





Time = 120000 Number of Craters= 51.0

```

x x x      x - x      x x - - - x      0      x - x      0      x x x - - - x      x -
x x x      x      x x - - - x      x - x      0      x x x - - - x      0      x -
x x      0      x x x x x      x x - - - x x x x x - x      x x x x x - - - x      x -
x x      x      x      x x - - - x x      x - - x x x x x      x x - - x      x      x -
x x x      x x x x x x x x - - - x      0      x - - x x      0      x - x      x x x x x -
- x x x x x      x      x x - - - x      0      x x x x x      0      x - x      0      x -
- - - - - x x      x      x - - - - x      x x x      x      x - x      x      x x x
- - - x x x x      0      x x x - - - x      x      x      x      x x x x x      0      x
- - x      x x x x x      x x - - - x x x x      x      0      x x x x      x x x x
- - x      x x      x x - - - x      x      x      x      x      x      x x x x      x x x
x x x x      x x      0      x - - - - x      x x x x x x x      0      x - - x x x x x
x      x      x      x x - - - x x      x      x      x      x      x      x - - x      0
0      x      x      x x x - - x      0      x      x x x x - - x x x x x - - - x x x
x      x      x      x x - - - x      0      x      x      x      x      x      x - - x
x x x x      x x x x x x x x - - - x      x      x      0      x - - - - x x x x x
- - - x      0      x      x - - - x x x x x - - x x x x      x - - - - x      x - - -
- - - x      x      x      x - - - - x      x x x      x      x x x x x - x      x - - -
- - - - x      0      x x x x x x - - - x      0      x x x x x x x x x - x      0      x -
- - - - x x x x      x      x - - - - x      0      x      x      x x x x      x - - -
- - - - x      x      x      x - - - x x      x      x      0      x      x x x x x -
- - x x x x x x x x      0      x - - x x x      x      x      0      x      x      x -
- - x      x      x - - x      x - - x x x x x      x      0      x      x      x -
- - x      0      x x x - x x x x x x x      0      x x x x x x x x x      x x
- x x      x - - - x      x x      x      x      x - - x x x x x      x x x x      x x x x
x x      x      x - - x x      x      x      x x x x      0      x      x x x x      0
x x x x      x x x      x      x      x      x      x x x x x      x      x      0
- x      x      x x      x      x      0      x x x x x x x      x x x x      x      x
- - x      x      x x x      x      x x x x x x - - x      x x      x x x x      x x x x
x x      x      x x x x x x      x      x      x - x      0      x      x      x
x      x      0      x      x - - x x x      x x - x      0      x      0      x x x x x x x
x x      0      x x x x x - - x x      x x - - - x x x      x      x      x x x x x x 0
x x      x      x - - - x      x      x - - - - x x x      x      x      x      x x x
x x x x x x      x x x x x - - x x x x      x - - - - x      0      x      x      x
x      0      x      x      x - - x      x - - - - x      x      0      x      x      x
x      x      x      x x x - x      x - - - - x      0      x x x      0      x      x
0      x x x x x x      x      x      x - - x      x - - - - x      0      x x x x x x x
x      x - - - - x      0      x - - x      x - - - x x x      x      x      x x x x x
x      x - - - - x x x x      x - - x      0      x - - - - x      x      x x x x x -
x x x - x - - - - x      x - - - x      x - - - - x x x x x x x x - - - -

