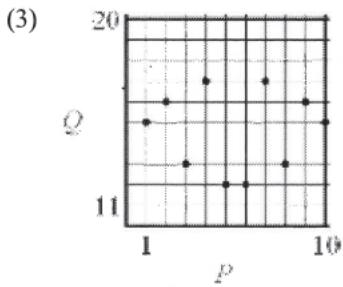
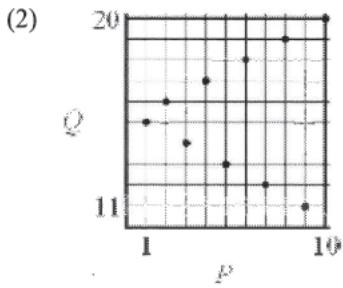
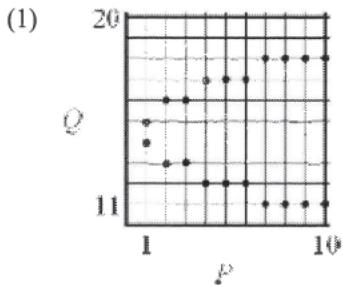


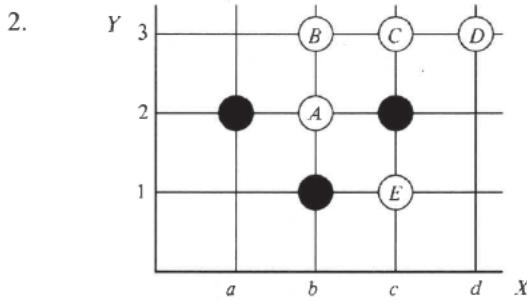
1. Given  $P = \{1, 2, 3, \dots, 10\}$ ,  
 $Q = \{11, 12, 13, \dots, 20\}$ ,

Which of the following three relations from  $P$  to  $Q$  illustrated in the graphs are mappings?



- A. (2) only  
B. (1) and (2) only  
C. (1) and (3) only  
D. (2) and (3) only  
E. (1), (2) and (3)

[1972-CE-MATHS B1-10]



$$X = \{a, b, c, d\}, \quad Y = \{1, 2, 3\}.$$

In the above figure, which one of the lettered circles should be blackened so that the graph represents a map from  $X$  into  $Y$ ?

- A. A  
B. B  
C. C  
D. D  
E. E

[SP-CE-MATHS 2-56]

3. If  $f(x) = \frac{1}{x+1}$ , then  $f(\frac{1}{x+1}) =$
- A.  $x$ .  
B.  $x + 1$ .  
C.  $\frac{1}{x}$ .  
D.  $\frac{x}{x+1}$ .  
E.  $\frac{x+1}{x+2}$ .

[1978-CE-MATHS 2-37]

4. If  $f(x) = x^2 + x + 1$ , then  $f(x+1) - f(x) =$
- A. 1.  
B. 3.  
C.  $2x + 1$ .  
D.  $2x + 2$ .  
E.  $x^2 + x + 1$ .

[1981-CE-MATHS 2-7]

5. If  $f(x) = 5^x + 1$ , then  $f(x+1) - f(x) =$
- A. 1.  
B. 6.  
C.  $4 \cdot 5^x$ .  
D.  $5 \cdot 5^x$ .  
E.  $4 \cdot 5^x + 1$ .

[1982-CE-MATHS 2-29]

6. A function  $f(x)$  is called an even function if  $f(x) = f(-x)$ . Which of the following functions is/are even functions?

- (1)  $f_1(x) = \frac{1}{x}$   
(2)  $f_2(x) = x^2$   
(3)  $f_3(x) = x^3$   
A. (1) only  
B. (2) only  
C. (3) only  
D. (1) and (2) only  
E. (2) and (3) only

[1983-CE-MATHS 2-37]

7. If  $f(x) = (\log_{10} 2x) - x$ , then  $f(x+1) - f(x) =$
- A.  $\log_{10} 2 - 1$ .  
B.  $\log_{10} \frac{x+1}{x}$ .  
C.  $\log_{10} \frac{10(x+1)}{x}$ .  
D.  $\log_{10} \frac{x+1}{10x}$ .  
E.  $\log_{10} \frac{x+1}{x} - 2x$ .

[1984-CE-MATHS 2-36]

8. If  $f(2x) = 8x^3 + 4x$ , then  $f(3a) =$

- A.  $9a^3 + 6a$ .
- B.  $12a^3 + 6a$ .
- C.  $27a^3 + 6a$ .
- D.  $108a^3 + 6a$ .
- E.  $216a^3 + 12a$ .

[1985-CE-MATHS 2-40]

9. If  $f(x) = x^2 + 1$ , then  $f(x-1) =$

- A.  $x^2$ .
- B.  $x^2 - 1$ .
- C.  $x^2 + 2$ .
- D.  $x^2 - 2x$ .
- E.  $x^2 - 2x + 2$ .

[1987-CE-MATHS 2-10]

10. If  $f(x) = 3 + 2^x$ , then  $f(2x) - f(x) =$

- A.  $2^x$ .
- B.  $2^{3x}$ .
- C.  $3 + 2^x$ .
- D.  $2^x(2^x + 1)$ .
- E.  $2^x(2^x - 1)$ .

[1988-CE-MATHS 2-34]

11. If  $f(x) = \frac{x}{1-x}$ , then  $f(\frac{1}{x}) =$

- A.  $\frac{1}{x-1}$ .
- B.  $\frac{1}{1-x}$ .
- C.  $\frac{x}{x-1}$ .
- D.  $\frac{x}{1-x}$ .
- E.  $\frac{1-x}{x}$ .

[1989-CE-MATHS 2-4]

12. If  $f(n) = \frac{1}{2}n(n-1)$ , then  $f(n+1) - f(n) =$

- A.  $f(1)$ .
- B.  $f(n)$ .
- C.  $\frac{n}{2}$ .
- D.  $1$ .
- E.  $n$ .

[1990-CE-MATHS 2-4]

13. If  $f(x) = x - \frac{1}{x}$ , then  $f(x) - f(\frac{1}{x}) =$

- A.  $0$ .
- B.  $2x$ .
- C.  $-\frac{2}{x}$ .
- D.  $2(x - \frac{1}{x})$ .
- E.  $2(\frac{1}{x} - x)$ .

[1991-CE-MATHS 2-35]

14. If  $f(x) = 10^{2x}$ , then  $f(4y) =$

- A.  $10^{4y}$ .
- B.  $10^{2+4y}$ .
- C.  $10^{8y}$ .
- D.  $40^y$ .
- E.  $40^{2y}$ .

[1993-CE-MATHS 2-1]

15. If  $f(x) = x^2 + 2x$ , then  $f(x-1) =$

- A.  $x^2$ .
- B.  $x^2 - 1$ .
- C.  $x^2 + 2x - 1$ .
- D.  $x^2 + 2x - 3$ .
- E.  $x^2 + 4x - 1$ .

[1994-CE-MATHS 2-1]

16. If  $f(x) = \frac{x}{1-x}$ , then  $f(\frac{1}{x})f(-x) =$

- A.  $-\frac{1}{2}$ .
- B.  $-1$ .
- C.  $-\frac{1-x}{1+x}$ .
- D.  $\frac{x}{1-x^2}$ .
- E.  $\frac{x}{x^2-1}$ .

[1995-CE-MATHS 2-35]

17. If  $f(x) = 3x^2 + bx + 1$  and  $f(x) = f(-x)$ , then  $f(-3) =$

- A.  $-26$ .
- B.  $0$ .
- C.  $3$ .
- D.  $25$ .
- E.  $28$ .

[1997-CE-MATHS 2-27]

18. If  $f(x) = x^2 - 3x - 1$ , then  $f(a) + f(-a) =$
- $2a^2$ .
  - $2a^2 - 2$ .
  - $6a$ .
  - $-6a$ .
  - $-2$ .

[1998-CE-MATHS 2-2]

19. If  $f(x) = x^2 - 1$ , then  $f(a-1) =$
- $a^2 - 2a$ .
  - $a^2 - 3a$ .
  - $a^2 - 3a - 2$ .
  - $a^2 - 1$ .
  - $a^2 - 2$ .

[1999-CE-MATHS 2-1]

20. Let  $f(x) = 3x^2 + ax - 7$ . If  $f(-1) = 0$ , find  $f(-2)$ .
- 27
  - 11
  - 3
  - 1
  - 13

[2000-CE-MATHS 2-4]

21. Let  $f(x) = x^2 - x - 3$ . If  $f(k) = k$ , then  $k =$
- 1.
  - 1 or 3.
  - 3 or 1.
  - $-\sqrt{3}$  or  $\sqrt{3}$ .

[2002-CE-MATHS 2-2]

22. If  $f(x) = 2x^2 + kx - 1$  and  $f(-2) = f(\frac{1}{2})$ , then  $k =$
- $\frac{-17}{3}$ .
  - 5.
  - 3.
  - $\frac{31}{5}$ .

[2003-CE-MATHS 2-1]

23. If  $f(x) = x^2 - x + 1$ , then  $f(x+1) - f(x) =$
- 0.
  - 2.
  - $2x$ .
  - $4x$ .

[2004-CE-MATHS 2-3]

24. If  $f(x) = 2x^2 - 3x + 4$ , then  $f(1) - f(-1) =$
- 6.
  - 2.
  - 2.
  - 6.

[2005-CE-MATHS 2-3]

25. If  $f(x) = \frac{x}{1+x}$ , then  $f(3)f(\frac{1}{3}) =$
- $\frac{3}{16}$ .
  - $\frac{1}{2}$ .
  - $\frac{3}{4}$ .
  - 1.

[2006-CE-MATHS 2-5]

26. Let  $f(x) = x^2 - ax + 2a$ , where  $a$  is a constant. If  $f(-3) = 29$ , then  $a =$
- 38.
  - 20.
  - 4.
  - 4.

[2007-CE-MATHS 2-8]

27. Let  $f(x) = x^2 + kx + 7$ , where  $k$  is a constant. If  $f(4) - f(3) = 21$ , then  $k =$
- 0.
  - 4.
  - 14.
  - 28.

