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## Tables and Figures

### - Frequency Table

Previous Ownership	Frequency	Relative Frequency
None	85	$\frac{85}{500} = 0.17$
Windows	60	$\frac{60}{500} = 0.12$
Macintosh	355	$\frac{355}{500} = 0.71$
Total	500	$\frac{500}{500} = 1$

### - Stem and Leaf

3 2337 2 001112223889 1 2244456888899 0 69
-----------------------------------------------------

3 7 3 233 2 889 2 001112223 1 56888899 1 22444 0 69
-----------------------------------------------------------------------

11	4	
	3	7
332	3	233
8865	2	889
44331110	2	001112223
987776665	1	56888899
321	1	22444
7	0	69

# Formulas

## 1. Box and Plot

Name	Formula
25th Quartile / Lower Hinge	$\frac{(n+1)}{4}$ th term
50th Quartile / Median	When n is odd: $\frac{(n+1)}{2}$ th term  When n is even: $\frac{(\frac{n}{2})th\ term + ((\frac{n}{2})+1)th\ term}{2}$
75th Quartile / Upper Hinge	$\frac{3(n+1)}{4}$ th term
IQR / H-spread	Upper Hinge - Lower Hinge
Step	$1.5 \times HSpread$
Upper Inner Fence	Upper Hinge + 1 Step
Lower Inner Fence	Lower Hinge - 1 Step
Upper Outer Fence	Upper Hinge + 2 Step
Lower Outer Fence	Lower Hinge - 2 Step
Upper Adjacent	Largest value below Upper Inner Fence
Lower Adjacent	Smallest value below Lower Inner Fence
Outlier	Values beyond Upper and Inner Fence
Extreme outlier	Values beyond Upper and Outer Fence

Outside Value	A value beyond an Inner fence but not beyond an Outer Fence
Far Out Value	A value beyond an Outer Fence

## 2. Trimean

$$- \text{Trimean} = \frac{Q_1 + 2Q_2 + Q_3}{4}$$

## 3. Geometric Mean

$$- \bar{x}_{geom} = \sqrt[n]{x_1 \times x_2 \times \dots \times x_n}$$

## 4. Trimmed Mean

- Remove the values in the bottom X% and top X% of the dataset. Then, calculate the mean of the remaining values.

## 5. Pearson's correlation

$$○ r = \frac{\Sigma xy}{\sqrt{\Sigma x^2 \Sigma y^2}}, \text{ where } x \text{ is } X - \bar{X} \text{ and } y \text{ is } Y - \bar{Y}$$

## 6. Probability of a Single Event

$$○ \text{probability} = \frac{\text{possible outcomes}}{\text{total outcomes}}$$

## 7. Probability of 2 or more independent events

$$○ P(A \text{ and } B) = P(A) \times P(B)$$

## 8. Probability of 2 or more dependent events

- $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$
- It covers 3 possibilities:
  - 1) A occurs and B doesn't occur
  - 2) B occurs and A doesn't occur
  - 3) Both A and B occur

## 9. Permutations

- Used when the order matters
- ${}_nP_r = \frac{n!}{(n-r)!}$

## 10. Combinations

- Used when the order doesn't matter
- ${}_nC_r = \frac{n!}{r!(n-r)!}$

## 11. Binomial Distribution

- $P(x) = \frac{N!}{x!(N-x)!} \pi^x (1 - \pi)^{N-x}$
- $N$  = number of trials
- $x$  = number of successes
- $\pi$  = probability of success
- $mean = N \times \pi$
- $\sigma^2 = N\pi(1 - \pi) \rightarrow$  variance

## 12. Poisson Distribution

- A discrete (countable) probability distribution, used to predict the number of times an event occurs.
- $p = \frac{e^{-\mu} \mu^x}{x!}$

# Step-by-Step Tutorials

Reminder: Critical Values and p-values are different variables.

1. Critical Values are obtained from the distribution tables for certain tests:
  - t-table ([one-tailed](#) / [two tailed](#))
    - One-tailed t-table critical values only cover left side, so if hypothesis asks for something increasing/involves using  $\geq$ , then it's  $1 - P(X)$
    - Two-tailed critical value is  $\pm$ , reject null hypothesis if t-value is within the crit value
  - z-table ([negative](#) / [positive](#))
    - Left side describes the first two parts of the decimal of your calculated Z value.
    - Top side describes the hundredths place of your Z value.
  - f-table (  $\alpha =$  [0.10](#) / [0.05](#) / [0.01](#) )
2. P-values are more of the probability, which you need to use a calculator to get. Usually, the p-value you can get from the calculated statistic and degree of freedom. After getting the p-value, compare it with the significance level which is the  **$\alpha$** .

