

# Praktikum Pemodelan Statistika terapan

## Peramalan Deret Waktu

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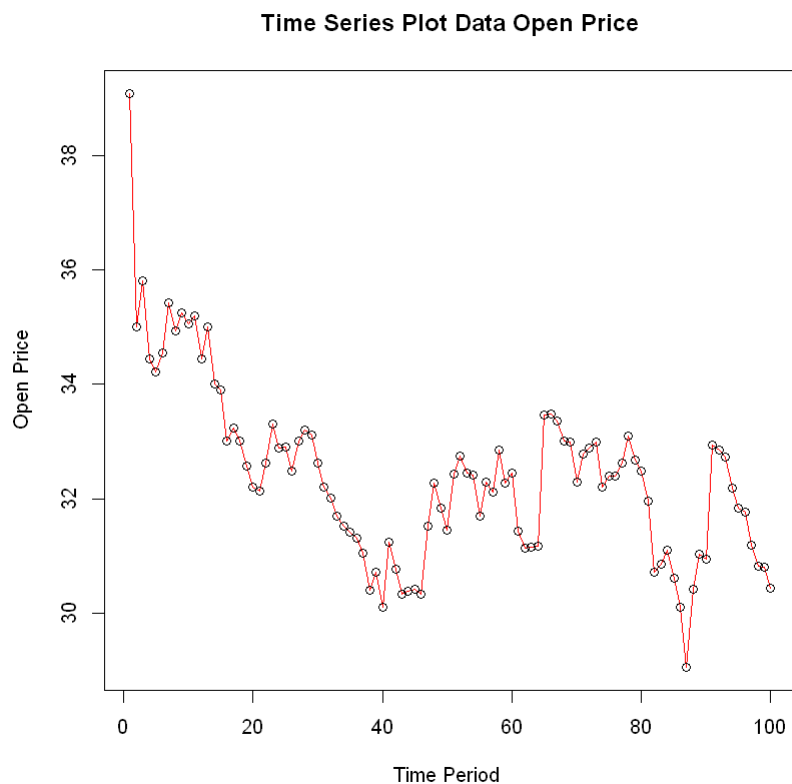
# Percobaan ke-1: Studi Kasus 1

```
In [ ]: library("forecast")  
library("TTR")
```

```
In [ ]: data = read.csv("AABA_06sd18.csv", header = TRUE)  
data.ts = data$Open[10:109]  
data.ts
```


39.09 · 35.01 · 35.82 · 34.44 · 34.22 · 34.55 · 35.43 · 34.94 · 35.26 · 35.06 · 35.2 · 34.45 · 35.01 ·  
34 · 33.9 · 33.01 · 33.24 · 33.01 · 32.58 · 32.21 · 32.14 · 32.62 · 33.3 · 32.88 · 32.9 · 32.49 · 33.01 ·  
33.2 · 33.11 · 32.63 · 32.21 · 32.01 · 31.7 · 31.53 · 31.42 · 31.31 · 31.05 · 30.4 · 30.72 · 30.1 ·  
31.25 · 30.77 · 30.34 · 30.38 · 30.42 · 30.33 · 31.52 · 32.28 · 31.84 · 31.45 · 32.44 · 32.75 · 32.45 ·  
32.41 · 31.69 · 32.3 · 32.12 · 32.85 · 32.28 · 32.45 · 31.44 · 31.14 · 31.16 · 31.17 · 33.47 · 33.48 ·  
33.36 · 33.01 · 32.99 · 32.3 · 32.79 · 32.88 · 32.99 · 32.2 · 32.4 · 32.4 · 32.63 · 33.09 · 32.68 ·  
32.48 · 31.96 · 30.71 · 30.85 · 31.1 · 30.61 · 30.1 · 29.05 · 30.42 · 31.04 · 30.95 · 32.94 · 32.86 ·  
32.73 · 32.19 · 31.83 · 31.77 · 31.19 · 30.83 · 30.8 · 30.43

```
In [ ]: ts.plot(data.ts, xlab="Time Period ", ylab="Open Price", main= "Time Series Plot  
points(data.ts)
```




```
In [ ]: data.sma = SMA(data.ts, n=4)  
data.sma
```

<NA> · <NA> · <NA> · 36.09 · 34.8725 · 34.7575 · 34.66 · 34.785 · 35.045 · 35.1725 · 35.115 · 34.9925 · 34.93 · 34.665 · 34.34 · 33.98 · 33.5375 · 33.29 · 32.96 · 32.76 · 32.485 · 32.3875 · 32.5675 · 32.735 · 32.925 · 32.8925 · 32.82 · 32.9 · 32.9525 · 32.9875 · 32.7875 · 32.49 · 32.1375 · 31.8625 · 31.665 · 31.49 · 31.3275 · 31.045 · 30.87 · 30.5675 · 30.6175 · 30.71 · 30.615 · 30.685 · 30.4775 · 30.3675 · 30.6625 · 31.1375 · 31.4925 · 31.7725 · 32.0025 · 32.12 · 32.2725 · 32.5125 · 32.325 · 32.2125 · 32.13 · 32.24 · 32.3875 · 32.425 · 32.255 · 31.8275 · 31.5475 · 31.2275 · 31.735 · 32.32 · 32.87 · 33.33 · 33.21 · 32.915 · 32.7725 · 32.74 · 32.74 · 32.715 · 32.6175 · 32.4975 · 32.4075 · 32.63 · 32.7 · 32.72 · 32.5525 · 31.9575 · 31.5 · 31.155 · 30.8175 · 30.665 · 30.215 · 30.045 · 30.1525 · 30.365 · 31.3375 · 31.9475 · 32.37 · 32.68 · 32.4025 · 32.13 · 31.745 · 31.405 · 31.1475 · 30.8125