```

Time = 150000 Number of Craters= 52.0

```

x x x      x - x      x x      0      x      0      x - x      x      x x x - - - x      x -
x x      x      x x x x x      0      x - x x      x x x - - - x      0      x -
x x      0      x x x x      x      x x x x x x - - x      0      x x x - x x x x      x -
x x      x      x      x x x x      0      x x x x x      x - - x      x x x - x x x x -
x x x x      x      x - - - - x      0      x x x x x x x x x x x x - x x      x -
- x x x x      x      x - - - - x      x      x      x      x      0      x x x x
x      x      0      x x x x x - - - x      x      0      x x x x x      x x x      x
x      0      x      x x x      x - - - - x      x      x      x x x x x x x x x x x x
x      x x x x      0      x      x - - - - x      x      x      x x x x      x x x x
x x x x x x      x x x x x - - x x      x      x      0      x      x      x      0
0      x      x      x      x x x - x      x      x      0      x      x      x      0
x      x      x      x      0      x x x      0      x x x x x      x      x      x x x x
x x x      x      0      x - x x      x x      x      x      x x x x x      x - - x x x x
x x x x - x x x x      x      x - - x x x      0      x x x x      x      x      x -
- - - x      0      x x x x x - - x x x      x      x      x - x x x      x      x -
- - - x      x      x - - - - x      x      x      0      x x - x x x      x      x -
- - - - x      0      x x x x x - x x x      0      x x x x x      x x x x      x -
- - - - x      x      x      x - - - x x x      x      x      x      x x x x x      x -
- - - - x      x      x      x - - - x x x      x      x      x      x x x x      x -
- - x x x x x x x x      0      x - - x x x x x x      x      0      x      x      0
- - x      x      x - - - x      x x x x      x x x      x      x      x      x      0
- x x      0      x x x - x x x x x x x      0      x x x x x x x x x      x x x
- x x      x - - - x      x x      x      x      0      x - x x x x      x x x x x x
x x      x      x - - x x      x      x      x - x x x x x      x x x x x x x x
x x x x x x x x x      0      x x x x      x      x      x      x      x x x x x
x x x x      x x x      x x x x x x x x x x x x x x x x      x      x      x 0
- x      x      x      x      x x x x x x      x x      0      x x x      0      x
- x x x x x x x      x x x      x x x x x x      x x      x      x - x x      x x x
- x      x      x x x x      0      x x x x x x      x      0      x x x x      x x x
x x      x x x x x x x x      x      x      0      x x x x x      x      x      x
x x      x      x      x x x x      x x x      x      x      0      x      x x x x x
x x      0      x x x x      x      x      x - x x x x x x x x      x x x x x x
x x x      x      0      x x      x x x - - - - x x x x      x - x      x -
x x      x      x      x x x x      x x - - - - x x x x      x      x      0
x x x x      0      x      x x      x x - - - - x      x      0      x x x x 0
x      x      x x x x x x x x      x - - - x x x x      x      x      x x x x
x x x x x x      x x x      x      x      x - - x      0      x      x      x
x      0      x x x x x x      x      x - - x      x x x x x x x      x      x
x      x      x      x      0      x      x - - - x      0      x      x      x      0
x      x      x      x      x x x x x x x      x      x      0      x      x
0      x x x x      0      x      x      x - - x      x x x      x x x      x      x
x      x - - x      x x x x x      x - - x      0      x x x x x      x      x x x x x
x x x - x - - x x x x x      x - - x      0      x - - - - x x x x x x x - - -

