

GW190521 may be an intermediate mass ratio inspiral

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ABSTRACT

GW190521 is the first confident observation of a binary black hole merger with total mass $M > 100 M_{\odot}$. Given the lack of observational constraints at these masses, we analyze GW190521 considering two different priors for the binary's masses: uniform in mass ratio and source-frame total mass, and uniform in source-frame component masses. For the uniform in mass-ratio prior, we find that the component masses are $m_1^{\text{src}} = 168^{+15}_{-61} M_{\odot}$ and $m_2^{\text{src}} = 16^{+33}_{-3} M_{\odot}$. The uniform in component-mass prior yields a bimodal posterior distribution. There is a low-mass-ratio mode ($q < 4$) with $m_1^{\text{src}} = 100^{+17}_{-18} M_{\odot}$ and $m_2^{\text{src}} = 57^{+17}_{-16} M_{\odot}$ and a high-mass-ratio mode ($q \geq 4$) with $m_1^{\text{src}} = 166^{+16}_{-35} M_{\odot}$ and $m_2^{\text{src}} = 16^{+14}_{-3} M_{\odot}$. Although the two modes have nearly equal posterior probability, the maximum-likelihood parameters are in the high-mass ratio mode, with $m_1^{\text{src}} = 171 M_{\odot}$ and $m_2^{\text{src}} = 16 M_{\odot}$, and a signal-to-noise ratio of 16. These results are consistent with the proposed "mass gap" produced by pair-instability in supernova. Our results are inconsistent with those published in Abbott et al. (2020b). We find that a combination of the prior used and the constraints applied may have prevented that analysis from sampling the high-mass-ratio mode. An accretion flare in AGN J124942.3+344929 was observed in possible coincidence with GW190521 by the Zwicky Transient Facility (ZTF). We report parameters assuming a common origin; however, the spatial agreement of GW190521 and the EM flare alone does not provide convincing evidence for the association ($\ln \mathcal{B} \gtrsim -4$).

Keywords: gravitational waves — black holes — compact binary stars

1. INTRODUCTION

Gravitational-wave astronomy began with the observation of GW150914 (Abbott et al. 2016) by the twin LIGO-Hanford and Livingston observatories (Aasi et al. 2015) with the merger of two $\sim 30 M_{\odot}$ black holes, significantly heavier than previously known black holes in X-ray binaries (Corral-Santana et al. 2016). These heavy binary black holes (BBHs) opened a new window into stellar evolution (Taylor & Gerosa 2018; Dvorkin et al. 2018; Piran & Hotekezaka 2020) and even sparked renewed interest in primordial black holes as a component of dark matter (Green & Kavanagh 2020; Nitz & Wang 2020; Abbott et al. 2019a). Since then, the Virgo observatory (Acernese et al. 2015) has joined the growing worldwide observatory network and over a dozen binary black hole mergers have been observed (Nitz et al. 2019a,b, 2020; Venumadhav et al. 2019a,b; Zackay et al.

2019; Abbott et al. 2019b), with many additional candidates awaiting publication (LVC 2019).

With the exception of the marginal BBH candidates GW151205 and 170817+03:02:46UTC (Nitz et al. 2019b; Zackay et al. 2019), all prior confident detections were consistent with sources in which both component black holes have mass less than $50 M_{\odot}$ (Abbott et al. 2019c). This observed limit may hint at the existence of an upper mass gap (Abbott et al. 2019c; Roulet et al. 2020). Formation models which include the effects of pulsational pair instability supernovae (PPISNe) or pair-instability supernovae (PISNe) in stellar evolution preclude the direct formation of a black hole with remnant mass $\sim 50\text{--}120 M_{\odot}$ (Yoshida et al. 2016; Woosley 2017; Belczynski et al. 2016; Marchant et al. 2019; Woosley 2019; Stevenson et al. 2019; van Son et al. 2020).

On May 21st, 2019 at 03:02:29 UTC, GW190521 was detected by the PyCBC Live low-latency analysis (Nitz et al. 2018a; Dal Canton et al. 2020), producing a 765 deg² Bayestar sky localization (Singer & Price 2016). Continued monitoring of the low-latency localiza-

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tion region was conducted by ZTF (Bellm et al. 2019), which detected a flare weeks later that was consistent with AGN J124942.3+344929 (ZTF19abahrhr) (Graham et al. 2020) at $z = 0.438$ from the Million Quasar Catalog (Flesch 2019). If there is a common origin for the gravitational-wave and EM flare, it would be proof that the binary merger occurred within the accretion disk of an active galactic nuclei.

The initial analysis of GW190521 by the LIGO and Virgo Collaborations (LVC) estimated that it had a primary m_1^{src} and secondary mass m_2^{src} of $85^{+21}_{-14} M_{\odot}$ and $66^{+17}_{-18} M_{\odot}$, respectively (Abbott et al. 2020b). This would mean one or both of the black holes lie within the PISN mass gap. If true, GW190521 would either challenge existing stellar formation theory, or provide the first instance of a new class of hierarchically formed binaries. Several papers, including the original announcement, explored this and other possibilities (Abbott et al. 2020b; De Luca et al. 2020; Kremer et al. 2020; Costa et al. 2020; Ziegler & Freese 2020; Safarzadeh & Haiman 2020; Belczynski 2020).