 **Analisis :** menampilkan SMA(Simple moving Average) dengan rata-rata 4 jeda baris elemen secara berurutan.

```
In [ ]: data.peramalan = c(NA,data.sma)
data.peramalan
```

<NA> · <NA> · <NA> · <NA> · 36.09 · 34.8725 · 34.7575 · 34.66 · 34.785 · 35.045 · 35.1725 · 35.115 · 34.9925 · 34.93 · 34.665 · 34.34 · 33.98 · 33.5375 · 33.29 · 32.96 · 32.76 · 32.485 · 32.3875 · 32.5675 · 32.735 · 32.925 · 32.8925 · 32.82 · 32.9 · 32.9525 · 32.9875 · 32.7875 · 32.49 · 32.1375 · 31.8625 · 31.665 · 31.49 · 31.3275 · 31.045 · 30.87 · 30.5675 · 30.6175 · 30.71 · 30.615 · 30.685 · 30.4775 · 30.3675 · 30.6625 · 31.1375 · 31.4925 · 31.7725 · 32.0025 · 32.12 · 32.2725 · 32.5125 · 32.325 · 32.2125 · 32.13 · 32.24 · 32.3875 · 32.425 · 32.255 · 31.8275 · 31.5475 · 31.2275 · 31.735 · 32.32 · 32.87 · 33.33 · 33.21 · 32.915 · 32.7725 · 32.74 · 32.74 · 32.715 · 32.6175 · 32.4975 · 32.4075 · 32.63 · 32.7 · 32.72 · 32.5525 · 31.9575 · 31.5 · 31.155 · 30.8175 · 30.665 · 30.215 · 30.045 · 30.1525 · 30.365 · 31.3375 · 31.9475 · 32.37 · 32.68 · 32.4025 · 32.13 · 31.745 · 31.405 · 31.1475 · 30.8125

 **Analisis :** Kali ini untuk teknik time seriesnya menambahkan nilai NA untuk memperluas data deret waktu dengan nilai prediksi Simple moving average tadi.

```
In [ ]: dataku <- cbind(aktual=c(data.ts,rep(NA,5)),pemulusan=c(data.sma,rep(NA,5)) ,ram
dataku
```

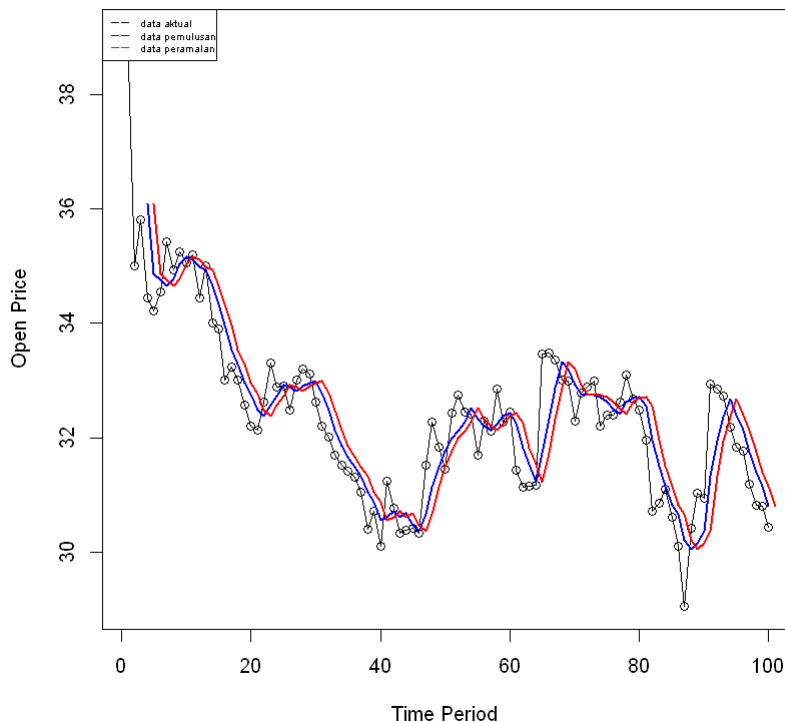
A matrix: 105 × 3 of type dbl


aktual	pemulusan	ramalan
39.09	NA	NA
35.01	NA	NA
35.82	NA	NA
34.44	36.0900	NA
34.22	34.8725	36.0900
34.55	34.7575	34.8725
35.43	34.6600	34.7575
34.94	34.7850	34.6600
35.26	35.0450	34.7850
35.06	35.1725	35.0450
35.20	35.1150	35.1725
34.45	34.9925	35.1150
35.01	34.9300	34.9925
34.00	34.6650	34.9300
33.90	34.3400	34.6650
33.01	33.9800	34.3400
33.24	33.5375	33.9800
33.01	33.2900	33.5375
32.58	32.9600	33.2900
32.21	32.7600	32.9600
32.14	32.4850	32.7600
32.62	32.3875	32.4850
33.30	32.5675	32.3875
32.88	32.7350	32.5675
32.90	32.9250	32.7350
32.49	32.8925	32.9250
33.01	32.8200	32.8925
33.20	32.9000	32.8200
33.11	32.9525	32.9000
32.63	32.9875	32.9525
⋮	⋮	⋮
32.40	32.4975	32.6175

