

TRABAJO PRACTICO

```

PUBLIC STATIC String ConcatNro(int[] arq, int n) {
    String result = "";
    int i = n;
    while (i > n/2) {
        for (int j = n; j >= 1; j -= 4) {
            for (int k = 1; k <= n; k += 2) {
                result += "," + arq[k];
            }
            i /= 2;
        }
        return result;
    }
}

```

$T_1(n)$ {
 $T_2(n)$ {
 $T_3(n)$ {

↳ se ejecuta en una computadora que procesa 100.000 operaciones por segundos. calcular $T(n)$ considerando orden de ejecución, tomando $n = 300.000$

$$n = 300.000, \quad PC = 100.000 \text{ OP/D} \quad 18.19$$

$$O(n) = n \cdot \log(n) \Rightarrow O(300.000) = 300.000 \times \log(300.000)$$

$$300.000 \times 18.19 = 5.457.000 \text{ OP}$$

$$\frac{5.457.000 \text{ OP}}{100.000 \text{ OP/D}} = 54.57 \text{ seg}$$

PROVA $T_3(n)$:

$$T_3(n) = C_0 + \sum_{k=1}^{\log(n)+1} C_1$$

Iteration k	Indice k	$k < n$
1	$1 \rightarrow 2^0$	$2^{k-1} < n$
2	$2 \rightarrow 2^1$	$k-1 < \log(n)$
3	$4 \rightarrow 2^2$	$k < \log_2(n)+1$
4	$8 \rightarrow 2^3$	

$$T_3(n) = C_0 + (\log_2(n)+1) \cdot C_1 \Rightarrow O(n) = \log_2(n)$$

PROVA $T_2(n)$

$$T_2(n) = C_{10} + \sum_{j=1}^{n/4} (C_{20} + T_3(n))$$

$$= C_{10} + \frac{n}{4} \cdot (C_{20} + C_0 + (\log(n)+1) \cdot C_1) \Rightarrow O(n) = n$$

$$T_2(n) = C_{10} + \frac{n}{4} \cdot (C_{21} + (\log_2(n)+1) \cdot C_1); C_{21} = C_{20} + C_0;$$

$$\hookrightarrow O(n) = O(n) \cdot O(\log_2(n)) \Rightarrow O(n) = O(n \cdot \log_2(n))$$

Iteration k	Indice I = n
1	n
2	n-4
3	n-4-4
4	n-4-4-4

$$\left. \begin{array}{l} J = n-4(k-1) \\ J \geq 1 \\ n-4(k-1) \geq 1 \\ -4(k-1) \geq 1-n \\ k-1 \geq \frac{n-1}{4} \end{array} \right\}$$

PARA $T_1(n)$

Iteración k	Iteración $i=n$
1	n
2	$n/2$
3	$n/4$
4	$n/8$

$T = n/2^{k-1}$

$$1 \geq n/2$$

$$\frac{n}{2^{k-1}} \geq \frac{n}{2}$$

$$n \geq \frac{n}{2} \cdot 2^{k-1}$$

$$2n \geq 2^{k-1}$$

$$2 \geq 2^{k-1}$$

$$\log(2) \geq k-1$$

$$1+1 \geq k$$

$$2 \geq k$$

\Rightarrow POR LO TANTO ITERO
2 veces

$$T_1(n) = C_{40} + \sum_{i=1}^{k=2} (T_2(n) + C_{33}) \Rightarrow C_{40} = C_{30} + C_{31} + C_{32}$$

$$T_1(n) = C_{40} + 2 \left(C_{43} + \frac{n}{4} (C_{21} + (\log_2(n) + 1) \cdot C_1) + C_{33} \right)$$

$$T_1(n) = C_{40} + 2 \left(C_{43} + \frac{n}{4} (C_{21} + \log_2(n) + 1) \cdot C_1 \right); C_{43} = C_1 + C_3$$

$$T_1(n) = C_{40} + 2C_{43} + \frac{n}{2} (C_{21} + (\log_2(n) + 1) \cdot C_1)$$

$$T_1(n) = C_{50} + \frac{n}{2} (C_{21} + (\log_2(n) + 1) \cdot C_1); C_{50} = C_{40} + 2C_{43}$$

$$O(n) = O(1) \cdot O(n) \cdot O(\log_2(n))$$

$$O(n) = O(n \cdot \log(n))$$