = "D"  
Query is entailed by knowledge base

## Code

```
from sympy.logic.boolalg import Or, And, Not
from sympy.abc import A, B, C, D, E, F
from sympy import simplify_logic

def is_entailment(kb, query):
    # Negate the query
    negated_query = Not(query)

    # Combine the knowledge base with the negated query
    kb_with_negated_query = And(*kb, negated_query) # Combine all KB clauses and the negated query

    # Simplify the combined KB to CNF (Conjunctive Normal Form)
    simplified_kb = simplify_logic(kb_with_negated_query, form="cnf")

    # If the simplified KB evaluates to False, the query is entailed
    return simplified_kb == False

# Define a larger Knowledge Base (kb)
kb = [
    Or(A, B),      #  $A \vee B$ 
    Or(Not(A), C), #  $\neg A \vee C$ 
    Or(Not(B), D), #  $\neg B \vee D$ 
    Or(Not(D), E), #  $\neg D \vee E$ 
    Or(Not(E), F), #  $\neg E \vee F$ 
]

# Query to check ( $C \vee F$ )
query = Or(C, F)

# Check entailment
```

```
result = is_entailment(kb, query)
```

```
# Output the result with Vyom Gupta's details
```

```
print(f"Vyom Gupta (1BM22CS333)\n")
```

```
print(f"Is the query '{query}' entailed by the knowledge base? {'Yes' if result else 'No'}")
```

## **OUTPUT:**

```
Vyom Gupta (1BM22CS333)
```

```
Is the query 'C | F' entailed by the knowledge base? Yes
```

## Program 8 - Knowledge base using propositional logic and prove the given query using resolution.

### Algorithm

Date: 10/12/24 Lab-8

Q. Creating a knowledge base using propositional logic and proving query using resolution.

Ans. → Input: Knowledge Base with propositional logic statements.

Input Query.

Convert Knowledge base into CNF clauses.

Add  $\neg$  Query to CNF clauses.

while (True):

    Select 2 clauses from CNF clauses.

    Resolve the clauses to form new clause.

    if new clause is empty:

        print("Proved")

        return

    if new clause is not already there in CNF clauses:

        add new clause to CNF clauses.

    if no new clause is generated:

        print("can't be proven")

        return

Output →

For Knowledge base = ["A", "A", "A  $\vee$  B  $\Rightarrow$  C", "C  $\Rightarrow$  D"]

Query = 'D'

Query is proven using resolution.

*Resolution*



## Code

```
def negation(p):

    """Negate a literal."""

    if p.startswith("~"):

        return p[1:] # remove the '~' from negated literals

    return f"~{p}"


def resolution(kb, query):

    """Perform resolution on the knowledge base to prove the query."""

    # Add the negation of the query to the knowledge base (for proof by contradiction)

    kb.append(negation(query))

    # Apply the resolution rule until we reach an empty clause (which means contradiction)

    new_clauses = set(kb) # Keep track of all unique clauses in the knowledge base

    print(f"Initial Knowledge Base + negation of query: {kb}")

    while True:

        added_new_clause = False
```

```

# Try to resolve every pair of clauses

clauses = list(new_clauses)

for i in range(len(clauses)):

    for j in range(i + 1, len(clauses)):

        clause1 = clauses[i]

        clause2 = clauses[j]

        # Try to resolve these two clauses

        resolvent = resolve(clause1, clause2)

        if resolvent is not None:

            print(f"Resolving clauses: {clause1} and {clause2}")

            print(f"Resolved to: {resolvent}")

            # If resolvent is empty, we found a contradiction

            if not resolvent:

                return True # Found a contradiction, so the query is provable

        # Add the new clause if it's not already in the set

```

```

        if resolvent not in new_clauses:

            new_clauses.add(resolvent)

            added_new_clause = True

    # If no new clause was added, resolution has terminated without a contradiction

    if not added_new_clause:

        break

    return False # No contradiction found, so the query is not provable


def resolve(clause1, clause2):

    """Resolve two clauses if possible and return the resolvent."""

    # Split clauses into literals

    literals1 = set(clause1.split(" v "))

    literals2 = set(clause2.split(" v "))

    # Try to find complementary literals

    for literal in literals1:

```

```
neg_literal = negation(literal)
```

```
if neg_literal in literals2:
```

```
    # Resolve the two clauses by removing complementary literals
```

```
    new_clause = literals1.union(literals2) - {literal, neg_literal}
```

```
    return " v ".join(sorted(new_clause)) # Return the resolved clause as a string
```

```
return None # No resolvent found
```

```
# Example knowledge base and query (where T is provable)
```

```
kb = [
```

```
    "P v Q",      # P or Q
```

```
    "~P v R",     # Not P or R
```

```
    "Q v ~R",     # Q or Not R
```

```
    "R v T"       # R or T
```

```
]
```

```
query = "T" # Query to prove (e.g., prove T)
```

```
# Perform resolution to prove the query
```

```
result = resolution(kb, query)
```

```
if result:
```

```
    print(f"\nQuery '{query}' is provable from the knowledge base.")
```

```
else:
```

```
    print(f"\nQuery '{query}' is not provable from the knowledge base.")
```

## Output

```
Vyom Gupta (1BM22CS333)

Initial Knowledge Base + negation of query: ['P v Q', '~P v R', 'Q v ~R', 'R v T', '~T']
Resolving clauses: P v Q and ~P v R
Resolved to: Q v R
Resolving clauses: Q v ~R and ~P v R
Resolved to: Q v ~P
Resolving clauses: Q v ~R and R v T
Resolved to: Q v T
Resolving clauses: ~T and R v T
Resolved to: R
Resolving clauses: Q v R and Q v ~R
Resolved to: Q
Resolving clauses: P v Q and Q v ~P
Resolved to: Q
Resolving clauses: P v Q and ~P v R
Resolved to: Q v R
Resolving clauses: Q v T and ~T
Resolved to: Q
Resolving clauses: Q v ~R and ~P v R
Resolved to: Q v ~P
Resolving clauses: Q v ~R and R v T
Resolved to: Q v T
Resolving clauses: Q v ~R and R
Resolved to: Q
Resolving clauses: ~T and R v T
Resolved to: R
Resolving clauses: Q v R and Q v ~R
Resolved to: Q
Resolving clauses: P v Q and Q v ~P
Resolved to: Q
Resolving clauses: P v Q and ~P v R
Resolved to: Q v R
```

```
Resolving clauses: Q v T and ~T
Resolved to: Q
Resolving clauses: Q v ~R and ~P v R
Resolved to: Q v ~P
Resolving clauses: Q v ~R and R v T
Resolved to: Q v T
Resolving clauses: Q v ~R and R
Resolved to: Q
Resolving clauses: ~T and R v T
Resolved to: R

Query 'T' is not provable from the knowledge base.

...Program finished with exit code 0
Press ENTER to exit console.
```

## Program 9 – Unification in First Order Logic.

### Algorithm

Date  $\rightarrow$  22/11/2024 :-  
Lab-6

Unification Algorithm:

Step (1): If  $\psi_1$  and  $\psi_2$  are a variable or constant, then:

- If  $\psi_1$  or  $\psi_2$  are identical, then return NIL.
- Else if  $\psi_1$  is a variable,
  - Then if  $\psi_1$  occurs in  $\psi_2$ , then return Failure
  - Else return  $\{(\psi_1/\psi_2)\}$
- Else if  $\psi_2$  is a variable,
  - if  $\psi_2$  occurs in  $\psi_1$ , then return Failure
  - Else return  $\{(\psi_2/\psi_1)\}$
- Else return Failure.

Step (2): If the initial Predicate symbol of  $\psi_1$  and  $\psi_2$  are not the same, then Failure.

Step (3): If  $\psi_1$  and  $\psi_2$  have a different number of arguments, then return Failure.

Step (4): Set substitution set (SUBST) to NIL.

Step (5): For  $i=1$  to the number of elements in  $\psi_1$ ,

- Call unify function with the  $i$ th element of  $\psi_1$  and the  $i$ th element of  $\psi_2$ , and put the result into S.
- If  $S = \text{Failure}$  then return Failure
- If  $S = \text{NIL}$ , then do,
  - Apply S to remainder of both  $L1$  and  $L2$ .
  - $\text{SUBST} = \text{APPEND}(S, \text{SUBST})$

Step (6): Return SUBST.

Output:

Enter two terms to unify  
Enter first term:  $f(x, y)$   
Enter second term:  $f(a, b)$   
Unifying terms: ('f', 'x', 'y') and ('f', 'a', 'b')

Unification successful!