aktual	pemulusan	ramalan
32.63	32.4075	32.4975
33.09	32.6300	32.4075
32.68	32.7000	32.6300
32.48	32.7200	32.7000
31.96	32.5525	32.7200
30.71	31.9575	32.5525
30.85	31.5000	31.9575
31.10	31.1550	31.5000
30.61	30.8175	31.1550
30.10	30.6650	30.8175
29.05	30.2150	30.6650
30.42	30.0450	30.2150
31.04	30.1525	30.0450
30.95	30.3650	30.1525
32.94	31.3375	30.3650
32.86	31.9475	31.3375
32.73	32.3700	31.9475
32.19	32.6800	32.3700
31.83	32.4025	32.6800
31.77	32.1300	32.4025
31.19	31.7450	32.1300
30.83	31.4050	31.7450
30.80	31.1475	31.4050
30.43	30.8125	31.1475
NA	NA	30.8125
NA	NA	30.8125
NA	NA	30.8125
NA	NA	30.8125
NA	NA	30.8125

```
In [ ]: ts.plot(data.ts, xlab="Time Period ", ylab="Open Price", main= "SMA N=4 Data Ope
points(data.ts)
lines(data.sma,col="blue",lwd=2)
lines(data.peramalan,col="red",lwd=2)
legend("topleft",c("data aktual","data pemulusan","data peramalan"), lty=5, col=
```

SMA N=4 Data Open Price



 **Analisis :** Dataset di atas merupakan hasil analisa dari peramalan deret waktu. Hasil plot di atas merupakan hasil visualisasi dari 3 data yaitu data aktual, data smoothing dan data forecasting yang ketiganya memiliki pergerakan yang hampir mirip

```
In [ ]: error=data.ts-data.peramalan[1:length(data.ts)]
SSE=sum(error[5:length(data.ts)]^2)
SSE
```


61.3459624999998

```
In [ ]: MSE=mean(error[5:length(data.ts)]^2)
MSE
```

0.639020442708332

```
In [ ]: MAPE=mean(abs((error[5:length(data.ts)]/data.ts[5:length(data.ts)])*100))
MAPE
```

1.94089892445136

 **Analisis :** Disini untuk 3 teknik yang dipakai untuk evaluasi model yaitu melakukan perhitungan error, MSE, dan MSE. Nilai-nilai tersebut menunjukkan bahwa model cukup akurat.

## Percobaan ke-2: Studi Kasus 2

```
In [ ]: AirPassengers
```

A Time Series: 12 × 12

	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
1949	112	118	132	129	121	135	148	148	136	119	104	118
1950	115	126	141	135	125	149	170	170	158	133	114	140
1951	145	150	178	163	172	178	199	199	184	162	146	166
1952	171	180	193	181	183	218	230	242	209	191	172	194
1953	196	196	236	235	229	243	264	272	237	211	180	201
1954	204	188	235	227	234	264	302	293	259	229	203	229
1955	242	233	267	269	270	315	364	347	312	274	237	278
1956	284	277	317	313	318	374	413	405	355	306	271	306
1957	315	301	356	348	355	422	465	467	404	347	305	336
1958	340	318	362	348	363	435	491	505	404	359	310	337
1959	360	342	406	396	420	472	548	559	463	407	362	405
1960	417	391	419	461	472	535	622	606	508	461	390	432

```
In [ ]: t=1:length(AirPassengers)
y=AirPassengers
trend_analysis = lm(y~t)
summary(trend_analysis)
```

Call:  
lm(formula = y ~ t)

Residuals:

Min	1Q	Median	3Q	Max
-93.858	-30.727	-5.757	24.489	164.999

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	87.65278	7.71635	11.36	<2e-16 ***
t	2.65718	0.09233	28.78	<2e-16 ***