[2008-CE-MATHS 2-6]

28. Let  $f(x) = x^2 - 9x + c$ , where  $c$  is a constant. If  $f(-1) = 8$ , then  $c =$
- 2.
  - 0.
  - 16.
  - 18.

[2009-CE-MATHS 2-6]

29. If  $f(x) = x^2 - 3x + 17$ , then  $3f(2) - 1 =$
- 27.
  - 34.
  - 44.
  - 70.

[2010-CE-MATHS 2-6]

30. Let  $f(x) = x^2 + 2x + k$ , where  $k$  is a constant.  
Find  $f(5) - f(3)$ .

- A. 20
- B.  $k + 8$
- C.  $k + 35$
- D.  $2k + 50$

[2011-CE-MATHS 2-8]

### HKDSE Problems

31. Let  $k$  be a constant. If  $f(x) = 2x^2 - 5x + k$ ,  
then  $f(2) - f(-2) =$

- A. -20.
- B. 0.
- C. 16.
- D.  $2k$ .

[2017-DSE-MATHS 2-6]

32. If  $f(x) = 3x^2 - 2x + 1$ , then  $f(2m - 1) =$

- A.  $6m^2 - 4m + 2$
- B.  $6m^2 - 4m + 6$
- C.  $12m^2 - 16m + 2$
- D.  $12m^2 - 16m + 6$

[2018-DSE-MATHS 2-7]

33. Let  $c$  be a constant. If  $f(x) = x^3 + cx^2 + c$ , then  
 $f(c) + f(-c) =$

- A. 0
- B.  $2c$
- C.  $2c^3 + 2c$
- D.  $-2c^3 + 2c$

[2019-DSE-MATHS 2-8]

34. Let  $f(x) = 3x^2 - x - 2$ . If  $\beta$  is a constant,  
 $f(1 + \beta) - f(1 - \beta) =$

- A.  $2\beta$
- B.  $10\beta$
- C.  $6\beta^2 - 2$
- D.  $6\beta^2 - 26\beta^2 - 2$

[2020-DSE-MATHS 2-5]

**Completing Squares**

1. Which of the following functions has its minimum value of 3, when  $x = 1$ ?

- A.  $y = (x - 1)^2 - 3$
- B.  $y = 3 - (x - 1)^2$
- C.  $y = (x + 1)^2 + 3$
- D.  $y = 3 - (x + 1)^2$
- E.  $y = (x - 1)^2 + 3$

[1972-CE-MATHS B1-18]

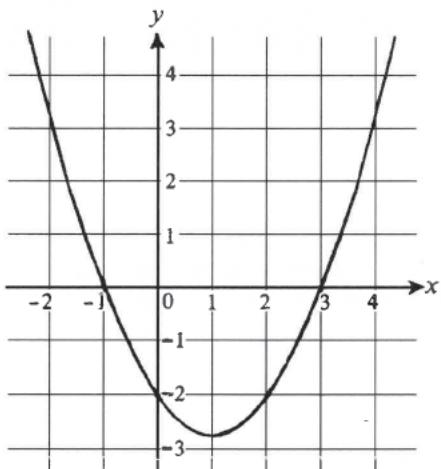
2. What number should be added to the expression  $4x^2 + 12x + 2$  in order to make it a perfect square?

- A. 10
- B. 7
- C. 6
- D. 4
- E. 2

[1979-CE-MATHS 2-48]

**Properties of Quadratic Graphs**

3.



The figure above shows the graph of

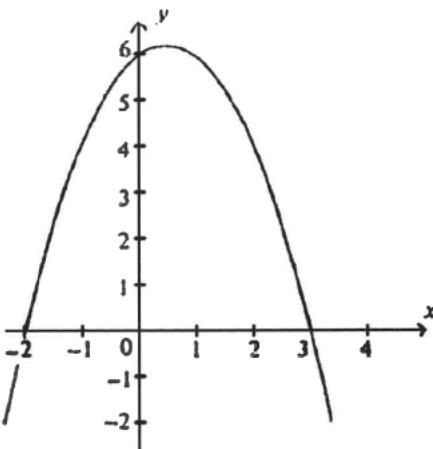
$$y = px^2 + qx + r.$$

The value of  $r$  is

- A. -2.
- B. -1.
- C. 0.
- D. 2.
- E. 3.

[SP-CE-MATHS 2-13]

4.



The figure above shows the graph of

- A.  $y = (x + 2)(x - 3)$ .
- B.  $y = (x - 2)(x + 3)$ .
- C.  $y = (x - 2)(x - 3)$ .
- D.  $y = -(x + 2)(x - 3)$ .
- E.  $y = -(x - 2)(x + 3)$ .

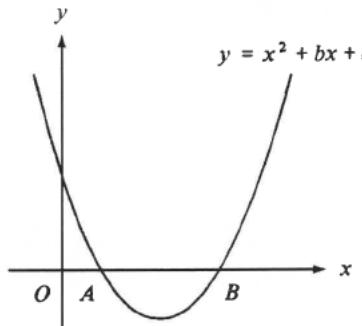
[1979-CE-MATHS 2-36]

5. The graph of  $y = x^2 + ax + b$  ( $a$  and  $b$  being constants) cuts the  $x$ -axis at  $(2, 0)$  and  $(h, 0)$ , and cuts the  $y$ -axis at  $(0, -2)$ .  $h =$

- A. -3.
- B. -2.
- C. -1.
- D. 0.
- E. 1.

[1984-CE-MATHS 2-34]

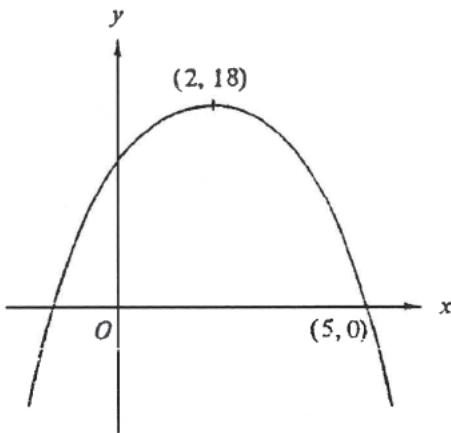
6. In the figure, the graph of  $y = x^2 + bx + c$  cuts the  $x$ -axis at  $A$  and  $B$ .  $OA + OB =$



- A.  $b$ .
- B.  $c$ .
- C.  $-b$ .
- D.  $-c$ .
- E.  $-\frac{b}{c}$ .

[1987-CE-MATHS 2-9]

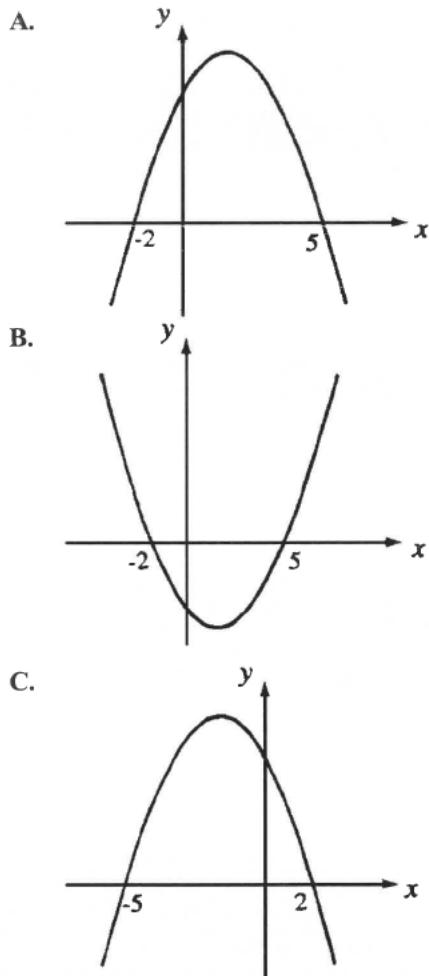
7. The figure shows the graph of a quadratic function  $y = f(x)$ . Given that the graph has vertex  $(2, 18)$  and it cuts the  $x$ -axis at  $(5, 0)$ , find the quadratic function.



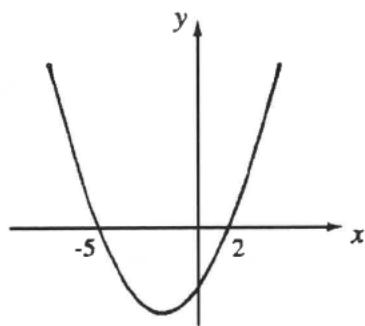
- A.  $y = (x - 2)^2 + 18$   
 B.  $y = -(x - 2)^2 + 18$   
 C.  $y = (x + 1)(x - 5)$   
 D.  $y = -2(x + 1)(x - 5)$   
 E.  $y = 2(x - 1)(x + 5)$

[1989-CE-MATHS 2-45]

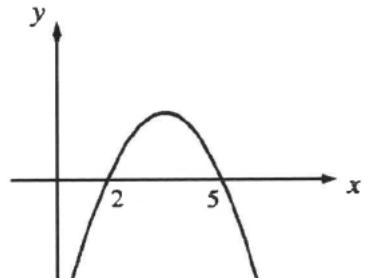
8. Which of the following may represent the graph of  $y = -x^2 + 3x + 10$ ?



D.

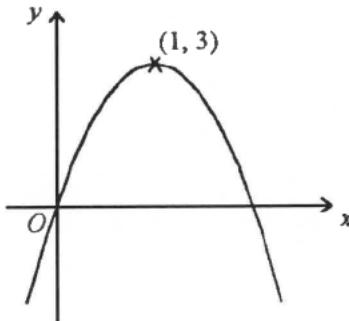


E.