Table 1. The 90% credible marginal intervals for GW190521 using the IMRPhenomXPHM model. In order, the intervals for the gravitational-wave only prior using either a uniform in mass ratio q and source-frame total mass M^{src} prior, uniform in source-frame component masses $m_{1,2}$ prior, and the maximum-likelihood parameters. We show the marginal intervals separately for both the low- q ($q < 4$) and high- q ($q > 4$) modes evident when using a uniform in $m_{1,2}^{\text{src}}$ prior. On the right are the intervals when we limit to the observed location of the EM flare for the uniform in q - M prior.

| Parameter | GW-only | | GW+EM | | |
|--------------------------------|------------------------------|-------------------------------|--------------------------------|------------------------------|-------------------------|
| | q - M^{src} prior | $m_{1,2}^{\text{src}}$ prior | ML | q - M^{src} prior | |
| $m_1^{\text{src}} [M_{\odot}]$ | 168^{+15}_{-61} | low- q 100^{+17}_{-18} | high- q 166^{+16}_{-35} | 171 | 108^{+33}_{-12} |
| $m_2^{\text{src}} [M_{\odot}]$ | 16^{+33}_{-3} | 57^{+17}_{-16} | 16^{+14}_{-3} | 16 | 47^{+22}_{-23} |
| $M^{\text{src}} [M_{\odot}]$ | 184^{+15}_{-30} | 156^{+21}_{-15} | 183^{+15}_{-27} | 187 | 156^{+17}_{-14} |
| q | $10.7^{+2.4}_{-8.6}$ | $1.8^{+1.0}_{-0.6}$ | $10.3^{+2.4}_{-5.7}$ | 10.6 | $2.2^{+3.3}_{-0.8}$ |
| χ_{eff} | $-0.51^{+0.24}_{-0.11}$ | $-0.16^{+0.42}_{-0.40}$ | $-0.53^{+0.14}_{-0.12}$ | -0.55 | $-0.45^{+0.40}_{-0.23}$ |
| $ \chi_1 $ | $0.85^{+0.11}_{-0.25}$ | $0.72^{+0.25}_{-0.59}$ | $0.87^{+0.10}_{-0.16}$ | 0.89 | $0.92^{+0.06}_{-0.28}$ |
| $d_L [\text{Mpc}]$ | 1060^{+1400}_{-280} | 3130^{+2260}_{-1500} | 1100^{+900}_{-310} | 950 | - |

In this letter, we analyze GW190521 using a standard astrophysical prior that the rate is uniform in comoving volume. Current estimates for the mass ratio distribution from the gravitational-wave observation of lighter stellar-mass black hole mergers are still weakly constrained (Abbott et al. 2020c); given that GW190521 is a population outlier, it may be the first instance of a separate population. In light of this, we consider two priors for the binary’s masses: (1) flat in mass ratio q (where we define $q \geq 1$; i.e., as the ratio of the larger mass to the smaller mass) and source-frame total mass M^{src} , and (2) uniform in source-frame component masses $m_{1,2}^{\text{src}}$. We also separately combine the distance and sky location information from the electromagnetic observation under the assumption of a common origin.

We find that GW190521 has posterior support for larger mass ratio than previously reported under both mass priors. With the uniform in mass ratio prior, 93% of the posterior is at $q > 4$. The uniform in component mass prior yields a bimodal posterior in mass ratio, with 51% of the posterior has $q > 4$. The component masses are consistent with neither component lying within the mass gap from pair-instability supernova. If one considers even a moderate prior for the existence of a mass gap, then the high-mass-ratio mode is selected for at high confidence. This could make it the first intermediate-mass-ratio inspiral (IMRI) observed (Brown et al. 2007). The LIGO and Virgo Collaborations (LVC) also used a prior uniform in component mass in their analysis of GW190521, but did not find the high-mass-ratio mode in the posterior (Abbott et al. 2020b). We find that this discrepancy is likely due to a combination of constraints used in the LVC analysis that excised the highest likelihood regions, along with a difference in distance prior, and the overall complexity of sampling the parameter space.

2. GRAVITATIONAL-WAVE INFERENCE

We estimate the source parameters of GW190521 using the open-source PyCBC Inference library (Biwer et al. 2019; Nitz et al. 2018b) along with the Dynesty nested sampler (Speagle 2020) and the public LIGO and Virgo data (Vallisneri et al. 2015; Abbott et al. 2019d). A low and high frequency cutoff at 20 and 500 Hz, respectively, are used for the evaluation of the likelihood. We empirically find that the likelihood surface for GW190521 has a complex multi-modal structure. To obtain an accurate estimate of the posterior density, we found it necessary to numerically marginalize over the polarization angle ψ and the coalescence phase ϕ_c using a 1000×240 grid. These parameters are strongly coupled to each other and the inclination an-

