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import numpy as np
import random
from scipy.special import gamma # Import the gamma function

# Objective function (fitness function) to minimize waiting time at the intersection
def traffic_waiting_time(signal_timings):
    # This is a simplified model of the traffic flow; the function can be more complex.
    flow = np.array([1000, 1200, 1100, 1300]) # hypothetical vehicle flow for each phase (vehicles per hour)
    max_capacity = np.array([1500, 1500, 1500, 1500]) # maximum capacity for each phase (vehicles per hour)

    # The waiting time can be roughly modeled as the inverse of the flow divided by the capacity.
    waiting_time = np.sum((signal_timings * flow) / max_capacity) # total waiting time for vehicles
    return waiting_time

# Levy flight for exploration
def levy_flight(dim, beta=1.5):
    sigma_u = (gamma(1 + beta) * np.sin(np.pi * beta / 2) /
               (gamma((1 + beta) / 2) * beta * 2 ** ((beta - 1) / 2))) ** (1 / beta)
    u = np.random.normal(0, sigma_u, dim)
    v = np.random.normal(0, 1, dim)
    step = u / (np.abs(v) ** (1 / beta))
    return step

# Cuckoo Search algorithm
def cuckoo_search(num_nests=50, num_iterations=100, dim=4, alpha=0.01, beta=1.5, pa=0.25):
    # Initialize the nests with random values (signal timings)
    nests = np.random.uniform(10, 60, (num_nests, dim)) # Signal timings between 10 and 60 seconds for each phase
    fitness = np.array([traffic_waiting_time(nest) for nest in nests]) # Initial fitness for each nest

    # Find the best solution
    best_nest = nests[np.argmin(fitness)]
    best_fitness = np.min(fitness)

    # Main loop
    for iteration in range(num_iterations):
        # Generate a new solution using Levy flight
        new_nests = nests + alpha * levy_flight(dim, beta) # Perturb the nests

        # Apply bounds to signal timings (e.g., between 10 and 60 seconds)
        new_nests = np.clip(new_nests, 10, 60)

        # Evaluate the fitness of the new nests
        new_fitness = np.array([traffic_waiting_time(nest) for nest in new_nests])

        # Replace worse nests with better ones
        for i in range(num_nests):
            if new_fitness[i] < fitness[i]:
                nests[i] = new_nests[i]
                fitness[i] = new_fitness[i]

        # Replace some nests randomly based on probability 'pa'
        for i in range(num_nests):
            if random.random() < pa:
                nests[i] = np.random.uniform(10, 60, dim) # Randomly reinitialize the nest
                fitness[i] = traffic_waiting_time(nests[i])

        # Find the best nest in the current iteration
        min_index = np.argmin(fitness)
        if fitness[min_index] < best_fitness:
            best_fitness = fitness[min_index]
            best_nest = nests[min_index]

        # Print progress for each iteration
        print(f"Iteration {iteration + 1}, Best waiting time: {best_fitness}")

    return best_nest, best_fitness

# Run Cuckoo Search for traffic signal optimization
best_signal_timings, best_waiting_time = cuckoo_search(num_nests=50, num_iterations=100, dim=4)

# Output the best signal timings and their corresponding waiting time
print("\nBest traffic signal timings (seconds per phase):", best_signal_timings)
print("Best waiting time:", best_waiting_time)

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↩ Iteration 1, Best waiting time: 65.28444121939238
Iteration 2, Best waiting time: 65.24959706464918
Iteration 3, Best waiting time: 53.447520189990975
Iteration 4, Best waiting time: 53.438535088241544
Iteration 5, Best waiting time: 53.438535088241544
Iteration 6, Best waiting time: 53.438535088241544
Iteration 7, Best waiting time: 53.438535088241544
Iteration 8, Best waiting time: 53.438535088241544
Iteration 9, Best waiting time: 53.438535088241544
Iteration 10, Best waiting time: 53.438535088241544
Iteration 11, Best waiting time: 53.438535088241544
Iteration 12, Best waiting time: 53.438535088241544
Iteration 13, Best waiting time: 53.438535088241544
Iteration 14, Best waiting time: 53.438535088241544
Iteration 15, Best waiting time: 53.438535088241544
Iteration 16, Best waiting time: 53.438535088241544
Iteration 17, Best waiting time: 53.438535088241544
Iteration 18, Best waiting time: 53.438535088241544
Iteration 19, Best waiting time: 49.73998063487575
Iteration 20, Best waiting time: 49.73998063487575
Iteration 21, Best waiting time: 49.73998063487575
Iteration 22, Best waiting time: 49.73998063487575
Iteration 23, Best waiting time: 49.73998063487575
Iteration 24, Best waiting time: 49.73998063487575
Iteration 25, Best waiting time: 49.73998063487575
Iteration 26, Best waiting time: 49.73998063487575
Iteration 27, Best waiting time: 49.73998063487575
Iteration 28, Best waiting time: 49.73998063487575
Iteration 29, Best waiting time: 49.73998063487575
Iteration 30, Best waiting time: 49.73998063487575
Iteration 31, Best waiting time: 49.73998063487575
Iteration 32, Best waiting time: 49.73998063487575
Iteration 33, Best waiting time: 49.73998063487575
Iteration 34, Best waiting time: 49.73998063487575
Iteration 35, Best waiting time: 49.73998063487575
Iteration 36, Best waiting time: 49.17892904882953
Iteration 37, Best waiting time: 49.17315886020306
Iteration 38, Best waiting time: 49.17315886020306
Iteration 39, Best waiting time: 49.17315886020306
Iteration 40, Best waiting time: 49.17315886020306
Iteration 41, Best waiting time: 49.17315886020306
Iteration 42, Best waiting time: 49.17315886020306
Iteration 43, Best waiting time: 49.17315886020306
Iteration 44, Best waiting time: 49.17315886020306
Iteration 45, Best waiting time: 49.17315886020306
Iteration 46, Best waiting time: 49.17315886020306
Iteration 47, Best waiting time: 49.17315886020306
Iteration 48, Best waiting time: 49.17315886020306
Iteration 49, Best waiting time: 49.17315886020306
Iteration 50, Best waiting time: 49.17315886020306
Iteration 51, Best waiting time: 49.17315886020306
Iteration 52, Best waiting time: 49.17315886020306
Iteration 53, Best waiting time: 49.17315886020306
Iteration 54, Best waiting time: 49.17315886020306
Iteration 55, Best waiting time: 49.17315886020306
Iteration 56, Best waiting time: 49.17315886020306
Iteration 57, Best waiting time: 49.17315886020306
Iteration 58, Best waiting time: 49.17315886020306