[1995-CE-MATHS 2-41]

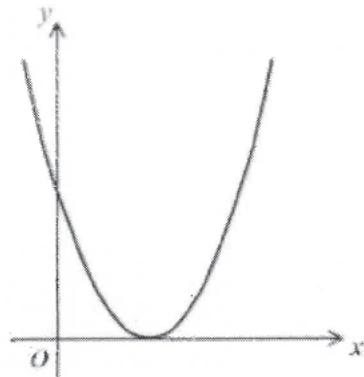
9. The figure shows the graph of a quadratic function  $f(x)$ . If the vertex of the graph is  $(1, 3)$ , then  $f(x) =$



- A.  $-3(x - 1)^2 + 3$ .  
 B.  $-3(x + 1)^2 + 3$ .  
 C.  $-(x - 1)^2 + 3$ .  
 D.  $-(x + 1)^2 + 3$ .  
 E.  $3(x - 1)^2 - 3$ .

[1997-CE-MATHS 2-34]

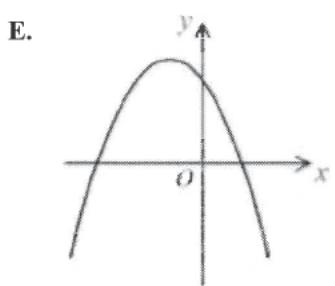
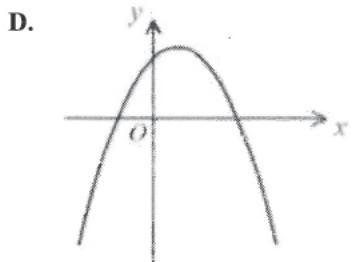
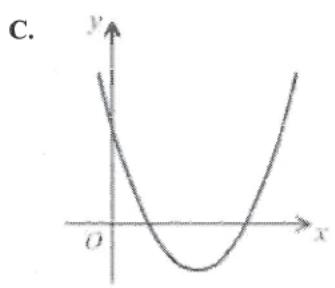
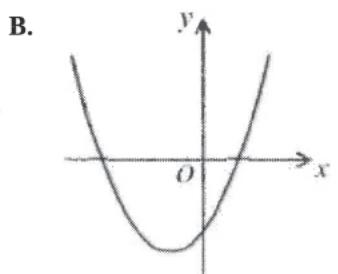
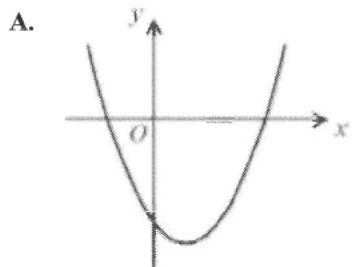
10. In the figure, the graph of  $y = x^2 - 6x + k$  touches the  $x$ -axis. Find  $k$ .



- A.  $k \geq 0$   
 B.  $k \geq 9$   
 C.  $k = -9$   
 D.  $k = 0$   
 E.  $k = 9$

[1999-CE-MATHS 2-5]

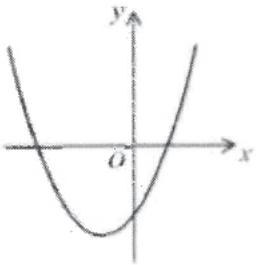
11. Which of the following may represent the graph of  $y = x^2 - 3x - 18$ ?



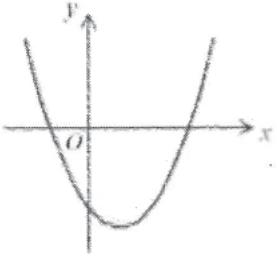
[1999-CE-MATHS 2-9]

12. Which of the following may represent the graph of  $y = -x^2 + 2x - 3$ ?

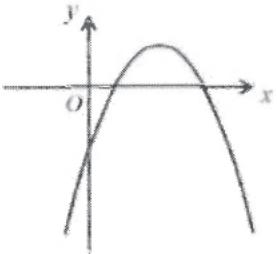
A.



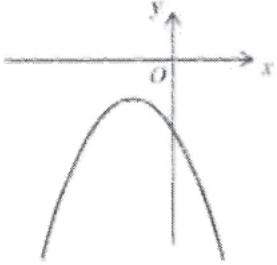
B.



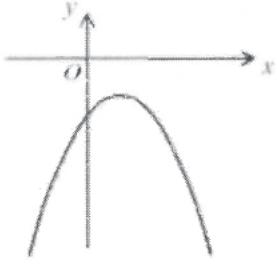
C.



D.

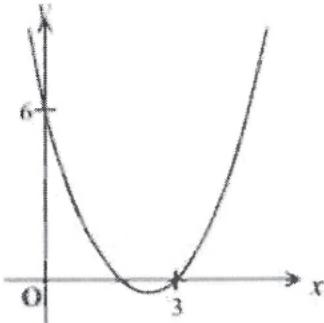


E.



[2000-CE-MATHS 2-39]

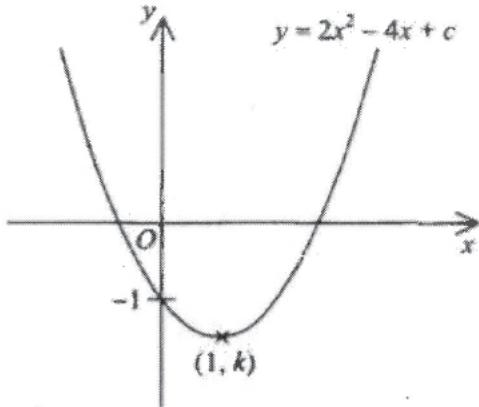
13. The figure shows the graph of  $y = x^2 + bx + c$ . Find  $b$ .



- A.  $\frac{-11}{2}$   
 B. -5  
 C. 5  
 D.  $\frac{11}{2}$

[2002-CE-MATHS 2-5]

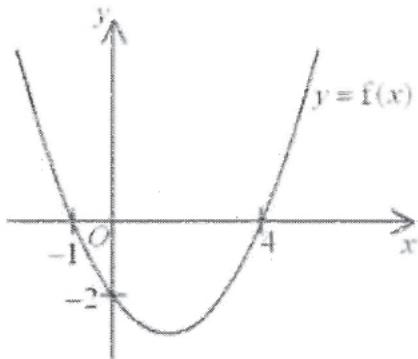
14. In the figure, the graph of  $y = 2x^2 - 4x + c$  passes through the point  $(1, k)$ . Find the value of  $k$ .



- A. -5  
 B. -4  
 C. -3  
 D. -2

[2004-CE-MATHS 2-5]

15. The figure shows the graph of  $y = f(x)$ . If  $f(x)$  is a quadratic function, then  $f(x) =$



- A.  $\frac{1}{2}(x+1)(x-4)$ .  
 B.  $2(x+1)(x-4)$ .  
 C.  $\frac{1}{2}(x-1)(x+4)$ .  
 D.  $2(x-1)(x+4)$ .

[2006-CE-MATHS 2-7]

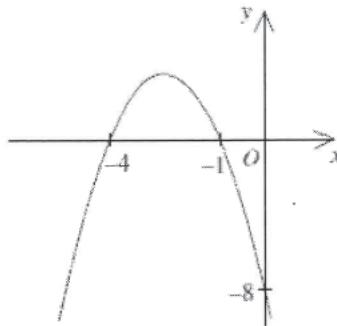
16. Which of the following statements about the graph of  $y = (x+1)^2 - 4$  is true?

- A. The coordinates of the vertex of the graph are  $(-1, 4)$ .

- B. The equation of the axis of symmetry of the graph is  $x = 1$ .  
 C. The  $x$ -intercepts of the graph are -1 and 3.  
 D. The  $y$ -intercept of the graph is -3.

[2007-CE-MATHS 2-5]

17. The equation of the quadratic graph shown in the figure is



- A.  $y = (x-1)(x-4)$ .  
 B.  $y = -(x+1)(x+4)$ .  
 C.  $y = -2(x+1)(x+4)$ .  
 D.  $y = -2(x-1)(x-4)$ .

[2010-CE-MATHS 2-9]

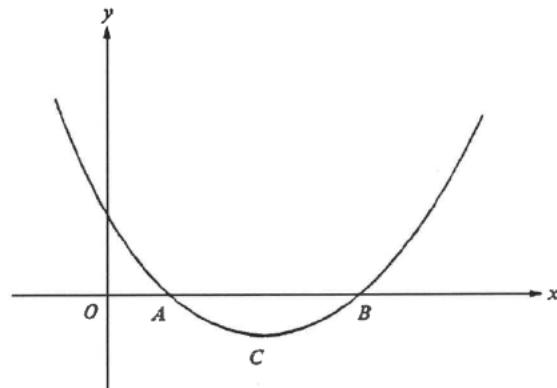
18. Which of the following statements about the graph of  $y = 25 - (x-3)^2$  is true?

- A. The  $x$ -intercepts of the graph are -2 and 8.  
 B. The  $y$ -intercept of the graph is 25.  
 C. The equation of the axis of symmetry of the graph is  $x = -3$ .  
 D. The  $y$ -coordinate of the vertex of the graph is 16.

[2011-CE-MATHS 2-7]

### Areas in Quadratic Graphs

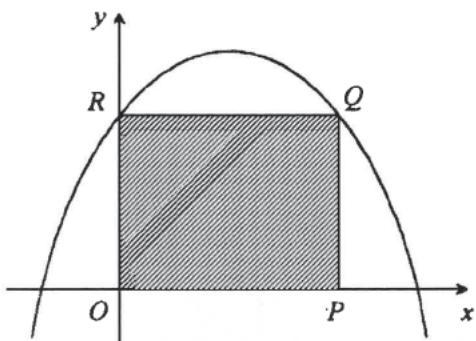
19. In the figure, the equation of the curve is  $y = (x-2)^2 - 1$ . The curve intersects the  $x$ -axis at  $A$  and  $B$ .  $C$  is the vertex of the curve. The area of  $\triangle ABC$  is



- A. 1.  
B. 1.5.  
C. 2.  
D. 2.5.  
E. 3.