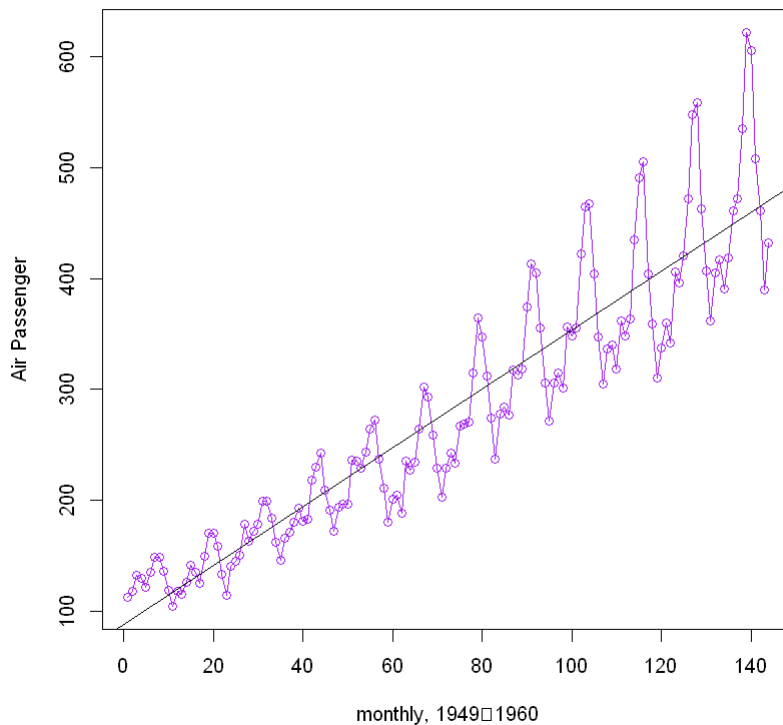
---


Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 46.06 on 142 degrees of freedom  
Multiple R-squared: 0.8536, Adjusted R-squared: 0.8526  
F-statistic: 828.2 on 1 and 142 DF, p-value: < 2.2e-16

```
In [ ]: plot(t,y,type="o", xlab="monthly, 1949-1960", ylab="Air Passenger",col="purple")
plot
abline(trend_analysis)
```

function (x, y, ...)  
UseMethod("plot")



 **Analisis :** Dataset AirPassengers berisi data jumlah penumpang pesawat internasional bulanan dari tahun 1949 hingga 1960. Berdasarkan summary trend analysis, dapat disimpulkan bahwa parameter intercept dan t signifikan secara statistik karena nilai p-value nya di bawah 0.05. Selain itu, nilai Multiple R-squared dan Adjusted R-squared cukup besar, yaitu masing-masing 0.8536 dan 0.8526, menunjukkan bahwa model memiliki kemampuan yang baik dalam menjelaskan variasi data. Plot yang dihasilkan menunjukkan garis trend positif tiap bulan hingga beberapa puluhan tahun ke depan.