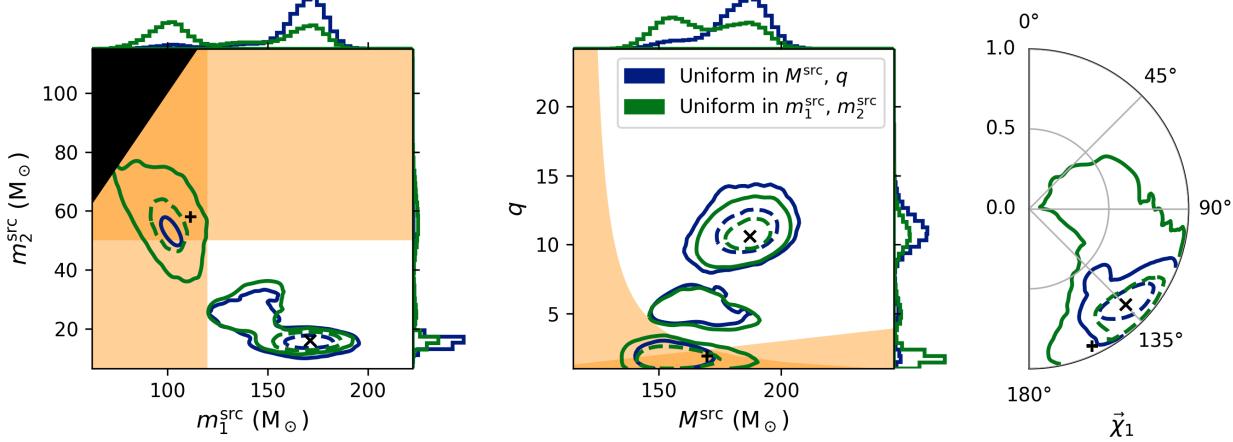


Figure 1. Posterior distribution for GW190521 using a prior uniform in mass ratio q and source-frame total mass M_{src} (blue) and using a prior uniform in source-frame component masses $m_{1,2}^{\text{src}}$ (green). In both cases a prior uniform in comoving volume and isotropic in sky location is used. Shown are the source-frame component masses $m_{1,2}^{\text{src}}$ (left), mass ratio q versus source-frame total mass M^{src} (center), and dimensionless spin of the more massive black hole $\vec{\chi}_1$ (right). The $\vec{\chi}_1$ angle is measured with respect to the orbital angular momentum at a fiducial gravitational-wave frequency of 20 Hz, with 0° corresponding to aligned spin. Orange regions indicate parts of parameter space where one or both component objects are in the “mass gap” $[50, 120] M_\odot$. Dashed and solid contours indicate the 50% and 90% credible regions, respectively. Contours are drawn by applying a multimodal kernel density estimate (Farr & Farr 2015) to the samples. The one dimensional marginal distributions are shown along the axes for the left and middle panels along with the 90% credible interval. The black plus and cross in the left and middle plots are the maximum-likelihood points in the regions $q \in [1, 2]$ and $q \in [2, 25]$, respectively. The gravitational waveform corresponding to each of these points is shown in Fig. 4.

gle ι due to the the relatively few observable cycles in GW190521. Typical gravitational-wave analyses have found self-consistent posteriors using Dynesty with 3–5000 live points (Romero-Shaw et al. 2020a). However, to ensure sampling of the parameter space with separated modes that occupy vastly different volumes of the prior space, we conduct our analysis with 20–40 000 live points. This helps guard against mode “die-off” whereby the sampler neglects entire modes if they are not populated by live points early enough in the analysis.

We consider two priors for the black hole masses: a prior that is flat in the source-frame total mass M^{src} between $80 - 300 M_\odot$ and is uniform in the mass ratio q from $1 - 25$, along with a prior which is uniform in component masses within the same bounds. We achieve the latter posterior by re-weighting our analysis which used a uniform in mass ratio prior. We also separately consider the possibility that the EM flare and GW merger share a common origin. In all cases, we use a prior isotropic in orientation and uniform in magnitude between 0 and 0.99 for each object’s dimensionless spin $\vec{\chi}_{1,2}$. The binary orientation given by its inclination ι and polarization angle ψ is chosen to be isotropic. In the case where we are agnostic to a possible common origin for the observed flare and gravitational-wave merger, we use a prior that is uniform in comoving volume and

isotropic in sky location. When assuming a common origin for the GW and flare observations, we use the sky location and redshift of the flare as a prior to constrain the inference from the gravitational-wave data.

To model the gravitational waveform we use the recently developed IMRPhenomXPHM model (Pratten et al. 2020). This waveform models a circular BBH merger including sub-dominant harmonics and the effects of precession. IMRPhenomXPHM includes improvements over the IMRPhenomPv3HM model (Khan et al. 2019), which is one of the models used in the original analysis of GW190521 (Abbott et al. 2020b). These improvements include calibration of the sub-dominant harmonics against numerical relativity simulations and high-mass-ratio waveforms produced through perturbative expansions of general relativity.

For comparison to IMRPhenomXPHM, we also analyze GW190521 with NRSur7dq4 (Varma et al. 2019), which is a model based on the interpolation of numerical relativity simulations up to $q = 4$ and includes an extrapolation up to $q = 6$. Due to the limited range of the model, we cannot perform a full comparison to the results of IMRPhenomXPHM. However, we can use NRSur7dq4 to crosscheck IMRPhenomXPHM within the models’ common regions of validity.

