Exercise 23.4.1(*)

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$$\frac{X_1 \vdash double : \forall X_2. \ (X_2 \rightarrow X_2) \rightarrow X_2 \rightarrow X_2}{X_1 \vdash double \ [X_1 \rightarrow X_1] : T_2 \rightarrow T_1} \text{ T-TAPP} \qquad \frac{X_1 \vdash double : \forall X_3. \ (X_3 \rightarrow X_3) \rightarrow X_3 \rightarrow X_3}{X_1 \vdash double \ [X_1] : T_2} \text{ T-TAPP} \\ \frac{X_1 \vdash double \ [X_1 \rightarrow X_1] \ (double \ [X_1]) : T_1}{\vdash \lambda X_1. \ double \ [X_1 \rightarrow X_1] \ (double \ [X_1]) : \forall X_1. \ T_1} \text{ T-TABS}}$$

$$\frac{X_1 \vdash double : \forall X_2. \ (X_2 \rightarrow X_2) \rightarrow X_2 \rightarrow X_2}{X_1 \vdash double \ [X_1 \rightarrow X_1] : [X_2 \mapsto X_1 \rightarrow X_1] : ((X_2 \rightarrow X_2) \rightarrow X_2 \rightarrow X_2)} \text{ T-TAPP} \\ \frac{X_1 \vdash double \ [X_1 \rightarrow X_1] : [X_2 \mapsto X_1 \rightarrow X_1] : ((X_2 \rightarrow X_2) \rightarrow X_2 \rightarrow X_2)}{X_1 \vdash double \ [X_1 \rightarrow X_1] : ((X_1 \rightarrow X_1) \rightarrow X_1 \rightarrow X_1) \rightarrow ((X_1 \rightarrow X_1) \rightarrow X_1 \rightarrow X_1)} \text{ substitution} \\ \frac{X_1 \vdash double \ [X_1] : [X_3 \rightarrow X_1] : ((X_3 \rightarrow X_3) \rightarrow X_3 \rightarrow X_3)}{X_1 \vdash double \ [X_1] : (X_1 \rightarrow X_1) \rightarrow X_1 \rightarrow X_1} \\ \frac{X_1 \vdash double \ [X_1 \rightarrow X_1] : ((X_1 \rightarrow X_1) \rightarrow ((X_1 \rightarrow X_1) \rightarrow X_1 \rightarrow X_1)}{X_1 \vdash double \ [X_1 \rightarrow X_1] : ((X_1 \rightarrow X_1) \rightarrow ((X_1 \rightarrow X_1) \rightarrow X_1 \rightarrow X_1)} \\ \frac{X_1 \vdash double \ [X_1 \rightarrow X_1] : ((X_1 \rightarrow X_1) \rightarrow ((X_1 \rightarrow X_1) \rightarrow ((X_1 \rightarrow X_1) \rightarrow X_1 \rightarrow X_1) \rightarrow ((X_1 \rightarrow$$