JOURNAL OF APPLIED PHYSICS VOLUME 86, NUMBER 6 15 SEPTEMBER 1999

Vacancy-enhanced intermixing in highly strained InGaAs/GaAs multiple quantum well photodetector

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(Received 22 October 1998; accepted for publication 6 May 1999)

Impurity-free vacancy disordering techniques using rapid thermal annealing with electron-beam evaporated SiO₂ encapsulant was utilized to study its effect on the optical and electrical properties of the highly strained InGaAs/GaAs quantum well infrared photodetector. The photoluminescence peak is blueshifted and its line width does not increase much, indicating the compositional disordering of the quantum well structure and there is no strain relaxation or minimal deterioration of the heterostructure quality. Both transverse electric and transverse magnetic infrared intersubband transitions are retained and observed after intermixing. The absorption peak wavelength is redshifted from the as grown 10.2 μ m to the interdiffused 10.5 and 11.2 μ m, for 5 and 10 s annealing at 850 °C, respectively, without appreciable degradation in absorption strength. Theoretical calculations of the absorption spectra are in good agreement with the experimental data. Annealed responsivity spectra of both 0° and 90° polarization are of comparable amplitude but with narrower spectra line width. Dark current of the annealed devices is found to be an order of magnitude larger than the as-grown one at 77 K. © 1999 American Institute of Physics. [S0021-8979(99)04416-3]

I. INTRODUCTION

The study of long wavelength quantum well infrared photodetector (QWIP) based on intersubband transitions (ITs) has attracted much research interest and progressed rapidly¹⁻⁸ since the first experimental demonstration of large dipole moment in AlGaAs/GaAs multiple quantum well (MQW). However, most of the studies have been limited to an AlGaAs/GaAs MQW system owing to the mature growth and processing technology. Because of the polarization selection rule, only incident light with a component of the electric field parallel to the growth direction (z axis) can be absorbed in a n-type QW. Normal incidence is possible only with other optical coupling schemes. 10 With the development of strained layer QW and band gap engineering, a high quality pseudomorphic QW is achievable. It has been demonstrated that normal incident strained InGaAS/GaAs QWIP¹¹ are possible without grating coupling. Due to the smaller effective mass and the higher electron mobility, n-typed InGaAs/GaAs QWIPs offer better infrared detector properties than AlGaAs/GaAs material. But the thermal stability of strained layers, when subjected to heat treatment, is of prime importance in photonic integrated circuits applications, especially for structures with a higher In concentration. This is because the critical layer thickness is smaller in highly strained heterostructure and there is an increased risk of strain relaxation by the generation of misfit dislocation during thermal annealing.

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QW intermixing has attracted increasing attention recently as a useful tool not only for spatially selective tuning of the QW band gap, but also as a means to monolithically integrate devices of differing functionality on a single substrate without requiring additional lithography. 12 Postgrowth tuning of the AlGaAs/GaAs IT absorption peak wavelength¹³ and QWIP detection wavelength range 14,15 have also been demonstrated by this technology. In this article, the influence of layers interdiffusion on the performance of a highly strained n-doped In_{0.3}Ga_{0.7}As/GaAs QWIP at 850 °C is studied. We demonstrate in our experiments that the QWIP absorption wavelength can be tuned to a redshift of $\sim 1 \mu m$ and the heterostructure quality is not deteriorated by means of impurity-free vacancy disordering. Both the TE and TM intersubband transitions are observed after intermixing and the responsivity of these annealed devices is comparable to the as-grown device. Theoretical calculation of the absorption spectra, taking into account the interdiffusion and strain effects, is shown to be in good agreement with the experimental results. We also show that the dark current characteristics and the carriers transport properties under an applied electric field have been modified after interdiffusion.

