

- Data Structure \rightarrow Way of collecting and organising data.
 - Used to increase efficiency of programs & reduce complexity of programs.

Algorithm + data structure = program

- Algorithm: Stepwise solution of a problem
- Abstract data type: Specifies type of data stored, operations supported on them and so on. Provides concept for data abstraction & data hiding.
- Dynamic memory allocation: Process of manually allocating memory during runtime.
 - malloc \rightarrow used to allocate memory dynamically
 - realloc \rightarrow used to allocate multiple blocks of memory
 - realloc \rightarrow change the size of memory block allocated
 - free \rightarrow used to deallocate the dynamically allocated memory
- Algorithm complexity: - Gives the running time and storage space required by the algorithm in terms of input size.
 - * Space complexity: - Represents the amount of memory space required by the algorithm
 - * Time complexity: Represents the amount of time required by the algorithm to run to completion

- Asymptotic Notation: Mathematical notation to calculate time complexity of algorithms.
 - * (Big Oh Notation): used to classify algorithms according to how their running time or space requirement grows as the input size grows.

Stack: Linear data structure based on the concept of LIFO. Elements may be inserted or deleted using push and pop operation from the end.

Applications:

- \rightarrow Evaluate postfix & prefix exp, Used in recursion
- \rightarrow Page-visited history on web pages, perform undo in text editors

Queue: Linear data structure based on the concept of FIFO. ordered collection of objects. Items may be deleted from front end and inserted from rear end. Enqueue & dequeue are used to insert & delete elements.

Applications:

- \rightarrow Task waiting for printing
- \rightarrow Time sharing system for use of CPU
- \rightarrow Task scheduling in operating system

Linear queue: Ordered list in which elements are organised in sequential order. Insertion & deletion is fixed: i.e. front & rear. wastes memory space.

Circular queue: stored data in circular fashion. Capable of inserting & deleting from any point until it is occupied. Makes efficient use of memory space.

Priority Queue: collection of elements such that each element is assigned a priority. Element with higher priority is processed before element with lower priority. If equal priority, then processed according to order in which they were added to the queue.

Applications: i) CPU scheduling. ii) Priority based jobs. iii) Time sharing system.

Deque: Linear list, in which elements can be added or removed at either end but not middle. Under Double-Ended Queue. It is maintained by a circular array with pointer LEFT & RIGHT which points to the two ends of the queue.

Linked List: Linear collection of data elements whose order is not given by their physical placement in memory. Instead each element points to next. It is basically the collection of nodes which together represents a sequence.

Array
→ collection of data elements whose size is fixed (insertion & deletion is difficult)
→ same amount of time req'd to access each element
→ If we have to go to a particular element, then we can reach directly, & it is more expensive

Linked List
→ " " " size is not fixed
→ different amount of time
→ If we have to go " " " we have to go through all nodes that come before that node.

Singly Linked List: Each node contains two fields: info field & link field.
info → used to store data items.
next link → point to the next node in sequence.

Doubly Linked List: Node contains three fields.
prev → point to previous node in sequence
info → used to store data
next → point to next node in sequence

Circular Linked List: It is a linked list where the link field of last node points to the very first node of the list.