## Percobaan ke-3: Studi Kasus 3

```
In [ ]: data_co2 = co2
        data_co2
```

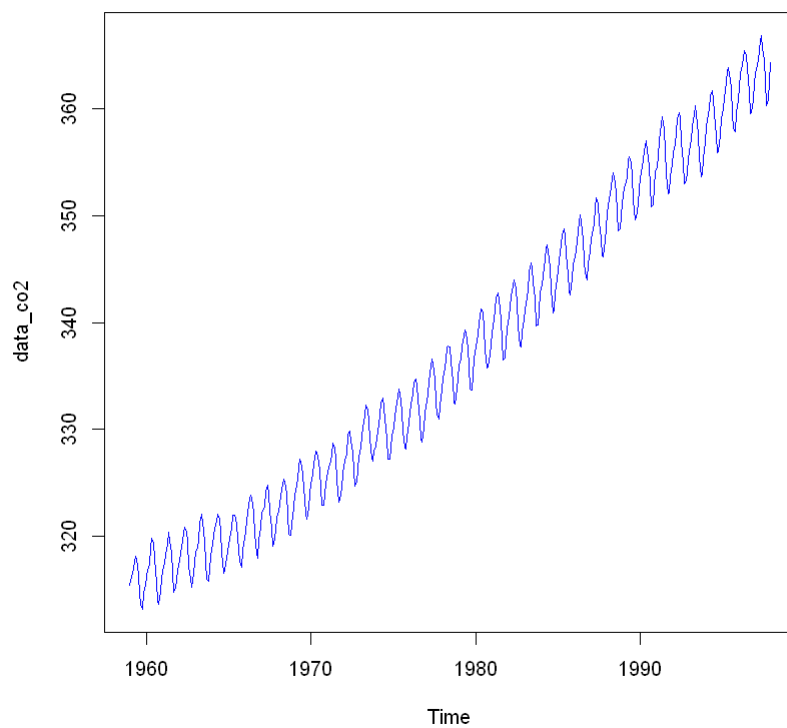


A Time Series: 39 × 12

	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	No
1959	315.42	316.31	316.50	317.56	318.13	318.00	316.39	314.65	313.68	313.18	314.6
1960	316.27	316.81	317.42	318.87	319.87	319.43	318.01	315.74	314.00	313.68	314.8
1961	316.73	317.54	318.38	319.31	320.42	319.61	318.42	316.63	314.83	315.16	315.9
1962	317.78	318.40	319.53	320.42	320.85	320.45	319.45	317.25	316.11	315.27	316.5
1963	318.58	318.92	319.70	321.22	322.08	321.31	319.58	317.61	316.05	315.83	316.9
1964	319.41	320.07	320.74	321.40	322.06	321.73	320.27	318.54	316.54	316.71	317.5
1965	319.27	320.28	320.73	321.97	322.00	321.71	321.05	318.71	317.66	317.14	318.7
1966	320.46	321.43	322.23	323.54	323.91	323.59	322.24	320.20	318.48	317.94	319.6
1967	322.17	322.34	322.88	324.25	324.83	323.93	322.38	320.76	319.10	319.24	320.5
1968	322.40	322.99	323.73	324.86	325.40	325.20	323.98	321.95	320.18	320.09	321.1
1969	323.83	324.26	325.47	326.50	327.21	326.54	325.72	323.50	322.22	321.62	322.6
1970	324.89	325.82	326.77	327.97	327.91	327.50	326.18	324.53	322.93	322.90	323.8
1971	326.01	326.51	327.01	327.62	328.76	328.40	327.20	325.27	323.20	323.40	324.6
1972	326.60	327.47	327.58	329.56	329.90	328.92	327.88	326.16	324.68	325.04	326.3
1973	328.37	329.40	330.14	331.33	332.31	331.90	330.70	329.15	327.35	327.02	327.9
1974	329.18	330.55	331.32	332.48	332.92	332.08	331.01	329.23	327.27	327.21	328.2
1975	330.23	331.25	331.87	333.14	333.80	333.43	331.73	329.90	328.40	328.17	329.3
1976	331.58	332.39	333.33	334.41	334.71	334.17	332.89	330.77	329.14	328.78	330.1
1977	332.75	333.24	334.53	335.90	336.57	336.10	334.76	332.59	331.42	330.98	332.2
1978	334.80	335.22	336.47	337.59	337.84	337.72	336.37	334.51	332.60	332.38	333.7
1979	336.05	336.59	337.79	338.71	339.30	339.12	337.56	335.92	333.75	333.70	335.1
1980	337.84	338.19	339.91	340.60	341.29	341.00	339.39	337.43	335.72	335.84	336.9
1981	339.06	340.30	341.21	342.33	342.74	342.08	340.32	338.26	336.52	336.68	338.1
1982	340.57	341.44	342.53	343.39	343.96	343.18	341.88	339.65	337.81	337.69	339.0
1983	341.20	342.35	342.93	344.77	345.58	345.14	343.81	342.21	339.69	339.82	340.9
1984	343.52	344.33	345.11	346.88	347.25	346.62	345.22	343.11	340.90	341.18	342.8
1985	344.79	345.82	347.25	348.17	348.74	348.07	346.38	344.51	342.92	342.62	344.0
1986	346.11	346.78	347.68	349.37	350.03	349.37	347.76	345.73	344.68	343.99	345.4
1987	347.84	348.29	349.23	350.80	351.66	351.07	349.33	347.92	346.27	346.18	347.6
1988	350.25	351.54	352.05	353.41	354.04	353.62	352.22	350.27	348.55	348.72	349.9
1989	352.60	352.92	353.53	355.26	355.52	354.97	353.75	351.52	349.64	349.83	351.1
1990	353.50	354.55	355.23	356.04	357.00	356.07	354.67	352.76	350.82	351.04	352.6

	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	No
<b>1991</b>	354.59	355.63	357.03	358.48	359.22	358.12	356.06	353.92	352.05	352.11	353.6
<b>1992</b>	355.88	356.63	357.72	359.07	359.58	359.17	356.94	354.92	352.94	353.23	354.0
<b>1993</b>	356.63	357.10	358.32	359.41	360.23	359.55	357.53	355.48	353.67	353.95	355.3
<b>1994</b>	358.34	358.89	359.95	361.25	361.67	360.94	359.55	357.49	355.84	356.00	357.5
<b>1995</b>	359.98	361.03	361.66	363.48	363.82	363.30	361.94	359.50	358.11	357.80	359.6
<b>1996</b>	362.09	363.29	364.06	364.76	365.45	365.01	363.70	361.54	359.51	359.65	360.8
<b>1997</b>	363.23	364.06	364.61	366.40	366.84	365.68	364.52	362.57	360.24	360.83	362.4

```
In [ ]: plot(data_co2, col = "blue")
```



```
In [ ]: model <- HoltWinters(data_co2)
model
```

Holt-Winters exponential smoothing with trend and additive seasonal component.

Call:

```
HoltWinters(x = data_co2)
```

Smoothing parameters:

```
alpha: 0.5126484  
beta : 0.009497669  
gamma: 0.4728868
```

Coefficients:

```
      [,1]  
a  364.7616237  
b    0.1247438  
s1   0.2215275  
s2   0.9552801  
s3   1.5984744  
s4   2.8758029  
s5   3.2820088  
s6   2.4406990  
s7   0.8969433  
s8  -1.3796428  
s9  -3.4112376  
s10 -3.2570163  
s11 -1.9134850  
s12 -0.5844250
```