II. EXPERIMENT

The QWIP samples used in this study were grown by molecular beam epitaxy (MBE) on a (100) semi-insulating GaAs substrate. The MQW consists of 50 periods of 40 Å wide $In_{0.3}Ga_{0.7}As$ wells and 300-Å-thick undoped GaAs barrier layers. The wells were doped with Si to a density of about 2×10^{18} cm⁻³. The top and bottom of the MQW had

 n^+ GaAs cap (0.5 μ m) and buffer (1 μ m) layers, respectively, for ohmic contacts. Each QW was designed to have only one bound state inside the well and the first excited state in the continuum above the barrier. The energy difference between the first two eigenstates approximately corresponds to wavelength $\cong 10 \ \mu \text{m} \ (\hbar \omega = 124 \ \text{meV})$. Prior to annealing process, approximately a 250-nm-thick SiO₂ dielectric layer was deposited on the samples surface using an electron-beam evaporator. Rapid thermal annealing (RTA) was carried out using a halogen lamp annealing system (AST SHS 10) with double strip graphite heater in nitrogen ambient. During annealing, the sample surfaces were protected from surface degradation by means of a GaAs proximity cap. One of the samples was annealed for anneal time $t_A = 5$ s at 850 °C while the other for $t_A = 10 \text{ s}$ at the same temperature. Mesa diode $(200\times200 \,\mu\text{m}^2)$ were fabricated using standard lithographic technique and wet chemical etching. AuGe/Ni/Au alloyed ohmic contacts were made to the top and bottom contact layers of the device.

III. THEORETICAL MODEL

The interdiffusion process in this model is based on the thermal induced intermixing of Ga and In atoms in the InGaAs/GaAs MQW. The diffusion of group III atoms in the model is described by the Fick's law with equal and constant diffusion coefficients¹⁶ in both the well and barrier layers. The extent of interdiffusion is characterized by the diffusion length $L_d = (Dt)^{1/2}$, where D is diffusion coefficient and t is diffusion time. The In composition profile, w(z), as a function of L_d is given by

$$w(z) = \frac{w_0}{2} \left\{ \operatorname{erf} \left[\frac{L_z + 2z}{4L_d} \right] + \operatorname{erf} \left[\frac{L_z - 2z}{4L_d} \right] \right\}, \tag{1}$$

where w_0 is the as-grown In mole fraction, z denotes the coordinate along the crystal growth direction, L_z is the asgrown well width, and erf(y) denotes the error function. From the diffused In composition profile defined by Eq. (1), interdiffused QW parameters can be calculated separately, including band gap, $E_g(z) = E_g[w = w(z)]$, well-barrier discontinuity, $\Delta E_g(z) = E_g(z) - E_g(z=0)$, and well depth, $V_c(z) = Q_c \Delta E_g(z)$, where the subscript C denotes the electron in the conduction band and Q_c is the conduction band offset. To account for the effect of strain, the interdiffusion induced QW confinement profile, $U_c(z)$, is defined as: $U_c(z) = Q_c[E_g(z) - E_g(z=0)] - S_{\perp c}(z)$, where $S_{\perp c}(z)$ $=Q_cS_{\perp}(z)$. The change in the bulk band gap, $S_{\perp}(z)$, due to the biaxial component of strain is given by $S_{\perp}(z)$ = $-2a[(c_{11}-c_{12})/c_{11}]\epsilon$, where a is the hydrostatic deformation potential, c_{ii} 's are the elastic stiffness, and ϵ is the in-plane strain. With the material parameters listed in Table I and the interdiffused QW parameters obtained earlier, the energies and envelope functions of the electron subband edge at the zone center of the Brillouin zone, and the intersubband absorption are calculated based on the models described in Ref. 25. The diffusion coefficient D is determined by fitting the calculated intersubband transition energies with

TABLE I. List of parameters used in the numerical calculation. Note that the value of D and Γ are fitting parameters.