```

Time = 180000 Number of Craters= 56.0

```
x x x      x - x      x x      x 0      x - x      x x      x - - - x      x -
x x      x x      x x x x x      0      x      x - x x      x x x - - - x      0      x -
x x      0      x x x      x      x x x x x x x - x      0      x x x - x x x x      x -
x x      x x      x      x      x x x      x - x      x      x x x x x x x x      x -
- x x x x      x      x      x - - - x      0      x x x x x x x x x      x -
- x x x x      x      x      x - - - x      x      x x      x      0      x 0      x x x x
- x      0      x x x x x - - - x      x      x x      x      x      x
x      x      x x x      x - - - x x x      0      x x x x x x      x      x
x x x x x      x      x      x - - - x x      x x x x x x x x x x x x x x x
x      x      x x x x      0      x - - - x      x x x x x x      x x - - x x x x
0      x x      0      x      x - - x x x x x x x x      x      0      x - - x      0
x      x      x      x      x x - x      x      x      0      x      x - - x x x
x      x      x      x      x x x x x x x x x      x x x x x x x x x x - - x
x x x x      0      x      x x x x x - x x      x x      x      x x x x x x - - x
- - - x      x      x      x x x      0      x x x x x x      x - x      0      x x      x - -
- x x x x x x x      0      x x      x x      x x      x - x      x x      x - -
- x      x      x      x      x      x      x      x x      x x      0      x - -
x      0      x      0 x      x x      x x x x x      0      x x x x x x x x x x      x -
x      x      x      x      x      x      x      x      x      x      x      x x x -
x      x      x x x x x x x x x x x x x x x x      0 x      x x      0      x
x      x      x      x      x      x x x x x x      x x x      x      x      x
x      0      x x x x      0      x      x      x x x x x x x x      x      x      x
x x x x      x - x      x      x      0      x      0      x - x x x x x x x x x x x
x x      x      x - x x x x x      0      x x x x x      x - x x x x x x      x
x x x x x      x x      x      x      x      x      x      x      0      x      x x 0
x      x      x      0      x x x x x      0      x      0      x 0 x      x      x x
0      x x      x      x      x      x      x      0      x      x      0      x x x
0      x x      x      x      x      x      x      x      x      x      x      x x x
x      x      x      x      x      x      x      x      x      x      0      x x x x x x
x x      x      x      x      x      x      x      x      x      x      0      x - - -
x x      x      x      x      x      x      x      x      x      x      x      x x x x
x x x      0      x x      0      x x      x x      x      0      x x x x      x - x      x -
x x      x      x      x      x x x      x - - x      x x x      x x x x x x
x x      x      x      x      x      x x x x x      x - - x      x      x x x x x
x x      x x x x      x      x      x x x x x      x - - x      x      x x x x x
x x      x x x x      x x x x x      x      x      x - - x x x x x      0      x x
x      0      x x x x x x x      x      0      x x      x x x      0      x x x      x
x      x      x      x      0      x      x      x      x      x      0      x x x x x
x      x      x      x      x      x      x      x      x      0      x x      x
0 x x x x      0      x x      x x x x      x      x      x x x x      x x x x      x
x      x - x      x      x x x x x - x      x      x      x x x      0      x x x x x
x      x - x      x      x x      x - x      0      x x x x x - x      x      x x x x -
x x x - x - x      x x x x x      x - - x      x      x - - - - x x x x      x - - - -
```

Time = 210000 Number of Craters= 60.0

```
x x x      x x - x      x x      x 0      x - x      x x      x - - - x      x x x x
x x      x x      x x x x x      0      x      x - x      x x x - - - x      x
x x      0      x x x      x x x x x      x x x x x - x      0      x x x x x - x x x x
x x      x      x      x      x x x      x - x      x      x x x x x      0
x x      x x x      x      x      x x x      0      x x x x x      x      x
- x x x x      x      x      0      x - x      0      x x      x      0      x      x x x x
- x x x x      x      x      x - x      x      x      x      0      x 0      x 0      x x x x
- x      x x x x x x      x - - x      x x      0      x x      x      x      x
x      x      x      x x x x x - - x x x x      x x x x x      x      x
x x x x x      x      x      x - x x x x      x      x      x x x x x x x x x x x
x      x      0      x x      0      x      x x x x x x x x      x x - - x x x x
0      x      x      x      x      x      x      x      x      0      x - - x x x x
x      x      x x x x      x x - x      0      x      x      0      x      x - - x
x      x      x      x      x      x      x      x      0      x      x      x
x x      x      x      x - x x      x      0      x x x x x x x x x x      0      x
x x x x      0      x      x x x x x x x      0      x      x      x      x
x x x      x      x      x      x      x      x      x      x      x      x x x
- - - x      x      x      x x      0      x      x x x x x      x      0      x x x x x x
- x x x x x x      x      0      x x      0      x x x x x      x      x      x x x
- x      x      x      0      x      x      x      x      x      x      0      x x x
x      0      x x x      x x x x      x      x      x      0      x x x x x x x x
x      x      x      x      x      x      x      x      x      x      x      x
0      x x      x x x x      x x      0      x      x      x      0      x - - x
x      x      x      x      x      x      x      x      x      x      x      x
x x      0      x      x      x      x      0      x      x      x      x      x x x
x      x      x      x      x      x      x      x      x      x      x      x
x x x      x      x      x      x      x      x      x      x      x      x      x
x x      x      x      x      x      x      x      x      x      x      x      x
x x x x      x      x      x      x      x      x      x      x      x      0      x
x      x      x      x      0      x x x x      0      x      0      x      x      x
0      x x x x x x      x      x      x      x      0      x      x      x x x x x x
x      x      x      x x x x      x      x      x      x      x      x      x x x
x x      0      x x x x      x      x      x x x x      x      x      x      x x x
x x      x      x      x      x      x      x      x      x      x      x      x
x x x      x      x      x      x      x      x      x      x      x      x      x
x x      x x x x      x      x      x x x - x      0      x x x x      x      x
x x      x      x      x      0      x x      x - - x      x x x      x      x
x x      x      x      x x x x      x x x      x - - x      x      x x x x      0      x
x x      x x x      0      x x      x      x      x - - x x x x x      x      x
x      0      x x      x      x      0      x x      x      0      x x x      x x
x      x      x      x      x      x      x      x      x      x      x      x
x      x      x      x      x      x      x      x      x      0      x x x x x
0 x x x x      0      x x      x x x x      x      x      x x x x      x x x
x      x - x      x      x x x x x - x      x      x      x      0      x x x x x
x      x - x      x      x x      x - x      0      x x x x x - x      x      x x x x -
x x x - x - x      x x x x x      x - - x      x      x - - - - x x x x      x - - - -
```