[1985-CE-MATHS 2-35]

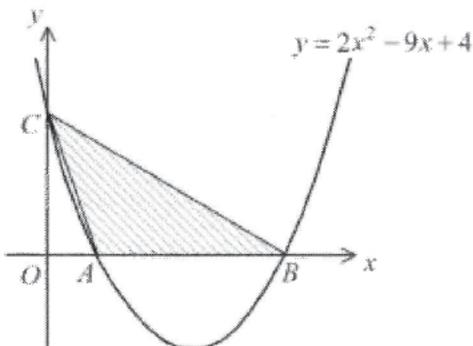
20. The curve in the figure is the graph of  $y = -x^2 + bx + c$ . Find the area of the rectangle  $OPQR$ .



- A.  $bc$   
B.  $b^2$   
C.  $c^2$   
D.  $b^2 - 4c$   
E.  $b^2 + 4c$

[1996-CE-MATHS 2-41]

21. In the figure, the graph of  $y = 2x^2 - 9x + 4$  cuts the  $x$ -axis at  $A$  and  $B$ , and the  $y$ -axis at  $C$ . Find the area of  $\triangle ABC$ .

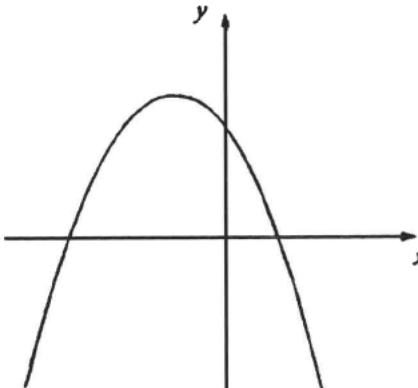


- A. 4  
B. 6  
C. 7  
D. 8  
E. 14

[2001-CE-MATHS 2-23]

### Sign of Coefficients in Quadratic Graphs

22.



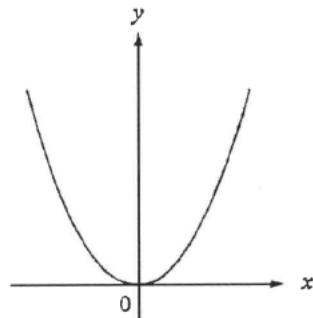
The figure above shows the graph of  $y = ax^2 + bx + c$ . Determine whether  $a$  and  $c$  are positive or negative.

- A.  $a > 0$  and  $c > 0$   
B.  $a < 0$  and  $c < 0$   
C.  $a > 0$  and  $c < 0$   
D.  $a < 0$  and  $c > 0$   
E. it cannot be determined from the given data

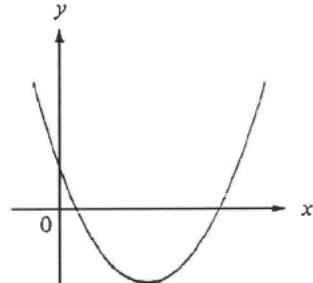
[1980-CE-MATHS 2-32]

23. If  $a$ ,  $b$  and  $c$  are positive numbers, which of the following is a possible graphical representation of  $y = ax^2 + bx + c$ ?

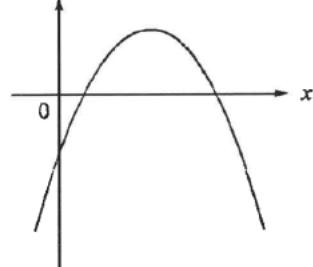
A.



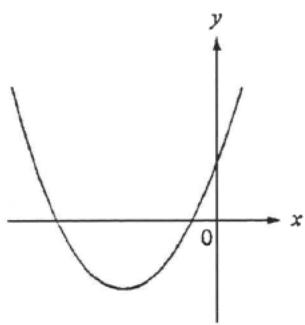
B.



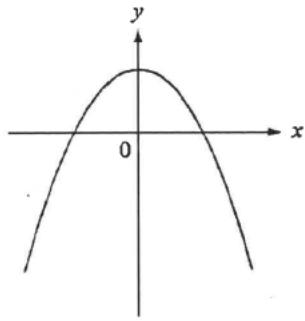
C.



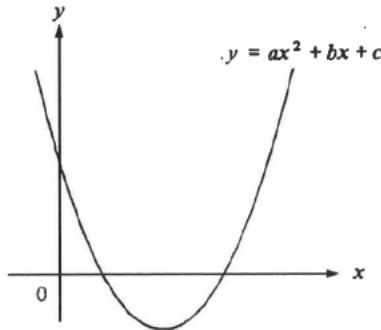
D.



E.



24.

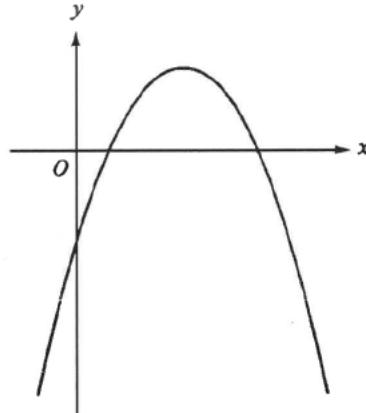


The figure shows the graph of  $y = ax^2 + bx + c$ . Which of the following is/are true?

- (1)  $a > 0$
- (2)  $b > 0$
- (3)  $c > 0$
- A. (1) only
- B. (1) and (2) only
- C. (1) and (3) only
- D. (2) and (3) only
- E. (1), (2) and (3)

[1987-CE-MATHS 2-39]

25.

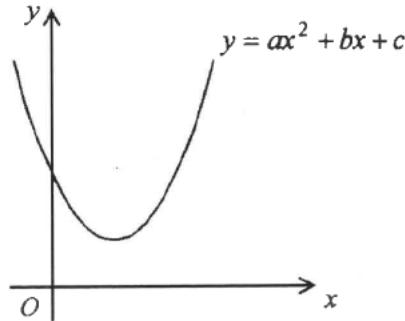


The graph of  $y = ax^2 + bx + c$  is given as shown. Which of the following is/are true?

- (1)  $a < 0$
- (2)  $b < 0$
- (3)  $c < 0$
- A. (1) only
- B. (1) and (2) only
- C. (1) and (3) only
- D. (2) and (3) only
- E. (1), (2) and (3)

[1990-CE-MATHS 2-31]

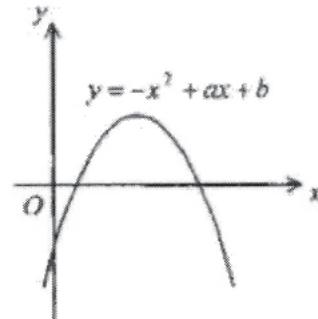
26. The figure shows the graph of  $y = ax^2 + bx + c$ . Which of the following is true?



- A.  $a > 0$ ,  $c > 0$  and  $b^2 - 4ac > 0$
- B.  $a > 0$ ,  $c > 0$  and  $b^2 - 4ac < 0$
- C.  $a > 0$ ,  $c < 0$  and  $b^2 - 4ac < 0$
- D.  $a < 0$ ,  $c > 0$  and  $b^2 - 4ac > 0$
- E.  $a < 0$ ,  $c < 0$  and  $b^2 - 4ac > 0$

[1998-CE-MATHS 2-12]

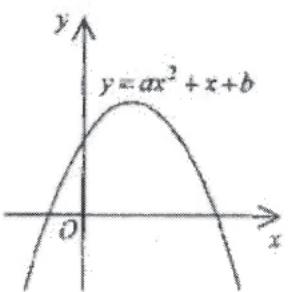
27. The figure shows the graph of  $y = -x^2 + ax + b$ . Which of the following is true?



- A.  $a < 0$  and  $b < 0$
- B.  $a < 0$  and  $b > 0$
- C.  $a > 0$  and  $b < 0$
- D.  $a > 0$  and  $b > 0$

[2003-CE-MATHS 2-42]

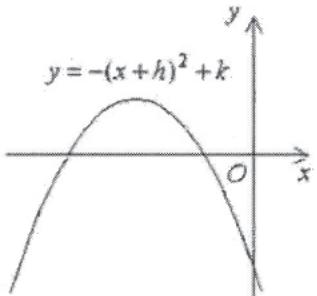
28. The figure shows the graph of  $y = ax^2 + x + b$ . Which of the following is true?



- A.  $a > 0$  and  $b < 0$
- B.  $a > 0$  and  $b > 0$
- C.  $a < 0$  and  $b < 0$
- D.  $a < 0$  and  $b > 0$

[2005-CE-MATHS 2-6]

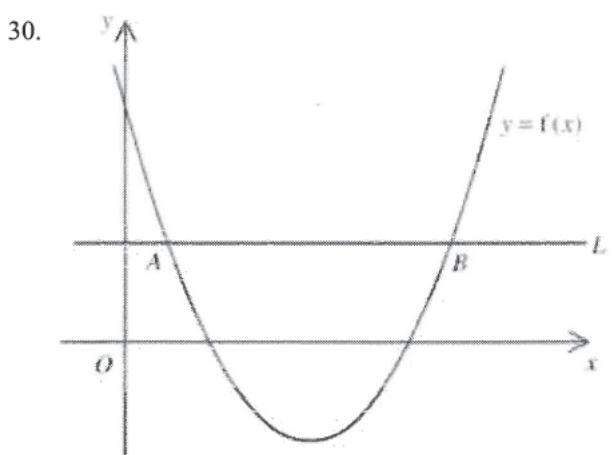
29. The figure shows the graph of  $y = -(x + h)^2 + k$ . Which of the following must be true?



