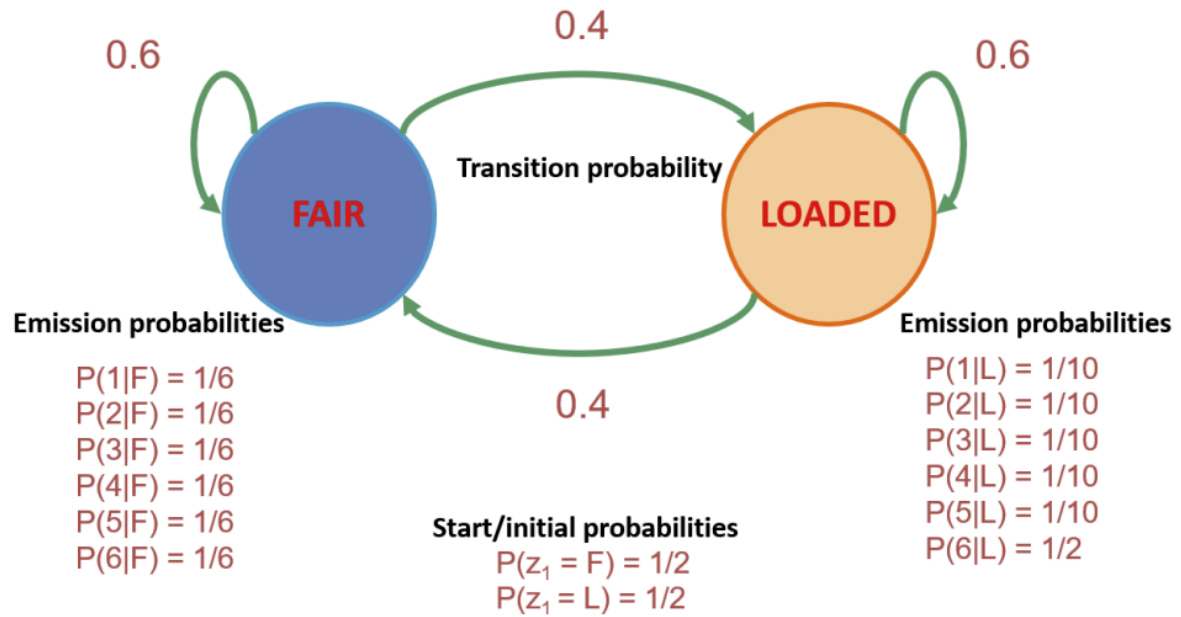


1 Calculate Joint Probabilities in HMM



$x = 6, 3, 1, 2, 4$

$z = \text{Load, Fair, Fair, Load, Load}$

$$P(x, z) = P(6|L) P(3|F) P(1|F) P(2|L) P(4|L) \\ \times \frac{1}{2} P(F|L) P(F|F) P(L|F) P(L|L)$$

$$P(x, z) = \frac{1}{2} \times \frac{1}{6} \times \frac{1}{6} \times \frac{1}{10} \times \frac{1}{10} \times$$


$$\frac{1}{2} \times 0.4 \times 0.6 \times 0.4 \times 0.6$$

$$\approx \frac{1}{250000} = 4 \times 10^{-6}$$

2 Viterbi algorithm

The V Matrix


	t = 1	t = 2	t = 3
k = 1 (Fair)	$\frac{1}{6} * \frac{1}{2} = \frac{1}{12}$	$\frac{1}{6} \max\left(0.6 \times \frac{1}{12}, 0.4 \times \frac{1}{20}\right) = \frac{1}{120}$	$\frac{1}{6} \max\left(0.6 \times \frac{1}{120}, 0.4 \times \frac{1}{60}\right) = \frac{1}{900}$
k = 2 (Loaded)	$\frac{1}{10} * \frac{1}{2} = \frac{1}{20}$	$\frac{1}{10} \max\left(0.4 \times \frac{1}{12}, 0.6 \times \frac{1}{20}\right) = \frac{1}{60}$	$\frac{1}{10} \max\left(0.4 \times \frac{1}{60}, 0.6 \times \frac{1}{60}\right) = \frac{1}{100}$



observation	"4"	"6"	"3"
-------------	-----	-----	-----

The Ptr Matrix

	t = 1	t = 2	t = 3
k = 1 (Fair)	0	$\arg \max\left(0.6 \times \frac{1}{12}, 0.4 \times \frac{1}{20}\right)$ $\arg \max\left(\frac{1}{20}, \frac{1}{50}\right) = 1$	$\arg \max\left(0.6 \times \frac{1}{120}, 0.4 \times \frac{1}{60}\right)$ $\arg \max\left(\frac{1}{200}, \frac{1}{150}\right) = 2$
k = 2 (Loaded)	0	$\arg \max\left(0.4 \times \frac{1}{12}, 0.6 \times \frac{1}{20}\right)$ $\arg \max\left(\frac{1}{30}, \frac{3}{100}\right) = 1$	$\arg \max\left(0.4 \times \frac{1}{60}, 0.6 \times \frac{1}{60}\right)$ $\arg \max\left(\frac{1}{300}, \frac{1}{100}\right) = 2$



observation	"4"	"6"	"3"
-------------	-----	-----	-----

$$P(x, z^*) = \max_k U_k(n) = \frac{1}{900}$$

$$z^* = \{ \text{fair}, \text{loaded}, \text{fair} \}$$

3 Feed Forward Neural Networks

These were the lines of code that were changed

```
function y = activation_tanh(alpha)
    %.
    y = tanh(alpha);
end
```

```
function gradient = activation_tanh_gradient(y)
    gradient = 1 - y.^2;
end
```

```
%% -----FORWARD PROPAGATION-----
X = X_batch; % dense1

layer1_alpha = weighted_sum(X, W1);
layer1_h = activation_tanh(layer1_alpha);

layer2_alpha = weighted_sum(layer1_h, W2);
layer2_h = activation_tanh(layer2_alpha);

output_layer_alpha = weighted_sum(layer2_h, W3);
output_layer = output_layer_alpha;

error = mean((output_layer-y_batch).^2);
```

```

% add some code below
% to calculate gradients of error w.r.t. alpha_2 (see defination of alpha_2 in the
layer2_alpha_gradient = layer2_h_gradient .* activation_tanh_gradient(layer2_h);

% calculate gradients w.r.t. W2 and h1 (see defination of W3 and h2 in the figure o
[W2_gradient, layer1_h_gradient] = compute_gradient_for_weights_and_one_layer_below

% add some code below
% to calculate gradients of error w.r.t. alpha_1 (see defination of alpha_1 in the
layer1_alpha_gradient = layer1_h_gradient .* activation_tanh_gradient(layer1_h);

```