Substitution:  $\{ 'a' \rightarrow 'x', 'b' \rightarrow 'y' \}$

Unified expression:

Term1 after substitution:  $( 'b', 'x', 'y' )$

Term2 after substitution:  $( 'b', 'x', 'y' )$

22/11/20



## Code

```
print("Vyom Gupta (1BM22CS333)\n")
```

```
def occurs_check(var, term):
```

```
    """Check if a variable occurs in a term."""
```

```
    if var == term:
```

```
        return True
```

```
    elif isinstance(term, tuple): # If the term is a function or a tuple
```

```
        return any(occurs_check(var, t) for t in term[1:])
```

```
    return False
```

```
def unify(term1, term2, substitution=None):
```

```
    """Attempt to unify two terms (or predicates)."""
```

```
    if substitution is None:
```

```
        substitution = {}
```

```
    # If both terms are the same, no unification needed
```

```
    if term1 == term2:
```

```
        return substitution
```

```

# If term1 is a variable, try to unify it with term2

if isinstance(term1, str) and term1.isupper():

    if term1 in substitution:

        return unify(substitution[term1], term2, substitution)

    if occurs_check(term1, term2):

        return None # Avoid circular unification (occurs check)

    substitution[term1] = term2

    return substitution


# If term2 is a variable, try to unify it with term1

if isinstance(term2, str) and term2.isupper():

    return unify(term2, term1, substitution)


# If both terms are functions or predicates (tuples), unify their components

if isinstance(term1, tuple) and isinstance(term2, tuple):

    if len(term1) != len(term2):

        return None # Different number of arguments

    for t1, t2 in zip(term1[1:], term2[1:]):

```

```

    substitution = unify(t1, t2, substitution)

    if substitution is None:

        return None # If any unification fails, return None

    return substitution

return None # If no other cases match, return None (failure)

# Example usage

term1 = ('P', 'X', 'a') # Predicate P(X, a)

term2 = ('P', 'b', 'a') # Predicate P(b, a)

# Attempt to unify

substitution = unify(term1, term2)

if substitution is not None:


    print("Unification succeeded with substitution:", substitution)

else:

    print("Unification failed")

```

## Output



```
Vyom Gupta (1BM22CS333)
```

```
Unification succeeded with substitution: {'X': 'b'}
```

```
...Program finished with exit code 0
```

```
Press ENTER to exit console. 
```

**Program 10 - Convert a given first order logic statement into Conjunctive Normal Form (CNF).**

**Algorithm**

Date: 13/12/21 Lab-3

Q.) Converting FOL into CNF.

Ans. Input: first order logic statements:

Eliminate implications: Replace  $A \rightarrow B$  with  $\neg A \vee B$

Move  $\neg$  (negation) inside using De Morgan's law

Standardize variables: each quantified should have unique variable

Skolemize: eliminate existential quantifiers to replace with skolem functions.

Drop universal Quantifiers.

Distribute  $\wedge$  over  $\vee$

Output CNF clauses.

Output:

Original statement:  $A \wedge B \Rightarrow C$

CNF form:  $\neg A \vee \neg B \vee C$

## Code

```
from sympy import symbols, Not, Or, And, Implies, Equivalent
from sympy.logic.boolalg import to_cnf

def fol_to_cnf(fol_expr):
    """
    Converts a First-Order Logic (FOL) statement to Conjunctive Normal Form (CNF).

    Arguments:
    fol_expr: A sympy logical expression representing the FOL statement.

    Returns:
    The CNF equivalent of the input expression.
    """
    # Step 1: Eliminate equivalences ( $A \leftrightarrow B$ ) using  $(A \rightarrow B) \wedge (B \rightarrow A)$ 
    fol_expr = fol_expr.replace(Equivalent, lambda a, b: And(Implies(a, b), Implies(b, a)))

    # Step 2: Eliminate implications ( $A \rightarrow B$ ) using  $(\neg A \vee B)$ 
    fol_expr = fol_expr.replace(Implies, lambda a, b: Or(Not(a), b))

    # Step 3: Convert to CNF
    cnf_form = to_cnf(fol_expr, simplify=True)

    return cnf_form

def main():
    # Define propositional symbols instead of first-order predicates
    P = symbols("P")
    Q = symbols("Q")
    R = symbols("R")

    # Example 1:  $P \rightarrow Q$ 
    fol_expr1 = Implies(P, Q)
    print("Example 1:  $P \rightarrow Q$ ")
    print("Original FOL Expression:")
    print(fol_expr1)
    # Convert to CNF
    cnf1 = fol_to_cnf(fol_expr1)
    print("\nCNF Form:")
    print(cnf1)

    # Example 2:  $(P \vee \neg Q) \rightarrow (Q \vee R)$ 
    fol_expr2 = Implies(Or(P, Not(Q)), Or(Q, R))
    print("\nExample 2:  $(P \vee \neg Q) \rightarrow (Q \vee R)$ ")
    print("Original FOL Expression:")
```

```
print(fol_expr2)
# Convert to CNF
cnf2 = fol_to_cnf(fol_expr2)
print("\nCNF Form:")
print(cnf2)

# Print name and USN at the start
print("Vyom Gupta (1BM22CS333)\n")

if __name__ == "__main__":
    main()
```

