

**MATHEMATICS Extended Part**  
**Module 1 (Calculus and Statistics)**  
**Question-Answer Book**

8:30 am – 11:00 am (2½ hours)  
This paper must be answered in English

**INSTRUCTIONS**

- (1) After the announcement of the start of the examination, you should first write your Candidate Number in the space provided on Page 1 and stick barcode labels in the spaces provided on Pages 1, 3, 5, 7, 9 and 11.
- (2) This paper consists of TWO sections, A and B.
- (3) Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question-Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
- (4) Graph paper and supplementary answer sheets will be supplied on request. Write your Candidate Number, mark the question number box and stick a barcode label on each sheet, and fasten them with string INSIDE this book.
- (5) Unless otherwise specified, all working must be clearly shown.
- (6) Unless otherwise specified, numerical answers should be either exact or given to 4 decimal places.
- (7) No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

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Candidate Number



**SECTION A (50 marks)**

1. The table below shows the probability distribution of a discrete random variable  $X$ , where  $a$  and  $b$  are constants such that  $6 < b < 15$ .

$x$	0	3	6	$b$	15
$P(X=x)$	0.3	$a$	0.1	0.2	0.2

It is given that  $\text{Var}(5X) = 739$ .

- (a) Find  $a$  and  $b$ .
- (b) Let  $C$  be the event that  $0 < X \leq 7$ .
- (i) Let  $D$  be the event that  $4 < X \leq 15$ . Are  $C$  and  $D$  independent? Explain your answer.
- (ii) Let  $E$  be an event such that  $P(E) \neq 0$ . If  $C$  and  $E$  are mutually exclusive, write down the greatest possible value of  $P(E)$ .

(7 marks)

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3. When a coin is tossed, the probability of getting a tail is  $p$ , where  $0 < p < 1$ . When the coin is tossed 20 times, the ratio of the probability of getting 1 tail to the probability of getting 3 tails is 49 : 57.

(a) Find  $p$ .

(b) The coin is tossed  $k$  times. Find the least value of  $k$  so that the probability of getting at least 1 tail is greater than 0.85.

(6 marks)

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(6 marks)

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5. Let  $n$  be a positive number.

(a) Expand  $\frac{2}{e^{nx}}$  in ascending powers of  $x$  as far as the term in  $x^3$ .

(b) Consider the expansion of  $(1+4x)^m + \frac{2}{e^{nx}}$ , where  $m$  is a positive integer. The coefficients of  $x$  and  $x^2$  in the expansion are 24 and 980 respectively. Find the coefficient of  $x^3$  in the expansion. (7 marks)

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This image shows a single sheet of white paper with horizontal blue or grey ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



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7. A computer programme adjusts the length and the breadth of a rectangular digital picture, such that the length of its diagonal remains constant while its breadth decreases at the constant rate of  $0.5 \text{ cm s}^{-1}$ . Initially, the length and the breadth of the picture are 20 cm and 15 cm respectively. Denote the breadth of the picture by  $x$  cm. Find the rate of change of the area of the picture when  $x = 7$ . (4 marks)

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(a)

$$\int_0^{0.5} \frac{-x^2}{e^2} dx$$

- (7 marks)

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Weight of a pumpkin ( $W$ kg)	$W \leq 3.6$	$3.6 < W \leq 5.7$	$W > 5.7$
Grade	C	B	A
Price (\$)	50	80	100

Suppose that 8 pumpkins are randomly chosen in the market and these pumpkins are put into a trolley.

- (i) Find the expected price of the pumpkins in the trolley.
  - (ii) Find the probability that there are at least 5 grade B pumpkins and at least 1 grade A pumpkin in the trolley.
- (6 marks)

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10. A courier delivers goods every day. The number of delays in delivery on a day follows a Poisson distribution with a mean of 1.6. A day is regarded as *smooth* if there are fewer than 3 delays on that day.
- (a) Find the probability that a certain day is *smooth*. (2 marks)
- (b) Find the probability that all the 7 days in a certain week are *smooth*. (2 marks)
- (c) Given that all the 7 days in a certain week are *smooth*, find the probability that there are exactly 10 delays in that week. (4 marks)
- (d) Given that there are no delays in at least 2 days in a certain week, find the probability that all the 7 days in that week are *smooth*. (4 marks)

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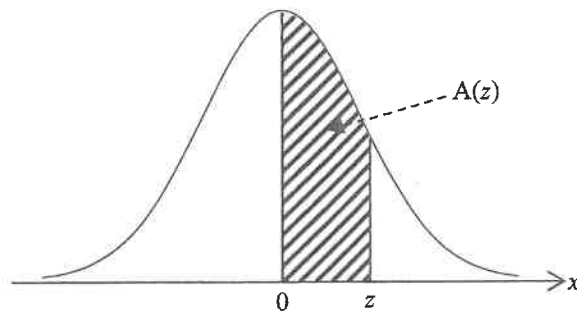
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Standard Normal Distribution Table

$z$	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998

Note : An entry in the table is the area under the standard normal curve between  $x = 0$  and  $x = z$  ( $z \geq 0$ ). Areas for negative values of  $z$  can be obtained by symmetry.



$$A(z) = \int_0^z \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}} dx$$