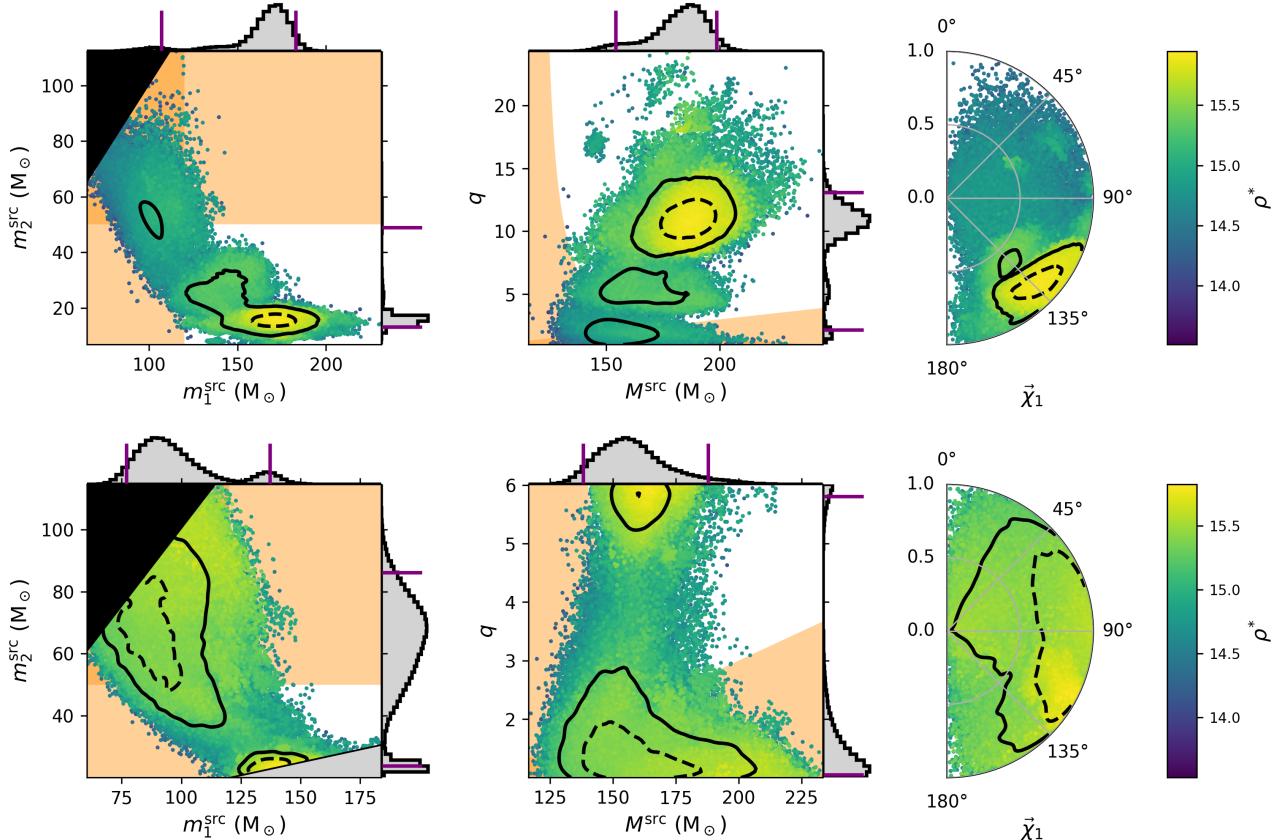


Figure 2. Posterior distribution for GW190521 with a uniform prior in mass ratio and source-frame total mass, as well as uniform in comoving volume and isotropic in sky location. Results for IMRPhenomXPHM (top) and NRSur7dq4 (bottom) are shown. Parameters shown, and the definition of contours and orange regions are the same as in Fig. 1. The gray region in the bottom component mass plot indicates the area of parameter space excluded by the NRSur7dq4 model. Posterior samples are colored by their signal-to-noise ratio $\rho \equiv (2 \ln \mathcal{L})^{1/2}$, where \mathcal{L} is the likelihood ratio at the given point. The one dimensional marginal distributions are shown along the axes for the left and middle panels along with the 90% credible interval.

3. RESULTS

The posterior results for GW190521 using just the gravitational-wave data and both mass priors are shown in Fig. 1. Figure 2 shows a comparison of the IMRPhenomXPHM and NRSur7dq4 models using the uniform in mass ratio prior. Figure 3 shows the posterior results when assuming a common source with the observed EM flare. The credible intervals for the IMRPhenomXPHM model are summarized in Table 1. Notably, all posteriors exhibit some level of multi-modality.

For the GW-only posteriors, we find that, within their common range of mass ratio ($q < 6$), both the IMRPhenomXPHM and NRSur7dq4 models give comparable results. In both cases, the maximum-likelihood point is at mass ratios > 5 . The NRSur7dq4 model is clearly limited by the inability to sample above $q = 6$. For the IMRPhenomXPHM model (which we allow to explore up to $q = 25$) we find that the highest likelihood is at $q \sim 11$.

When we constrain the sky location and redshift to those of the observed flare, we find that the two modes at $q \sim 1 - 2$ and $q \sim 5 - 6$ have approximately equal posterior support, but the highest mass ratio mode is nearly excluded. As there is a degeneracy between the mass ratio and distance — higher mass ratios imply a closer source — the substantial difference in preferred mass ratio arises from the tight distance constraint of the flare. The reality of the flare association will have a substantial impact on the understanding of GW190521’s source parameters.

We compare our results to those obtained in the original analysis (Abbott et al. 2020a) performed by the LVC in Fig 5. If we compare our posterior using a prior that is uniform in source-frame component masses, which is our most similar analysis to the one performed by the LVC, we find that there is still significant support (51%) for $q > 4$. We further reweight from our uniform in comoving volume prior to one which is uniform in the cube of the luminosity distance, which was used by the LVC.