## OUTPUT:

Vyom Gupta (1BM22CS333)

Example 1:  $P \rightarrow Q$

Original FOL Expression:

Implies(P, Q)

CNF Form:

$Q \mid \sim P$

Example 2:  $(P \vee \neg Q) \rightarrow (Q \vee R)$

Original FOL Expression:

Implies( $P \mid \sim Q$ ,  $Q \mid R$ )

CNF Form:

$Q \mid R$



## Program 11 - Knowledge base consisting of first order logic statements and prove the given query using forward reasoning..

### Algorithm

Date: 23/11/24 Lab-7

Forward Reasoning Algorithm

function FOL-FC ASK (KB, q) returns a substitution or false

Input: KB, the knowledge base, a set of first-order definite clauses  
q, the query, an atomic sentence

local variables: new, the new sentences introduced on each iteration

repeat until new is empty  
  new ← {}  
  for each rule in KB do  
     $(P_1 \wedge \dots \wedge P_n \Rightarrow Q) \leftarrow \text{STANDARDIZE\_VARIABLES}(\text{rule})$   
    for each D such that  $\text{SUBST}(Q, P_1 \wedge \dots \wedge P_n) = \text{SUBST}(Q, P_1 \wedge \dots \wedge P_n)$   
      for some  $P_1, \dots, P_n$  in KB  
         $q' \leftarrow \text{SUBST}(Q, q)$   
        if  $q'$  does not unify with  
          some sentence already in  
          KB or new then  
          add  $q'$  to new  
         $\phi \leftarrow \text{UNIFY}(q', \dots)$   
        if  $\phi$  is not fail

add new to KB  
return false

Output:

Robert is a criminal for selling weapons to a hostile nation!

Updated Facts for Robert:

name: Robert  
is\_american: True  
is\_hostile\_nation: True  
selling\_weapons: True  
is\_criminal: True

Updated Facts for John:

name: John  
is\_american: True  
is\_hostile\_nation: False  
selling\_weapons: True  
is\_criminal: False

Question: Write FOL:

a)  $\Rightarrow \text{Occupation}(\text{Emily}, \text{Surgeon}) \vee \text{Occupation}(\text{Emily}, \text{Actor})$

b)  $\Rightarrow \text{Occupation}(\text{Joe}, \text{Actor}) \wedge \exists O (O \neq \text{Actor} \wedge \text{Occupation}(O, \text{Occupation}))$

c)  $\Rightarrow \forall P (\text{Occupation}(P, \text{Surgeon}) \rightarrow \text{Occupation}(P, \text{Actor}))$

d.)  $\rightarrow \forall p (\text{Occupation}(p, \text{Lawyer}) \rightarrow \neg \text{Customer}(\text{Joe}, p))$

e.)  $\rightarrow \exists p (\text{Boss}(p, \text{Emily}) \wedge \text{Occupation}(p, \text{Lawyer}))$

f.)  $\exists p (\text{Occupation}(p, \text{Lawyer}) \wedge \forall q (\text{Customer}(\text{Joe}, q) \rightarrow \text{Occupation}(q, \text{Doctor})))$

g.)  $\forall p (\text{Occupation}(p, \text{Surgeon}) \rightarrow \exists q (\text{Customer}(\text{Betty}, q) \wedge \text{Occupation}(q, \text{Lawyer})))$