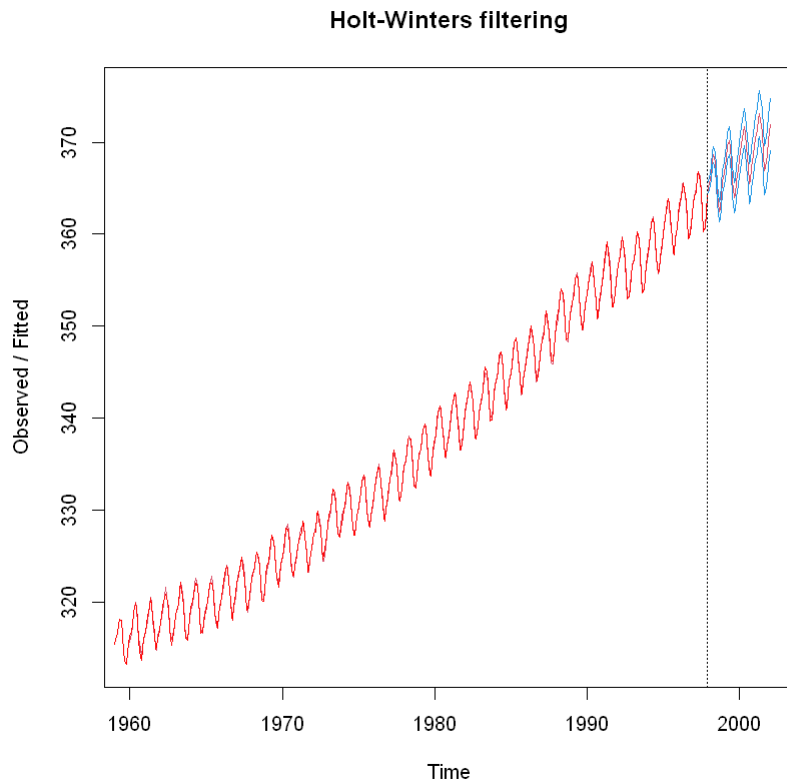
```
In [ ]: fore <- predict(model, 50, prediction.interval = TRUE)  
fore
```


A Time Series: 50 × 3

	<b>fit</b>	<b>upr</b>	<b>lwr</b>
<b>Jan 1998</b>	365.1079	365.7105	364.5053
<b>Feb 1998</b>	365.9664	366.6449	365.2879
<b>Mar 1998</b>	366.7343	367.4823	365.9864
<b>Apr 1998</b>	368.1364	368.9490	367.3238
<b>May 1998</b>	368.6674	369.5410	367.7937
<b>Jun 1998</b>	367.9508	368.8824	367.0192
<b>Jul 1998</b>	366.5318	367.5189	365.5446
<b>Aug 1998</b>	364.3799	365.4206	363.3392
<b>Sep 1998</b>	362.4731	363.5656	361.3806
<b>Oct 1998</b>	362.7520	363.8948	361.6093
<b>Nov 1998</b>	364.2203	365.4121	363.0285
<b>Dec 1998</b>	365.6741	366.9138	364.4345
<b>Jan 1999</b>	366.6048	367.9353	365.2744
<b>Feb 1999</b>	367.4633	368.8383	366.0884
<b>Mar 1999</b>	368.2313	369.6500	366.8125
<b>Apr 1999</b>	369.6333	371.0954	368.1713
<b>May 1999</b>	370.1643	371.6690	368.6596
<b>Jun 1999</b>	369.4477	370.9946	367.9008
<b>Jul 1999</b>	368.0287	369.6173	366.4401
<b>Aug 1999</b>	365.8769	367.5068	364.2469
<b>Sep 1999</b>	363.9700	365.6409	362.2991
<b>Oct 1999</b>	364.2490	365.9604	362.5375
<b>Nov 1999</b>	365.7172	367.4690	363.9655
<b>Dec 1999</b>	367.1710	368.9628	365.3793
<b>Jan 2000</b>	368.1017	369.9669	366.2366
<b>Feb 2000</b>	368.9602	370.8642	367.0563
<b>Mar 2000</b>	369.7282	371.6707	367.7857
<b>Apr 2000</b>	371.1303	373.1111	369.1494
<b>May 2000</b>	371.6612	373.6803	369.6421
<b>Jun 2000</b>	370.9446	373.0018	368.8874
<b>Jul 2000</b>	369.5256	371.6208	367.4305
<b>Aug 2000</b>	367.3738	369.5067	365.2408