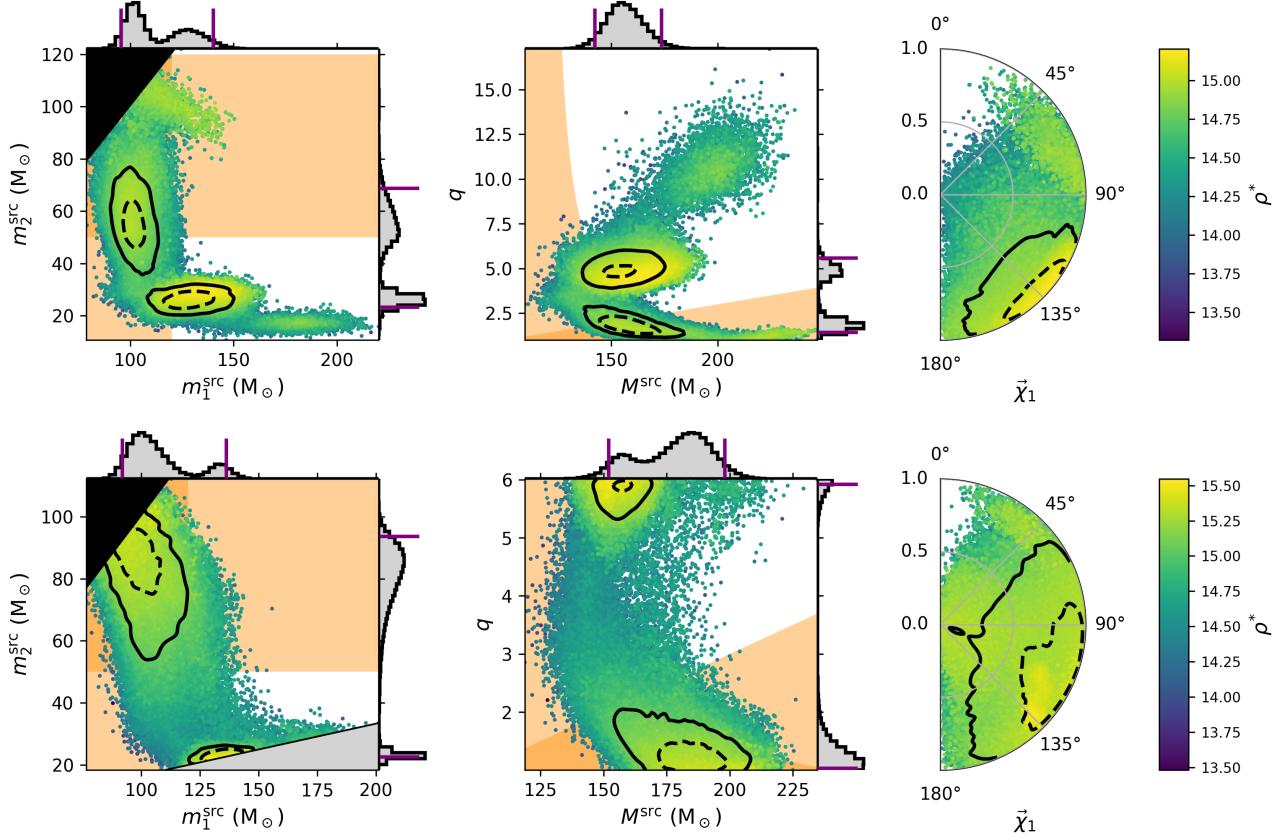


Figure 3. Posterior distribution for GW190521 using the location of the EM flare observed by ZTF to fix the sky location and redshift. Results for IMRPhenomXPHM (top) and NRSur7dq4 (bottom) are shown. See Fig. 2 for plot details.

The LVC analysis also applied strict constraints on the prior space (shown by the shaded areas) which prevents sampling the regions of parameter space we find with highest likelihood. Combined with the resampling efficiency, we find that our results are compatible with the LVC results only after reweighting the distance prior and also applying the constraints in the LVC analysis.

There is a clear multi-modal structure visible in our posteriors. We compare the gravitational waveform from the two dominant modes in the GW-only IMR-PhenomXPHM analysis in Fig. 4. As expected, we see that the waveforms are similar in both modes. Each waveform is a sum of a spin-weighted spherical harmonics. To date, only two events have had measurable sub-dominant harmonics, GW190412 (Abbott et al. 2020c) and GW190814 (Abbott et al. 2020d). If we just use the dominant harmonic in the waveform model, the signal-to-noise ratio is 14.3 and 14.5 for the low and high-mass-ratio waveforms, respectively. The total signal-to-noise ratio for the two waveforms, however, is 15.2 and 15.9, respectively. This means that nearly all of the additional signal-to-noise ratio of the maximum-likelihood waveform comes from the sub-dominant gravitational-wave harmonics.

The original LVC analysis of GW190521 used a lower-frequency cutoff of 11 Hz. We find no significant change in the likelihoods of our posterior samples if we extend our analysis down from 20 to 11 Hz. To further validate the qualitative features of the posteriors, we also performed an analysis with a simulated gravitational-wave signal whose parameters are drawn from our posterior. We find a similar multi-modal structure in the posterior for the simulated signal.

4. DISCUSSION

We have analyzed GW190521 using a prior uniform in mass ratio and total mass, as well as a using a prior uniform in source-frame component masses. We find that when considering the GW data alone the component masses are consistent with a source with $q > 4$ at 93% (51%) probability for the prior uniform in q , M^{src} ($m_{1,2}^{\text{src}}$). Given the likelihood of the existence of a mass gap, which would disfavor the lower-mass-ratio mode, we surmise that GW190521 is likely the first observed IMRI.

We also find that the reality of the flare association significantly impacts the parameter distribution. As suggested in Graham et al. (2020) this ambiguity may be

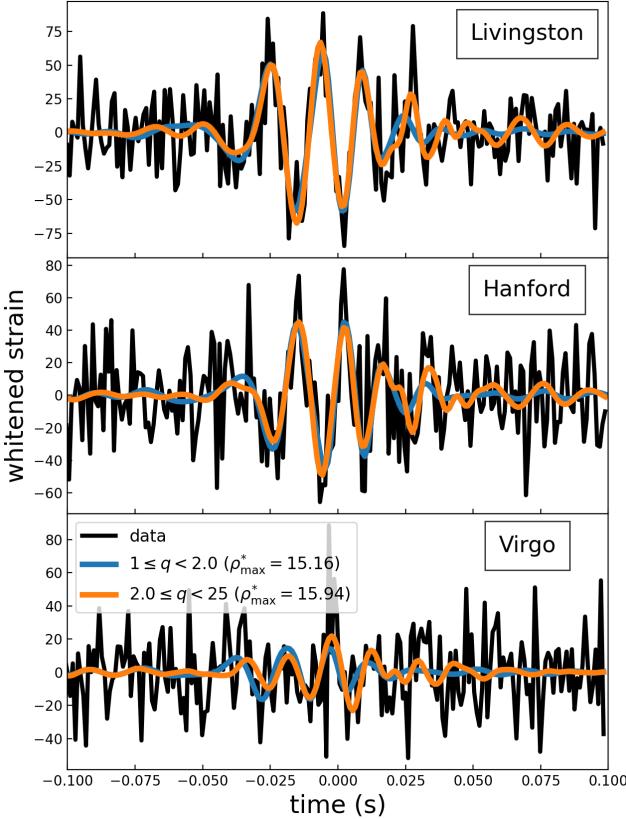


Figure 4. Whitened data and gravitational waveform model as seen in each detector. Shown are the maximum-likelihood IMRPhenomXPHM waveforms in the regions $q \in [1, 2)$ and $q \in [2, 25)$ (corresponding to the plus, and cross in the top plots of Fig. 1, respectively). These have network signal-to-noise ratios of 15.16 and 15.94, respectively. The data and waveforms are time shifted such that $t = 0$ corresponds to the coalescence time of the maximum-likelihood waveform in each detector.

resolved if a recurrence of the flare is observed at the predicted time. Preliminary estimates of the association probability do not provide significant support nor reject the possibility based on the spatial coincidence alone (Ashton et al. 2020). From our analysis, we find that the odds of a common spatial origin is $\ln \mathcal{B} \gtrsim -4$ when we assume that the localization volume was the primary focus of follow-up observation. As an optimistic upper bound can be obtained if assume that the entire prior volume we consider had been equally surveyed by ZTF and no other EM flares observed. However, even under this assumption, we only find $\ln \mathcal{B} \sim 2.3$ in favor of the association.

