

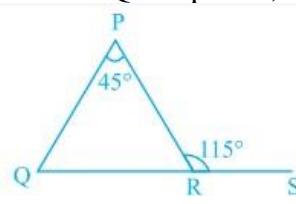


GRADE: IX CBSE
SUBJECT: MATHEMATICS

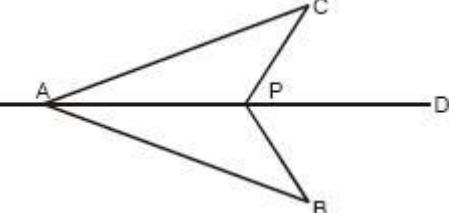
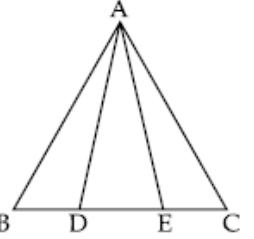
TOPIC: Triangles

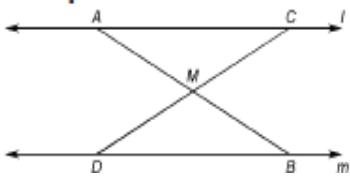
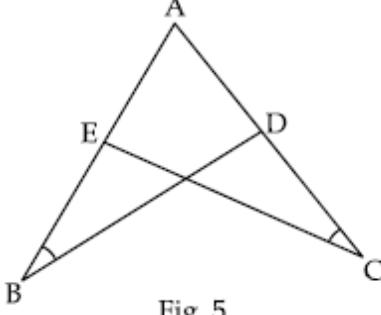
I. MCQ's

1	Which of the following is not a criterion for congruence of triangles? (A) SAS (B) ASA (C) SSA (D) SSS	(C)
2	If $AB = QR$, $BC = PR$ and $CA = PQ$, then (A) $\triangle ABC \cong \triangle PQR$ (B) $\triangle CBA \cong \triangle PRQ$ (C) $\triangle BAC \cong \triangle RPQ$ (D) $\triangle PQR \cong \triangle BCA$	(B)
3	In $\triangle ABC$, $AB = AC$ and $\angle B = 50^\circ$. Then $\angle C$ is equal to (A) 40° (B) 50° (C) 80° (D) 130°	(B)
4	In $\triangle ABC$, $BC = AB$ and $\angle B = 80^\circ$. Then $\angle A$ is equal to (A) 80° (B) 40° (C) 50° (D) 100°	(C)
5	In $\triangle PQR$, $\angle R = \angle P$ and $QR = 4$ cm and $PR = 5$ cm. Then the length of PQ is (A) 4 cm (B) 5 cm (C) 2 cm (D) 2.5 cm	(A)
6	It is given that $\triangle ABC \cong \triangle FDE$ and $AB = 5$ cm, $\angle B = 40^\circ$ and $\angle A = 80^\circ$. Then which of the following is true? (A) $DF = 5$ cm, $\angle F = 60^\circ$ (B) $DF = 5$ cm, $\angle E = 60^\circ$ (C) $DE = 5$ cm, $\angle E = 60^\circ$ (D) $DE = 5$ cm, $\angle D = 40^\circ$	(B)
7	In triangles ABC and PQR, $AB = AC$, $\angle C = \angle P$ and $\angle B = \angle Q$. The two triangles are (A) isosceles but not congruent (B) isosceles and congruent (C) congruent but not isosceles (D) neither congruent nor isosceles	(A)
8	In triangles ABC and DEF, $AB = FD$ and $\angle A = \angle D$. The two triangles will be congruent by SAS axiom if (A) $BC = EF$ (B) $AC = DE$ (C) $AC = EF$ (D) $BC = DE$	(B)
9	Side QR of a $\triangle PQR$ has been produced to the point S. If $\angle PRS = 115^\circ$ and $\angle P = 45^\circ$, then $\angle Q$ is equal to, (a) 70° (b) 105° (c) 51° (d) 80°	(a)