## - One Way ANOVA - Independent Measures

$N$  = Total no. of ppl/objects in the experiment

$n$  = No. of ppl/objects per group

$a$  = No. of experimental groups/conditions

$\mu$  = Sample mean

$SS$  = Sum of Squares

1. State Null and Alternate Hypothesis
  - $H_0 = \mu_1 = \mu_2 = \dots = \mu_n$ .
  - $H_1$  = Not all  $\mu$ 's are the same.
2. Find degrees of freedom
  - $df_{\text{between}} = a - 1$  (df numerator)
  - $df_{\text{within}} = N - a$  (df denominator)
  - $df_{\text{total}} = N - 1$

3. Find critical value with the 2 df's calculated.

- [Calculator](#) / [Table](#)

4. Calculate F-Statistic Value:

- $SS_{\text{between}} = \frac{\Sigma(\Sigma a_i)^2}{n} - \frac{T^2}{N}$  where:

- i.  $\Sigma(\Sigma a_i)^2$  is the sum of squared sums of all groups.  $[(\Sigma A)^2 + (\Sigma B)^2 + \dots + (\Sigma Z)^2]$

- Find total for Group A and square it, find total for Group B and square it, and so on for all groups.

- ii.  $T^2$  is the sum of all elements and then squared  $[(\Sigma A) + (\Sigma B) + \dots + (\Sigma Z)]^2$

- Add all elements together, then square it.

**OR USE THIS:**

Stupid Language Formula:

- $SS_{\text{between}} = n [(\text{mean of every group} - \text{grand mean})^2 + \dots + (\text{mean of every group} - \text{grand mean})^2]$

- $SS_{\text{within}} = \Sigma Y^2 - \frac{\Sigma(\Sigma a_i)^2}{n}$  where:

- i.  $\Sigma Y^2$  is the sum of each value squared  $[a^2 + b^2 + c^2 + \dots + z^2]$

**OR USE THIS:**

Stupid Language Formula:

- Calculate for every group:

- $SS_{\text{within}} (\text{group A}) = (\text{every value in group A} - \text{mean of group A})^2 + \dots + (\text{every value in group A} - \text{mean of group A})^2$

- $SS_{\text{within}} (\text{group B}) = (\text{every value in group B} - \text{mean of group B})^2 + \dots + (\text{every value in group B} - \text{mean of group B})^2$

- Continue for all groups

- $SS_{\text{within}} = \text{Sum of all } SS_{\text{within}} \text{ groups}$

- $SS_{\text{total}} = SS_{\text{between}} + SS_{\text{within}}$

5. Find Mean Squares:



- $MS_{\text{between}} = \frac{SS_{\text{between}}}{df_{\text{between}}}$
- $MS_{\text{within}} = \frac{SS_{\text{within}}}{df_{\text{within}}}$

6. Calculate F Statistic:

- $F = \frac{MS_{\text{between}}}{MS_{\text{within}}}$

7. Compare F with the Critical Value:

- If calculated F-statistic > critical value, reject the null hypothesis.
- If calculated p-value < significance level, reject null hypothesis

- **Two Way ANOVA**

N = Total no. of ppl/objects in the experiment

n = No. of ppl/objects per group

a = No. of experimental groups/conditions

$\mu$  = Sample mean

SS = Sum of Squares

p = number of categories in Group 1

q = number of categories in Group 2

1. State Null and Alternate Hypothesis:

- $H_0$  = Means across Group 1 is the same
- $H_0$  = Means across Group 2 is the same
- $H_0$  = There is no interaction between Group 1 and Group 2

2. Calculate:

- Grand Mean =  $\frac{\text{sum of all values}}{N}$
- Mean of Group 1
- Mean of Group 2
- Mean of every combination of every category for Group 1 and Group 2

3. Total:

- $SS_{\text{total}} = (\text{every value} - \text{grand mean})^2 + \dots + (\text{every value} - \text{grand mean})^2$
- $df_{\text{total}} = n \times p \times q - 1$
- Mean Squares  $_{\text{total}} = \frac{SS_{\text{total}}}{df_{\text{total}}}$

4. Between:

- $SS_{\text{between}} = n \times (\text{mean of every category} - \text{grand mean})^2 + \dots + (\text{mean of every category} - \text{grand mean})^2$
- $df_{\text{between}} = p \times q - 1$
- Mean Squares  $_{\text{between}} = \frac{SS_{\text{between}}}{df_{\text{between}}}$

5. Group 1:

- $SS_{\text{group 1}} = n \times q \times (\text{mean of every category for group 1} - \text{grand mean})^2 + \dots + (\text{mean of every category for group 1} - \text{grand mean})^2$

- $Df_{\text{group 1}} = p - 1$
- $\text{Mean Squares}_{\text{group 1}} = \frac{SS_{\text{group 1}}}{df_{\text{group 1}}}$

6. Group 2:

- $SS_{\text{group 2}} = n \times p \times (\text{mean of every category for group 2} - \text{grand mean})^2 + \dots + (\text{mean of every category for group 2} - \text{grand mean})^2$
- $Df_{\text{group 2}} = q - 1$
- $\text{Mean Squares}_{\text{group 2}} = \frac{SS_{\text{group 2}}}{df_{\text{group 2}}}$