- A.  $h > 0$  and  $k > 0$
- B.  $h > 0$  and  $k < 0$
- C.  $h < 0$  and  $k > 0$
- D.  $h < 0$  and  $k < 0$

[2008-CE-MATHS 2-9]

### HKDSE Problems

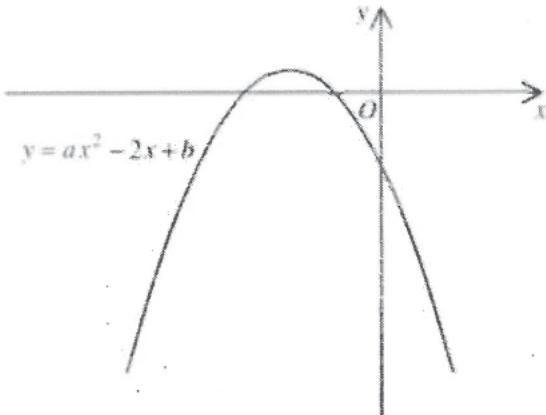


In the figure, the quadratic graph of  $y = f(x)$  intersects the straight line  $L$  at  $A(1, k)$  and  $B(7, k)$ . Which of the following are true?

- (1) The solution of the inequality  $f(x) > k$  is  $x < 1$  or  $x > 7$ .
  - (2) The roots of the equation  $f(x) = k$  are 1 and 7.
  - (3) The equation of the axis of symmetry of the quadratic graph of  $y = f(x)$  is  $x = 3$ .
- A. (1) and (2) only
  - B. (1) and (3) only
  - C. (2) and (3) only
  - D. (1), (2) and (3)

[SP-DSE-MATHS 2-8]

31.

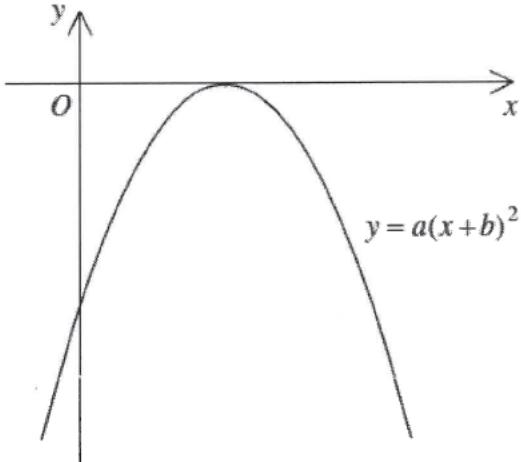


The figure shows the graph of  $y = ax^2 - 2x + b$ , where  $a$  and  $b$  are constants. Which of the following is/are true?

- (1)  $a > 0$
  - (2)  $b < 0$
  - (3)  $ab < 1$
- A. (1) only
  - B. (2) only
  - C. (1) and (3) only
  - D. (2) and (3) only

[PP-DSE-MATHS 2-8]

32. The figure shows the graph of  $y = a(x + b)^2$ , where  $a$  and  $b$  are constants. Which of the following is true?



- A.  $a > 0$  and  $b > 0$   
 B.  $a > 0$  and  $b < 0$   
 C.  $a < 0$  and  $b > 0$   
 D.  $a < 0$  and  $b < 0$

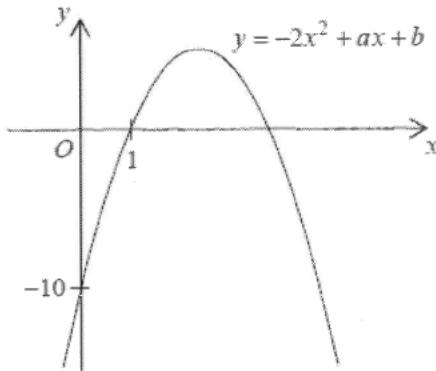
[2012-DSE-MATHS 2-6]

33. Let  $f(x)$  be a quadratic function. If the coordinates of the vertex of the graph of  $y = f(x)$  are  $(3, -4)$ , which of the following must be true?

- A. The roots of the equation  $f(x) = 0$  are integers.  
 B. The roots of the equation  $f(x) - 3 = 0$  are rational numbers.  
 C. The roots of the equation  $f(x) + 4 = 0$  are real numbers.  
 D. The roots of the equation  $f(x) + 5 = 0$  are nonreal numbers.

[2012-DSE-MATHS 2-34]

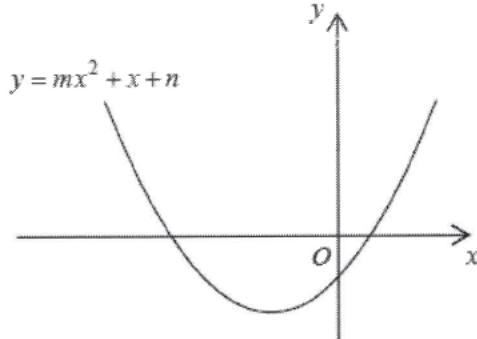
34. The figure shows the graph of  $y = -2x^2 + ax + b$ , where  $a$  and  $b$  are constants. The equation of the axis of symmetry of the graph is



- A.  $x = 2$ .  
 B.  $x = 3$ .  
 C.  $x = 5$ .  
 D.  $y = 8$ .

[2013-DSE-MATHS 2-7]

35. The figure shows the graph of  $y = mx^2 + x + n$ , where  $m$  and  $n$  are constants. Which of the following is true?



- A.  $m < 0$  and  $n < 0$   
 B.  $m < 0$  and  $n > 0$   
 C.  $m > 0$  and  $n < 0$   
 D.  $m > 0$  and  $n > 0$

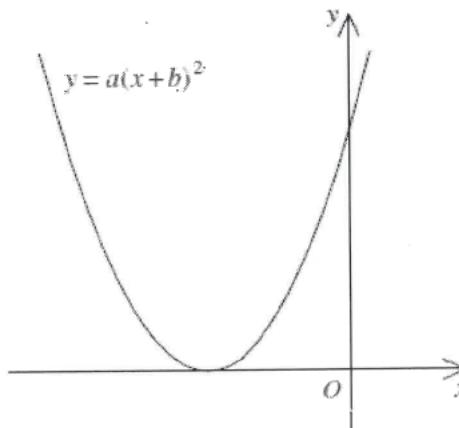
[2014-DSE-MATHS 2-5]

36. Let  $f(x) = 3x^2 - 6x + k$ , where  $k$  is a constant. If the  $y$ -coordinate of the vertex of the graph of  $y = f(x)$  is 7, then  $k =$

- A. 1.  
 B. 3.  
 C. 4.  
 D. 10.

[2014-DSE-MATHS 2-35]

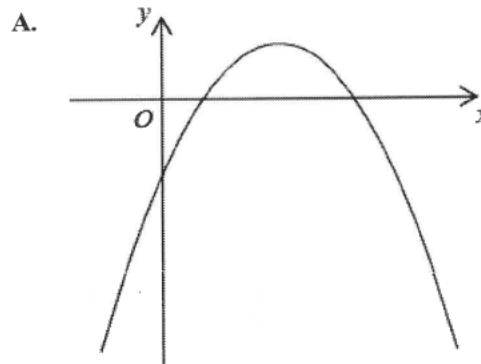
37. The figure shows the graph of  $y = a(x + b)^2$ , where  $a$  and  $b$  are constants. Which of the following is true?



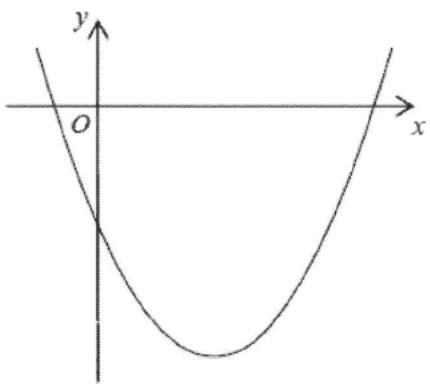
- A.  $a < 0$  and  $b < 0$   
 B.  $a < 0$  and  $b > 0$   
 C.  $a > 0$  and  $b < 0$   
 D.  $a > 0$  and  $b > 0$

[2015-DSE-MATHS 2-8]

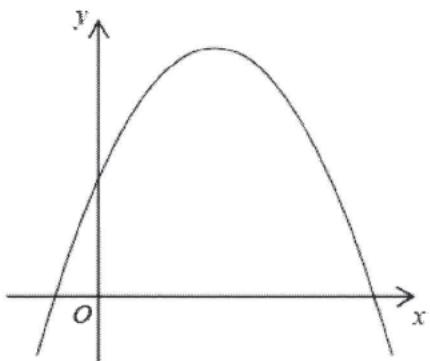
38. If  $-1 < a < 0$ , which of the following may represent the graph of  $y = (ax + 1)^2 + a$ ?



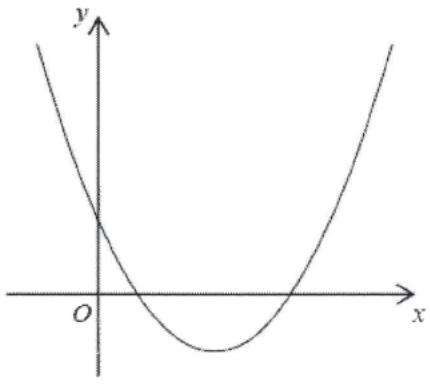
B.



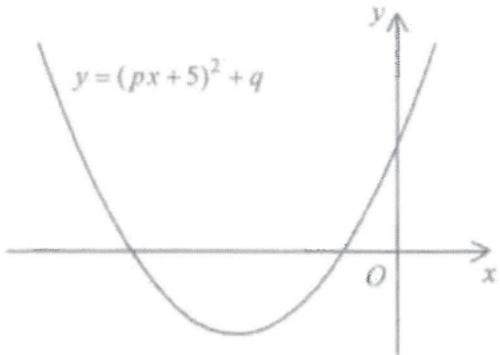
C.



D.



39. The figure shows the graph of  $y = (px + 5)^2 + q$ , where  $p$  and  $q$  are constants. Which of the following is true?