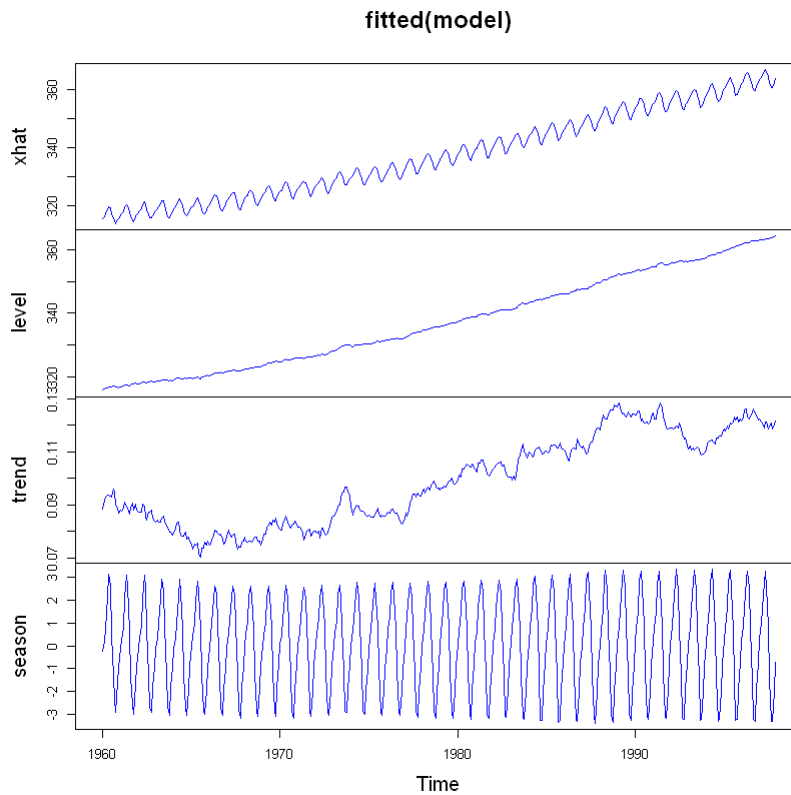
	fit	upr	lwr
<b>Sep 2000</b>	365.4669	367.6376	363.2963
<b>Oct 2000</b>	365.7459	367.9541	363.5376
<b>Nov 2000</b>	367.2142	369.4599	364.9684
<b>Dec 2000</b>	368.6680	370.9511	366.3848
<b>Jan 2001</b>	369.5987	371.9479	367.2494
<b>Feb 2001</b>	370.4572	372.8432	368.0711
<b>Mar 2001</b>	371.2251	373.6479	368.8023
<b>Apr 2001</b>	372.6272	375.0867	370.1677
<b>May 2001</b>	373.1581	375.6543	370.6619
<b>Jun 2001</b>	372.4416	374.9744	369.9087
<b>Jul 2001</b>	371.0226	373.5920	368.4531
<b>Aug 2001</b>	368.8707	371.4767	366.2647
<b>Sep 2001</b>	366.9639	369.6064	364.3213
<b>Oct 2001</b>	367.2428	369.9219	364.5637
<b>Nov 2001</b>	368.7111	371.4267	365.9955
<b>Dec 2001</b>	370.1649	372.9170	367.4128
<b>Jan 2002</b>	371.0956	373.9100	368.2812
<b>Feb 2002</b>	371.9541	374.8046	369.1036


In [ ]: `plot(model,fore,col="red")`



 **Analisis :** Dataset merupakan pengukuran konsentrasi karbondioksida (CO2) di Mauna Loa, Hawai pada tahun 1959 hingga 1997. Hasil insight didapat pola trend dan seasonal dan terdapat kenaikan setiap tahunnya. Kemudian melakukan predict untuk model dengan interval 50 prediksi ke depan dengan menggunakan metode HoltWintres.

```
In [ ]: plot(fitted(model), col="blue")
```



 **Analisis :** Model kemudian di fit kan. Dan dari hasil fitting model berhasil menangkap dan memvisualisasikan komponen-komponen penting dari data time series, yaitu level, trend, dan seasonality.