[illegible][illegible]

Years to Saturation: 319965

Time	Number of Craters
0	0
10000	10.0
20000	15.0
30000	20.0
40000	25.0
50000	27.0
60000	29.0
70000	33.0
80000	43.0
90000	49.0
100000	51.0
110000	54.0
120000	51.0
130000	51.0
140000	49.0
150000	52.0
160000	56.0
170000	57.0
180000	56.0
190000	55.0
200000	59.0
210000	60.0
220000	58.0
230000	56.0
240000	57.0
250000	59.0
260000	57.0
270000	56.0
280000	57.0
290000	60.0
300000	57.0
310000	58.0

Code:

```
#!/usr/bin/python

import random

# area is 500km x 500 km but is broken into a 10km grid
# therefore we can use a 50 x 50 area and have craters be 5 units large rather than 50
SIZE = 50
craterSize = SIZE/10
craters = [0]
time = 0
crater = 0.0
EMPTY = '-'
CENTER = 'O'
CRATER = ' '
DEBRIS = 'x'

# initialize empty, uncratered grid
grid = [[EMPTY for x in xrange(SIZE)] for x in xrange(SIZE)]

# function that goes through the grid and counts the number of crater centers
def numCraters(grid):
    crater = 0
    for i in range(SIZE-1):
        for j in range(SIZE-1):
            if(grid[i][j] == CENTER):
```

```

        crater += 1.0
    return crater

# Randomly pick a spot on the grid and make a crater centering at this location.
def makeImpact(grid):
    imp_i = random.randrange(0, SIZE-1)
    imp_j = random.randrange(0, SIZE-1)

    for i in range((craterSize/2)+2):
        for j in range(((craterSize/2)+2)-i/2):
            # must ensure that you won't write outside of the grid, if the center is near
            an edge of the grid

            # create circle of debris first, as this is the largest circle
            if(imp_i+i >= SIZE):
                if(imp_j+j >= SIZE):
                    grid[imp_i][imp_j-j] = DEBRIS
                    grid[imp_i-i][imp_j-j] = DEBRIS
                    grid[imp_i-i][imp_j] = DEBRIS
                if(imp_j-j <= 0):
                    grid[imp_i][imp_j+j] = DEBRIS
                    grid[imp_i-i][imp_j] = DEBRIS
                    grid[imp_i-i][imp_j+j] = DEBRIS
                if(imp_j+j < SIZE and imp_j-j > 0):
                    if(imp_j+j >= SIZE): print SIZE
                    grid[imp_i][imp_j-j] = DEBRIS
                    grid[imp_i][imp_j+j] = DEBRIS
                    grid[imp_i-i][imp_j-j] = DEBRIS
                    grid[imp_i-i][imp_j+j] = DEBRIS

            if(imp_i - i < 0):
                if(imp_j+j >= SIZE):
                    grid[imp_i][imp_j-j] = DEBRIS
                    grid[imp_i+i][imp_j-j] = DEBRIS
                    grid[imp_i+i][imp_j] = DEBRIS
                if(imp_j-j < 0):
                    grid[imp_i][imp_j+j] = DEBRIS
                    grid[imp_i+i][imp_j] = DEBRIS
                    grid[imp_i+i][imp_j+j] = DEBRIS
                if(imp_j+j < SIZE and imp_j-j>0):
                    if(imp_j+j >= SIZE): print SIZE
                    grid[imp_i][imp_j-j] = DEBRIS
                    grid[imp_i][imp_j+j] = DEBRIS
                    grid[imp_i+i][imp_j-j] = DEBRIS
                    grid[imp_i+i][imp_j+j] = DEBRIS

            if(imp_j+j >= SIZE):
                if(imp_i+i >= SIZE):
                    grid[imp_i-i][imp_j] = DEBRIS
                    grid[imp_i-i][imp_j-j] = DEBRIS
                    grid[imp_i][imp_j-j] = DEBRIS

                if(imp_i-i <= 0):
                    grid[imp_i-i][imp_j] = DEBRIS
                    grid[imp_i-i][imp_j-j] = DEBRIS
                    grid[imp_i][imp_j-j] = DEBRIS

            if((imp_i+i < SIZE) and imp_i-i >0):
                grid[imp_i-i][imp_j] = DEBRIS
                grid[imp_i+i][imp_j] = DEBRIS
                grid[imp_i-i][imp_j-j] = DEBRIS
                grid[imp_i+i][imp_j-j] = DEBRIS