	$In_xGa_{1-x}As/GaAs$
E_{o} (eV)	$1.425 - 1.501x + .436x^2$
m_c°/m_0	0.0632 - 0.0419x
m_{hh}/m_0	0.5 - 0.09x
m_{lh}/m_0	0.088 - 0.064x
$C_{11}(10^{11} \text{dyn/cm}^2)$	11.9 - 3.571x
$C_{12}(10^{11} \text{dyn/cm}^2)$	5.38 - 0.854x
T(K)	300
$D \text{ (cm}^2\text{/s)}$	1.3×10^{-15}
Γ (eV)	0.028
Q_c	0.7

the measured energy shift of the absorption spectra in Fig. 2. It gives a value of $D = 1.3 \times 10^{-15} \text{ cm}^2 \text{ s}^{-1}$ to an error within 0.1 meV.

IV. RESULT AND DISCUSSION

Photoluminescence (PL) measurements were performed at 4.5 K using the 514.5 nm argon laser at a power of 200 mW prior to and following the annealing. Figure 1 shows the PL spectra of the as-grown and annealed MQW. The PL peak shifts progressively to higher energy with anneal time from as-grown 1.316–1.319 and 1.323 eV, respectively. The blueshift of the band gap energy indicates the intermixing of group III elements near the heterostructure interfaces and the changes in the ground state energy of both the conduction and valence bands. The peak intensity of the $t_A = 5$ s sample is increased by nearly one fold in magnitude, while that of the $t_A = 10$ s sample is decreased by almost the same order, with respect to the as-grown sample. The increase in the peak luminescent intensity may be due to the removal of nonradiative centers from the InGaAs/GaAs interfaces. And the reduction in intensity with successive intermixing is most likely due to the defects that act as trapping centers introduced during the annealing process. The full width at half maximum (FWHM) PL line width of the annealed samples does not increase much as compare to the as-grown sample;

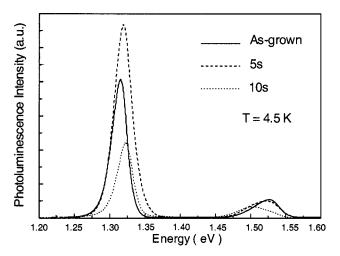


FIG. 1. PL spectra of the as-grown, 5 and 10 s interdiffused InGaAs/GaAs MQW at $T\!=\!4.5~\mathrm{K}.$

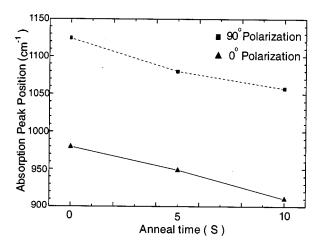


FIG. 2. The redshift of the absorption peak as a function of annealing time for 0° and 90° polarizations. The lines are an aid to the eye.

about 4 and 1 meV, for the 5 and 10 s annealed samples, respectively. Since the well width is below the critical thickness for 30% In concentration, the small variation in PL FWHM may indicate that the onset of strain relaxation or misfit dislocation formation has not been initiated and that there may even be a recovery of strain or an improvement in the heterostructural quality after RTA. ^{18,19} The PL peak broadening for the shorter annealed sample is believed due to the native defects near the surface incorporated during growth. Peaks were also observed at about 1.5 eV, which are redshifted with interdiffusion, in contrast to the PL peaks observed earlier. These peaks may be due to the luminescence from the GaAs either in the top cap layer or the bottom buffer layer of the MQW.