- A.  $p < 0$  and  $q < 0$
- B.  $p < 0$  and  $q > 0$
- C.  $p > 0$  and  $q < 0$
- D.  $p > 0$  and  $q > 0$

[2017-DSE-MATHS 2-9]

40. Which of the following statements about the graph of  $y = 16 - (x - 6)^2$  is true?

- A. The graph cuts the  $x$ -axis.
- B. The graph opens upwards.
- C. The  $y$ -intercept of the graph is 16.
- D. The graph passes through the origin.

[2018-DSE-MATHS 2-5]

41. Which of the following statements about the graph of  $y = (3 - x)(x + 2) + 6$  is / are true?

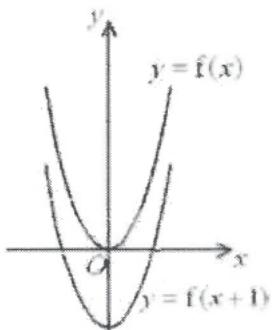
- I. The graph opens downwards.
  - II. The graph passes through the point  $(1, 10)$ .
  - III. The  $x$ -intercepts of the graph are  $-2$  and  $3$ .
- A. I only
  - B. II only
  - C. I and III only
  - D. II and III only

[2019-DSE-MATHS 2-10]

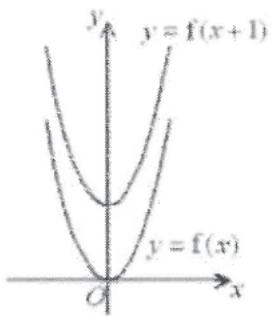
## Transformations of Graphs

1. Which of the following may represent the graph of  $y = f(x)$  and the graph of  $y = f(x+1)$  on the same rectangular coordinate system?

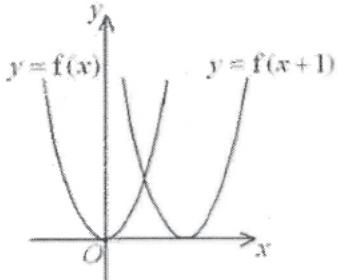
A.



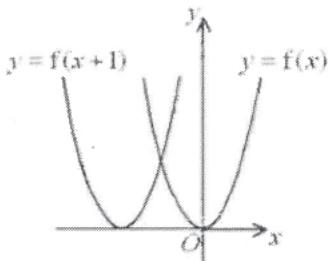
B.



C.



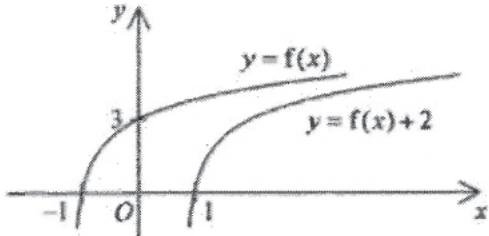
D.



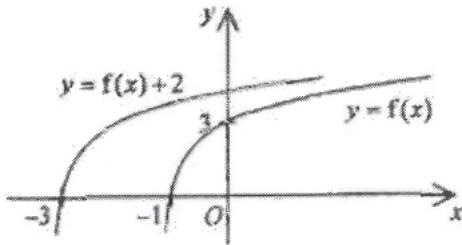
[2007-CE-MATHS 2-38]

2. Which of the following may represent the graph of  $y = f(x)$  and the graph of  $y = f(x) + 2$  on the same rectangular coordinate system?

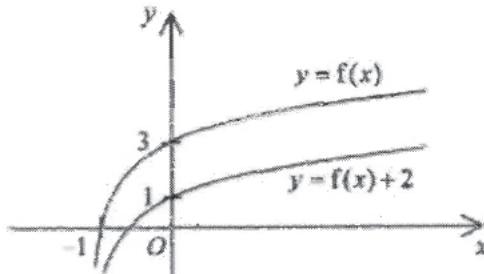
A.



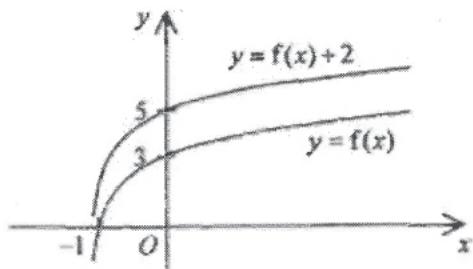
B.



C.

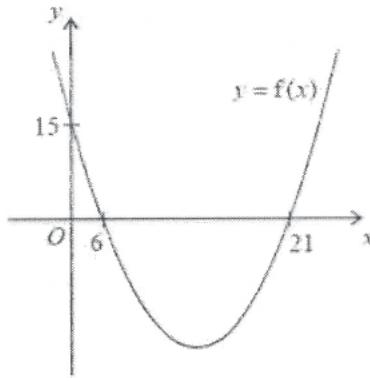


D.



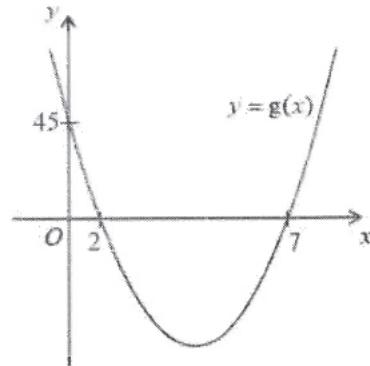
[2008-CE-MATHS 2-37]

3.

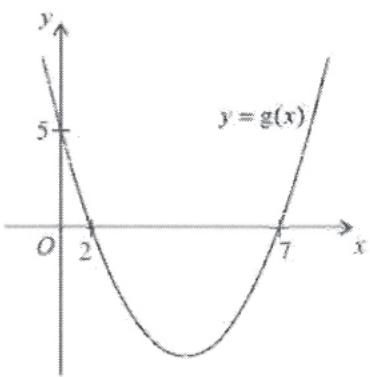


The figure above shows the graph of  $y = f(x)$ . If  $f(x) = 3g(x)$ , which of the following may represent the graph of  $y = g(x)$ ?

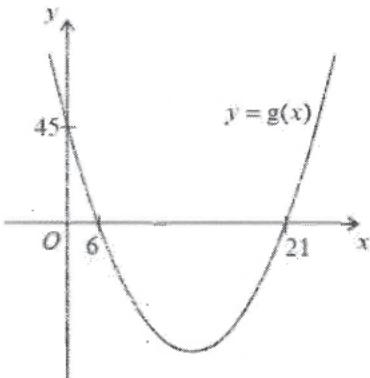
A.



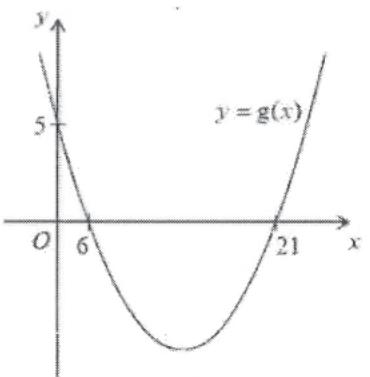
B.



C.

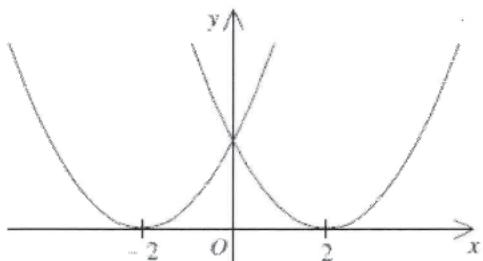


D.



[2009-CE-MATHS 2-37]

4.



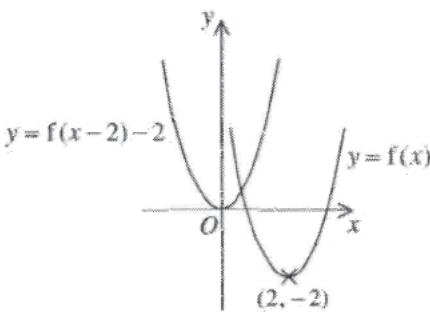
Let  $f(x)$  be a quadratic function. The figure shows the graph of  $y = f(x)$  and

- A. the graph of  $y = f(x - 2)$ .
- B. the graph of  $y = f(x + 2)$ .
- C. the graph of  $y = f(-x)$ .
- D. the graph of  $y = -f(x)$ .

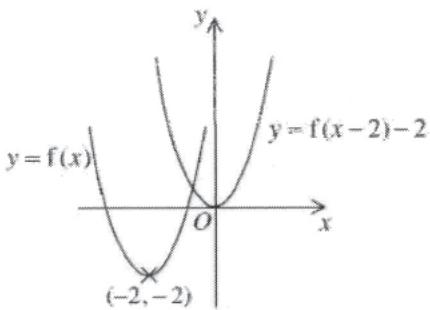
[2010-CE-MATHS 2-37]

5. Which of the following may represent the graph of  $y = f(x)$  and the graph of  $y = f(x - 2) - 2$  on the same rectangular coordinate system?

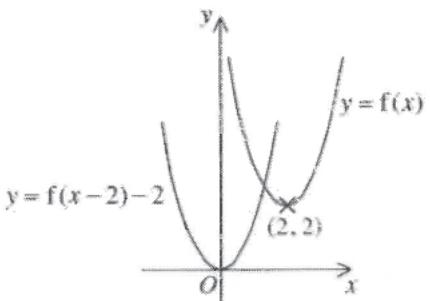
A.



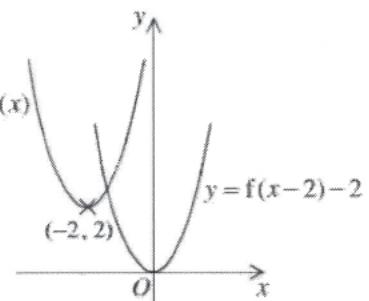
B.



C.



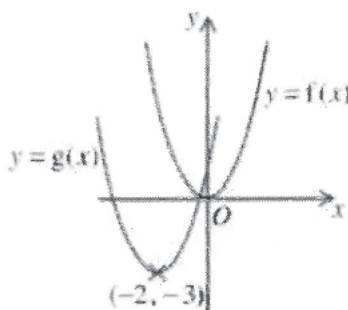
D.