Based on the gravitational-wave data alone, the component masses of GW190521 place both black holes outside the “mass gap” between $50 - 120 M_{\odot}$ at the 93% or 52% credible level if using either a uniform in q , M^{src} or $m_{1,2}^{\text{src}}$ prior, respectively. This suggests that a hierar-

chical merger scenario may not be required to explain GW190521. Another study has similarly suggested this based on a reweighting of the public results (Fishbach & Holz 2020). However, our analysis significantly increases the support for this scenario, as we find additional modes in the posterior missed by earlier analyses. For the high-mass-ratio mode, the merger is preferentially precessing with significant spin on the primary mass $\chi_1 > 0.7$ at the 90% credible level. Given the preference for spin anti-aligned with the orbital angular momentum, $\chi_{\text{eff}} < 0$ at 97% probability, this may suggest a dynamical capture (Postnov & Kuranov 2019; Bavera et al. 2020; Safarzadeh 2020).

A limitation of all current analyses of GW190521 is the lack of a complete description of all physical effects in a single waveform model. Several analyses have suggested that GW190521 may also be consistent with an eccentric merger (Gayathri et al. 2020; Romero-Shaw et al. 2020b; Calderón Bustillo et al. 2020). At this time no model exists that includes sub-dominant harmonics, precession, eccentricity, nearly extremal spins, and support for high mass ratios simultaneously. To achieve a complete understanding of GW190521 and mitigate systematic effects, it is necessary for the numerical relativity and modelling community to work towards such a comprehensive prescription.

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We make available posterior samples from our analyses along with the configuration files necessary to reproduce our results at <http://github.com/gwastro/gw190521>.

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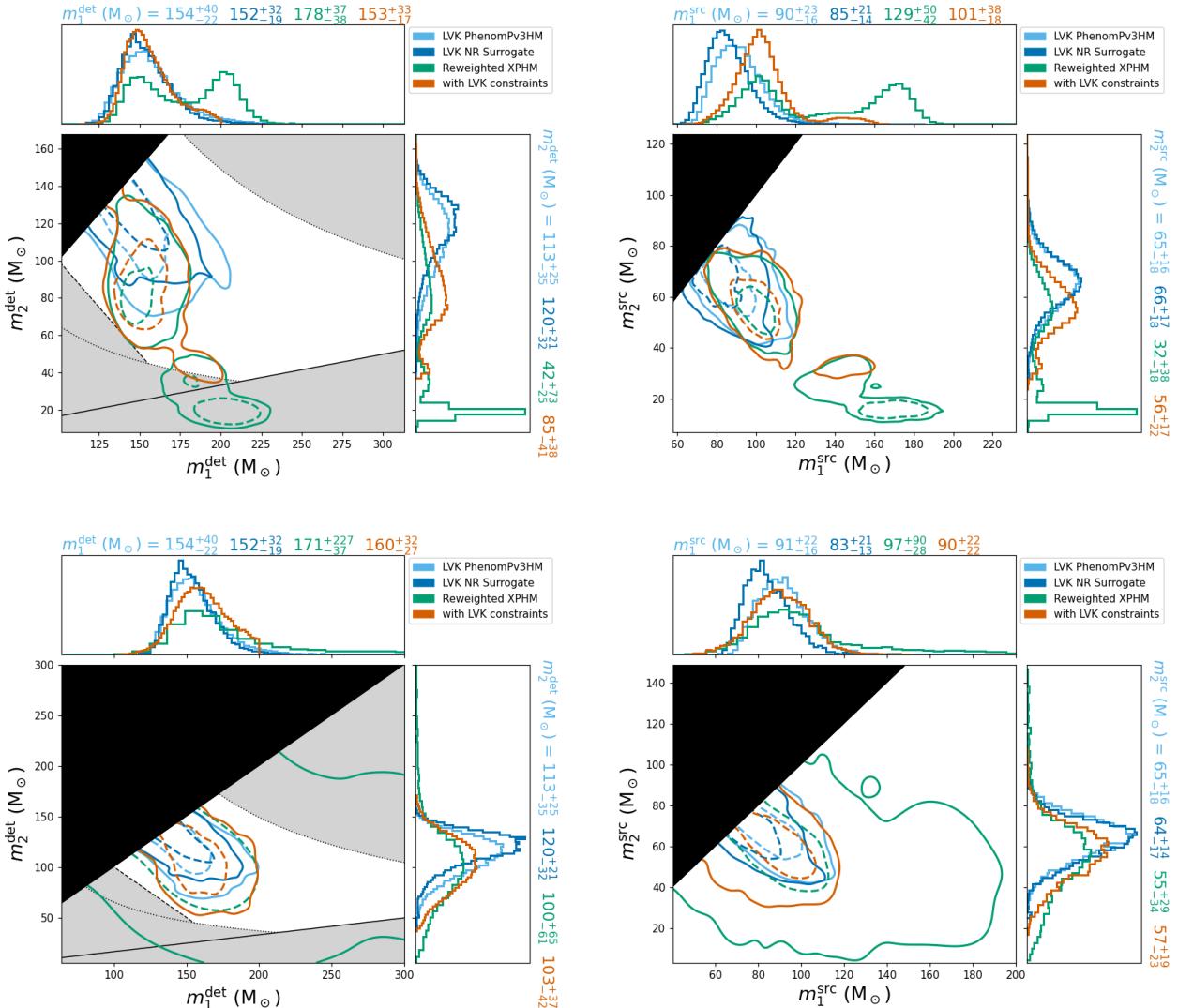


Figure 5. Comparison between our reweighted posteriors and posteriors published by the LIGO and Virgo collaborations (LVC) in Abbott et al. (2020b). The left column shows detector-frame masses; right column shows source-frame masses. The top row shows the result of reweighting our samples from a prior uniform in source-frame total mass and mass ratio to uniform in source-frame component masses. The bottom row shows the result when we additionally reweight from a prior uniform in comoving volume to a prior uniform in the cube of the luminosity distance; this is the prior most similar to what was used in the LVC analysis. Grayed regions indicate constraints used in the LVC analysis. The dotted, dashed, and solid boundaries correspond to the chirp mass, total mass, and mass ratio constraints that were used. The combination of the constraints excises the region in which we find the maximum-likelihood waveform, and which has the largest posterior support assuming a prior uniform in mass ratio, source-frame total mass, and comoving volume.