7. Interaction:

- $SS_{\text{interaction}} = SS_{\text{between}} - SS_{\text{group 1}} - SS_{\text{group 2}}$
- $Df_{\text{interaction}} = (p - 1)(q - 1)$
- $\text{Mean Squares}_{\text{interaction}} = \frac{SS_{\text{interaction}}}{df_{\text{interaction}}}$

8. Error:

- $SS_{\text{error}} = n \times p \times (\text{every sample} - \text{the mean of its respective category})^2 + \dots + (\text{every sample} - \text{the mean of its respective category})^2$
- $Df_{\text{error}} = (n - 1) \times p \times q$
- $\text{Mean Squares}_{\text{error}} = \frac{SS_{\text{error}}}{df_{\text{error}}}$

9. F-Values:

- F Value Group 1:  $\frac{\text{Mean Square}_{\text{Group 1}}}{\text{Mean Square}_{\text{Error}}}$
- F Value Group 2:  $\frac{\text{Mean Square}_{\text{Group 2}}}{\text{Mean Square}_{\text{Error}}}$
- F Value Interaction:  $\frac{\text{Mean Square}_{\text{Interaction}}}{\text{Mean Square}_{\text{Error}}}$

10. Null Hypothesis:

- Pick either method depending on what ur told to do in the question
- P-Value Method
  - Input into P Value Calculator, find P value.
  - Input F-Value Group 1,  $Df_{\text{group 1}}$  (df numerator), and  $Df_{\text{error}}$  (df denominator)

- Continue for F values of Group 2 and Interaction (df denominator is  $Df_{\text{error}}$  for all)
- If value is less than the alpha given in question (in this case 0.05), reject null hypothesis.
- If any of the f values are greater than the null hypothesis, then fail to reject hypothesis.
- F-Critical Method
  - Find F-Critical Value with calculator.
  - Input alpha ( $\alpha$ ),  $Df_{\text{group 1}}$  (df numerator), and  $Df_{\text{error}}$  (df denominator)
  - Find F-Critical Value for Group 2 and Interaction as well.
  - If F value greater than F-Critical, reject null hypothesis. If smaller than, fail to reject null hypothesis.
- **Chi Square**
  - 1)  $H_0$  = The 2 groups are independent  
 $H_1$  = The 2 groups are not independent.
  - 2) Calculate expected Frequency Table:  

$$E_{ij} = \frac{\text{Row Total} \times \text{Column Total}}{\text{Grand Total}}$$
  - 3) Calculate the Chi-Square  
 For every cell:  

$$X = \frac{(\text{Original value} - \text{expected frequency})^2}{\text{expected frequency}}$$

$$X^2 = \text{Sum of all } X \text{ from all cells}$$
  - 4) Calculate Degree of Freedom  

$$df = (\text{no of rows} - 1) \times (\text{no of columns} - 1)$$
  - 5) Get the critical value from the table or get p value with calculator.
  - 6) Reject  $H_0$  if  $X^2 > \text{critical value}$ .  
 Reject  $H_0$  if p value < significance level.

<https://www.socscistatistics.com/tests/chisquare2/default2.aspx>

## Links

1. 5 Number Summary + IQR + Inner Outer Fence + Outliers + Geometric Mean + Sum of Squares + Standard Deviation (Sample/Population) + Variance Calculator:
  - <https://www.hackmath.net/en/calculator/five-number-summary>
2. Trimmed Mean Calculator:
  - [Trimmed Mean Calculator](#)
3. Permutation Combination Calculator:
  - <https://www.calculator.net/permutation-and-combination-calculator.html>
4. Binomial Distribution (Singular and Cumulative):
  - <https://stattrek.com/online-calculator/binomial>
5. Pearson's Correlation Coefficient:
  - <https://www.socscistatistics.com/tests/pearson/default2.aspx>
6. One Way ANOVA - Independent Measures
  - <https://www.socscistatistics.com/tests/anova/default2.aspx>
7. One WAY ANOVA - Repeated Measures
  - <https://www.socscistatistics.com/tests/anovarepeated/default.aspx>
8. Single Sample T-Test:
  - <https://www.socscistatistics.com/tests/tsinglesample/default.aspx>
9. Chi-Square Test:
  - <https://www.socscistatistics.com/tests/chisquare2/default2.aspx>
10. P Value from F-Statistic:
  - <https://www.socscistatistics.com/pvalues/fdistribution.aspx>
11. Critical Value for Multiple Tests:
  - <https://www.socscistatistics.com/tests/criticalvalues/default.aspx>
12. P Value Calculator and F Critical Table:
  - <https://datatab.net/tutorial/f-distribution>
13. Pearson Edexcel Formula Book, Statistics S1, S2 and S3 with complete Z table, Normal Distribution Table, and Statistical Formula(Page 14 - 23)
  - <https://qualifications.pearson.com/content/dam/pdf/International%20Advanced%20Level/Mathematics/2018/Specification-and-Sample-Assessment/IAL-Mathematics-Formula-Book.pdf>