```



```

if(imp_j-j <= 0):
    if(imp_i+i >= SIZE):
        grid[imp_i-i][imp_j] = DEBRIS
        grid[imp_i-i][imp_j+j] = DEBRIS
        grid[imp_i][imp_j+j] = DEBRIS
    if(imp_i-i <= 0):
        grid[imp_i-i][imp_j] = DEBRIS
        grid[imp_i-i][imp_j+j] = DEBRIS
        grid[imp_i][imp_j+j] = DEBRIS
    if(imp_i+i < SIZE and imp_i-i>0):
        grid[imp_i-i][imp_j] = DEBRIS
        grid[imp_i+i][imp_j] = DEBRIS
        grid[imp_i-i][imp_j+j] = DEBRIS
        grid[imp_i+i][imp_j+j] = DEBRIS

if(imp_j+j < SIZE and imp_j-j >=0 and imp_i +i < SIZE and imp_i - i >=0):
    grid[imp_i-i][imp_j-j] = DEBRIS
    grid[imp_i+i][imp_j-j] = DEBRIS
    grid[imp_i-i][imp_j +j] = DEBRIS
    grid[imp_i+i][imp_j +j] = DEBRIS

```

make a smaller circle within the debris circle for the actual crater

```

for i in range((craterSize/2)+1):
    for j in range(((craterSize/2)+1)-i/2):
        if(imp_i+i >= SIZE):
            if(imp_j+j >= SIZE):
                grid[imp_i][imp_j-j] = CRATER
                grid[imp_i-i][imp_j-j] = CRATER
                grid[imp_i-i][imp_j] = CRATER
            if(imp_j-j <= 0):
                grid[imp_i][imp_j+j] = CRATER
                grid[imp_i-i][imp_j] = CRATER
                grid[imp_i-i][imp_j+j] = CRATER
            if(imp_j+j < SIZE and imp_j-j>0):
                grid[imp_i][imp_j-j] = CRATER
                grid[imp_i][imp_j+j] = CRATER
                grid[imp_i-i][imp_j-j] = CRATER
                grid[imp_i-i][imp_j+j] = CRATER

        if(imp_i - i < 0):
            if(imp_j+j >= SIZE):
                grid[imp_i][imp_j-j] = CRATER
                grid[imp_i+i][imp_j-j] = CRATER
                grid[imp_i+i][imp_j] = CRATER
            if(imp_j-j < 0):
                grid[imp_i][imp_j+j] = CRATER
                grid[imp_i+i][imp_j] = CRATER
                grid[imp_i+i][imp_j+j] = CRATER
            if(imp_j+j < SIZE and imp_j-j>0):
                grid[imp_i][imp_j-j] = CRATER
                grid[imp_i][imp_j+j] = CRATER
                grid[imp_i+i][imp_j-j] = CRATER
                grid[imp_i+i][imp_j+j] = CRATER

        if(imp_j+j >= SIZE):
            if(imp_i+i >= SIZE):
                grid[imp_i-i][imp_j] = CRATER
                grid[imp_i-i][imp_j-j] = CRATER
                grid[imp_i][imp_j-j] = CRATER

            if(imp_i-i <= 0):
                grid[imp_i-i][imp_j] = CRATER
                grid[imp_i-i][imp_j-j] = CRATER