II. Solve as directed

1	Prove that angles opposite to equal sides of an isosceles triangle are equal.	
2	In the given figure, AD is bisector of $\angle BAC$ and $\angle CPD = \angle BPD$. Prove that $\triangle CAP \cong \triangle BAP$.	
3	In $\triangle ABC$, BD and CE are two altitudes such that $BD = CE$. Prove that $\triangle ABC$ is isosceles.	
4	In the fig. 10, D and E are points on the base BC of a $\triangle ABC$ such that $AD = AE$ and $\angle BAD = \angle CAE$. Prove that $AB = AC$.	
5	The exterior angles, obtained on producing the base of a triangle both way are 104° and 136° . Find all the angles of the triangle.	$\angle ACB = 76^\circ$, $\angle BAC$

		$= 60^\circ$, $\angle AB$ $C =$ 44°
6	<p>In the figure, if m and M is the mid-point of AB. Prove that M is also the mid-point of CD.</p> 	
III. Solve the following		
1	In a triangle ABC, E and F respectively are mid-points of equal sides AB and AC of $\triangle ABC$. Show that $BF = CE$.	
2	AD is an altitude of an isosceles $\triangle ABC$ in which $AB = AC$. Show that AD bisects BC.	
3	AD is an altitude of an isosceles triangle ABC in which $AB = AC$. Show that AD is also the median of the triangle.	
4	In fig. 5, If $\angle ABD = \angle ACE$ and $AB = AC$. Prove that $\triangle ABD \cong \triangle ACE$.	
	 <p>Fig. 5</p>	

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In figure 6, $\triangle LMN$ is an isosceles triangle with $LM = LN$, and LP bisects $\angle NLQ$. Prove that $LP \parallel MN$.

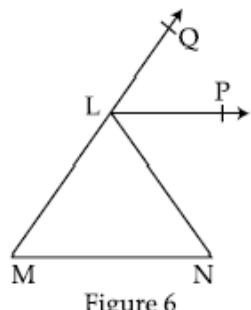


Figure 6

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In the fig. 9, the sides AB and AC of $\triangle ABC$ are produced to points E and D respectively. If bisectors BO and CO of $\angle CBE$ and $\angle BCD$ respectively meet at point O , then prove that

$$\angle BOC = 90^\circ - \frac{1}{2} \angle BAC.$$

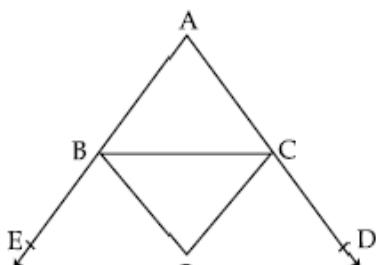
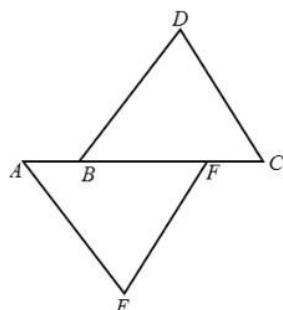


Fig. 9

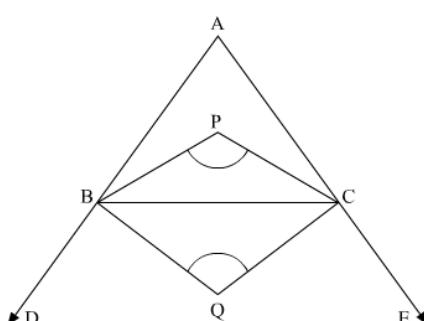
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In Fig. it is given that $AB = CF$, $EF = BD$ and $\angle AFE = \angle DBC$. Prove that $\triangle AFE \cong \triangle CBD$.