## Code

```
knowledge_base = {
    "facts": {
        "American(Robert)": True,
        "Enemy(A, America)": True,
        "Owns(A, T1)": True,
        "Missile(T1)": True,
    },
    "rules": [
        {"if": ["Missile(x)", "then": ["Weapon(x)"]},
        {"if": ["Enemy(x, America)", "then": ["Hostile(x)"]},
        {"if": ["Missile(x)", "Owns(A, x)", "then": ["Sells(Robert, x, A)"]},
        {
            "if": ["American(p)", "Weapon(q)", "Sells(p, q, r)", "Hostile(r)",
            "then": ["Criminal(p)"],
        },
    ],
}

def forward_chaining(kb):
    facts = kb["facts"].copy()
    rules = kb["rules"]
    inferred = set()
    while True:
        new_inferences = set()
        for rule in rules:
            if_conditions = rule["if"]
            then_conditions = rule["then"]
            substitutions = {}
            all_conditions_met = True
            for condition in if_conditions:
                predicate, args = condition.split("(")
                args = args[:-1].split(",")
                matched = False
                for fact in facts:
                    fact_predicate, fact_args = fact.split("(")
                    fact_args = fact_args[:-1].split(",")
                    if predicate == fact_predicate and len(args) == len(fact_args):
                        temp_subs = {}
                        for var, val in zip(args, fact_args):
                            if var.islower():
                                if var in temp_subs and temp_subs[var] != val:
                                    break
```

```

temp_subs[var] = val
elif var != val:
    break
else:
    matched = True
    substitutions.update(temp_subs)
    break
if not matched:
    all_conditions_met = False
    break
44if all_conditions_met:
    for condition in then_conditions:
        predicate, args = condition.split("(")
        args = args[:-1].split(",")
        new_fact = predicate + "(" + ",".join(substitutions.get(arg, arg) for arg in args)
        + ")"
        new_inferences.add(new_fact)
        if new_inferences - inferred:
            inferred.update(new_inferences)
            facts.update({fact: True for fact in new_inferences})
        else:
            break
    return inferred
result = forward_chaining(knowledge_base)
print('Vyom Gupta (1BM22CS333):')
if "Criminal(Robert)" in result:
    print("Proved: Robert is a criminal.")
else:
    print("Could not prove that Robert is a criminal.")

```

### **OUTPUT:**

```

Vyom Gupta (1BM22CS333):
Proved: Robert is a criminal.

```

## Program 12 - Implement Alpha-Beta Pruning.

### Algorithm

Lab-8

Q.1) Implement Alpha-Beta Pruning

Ans. \*

```
function alpha-beta-pruning (node, depth,
alpha, beta, maximizing-player) {
    v ← MAX-VALUE (state, -∞, +∞)
    return action in ACTIONS (state)
    with value v
}

function MAX-VALUE (state, alpha, beta)
    return utility value

    if Terminal-Test (state) then return
    utility (state)

    v ← -∞
    for each action a in actions (state) do
        v ← max (v, MIN-VALUE (Result
        (s, a),
        α, β))

        if v ≥ β return v

        α ← max (α, v)

    return v

function MIN-VALUE (state, α, β)
    return utility value

    if Terminal-Test (state) then return
    utility (state)

    v ← +∞
```

for each  $a$  in actions(state) do

$v \leftarrow \min(v, \text{MAX-VALUE}(\text{Result}(a, \text{state}), \beta, \gamma))$

if  $v \leq \alpha$  return  $v$

~~$\beta$~~   $\beta \leftarrow \min(\beta, v)$

return  $v$

Output:

For tree =  $[[3, 5, 6], [9, 1, 2], [0, 7, 4]]$

Optimal value = 6

*value*

## Code

```
import math
def alpha_beta_pruning(depth, node_index, is_maximizing_player, values, alpha, beta,
max_depth):
# Base case: when the maximum depth is reached
if depth == max_depth:
return values[node_index]
if is_maximizing_player:
best = -math.inf
# Recur for left and right children
for i in range(2):
val = alpha_beta_pruning(depth + 1, node_index * 2 + i, False, values, alpha, beta,
max_depth)
best = max(best, val)
alpha = max(alpha, best)
# Prune the remaining nodes
if beta <= alpha:
break
return best
else:
best = math.inf
# Recur for left and right children
for i in range(2):
val = alpha_beta_pruning(depth + 1, node_index * 2 + i, True, values, alpha, beta,
max_depth)
best = min(best, val)
beta = min(beta, best)
49# Prune the remaining nodes
if beta <= alpha:
break
return best
print(" Vyom Gupta (1BM22CS333):")
# Example usage
if __name__ == "__main__":
# Example tree represented as a list of leaf node values
values = [3, 5, 6, 9, 1, 2, 0, -1]
max_depth = 3 # Height of the tree
result = alpha_beta_pruning(0, 0, True, values, -math.inf, math.inf, max_depth)
print("The optimal value is:", result)
```

## OUTPUT:

```
Vyom Gupta (1BM22CS333):  
The optimal value is: 5  
  
...Program finished with exit code 0  
Press ENTER to exit console.
```