- **Searching:** A technique that helps to find the place or position of a given element or value in the list.
- **Linear / sequential search:** It is a method of finding an element in the list. It sequentially checks each element in the list until a match is found or the whole list is searched.
- **Binary search:** Another method of searching. It works only with sorted list. It compares search element with the middle element in the list.
- **Hashing:** Efficient searching technique. It calculates the position of the key in the hash table based on value of key. It uses a hash function.
- **Hash function:** Transforms a key into the table index value. It maps the key with corresponding key address or location. It will take any item & returns hash value betn the range 0 to n-1 where n is the size of hash table.
- **Hash table:** A data structure used for storing and accessing data very quickly during hashing. Insertion of data is based on key value.
- **Types of hash function:**
 - 1) Division: ^{hash key is} based on modulo i.e. remainder.
 - 2) Mid square: Key is squared & mid part is taken as hash key/index
 - 3) Digital folding:
- **Hash collision:** Also known as clash, is a situation when two distinct pieces of data have same hash value.
- **Collision resolution:** When hash collision occurs, there must be systematic method for placing the second item in table. This process is called:
 - * **Open hashing:** Chaining, hashing using bucket (same location is shared)
 - * **closed hashing:** (open addressing) \rightarrow Linear probing, Quadratic probing, Double hashing
 - * **Rehashing**
- \rightarrow **Chaining:** It allows each slot in table to hold a chain of items. Allows many items to exist at the same location.
- \rightarrow **Linear probing:** If data can't be placed at the index calculated by the hash function, we put it in next empty space in table. It has clustering problem.
- \rightarrow **Quadratic probing:** eliminates primary clustering problem.

There is no guarantee of finding slot after half full

 $(h + i^2) \% \text{table size}$, $h = \text{hash (index) value}$
 $i = \text{no. of collision occurred}$
- \rightarrow **Double hashing:** $(h_1(x) + i \cdot h_2(x)) \% (\text{table size})$, $h_1(x) = x \bmod \text{size of table}$
 $h_2(x) = P - (x \bmod P)$
- \rightarrow **Rehashing:** Hashing again. Load factor $(\alpha) = \frac{n}{N}$, $n = \text{no. of data elem}$, $N = \text{hash table size}$
 α must be ≤ 1 . If $n > N$, then we do rehash by increasing buckets or modify hash function

- **Recursion**: It is the process by which a function calls itself directly or indirectly to work in a smaller part of the program. A problem is solved by dividing it into smaller problems, which are similar in nature to the original problem. These smaller problems are solved & their solutions are applied to get the final result.
- A function is recursive if
 - i) It calls itself
 - ii) Function should have base case (stopping)
- **Tail Recursion**: A recursive function is tail recursive when recursive call is the last thing executed by the function. It is better than non-tail recursion, as there is no task left after recursive.
- Some recursive algorithm: factorial, gcd, Fibonacci series, To H
- Applications of recursion:
 - i) Used in Trees
 - ii) Sorting algorithms uses recursion
 - iii) searching " " "
- Advantages & disadvantages:

Advantages:	Disadvantages:
i) The code becomes easier to write.	i) slower than non-rec. function
ii) Reduces unnecessary calling of functions	ii) requires more memory.
	iii) difficult to think recursively
- **Sorting**: Process of ~~ordering~~^{arranging} the elements in specific order.
 - **Internal sorting**: Arranging the numbers within the array only, which is in computer's primary memory.
 - **External sorting**: Sorting of number from external file by reading from secondary memory.
 - **Uses of sorting**: Dictionary, index of book, banking applications
- * **Comparison Sorting algorithm**: Bubble sort, selection sort, insertion sort
- * **Divide & conquer algorithm**: Quick sort, merge sort, heap sort, shell sort
- **Bubble sort**: Simplest sorting alg. works by repeatedly swapping the adjacent elements if they are in wrong order.
- **Selection sort**: It is about picking smallest element from given array & placing it into sorted portion in 1st. Initially 1st element is considered to be min. & compared with other elements.
- **Insertion sort**: element gets compared & inserted into the correct position in the 1st. you consider 1 part of 1st to be sorted & another consider 1st element to be sorted posn, & other elements ---
- * **Divide & Conquer**: Important problem solving technique that makes use of recursion.
 - Divide: Smaller problems are solved recursively
 - Conquer: Solution of original problem is then formed from the solutions of
- **Quick-sort**: Fast D&C algorithm [partition & sort phase]
- **Merge-sort**: Merging two or more sorted files into a third sorted file.
- **Shell sort**: Improved version of insertion sort. Contains Gap.

Tree: A tree is a non-linear data structure, which is a collection of nodes linked with each other in a non-cyclic form.
A tree has a root, internal & leaf nodes.