Intersubband absorption measurement was taken using Nicolet Magna-IR 850 Fourier transform infrared spectrometer at room temperature with a 45° polished multipass waveguide geometry. The spatial resolution of this technique is about 4 cm⁻¹. Effect of interdiffusion on the intersubband optical absorption of annealed QWs is evidenced in Fig. 2 where the as-grown absorption peak is redshifted linearly with anneal time for both polarizations. For 0° angle polarization, i.e., a mixture of TE and TM polarizations that contains a component of photon electric field along the growth (z) direction as well as a component in the plane of the layers, the absorption peak is shifted from the as-grown 980 cm⁻¹ (at 10.2 μ m) to 949 (at 10.5 μ m) and 910 cm⁻¹ (11.2 μ m), for the 5 and 10 s annealed samples, respectively. Whereas for normal incident (TE) absorption (the result of band-mixing effects induced by the coupling between the conduction and valence band and is usually forbidden in conventional polarization selection rule),20 the absorption peak is shifted with increasing t_A from 1124 cm⁻¹ (at 8.9 μ m) to $1080 \text{ (at } 9.26 \ \mu\text{m}) \text{ and } 1057 \text{ cm}^{-1} \text{ (at } 9.46 \ \mu\text{m}), \text{ respectively.}$ The difference in the peak wavelength between the two polarizations is due to the D_{2d} tetragonal perturbation of the local crystal and strain field effects on the QW.²¹ The redshift of the absorption peaks may indicate the subband ground-state energy E_1 and the first excited-state energy E_2 (at which oscillator strength, f, is a maximum) are being modified (for e.g., E_1 being pushed higher or E_2 being

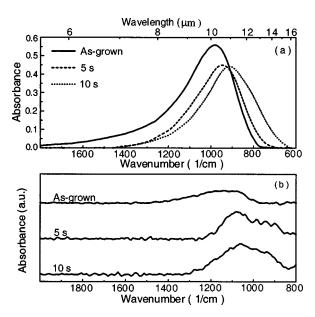


FIG. 3. Absorption spectra of the as-grown, 5 and 10 s annealed samples at 300 K as a function of wavelength for (a) 0° (TE+TM) polarization and (b) 90° (TE) polarizations. (The curves have been shifted vertically for clarity.)

pulled closer to the barrier height or both happen simultaneously) and/or the interdiffusion-induced changes in the doping-dependent depolarization shift,⁹ which result in the postgrowth tuning of the absorption wavelength.

Note in Fig. 3(a) that for 0° polarization, the annealed absorption spectra reduce in amplitude and undergo broadening with increasing anneal time. Also shown in Fig. 3 [curve (b)] is the absorption spectra at 90° polarization. The annealed spectra also broaden in shape even though its amplitude cannot be compared directly after the curves are being shifted vertically for clarity. It is known that Ga is very soluble in SiO₂ at an elevated temperature. As intermixing process proceeds, an increase in the concentration of group III vacancies in the QW is expected due to the diffusion of Ga into the SiO₂ dielectric layer. This will in turn increase the dopant (Si) diffusion rate across the heterointerfaces to the undoped GaAs barrier and the encapsulant layer, as a consequence of Fermi-level effect.²² The out diffusion of Si across the interfaces during interdiffusion process not only reduces the free carrier concentration but also enhances layers intermixing. Since absorption coefficient $\alpha(h\omega) \propto \rho_s$ (ρ_s is the two dimension electron density in the well), the reduction in the number of free carrier available to be excited by the incident IR radiation may render to a reduction in the absorbance. In addition to the reduction in carrier density, the impurity scattering together with the modification in subband structure give rise to the broadening and decrease in amplitude of the absorption spectra. But E_2 remains in the continuum under different annealed conditions produced here, as can be seen from the high-energy tail and the asymmetry of all the absorption spectra shown in Fig. 3(a), which are the characteristic features of bound-to-continuum intersubband transition in QWs.²³ Theoretical calculation of the normalized absorption spectra are shown in Fig. 4 (where broadening factor Γ = 28, 29, and 31 meV are adopted for the as-grown, $t_A = 5$ and 10 s samples), where the absorption

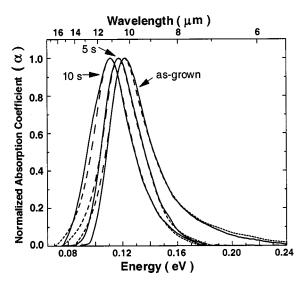


FIG. 4. Normalized absorption spectra of the as-grown, 5 and 10 s annealed samples (from right to left) at 300 K as a function of wavelength (solid line: experimental results, dotted line: calculated results).

peak, spectra width, and spectra shapes are in good agreement with the measured results.