```

```

        grid[imp_i][imp_j-j] = CRATER

        if((imp_i+i < SIZE) and imp_i-i >0):
            grid[imp_i-i][imp_j] = CRATER
            grid[imp_i+i][imp_j] = CRATER
            grid[imp_i-i][imp_j-j] = CRATER
            grid[imp_i+i][imp_j-j] = CRATER

        if(imp_j-j <= 0):
            if(imp_i+i >= SIZE):
                grid[imp_i-i][imp_j] = CRATER
                grid[imp_i-i][imp_j+j] = CRATER
                grid[imp_i][imp_j+j] = CRATER

            if(imp_i-i <= 0):
                grid[imp_i-i][imp_j] = CRATER
                grid[imp_i-i][imp_j+j] = CRATER
                grid[imp_i][imp_j+j] = CRATER

            if(imp_i+i < SIZE and imp_i-i>0):
                grid[imp_i-i][imp_j] = CRATER
                grid[imp_i+i][imp_j] = CRATER
                grid[imp_i-i][imp_j+j] = CRATER
                grid[imp_i+i][imp_j+j] = CRATER

        if(imp_j+j < SIZE and imp_j-j >=0 and imp_i +i < SIZE and imp_i - i >=0):
            grid[imp_i-i][imp_j-j] = CRATER
            grid[imp_i+i][imp_j-j] = CRATER
            grid[imp_i-i][imp_j +j] = CRATER
            grid[imp_i+i][imp_j +j] = CRATER

        grid[imp_i][imp_j] = CENTER    #finally place the center at the center of the
impact
    return grid

```

#returns true if there is saturation (ie less that 5% change when time doubles)

```

def checkSat(craters, time):
    if(time==0):
        curAvg = 0.0
        oldAvg = 0.0
    else:
        if((time/2)==0):
            curAvg = craters[time] / time
            oldAvg = 0.0
        else:
            curAvg = craters[time] / time
            oldAvg = craters[time/2] / (time/2)
    # if the number of craters changes by less than 5% when time is doubled
    # we have reached saturation
    if(abs(craters[time] - craters[time/2]) < craters[time/2]*0.05):
        # if there are less than 5 craters we definitely have not reached saturation
        # but test could still pass
        if(craters[time] < 5):
            return False
        else:
            return True
    else:
        return False

```

```

# while the grid is not saturated with craters continue randomly generating impacts and
increasing time
while not checkSat(craters, time):

```

```

# cratering rate is 1 impact every 1000 years, therefore every year chance of impact
is 1/1000
# generate a number between 1 and 1000
impact = random.randrange(1,1000)

# if the random number is some specific number make an impact
if(impact == 129):
    grid = makeImpact(grid)
    craters.append(numCraters(grid))
if(time % 30000 == 0):
    print "\nTime = ", time, " Number of Craters= ", craters[time]
    for x in grid:
        print(' '.join(x))
    time += 1

print "\n-----
results-----"
for x in grid:
    print(' '.join(x))
print "Number of Craters: ", numCraters(grid)
print "Years to Saturation: ", time
print "Time | Number of Craters"
for i in range(len(craters)):
    if(i % 10000 == 0):
        toprint = ""
        for x in range(int(craters[i])):
            toprint += "*"
        print i, " | ", toprint, " ", craters[i]

```

We are wanting to simulate a 500km x 500km area but we have divided it into 10km cells meaning we can do a simulation for a 50x50 area instead, which will run more quickly. Each year there is a 1/1000 chance an impact will occur. As long as we have not reached saturation, meaning the number of craters has changed by less than 5% when the time doubles, we continue allowing impacts to form.