REFERENCES

- Aasi, J., et al. 2015, Class. Quantum Grav., 32, 074001, doi: [10.1088/0264-9381/32/7/074001](https://doi.org/10.1088/0264-9381/32/7/074001)
- Abbott, B., et al. 2019a, Phys. Rev. Lett., 123, 161102, doi: [10.1103/PhysRevLett.123.161102](https://doi.org/10.1103/PhysRevLett.123.161102)
- . 2020a, Astrophys. J. Lett., 892, L3, doi: [10.3847/2041-8213/ab75f5](https://doi.org/10.3847/2041-8213/ab75f5)
- Abbott, B. P., et al. 2016, Phys. Rev. Lett., 116, 061102, doi: [10.1103/PhysRevLett.116.061102](https://doi.org/10.1103/PhysRevLett.116.061102)
- . 2019b, Phys. Rev. X, 9, 031040, doi: [10.1103/PhysRevX.9.031040](https://doi.org/10.1103/PhysRevX.9.031040)
- . 2019c, Astrophys. J., 882, L24, doi: [10.3847/2041-8213/ab3800](https://doi.org/10.3847/2041-8213/ab3800)
- Abbott, R., et al. 2019d. <https://arxiv.org/abs/1912.11716>
- . 2020b, Phys. Rev. Lett., 125, 101102, doi: [10.1103/PhysRevLett.125.101102](https://doi.org/10.1103/PhysRevLett.125.101102)