[2011-CE-MATHS 2-37]

### HKDSE Problems

6.

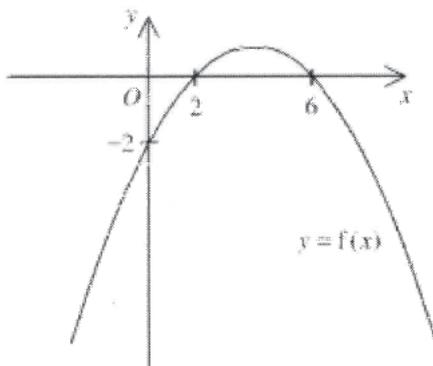


If the figure shows the graph of  $y = f(x)$  and the graph of  $y = g(x)$  on the same rectangular coordinate system, then

- A.  $g(x) = f(x - 2) - 3$ .
- B.  $g(x) = f(x - 2) + 3$ .
- C.  $g(x) = f(x + 2) - 3$ .
- D.  $g(x) = f(x + 2) + 3$ .

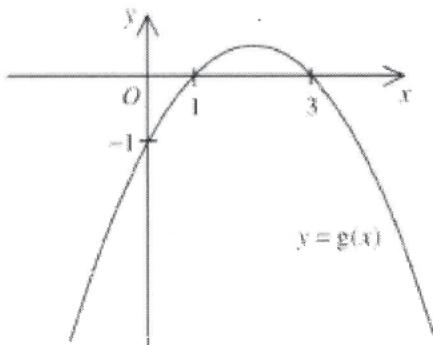
[SP-DSE-MATHS 2-37]

7.

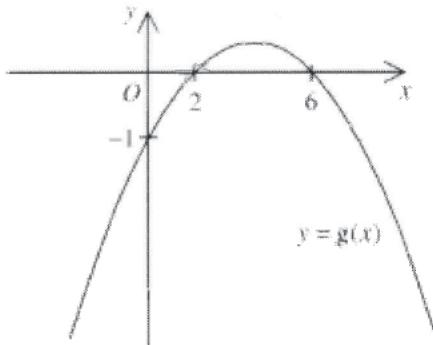


The figure above shows the graph of  $y = f(x)$ . If  $2f(x) = g(x)$ , which of the following may represent the graph of  $y = g(x)$ ?

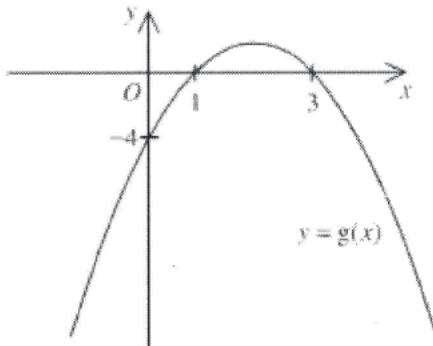
A.



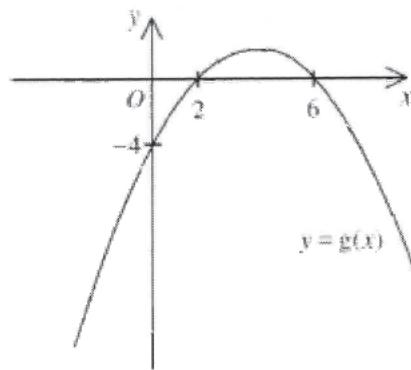
B.



C.



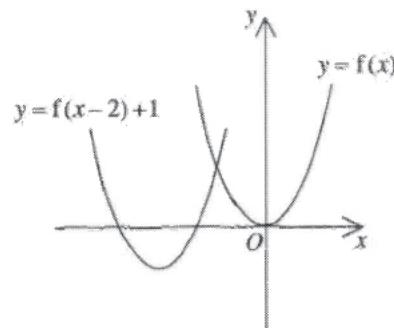
D.



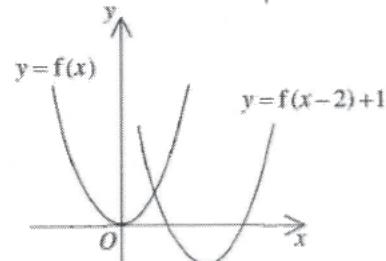
[PP-DSE-MATHS 2-31]

8. Which of the following may represent the graph of  $y = f(x)$  and the graph of  $y = f(x - 2) + 1$  on the same rectangular coordinate system?

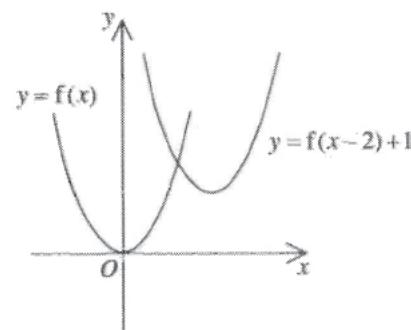
A.



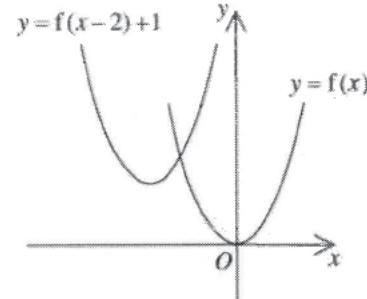
B.



C.

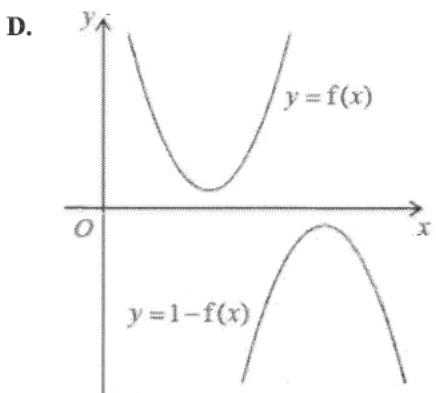
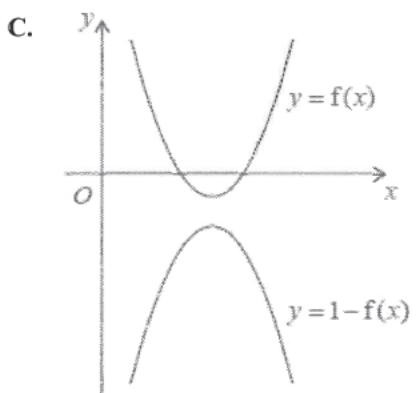
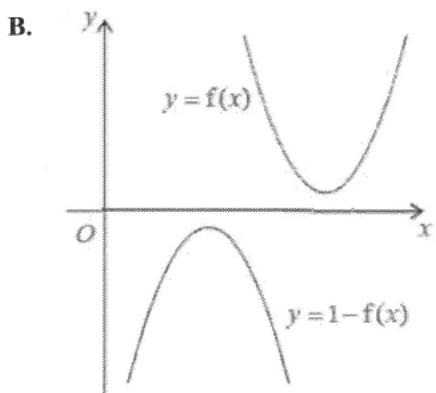
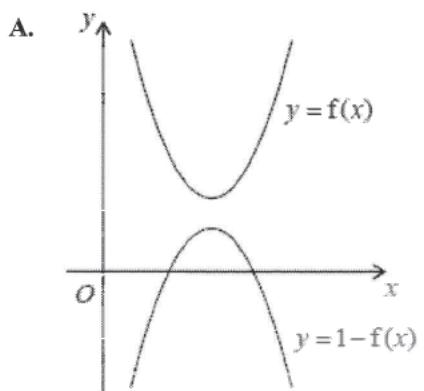


D.

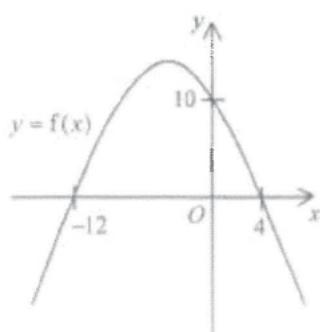


[2012-DSE-MATHS 2-38]

9. Which of the following may represent the graph of  $y = f(x)$  and the graph of  $y = 1 - f(x)$  on the same rectangular coordinate system?

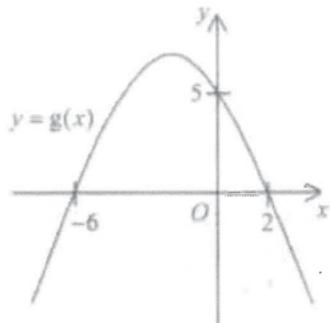


10.

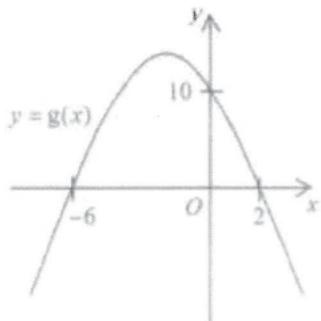


The figure above shows the graph of  $y = f(x)$ . If  $g(x) = f\left(\frac{x}{2}\right)$ , which of the following may represent the graph of  $y = g(x)$ ?

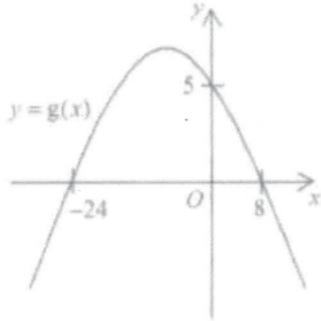
A.



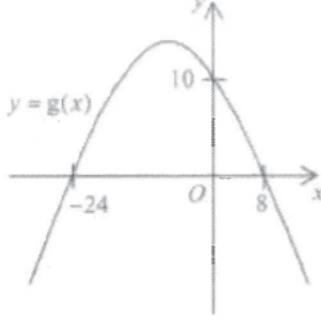
B.