Leakage current was measured with the sample mounted on a cold finger at 77 K using 4156A Parameter Analyzer. The (I-V) characteristic is shown in Fig. 5. Note the asymmetry of the I-V curves between the two polarities. For the as-grown sample, leakage current is higher in reverse bias (i.e., mesa top negative) than in forward bias, which is attributed to the diffusion of dopant species to the growth front during growth or the asymmetrical MBE growth between the GaAs and $In_{0.3}Ga_{0.7}As$ interfaces. ^{23,24} In contrast to this, the annealed devices exhibit an opposite trend, where the leakage currents are higher at forward bias, and they intersect and overlap with each other in reverse bias. We attribute this to the difference in diffusion rate of In and Ga species across the MQW interfaces, which results in lower barrier height²⁵ seen by the thermally excited electrons, and the redistribu-

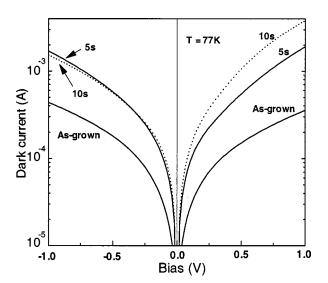


FIG. 5. I-V curve of the as-grown and annealed samples at $T=77~\rm K$ as a function of bias.

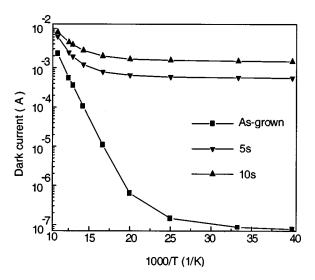


FIG. 6. Leakage current at $V=1~\rm V$ as a function of the reciprocal of temperature in the range between 25 and 90 K. The lines are an aid to the eye.

tion of dopant impurity as described earlier. These two factors together with the thinning of the 300 Å barrier not only result in the asymmetry I-V curves, but also give rise to nearly an order of magnitude higher in leakage current at 77 K, as a consequence of annealing.

Figure 6 shows the leakage currents as a function of the reciprocal of temperature. It is interesting to note that the annealed leakage currents are not very sensitive to temperature variation. The leakage currents remain approximately constant for $T < 50 \,\mathrm{K}$ and increase linearly with higher temperature. Note also that the leakage current of the annealed devices at $T < 50 \,\mathrm{K}$ is 4 or more orders of magnitude larger than the as-grown sample. At $T > 50 \,\mathrm{K}$ where thermionic emission mechanism is dominant, all leakage currents increase linearly to almost the same magnitude at T = 90 K. For temperature range from $T = 25 - 90 \,\mathrm{K}$, the overall dark current is increased by nearly one order of magnitude and by a factor of 8, for the $t_A = 5$ and 10 s samples, respectively; while the as-grown sample is increased by more than 5 orders of magnitude. Since the leakage current at low temperature is mainly dominated by a tunneling mechanism, the huge increase in leakage current at $T < 50 \,\mathrm{K}$ is probably related to the defect assisted tunneling.²⁶ This is most likely due to the intermixing of Si and group III constituent atoms in the heterostructure²² which introduce defects (group III vacancies) and dopant impurity into the barrier and result in significant increase of electron tunneling through the defect states in the barrier. A further demonstration of this is shown in Fig. 7 where the leakage currents of the annealed samples are very sensitive to bias even at a low temperature T = 25 K. The dark current of the t_A = 5 s sample increases more rapidly at bias $|V_b| > 170 \,\mathrm{mV}$; while the 10 s annealed device increases at a even higher slope, with the leakage current intersecting and surpassing that of the $t_A = 5$ s sample at $|V_b| \cong 370 \,\mathrm{mV}$. But the as-grown leakage current remains flattened throughout the range of bias considered.