- Abbott, R., Abbott, T. D., Abraham, S., et al. 2020c, Phys. Rev. D, 102, 043015, doi: [10.1103/PhysRevD.102.043015](https://doi.org/10.1103/PhysRevD.102.043015)
- Abbott, R., et al. 2020d, The Astrophysical Journal, 896, L44, doi: [10.3847/2041-8213/ab960f](https://doi.org/10.3847/2041-8213/ab960f)
- Acernese, F., et al. 2015, Class. Quantum Grav., 32, 024001, doi: [10.1088/0264-9381/32/2/024001](https://doi.org/10.1088/0264-9381/32/2/024001)
- Ashton, G., Ackley, K., Hernandez, I. M. n., & Piotrzkowski, B. 2020. <https://arxiv.org/abs/2009.12346>
- Bavera, S. S., Fragos, T., Qin, Y., et al. 2020, Astron. Astrophys., 635, A97, doi: [10.1051/0004-6361/201936204](https://doi.org/10.1051/0004-6361/201936204)
- Belczynski, K. 2020. <https://arxiv.org/abs/2009.13526>
- Belczynski, K., et al. 2016, Astron. Astrophys., 594, A97, doi: [10.1051/0004-6361/201628980](https://doi.org/10.1051/0004-6361/201628980)
- Bellm, E. C., Kulkarni, S. R., Graham, M. J., et al. 2019, PASP, 131, 018002, doi: [10.1088/1538-3873/aaecbe](https://doi.org/10.1088/1538-3873/aaecbe)
- Biwer, C. M., Capano, C. D., De, S., et al. 2019, Publ. Astron. Soc. Pac., 131, 024503, doi: [10.1088/1538-3873/aaef0b](https://doi.org/10.1088/1538-3873/aaef0b)
- Brown, D. A., Fang, H., Gair, J. R., et al. 2007, Phys. Rev. Lett., 99, 201102, doi: [10.1103/PhysRevLett.99.201102](https://doi.org/10.1103/PhysRevLett.99.201102)
- Calderón Bustillo, J., Sanchis-Gual, N., Torres-Forné, A., & Font, J. A. 2020. <https://arxiv.org/abs/2009.01066>
- Corral-Santana, J. M., Casares, J., Muñoz-Darias, T., et al. 2016, Astron. Astrophys., 587, A61, doi: [10.1051/0004-6361/201527130](https://doi.org/10.1051/0004-6361/201527130)
- Costa, G., Bressan, A., Mapelli, M., et al. 2020. <https://arxiv.org/abs/2010.02242>
- Dal Canton, T., Nitz, A. H., Gadre, B., et al. 2020. <https://arxiv.org/abs/2008.07494>
- De Luca, V., Desjacques, V., Franciolini, G., Pani, P., & Riotto, A. 2020. <https://arxiv.org/abs/2009.01728>
- Dvorkin, I., Uzan, J.-P., Vangioni, E., & Silk, J. 2018, Mon. Not. Roy. Astron. Soc., 479, 121, doi: [10.1093/mnras/sty1414](https://doi.org/10.1093/mnras/sty1414)
- Farr, B., & Farr, W. M. 2015, kombine: a kernel-density-based, embarrassingly parallel ensemble sampler, <https://github.com/bfarr/kombine>
- Fishbach, M., & Holz, D. E. 2020. <https://arxiv.org/abs/2009.05472>
- Flesch, E. W. 2019, arXiv e-prints, arXiv:1912.05614. <https://arxiv.org/abs/1912.05614>
- Gayathri, V., Healy, J., Lange, J., et al. 2020. <https://arxiv.org/abs/2009.05461>
- Graham, M., et al. 2020, Phys. Rev. Lett., 124, 251102, doi: [10.1103/PhysRevLett.124.251102](https://doi.org/10.1103/PhysRevLett.124.251102)
- Green, A. M., & Kavanagh, B. J. 2020. <https://arxiv.org/abs/2007.10722>
- Khan, S., Ohme, F., Chatzioannou, K., & Hannam, M. 2019. <https://arxiv.org/abs/1911.06050>
- Kremer, K., Spera, M., Becker, D., et al. 2020. <https://arxiv.org/abs/2006.10771>
- LVC. 2019, GraceDB — Gravitational-Wave Candidate Event Database. <https://gracedb.ligo.org/superevents/public/O3/>
- Marchant, P., Renzo, M., Farmer, R., et al. 2019, Astrophys. J., 882, 36, doi: [10.3847/1538-4357/ab3426](https://doi.org/10.3847/1538-4357/ab3426)
- Nitz, A. H., Capano, C., Nielsen, A. B., et al. 2019a, Astrophys. J., 872, 195, doi: [10.3847/1538-4357/ab0108](https://doi.org/10.3847/1538-4357/ab0108)
- Nitz, A. H., Dal Canton, T., Davis, D., & Reyes, S. 2018a, Phys. Rev. D, 98, 024050, doi: [10.1103/PhysRevD.98.024050](https://doi.org/10.1103/PhysRevD.98.024050)
- Nitz, A. H., Dent, T., Davies, G. S., & Harry, I. 2020, Astrophys. J., 897, 2, doi: [10.3847/1538-4357/ab96c7](https://doi.org/10.3847/1538-4357/ab96c7)
- Nitz, A. H., & Wang, Y.-F. 2020. <https://arxiv.org/abs/2007.03583>
- Nitz, A. H., Harry, I. W., Willis, J. L., et al. 2018b, PyCBC Software, <https://github.com/gwastro/pycbc>, GitHub
- Nitz, A. H., Dent, T., Davies, G. S., et al. 2019b, Astrophys. J., 891, 123, doi: [10.3847/1538-4357/ab733f](https://doi.org/10.3847/1538-4357/ab733f)
- Piran, T., & Hotokezaka, K. 2020, Who Ordered That? On the Origin of LIGO’s Merging Binary Black Holes, ed. L. Brink, V. Mukhanov, E. Rabinovici, & K. Phua (Singapur: World Scientific), 243–257, doi: [10.1142/9789811203961_0019](https://doi.org/10.1142/9789811203961_0019)
- Postnov, K., & Kuranov, A. 2019, Mon. Not. Roy. Astron. Soc., 483, 3288, doi: [10.1093/mnras/sty3313](https://doi.org/10.1093/mnras/sty3313)
- Pratten, G., et al. 2020. <https://arxiv.org/abs/2004.06503>
- Romero-Shaw, I., et al. 2020a, doi: [10.1093/mnras/staa2850](https://doi.org/10.1093/mnras/staa2850)
- Romero-Shaw, I. M., Lasky, P. D., Thrane, E., & Bustillo, J. C. 2020b. <https://arxiv.org/abs/2009.04771>
- Roulet, J., Venumadhav, T., Zackay, B., Dai, L., & Zaldarriaga, M. 2020. <https://arxiv.org/abs/2008.07014>
- Safarzadeh, M. 2020, Astrophys. J. Lett., 892, L8, doi: [10.3847/2041-8213/ab7cdc](https://doi.org/10.3847/2041-8213/ab7cdc)
- Safarzadeh, M., & Haiman, Z. 2020. <https://arxiv.org/abs/2009.09320>
- Singer, L. P., & Price, L. 2016, Phys. Rev. D, 93, 024013, doi: [10.1103/PhysRevD.93.024013](https://doi.org/10.1103/PhysRevD.93.024013)
- Speagle, J. S. 2020, Monthly Notices of the Royal Astronomical Society, 493, 3132, doi: [10.1093/mnras/staa278](https://doi.org/10.1093/mnras/staa278)
- Stevenson, S., Sampson, M., Powell, J., et al. 2019, doi: [10.3847/1538-4357/ab3981](https://doi.org/10.3847/1538-4357/ab3981)
- Taylor, S. R., & Gerosa, D. 2018, Phys. Rev. D, 98, 083017, doi: [10.1103/PhysRevD.98.083017](https://doi.org/10.1103/PhysRevD.98.083017)
- Vallisneri, M., Kanner, J., Williams, R., Weinstein, A., & Stephens, B. 2015, J. Phys. Conf. Ser., 610, 012021, doi: [10.1088/1742-6596/610/1/012021](https://doi.org/10.1088/1742-6596/610/1/012021)

- van Son, L., de Mink, S., Broekgaarden, F., et al. 2020, *Astrophys. J.*, 897, 100, doi: [10.3847/1538-4357/ab9809](https://doi.org/10.3847/1538-4357/ab9809)
- Varma, V., Field, S. E., Scheel, M. A., et al. 2019, *Phys. Rev. Research.*, 1, 033015, doi: [10.1103/PhysRevResearch.1.033015](https://doi.org/10.1103/PhysRevResearch.1.033015)
- Venumadhav, T., Zackay, B., Roulet, J., Dai, L., & Zaldarriaga, M. 2019a, *Phys. Rev. D*, 100, 023011, doi: [10.1103/PhysRevD.100.023011](https://doi.org/10.1103/PhysRevD.100.023011)
- . 2019b. <https://arxiv.org/abs/1904.07214>
- Woosley, S. E. 2017, *Astrophys. J.*, 836, 244, doi: [10.3847/1538-4357/836/2/244](https://doi.org/10.3847/1538-4357/836/2/244)
- . 2019, *The Astrophysical Journal*, 878, 49, doi: [10.3847/1538-4357/ab1b41](https://doi.org/10.3847/1538-4357/ab1b41)
- Yoshida, T., Umeda, H., Maeda, K., & Ishii, T. 2016, *MNRAS*, 457, 351, doi: [10.1093/mnras/stv3002](https://doi.org/10.1093/mnras/stv3002)
- Zackay, B., Dai, L., Venumadhav, T., Roulet, J., & Zaldarriaga, M. 2019. <https://arxiv.org/abs/1910.09528>
- Ziegler, J., & Freese, K. 2020. <https://arxiv.org/abs/2010.00254>