C.



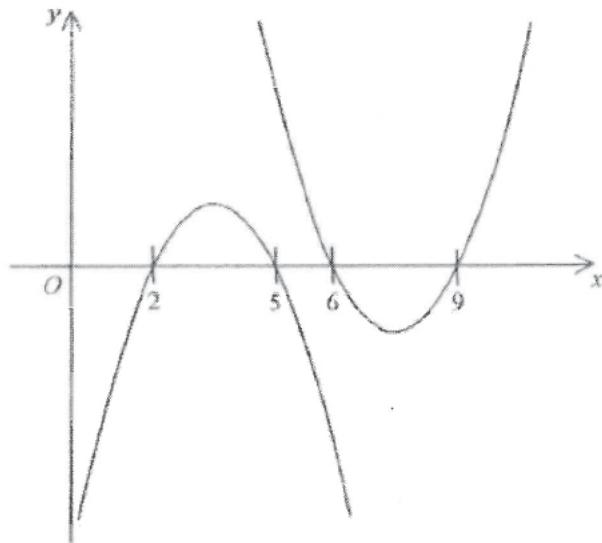
D.



[2014-DSE-MATHS 2-38]

[2017-DSE-MATHS 2-31]

11. Let  $f(x)$  be a quadratic function. The figure below may represent the graph of  $y = f(x)$  and

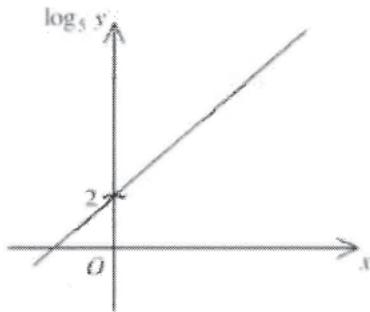


- A. the graph of  $y = -3f(x)$
- B. the graph of  $y = f(-3x)$
- C. the graph of  $y = -f(x + 4)$
- D. the graph of  $y = f(-x + 11)$

[2018-DSE-MATHS 2-31]

## HKDSE Problems

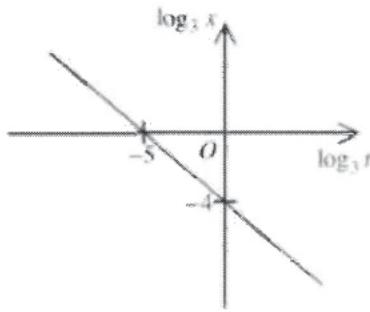
1. The graph in the figure shows the linear relation between  $x$  and  $\log_5 y$ . If  $y = ab^x$ , then  $a =$



- A. 1.  
B. 2.  
C. 5.  
D. 25.

[SP-DSE-MATHS 2-32]

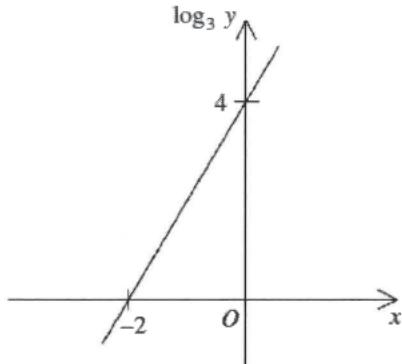
2. The graph in the figure shows the linear relation between  $\log_3 t$  and  $\log_3 x$ . If  $x = kt^a$ , then  $k =$



- A.  $\frac{1}{81}$ .  
B. 81.  
C.  $\frac{4}{5}$ .  
D.  $\frac{-5}{4}$ .

[PP-DSE-MATHS 2-37]

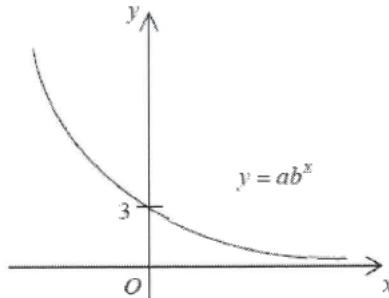
3. The graph in the figure shows the linear relation between  $x$  and  $\log_3 y$ . If  $y = mn^x$ , then  $n =$



- A.  $\frac{1}{81}$ .  
B.  $\frac{1}{9}$ .  
C. 9.  
D. 81.

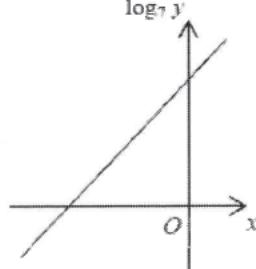
[2012-DSE-MATHS 2-32]

4.

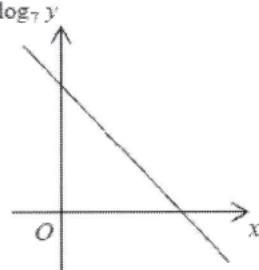


The figure above shows the graph of  $y = ab^x$ , where  $a$  and  $b$  are constants. Which of the following graphs may represent the relation between  $x$  and  $\log_7 y$ ?

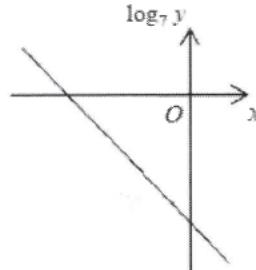
A.



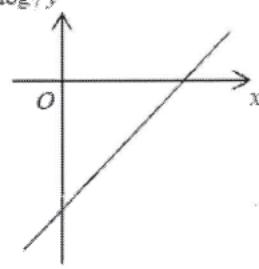
B.



C.

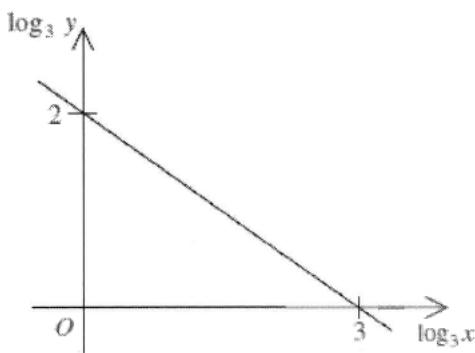


D.



[2013-DSE-MATHS 2-32]

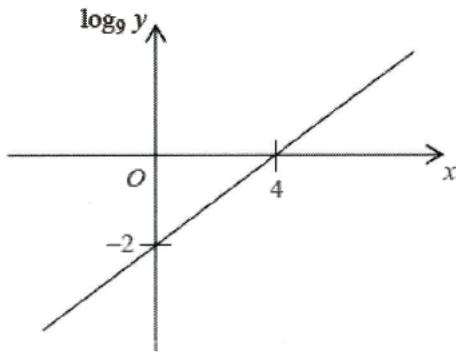
5. The graph in the figure shows the linear relation between  $\log_3 x$  and  $\log_3 y$ . Which of the following must be true?



- A.  $x^2y^3 = 729$   
 B.  $x^3y^2 = 729$   
 C.  $x^2 + y^3 = 729$   
 D.  $x^3 + y^2 = 729$

[2015-DSE-MATHS 2-32]

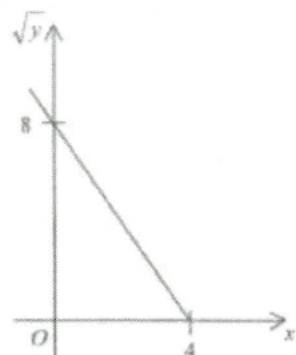
6. The graph in the figure shows the linear relation between  $x$  and  $\log_9 y$ . If  $y = ab^x$ , then  $b =$



- A. -2  
 B.  $\frac{1}{81}$   
 C.  $\frac{1}{2}$   
 D. 3

[2016-DSE-MATHS 2-32]

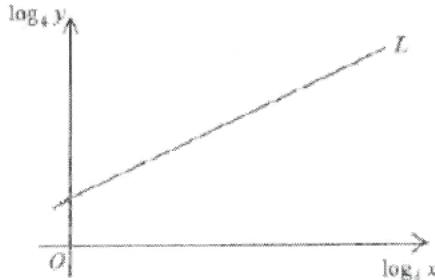
7. The graph in the figure shows the linear relation between  $x$  and  $\sqrt{y}$ . Which of the following must be true?



- A.  $y = x^2 - 4x + 8$   
 B.  $y = x^2 + 4x + 8$   
 C.  $y = 4x^2 - 32x + 64$   
 D.  $y = 4x^2 + 32x + 64$

[2017-DSE-MATHS 2-33]

8. In the figure, the straight line L shows the relation between  $\log_4 x$  and  $\log_4 y$ . It is given that L passes through the points (1, 2) and (9, 6). If  $y = kx^a$ , then  $k =$



- A.  $\frac{1}{2}$   
 B.  $\frac{3}{2}$   
 C. 2  
 D. 8

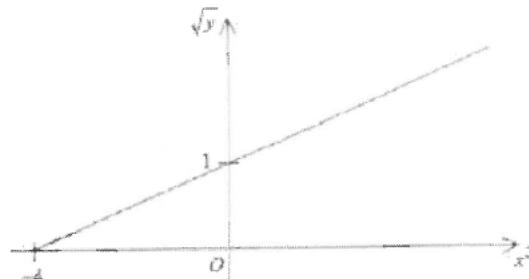
[2018-DSE-MATHS 2-33]

9. It is given that  $\log_9 y$  is a linear function of  $\log_3 x$ . The intercepts on the vertical axis and on the horizontal axis of the graph of the linear function are 7 and 8 respectively. Which of the following must be true?

- A.  $x^4y^7 = 3^{56}$   
 B.  $x^7y^4 = 3^{56}$   
 C.  $x^7y^8 = 3^{56}$   
 D.  $x^8y^7 = 3^{56}$

[2019-DSE-MATHS 2-31]

10. The graph in the figure shows the linear relation between  $x^3$  and  $\sqrt{y}$ . If  $x = 2$ ,  $y =$



- A. 3  
 B. 8  
 C. 9  
 D. 33

[2020-DSE-MATHS 2-34]