The photocurrent was measured using grating monochromator and glowbar source with lock-in detection. A 45° facet was polished at one end of the device to couple the IR

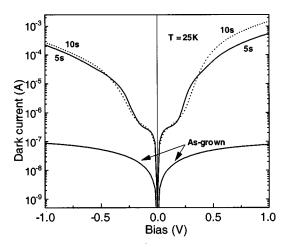


FIG. 7. I-V curve of the as-grown and annealed samples at $T=25~\mathrm{K}$ as a function of bias.

radiation into the detector structures.²⁷ A polarizer was inserted in front of the glowbar source in order to study the polarization dependence of the photoresponse. Figure 8 shows the response spectra for 0° and 90° polarizations as a function of wavelength at 25 K. The responsivity peaks are redshifted in both spectra, independent of polarization, with respect to the as-grown spectrum. Note in the as-grown spectra that a few satellite peaks appear at rather identical wavelength positions in both as-grown spectra. Since there is only one bound state in the well and the excited state is above the barrier in the continuum, these satellite peaks are most probably due to the intersubband transition from E_1 to other excited states in the continuum²⁸ or to the interaction between E_2 and other states in the continuum.²⁹ However, all these peaks are subdued, as shown in Fig. 8, except for the designed transition peaks that appear in the annealed spectra following RTA. We attribute this to the intermixing induced modification of the QW subband energy states both in the well and the continuum.

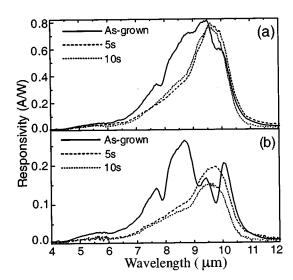


FIG. 8. Photoresponse spectra at 25 K of the as-grown, 5 and 10 s annealed samples bias at 2.5, 1.05, and 1.65 V for (a) 0° polarization and (b) 90° polarization, as a function of wavelength.

Figure 8(a) shows the measurement results for 0° polarized responsivity at T = 25 K. The responsivity amplitudes are 0.8, 0.79, and 0.77 A/W, respectively, for the as-grown (0 s) and annealed $(t_A=5 \text{ and } 10 \text{ s})$ detectors. The three spectra are of comparable magnitude except that the FWHM of the annealed spectra is smaller than the as-grown spectrum, as intersubband transitions to other continuum states are no longer prominent in the annealed spectra. Note that all the spectra have almost identical rising edge. This is as expected since the MQW properties and its structure have not been substantially modified or deteriorated after interdiffusion. The extent of intermixing may not have lowered the barrier height considerably such that those carriers being photoexcited to the extended state above the barrier "see" approximately the same height and are ready to be collected as photocurrent. It is known that the discrepancy of peak position between absorption and responsivity spectra is either due to the increase of barrier height when the temperature is lowered³⁰ or the applied electric field.³¹ However, unlike the annealed absorption spectra, the peak positions of the annealed photoresponse do not differ significantly at both polarizations. This phenomenon is probably due to the results of different extents of intermixing on the band structure, polarization effect, low temperature influence, and difference in applied bias. Further work is required to clarify this phenomenon. As the polarization angle is rotated from 0° to 90°, four pronounced response peaks are observed in the as-grown spectrum of Fig. 8(b). It is also interesting to note that, in contrast to 0° polarization, the continuum resonances are more dominant in the as-grown spectrum with the dominant peak response occurring at a shorter but not the designed wavelength. Each individual photoresponse spectrum exhibits a different cutoff wavelength under normal incidence illumination, as illustrated in Fig. 8(b). However, this phenomenon is not obvious in the annealed spectra where the photoresponse peak redshifts and locates at a wavelength position similar to that at 0° polarization. Note also that the responsivity of the $t_A = 5$ s sample has a larger amplitude than the as-grown and $t_A = 10 \,\mathrm{s}$ samples in the wavelength range of interest between 9 and 10 μ m.