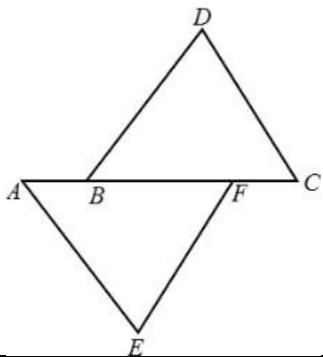


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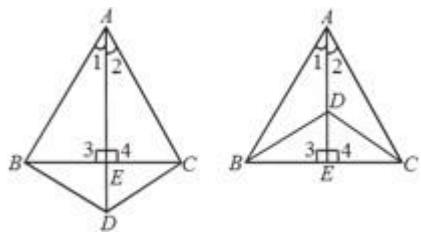
In a $\triangle ABC$, the internal bisectors of $\angle B$ and $\angle C$ meet at P and the external bisectors of $\angle B$ and $\angle C$ meet at Q . Prove that $\angle BPC + \angle BQC = 180^\circ$.



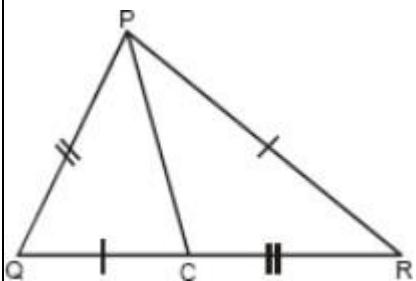
- 9** In Fig. it is given that $AB = CF$, $EF = BD$ and $\angle AFE = \angle DBC$. Prove that $\triangle AFE \cong \triangle CBD$.



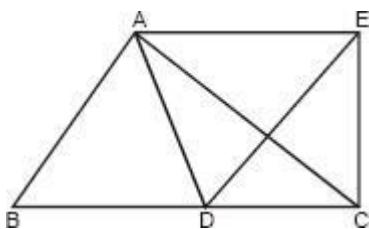
- 10** If two isosceles triangles have a common base, the line joining their vertices bisects them at right angles.



- 11** In the given figure, triangles PQC and PRC are such that $QC = PR$ and $PQ = CR$.
Prove that $\angle PCQ = \angle CPR$.



- 12** In the given figure, $AB = AD$, $AC = AE$ and $\angle BAD = \angle EAC$, then prove that $BC = DE$.



- 13** In Figure 11, $ABCD$ is a square and $\triangle DEC$ is an equilateral triangle. Prove that :

(i) $\triangle ADE \cong \triangle BCE$ (ii) $AE = BE$ (iii) $\angle DAE = 15^\circ$

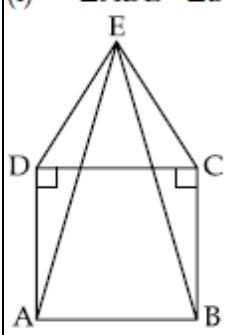


Figure 11

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In figure 10, if $AB = AC$ and $DB = DC$ then prove that $\angle ABD = \angle ACD$.

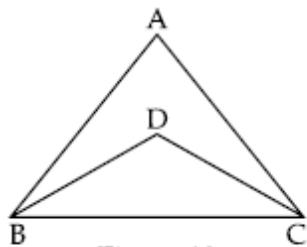


Figure 10

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In figure 11, PQRS is a square and SRT is an equilateral triangle. Prove that :

- (i) $\angle PST = \angle QRT$
- (ii) $PT = QT$
- (iii) $\angle QTR = 15^\circ$

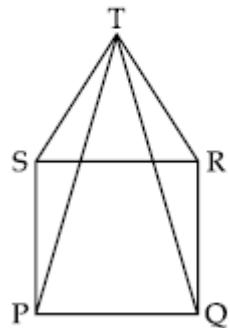


Figure 11

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In figure 9, ABC is a triangle with $\angle BAC = 90^\circ$ and $AL \perp BC$. Prove that $\angle CAL = \angle ABC$.

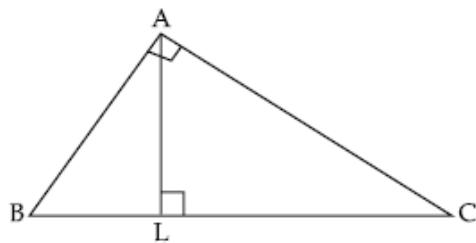


Figure 9
