

Assignment 2

1. a) $T_1 = (A'T_2)'$ $T_2 = (A'D)'$ $T_3 = A' + BC$

$F = T_1 T_3$ $G = (T_2 T_3)'$

b) $F = (A'T_2)'(A' + BC)$

$= (A + T_2)(A' + BC)$

$= (A + A'D)(A' + BC)$

$= AA' + ABC + A'D + A'DBC$

$= 0 + ABC + A'D + A'D(1 + BC)$

$= ABC + A'D + A'D + A'DBC$

$= ABC + A'D$

$G = T_2' + T_3'$

$= A'D + (A' + BC)'$

$= A'D + A(B' + C')$

$= AB' + AC' + A'D$

| (c) | A | B | C | D | F | G |
|-----|---|---|---|---|---|---|
| | 0 | 0 | 0 | 0 | 0 | 0 |
| | 0 | 0 | 0 | 1 | 1 | 1 |
| | 0 | 0 | 1 | 0 | 0 | 0 |
| | 0 | 0 | 1 | 1 | 1 | 1 |
| | 0 | 1 | 0 | 0 | 0 | 0 |
| | 0 | 1 | 0 | 1 | 1 | 1 |
| | 0 | 1 | 1 | 0 | 0 | 0 |
| | 0 | 1 | 1 | 1 | 1 | 1 |
| | 1 | 0 | 0 | 0 | 0 | 1 |
| | 1 | 0 | 0 | 1 | 0 | 1 |
| | 1 | 0 | 1 | 0 | 0 | 1 |
| | 1 | 0 | 1 | 1 | 0 | 1 |

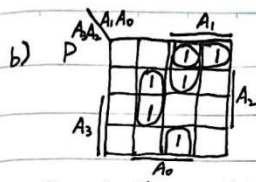
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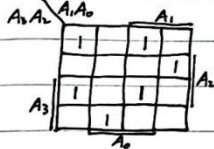
| A | B | C | D | F | G |
|---|---|---|---|---|---|
| 1 | 1 | 0 | 0 | 0 | 1 |
| 1 | 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 1 | 0 | 1 | 0 |
| 1 | 1 | 1 | 1 | 1 | 0 |

2. a)

| A_3 | A_2 | A_1 | A_0 | P | D |
|-------|-------|-------|-------|---|---|
| 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 | 1 | 0 |
| 0 | 0 | 1 | 1 | 1 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 |
| 1 | 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 0 | 1 |



$$P = A_2 A_1' A_0 + A_2' A_1 A_0 + A_2' A_1 A_0 + A_2' A_2' A_1$$

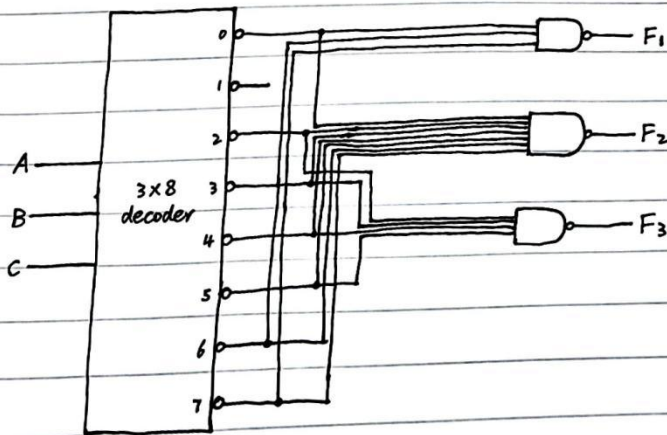


$$D = A_2' A_2' A_1' A_0' + A_2' A_2' A_1 A_0 + A_2' A_2 A_1 A_0' + A_2' A_2 A_1 A_0' + A_2 A_2 A_1 A_0 + A_2 A_2 A_1' A_0$$

3. $F_1 = AB + A'B'C' = \Sigma(0, 6, 7) = (m_0' \cdot m_6' \cdot m_7')'$

$$F_2 = A + B + C' = \Sigma(0, 2, 3, 4, 5, 6, 7) = (m_0' m_2' m_3' m_4' m_5' m_6' m_7')'$$

$$F_3 = A'B + AB' = \Sigma(2, 3, 4, 5) = (m_2' m_3' m_4' m_5')'$$



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4. $D_0 = x'y'z' = (x+y+z)'$

$D_1 = x'y'z = (x+y+z')$

$D_2 = x'yz' = (x+y'+z)'$

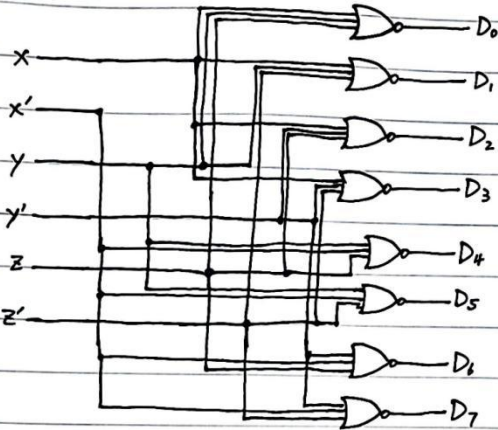
$D_3 = x'yz = (x+y'+z')$

$D_4 = xy'z' = (x'+y+z)'$

$D_5 = x'yz' = (x'+y+z')$

$D_6 = xyz' = (x'+y'+z)'$

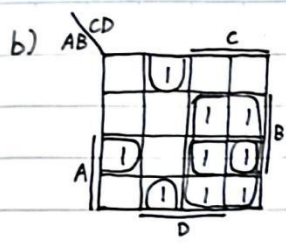
$D_7 = xyz = (x'+y'+z')$



5. a)

| A | B | C | D | F |
|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 1 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 0 | 1 | 0 |
| 1 | 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |

Annotations in the original image: $F=D$ (rows 1, 2, 9, 10), $F=0$ (rows 3, 4), $F=1$ (rows 7, 8, 13, 14, 15, 16), $F=D'$ (row 12).

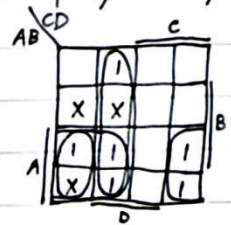


$$F(A,B,C,D) = AC + BC + B'C'D + ABD'$$

6. a)

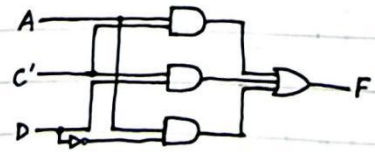
| A | B | C | D | F |
|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 0 | X |
| 0 | 1 | 0 | 1 | X |
| 0 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | X |
| 1 | 0 | 0 | 1 | 1 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 |

b) Simplify F by using K-map.



$$F(A,B,C,D) = AC' + C'D + AD'$$

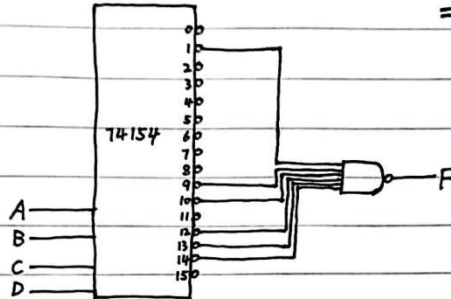
Logic diagram:



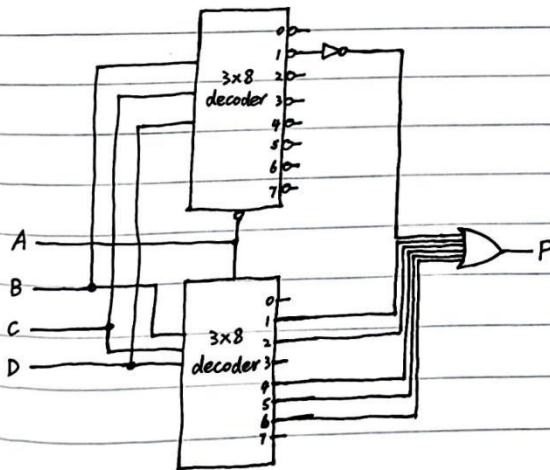
c) In order to use less standard components and gates,

we set $m_4 = m_5 = m_8 = 0$, then $F = \Sigma(1, 9, 10, 12, 13, 14)$

$$= (m_1' m_9' m_{10}' m_{12}' m_{13}' m_{14}')'$$



d) Take $m_4 = m_5 = m_8 = 0$, also take A to be enable.

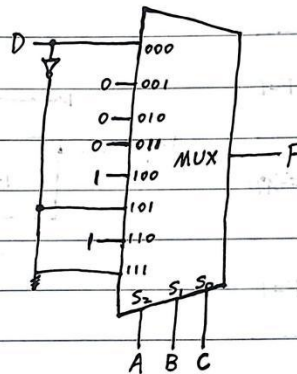


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e) From truth table, we can find the relation between F and D.

| A | B | C | D | F |
|---|---|---|---|----------|
| 0 | 0 | 0 | 0 | 0 $F=D$ |
| 0 | 0 | 1 | 0 | 0 $F=0$ |
| 0 | 1 | 0 | 0 | X $F=0$ |
| 0 | 1 | 1 | 0 | 0 $F=0$ |
| 1 | 0 | 0 | 0 | X $F=1$ |
| 1 | 0 | 1 | 0 | 1 $F=D'$ |
| 1 | 1 | 0 | 0 | 1 $F=1$ |
| 1 | 1 | 1 | 0 | 1 $F=D'$ |



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(f) From the truth table, we found the relationship.

| B | C | A | D | F |
|---|---|---|---|-----------|
| 0 | 0 | 0 | 0 | 0 $F=D$ |
| 0 | 0 | 1 | 0 | X $F=D$ |
| 0 | 1 | 0 | 0 | 0 $F=AD'$ |
| 0 | 1 | 1 | 0 | 1 $F=AD'$ |
| 1 | 0 | 0 | 0 | X $F=1$ |
| 1 | 0 | 1 | 0 | 1 $F=1$ |
| 1 | 1 | 0 | 0 | 0 $F=AD'$ |
| 1 | 1 | 1 | 0 | 1 $F=AD'$ |