The bias dependence of the responsivity at 0° polarization for both polarities is shown in Fig. 9. Interestingly, the photoresponse also shows a pronounced asymmetry similar to the I-V characteristic, i.e., the as-grown device has larger responsivity at negative bias while the annealed responsivities have larger magnitude at positive bias, with respect to the reversal of polarity. This indicates that both the photoexcited and nonphotoexcited carriers have similar escape direction under bias and that the transport characteristic is modified after interdiffusion. Since interdiffusion will introduce vacancies and dopand (Si), which act as a kind of defect, into both the barrier and the well, when an electric field is applied to collect the photoexcited carriers, some of the carriers may be trapped by this kind of defect. This may have resulted in the poorer collect efficiency of the interdiffused QWIP and, therefore, lower responsivity under different biases. The responsivity versus bias is quite linear for the three responses, which is an indication of another typical behavior for a bound-to-continuum QWIP. 32 This is because no tunneling is

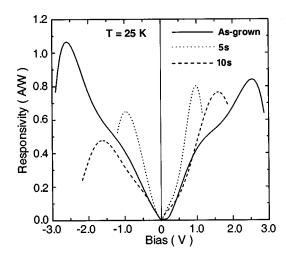


FIG. 9. Bias dependent responsivity of as-grown (solid line), 5 s annealed (dotted line), and 10 s annealed (dash line) samples as a function of bias at 0° polarization.

required and the photoexcited carriers that transport above the barrier have a relatively high mobility. The annealed responsivities increase with bias and reach a maximum at bias smaller than the as-grown device (the 5 s annealed response saturates and decreases at the lowest bias for both polarities), after which they strongly decrease with bias. Since the band structure is modified after intermixing, this is most probably due to the intervalley scattering 33 where the electrons in the Γ valley scatter into the L or X valley minima under an applied electric field, as a result of interdiffusion.

V. CONCLUSION

In conclusion, high In composition pseudomorphic interdiffused InGaAs/GaAs QWIP using dopant-enhanced interdiffusion has been demonstrated for its post-growth tunability. PL measurement results show that no strain relaxation or deterioration in structure quality is observed in the highly strained MQW heterostructure at 850 °C. The TE polarization IR intersubband transition, as a result of the bandmixing effects, is preserved, indicating that interdiffusion preserves the intrinsic optical characteristic of the QWIP material. With the modification of subband structure after RTA, both 0° and 90° polarizations annealed absorption peaks are redshifted with respect to the as-grown sample without much degradation in absorption strength. Photoresponse peaks due to resonances in the continuum states are subdued after interdiffusion. The annealed photoresponse spectra for 0° polarization are comparable to the as-grown device with a narrower FWHM, while the designed photoresponse peak becomes dominant at 90° polarization following RTA. The I-V characteristic of the annealed devices is about an order higher in amplitude than the as-grown one at 77 K due to the defect-assisted tunneling and is less sensitive to the variation in temperature range from 25 to 90 K. We believe the annealed leakage current can be lowered by optimizing the QWIP structure, such as with thinker barrier, to impede the tunneling mechanism. Thus, interdiffusion is shown to be a useful tool for its ability to fine tune the various aspects of photodetector's performance for grating-free normal incident broadband and multicolor IR applications.

ACKNOWLEDGMENTS

This work is supported in part by the CRCG grant of the University of Hong Kong, Research Grant Council—Earmarked Grants of Hong Kong, and National Science and Technology Board under Grant No. GR 6471. The authors would like to thank Prof. S. J. Chua for valuable suggestions, T. Mei, and Dr. S. J. Xu for technical assistance.

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