Root: A node with no parent.

Leaf: A node with no children.

Internal node: Node with at least one child.

Path: Sequence of edges from source to destination node.

Depth of node: Length of path from root to the node.

Height of node: Length of longest path from node to a leaf node.

Depth of tree: Depth of node that is maximum among all the nodes.

Height of tree: Height of root node.

Sibling: Nodes having same parents.

Binary tree: Tree in which each internal node has at most (max) two children.

Strictly binary tree: Each internal node has either 0 or 2 child.

Complete binary tree: Nodes at each level have only two child.

Almost complete binary: Nodes are filled from left to right from the parent node.

Binary Tree Traversal: Visiting each node exactly once in a systematic manner.
1) Pre-order: root, left, right
2) In-order: left, root, right
3) Post-order: left, right, root.

Binary Search Tree: A binary tree that is either empty or every node contains a key value that satisfies:
→ All keys in left subtree of root are smaller than root key.
→ " " " right subtree are greater than root node key.
→ The left & right subtree of the root are again BST.

AVL Tree: Balanced binary tree. It is a BST, where the balance factor at each node is -1, 0, or 1. Balance Factor = height of left subtree - height of right subtree.

Make non AVL tree to AVL: by rotation:

1) Left rotation: When tree becomes right skewed \rightarrow

2) Right rotation: When tree is left skewed: \rightarrow

3) Left-right rotation: \rightarrow

4) Right-left rotation: \rightarrow

- Graph: Graph is a non linear data structure which is a set of vertices V connected by edges E . $G(V, E)$. A graph may be directed or undirected. Each edge has one or two vertices associated with it.
- Directed graph: Direction of edges is specified.
- Simple graph: Graph with no multiple edges or loops.
- Multi graph: Graph with multiple edges.
- Pseudo graph: Graph with loops as well as multiple edges.
- Mixed graph: Graph with both directed & undirected edges.
- Application of graph:
 - Model geographic map of cities
 - Analyze the electrical circuits
 - Finding shortest paths.
- Representation of graph: Adjacency lists & adjacency matrix.
 - Adjacent vertices: Two vertices connected with common edge.
 - Adjacent edges: Two edges going out of a same vertex.
 - Adjacency list: Specifies the vertices adjacent to each vertex.
 - Adjacency matrix: n -by- n zero-one matrix $A = [a_{ij}]$

$$a_{ij} = \begin{cases} 1 & \text{if } v_i \text{ \& } v_j \text{ are adjacent} \\ 0 & \text{otherwise} \end{cases}$$
 - Incidence matrix: matrix formed by incidence of edges.
 - Complete graph: Simple graph that contains exactly one edge between each pair of vertices. K_n .

$$K_1 \cdot K_2 = K_3 \triangle K_4 \boxtimes$$
 - Connected graph: An undirected graph is connected if there is a path between every pair of distinct vertices of graph.
 - Graph Traversal: Visiting each vertex in a graph exactly once in a systematic manner.
 - Breadth First Search (BFS): uses Queue.
 - Depth First Search (DFS): uses Stack.
 - Shortest path: Shortest path ^{betⁿ} any two vertices with minimum weight.
 - Relaxation: Process of testing total weight of shortest path betⁿ any 2 vertices.
 - Dijkstra's Alg: ~~Short~~ Single Source Shortest path algorithm for the weighted graph.
 - Spanning Tree: A subgraph of a graph G with minimum possible ⁿ of edges. If G has n vertices, then its spanning tree has $n-1$ edges. It cannot form cycle, cannot be disconnected.
 - Minimum Spanning Tree: A m.s.t of a weighted graph G is a subgraph of G ~~with~~ that includes all vertices of G with min. possible edges & has min. weight than all other possible spanning tree.
 - Kruskal's Algorithm: M.S.T finding algorithm. It ~~is~~ ^{may not be} connected from beginning.
 - Prim's algorithm: It is always connected from beginning to end.