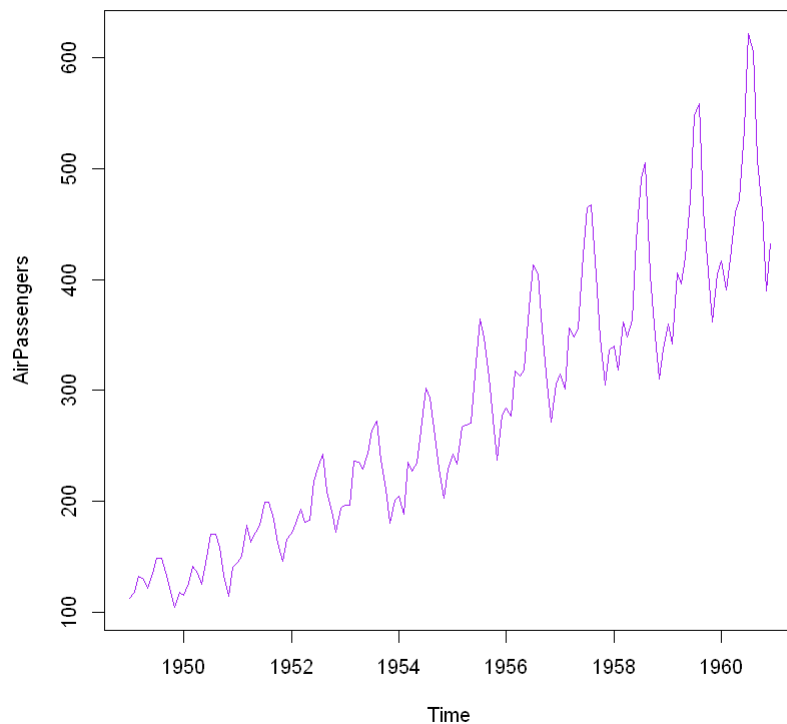
## Percobaan ke-4: Studi Kasus 4

In [ ]: AirPassengers

A Time Series: 12 × 12

	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
<b>1949</b>	112	118	132	129	121	135	148	148	136	119	104	118
<b>1950</b>	115	126	141	135	125	149	170	170	158	133	114	140
<b>1951</b>	145	150	178	163	172	178	199	199	184	162	146	166
<b>1952</b>	171	180	193	181	183	218	230	242	209	191	172	194
<b>1953</b>	196	196	236	235	229	243	264	272	237	211	180	201
<b>1954</b>	204	188	235	227	234	264	302	293	259	229	203	229
<b>1955</b>	242	233	267	269	270	315	364	347	312	274	237	278
<b>1956</b>	284	277	317	313	318	374	413	405	355	306	271	306
<b>1957</b>	315	301	356	348	355	422	465	467	404	347	305	336
<b>1958</b>	340	318	362	348	363	435	491	505	404	359	310	337
<b>1959</b>	360	342	406	396	420	472	548	559	463	407	362	405
<b>1960</b>	417	391	419	461	472	535	622	606	508	461	390	432

```
In [ ]: plot(AirPassengers, col = "purple")
```



```
In [ ]: model <- HoltWinters(AirPassengers, seasonal="mult")
model
```



Holt-Winters exponential smoothing with trend and multiplicative seasonal component.

Call:

```
HoltWinters(x = AirPassengers, seasonal = "mult")
```

Smoothing parameters:

```
alpha: 0.2755925  
beta : 0.03269295  
gamma: 0.8707292
```

Coefficients:

```
      [,1]  
a 469.3232206  
b   3.0215391  
s1  0.9464611  
s2  0.8829239  
s3  0.9717369  
s4  1.0304825  
s5  1.0476884  
s6  1.1805272  
s7  1.3590778  
s8  1.3331706  
s9  1.1083381  
s10 0.9868813  
s11 0.8361333  
s12 0.9209877
```

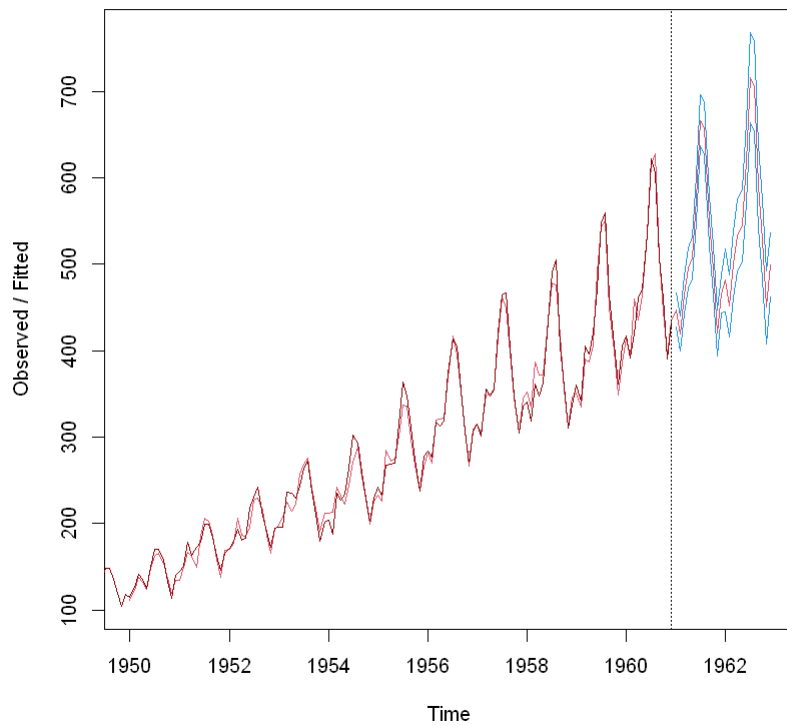
```
In [ ]: fore <- predict(model, 24, prediction.interval = TRUE)  
fore
```

A Time Series: 24 × 3

	<b>fit</b>	<b>upr</b>	<b>lwr</b>
<b>Jan 1961</b>	447.0559	466.8057	427.3061
<b>Feb 1961</b>	419.7123	440.2920	399.1326
<b>Mar 1961</b>	464.8671	486.7712	442.9630
<b>Apr 1961</b>	496.0839	519.3350	472.8329
<b>May 1961</b>	507.5326	531.9278	483.1375
<b>Jun 1961</b>	575.4509	602.1935	548.7083
<b>Jul 1961</b>	666.5923	696.5558	636.6288
<b>Aug 1961</b>	657.9137	688.6454	627.1821
<b>Sep 1961</b>	550.3088	578.9777	521.6398
<b>Oct 1961</b>	492.9853	520.9553	465.0153
<b>Nov 1961</b>	420.2073	446.9458	393.4688
<b>Dec 1961</b>	465.6345	487.9686	443.3004
<b>Jan 1962</b>	481.3732	517.8126	444.9337
<b>Feb 1962</b>	451.7258	488.0308	415.4207
<b>Mar 1962</b>	500.1008	538.8928	461.3088
<b>Apr 1962</b>	533.4477	574.3831	492.5122
<b>May 1962</b>	545.5202	587.8399	503.2005
<b>Jun 1962</b>	618.2550	664.8185	571.6915
<b>Jul 1962</b>	715.8704	768.3289	663.4118
<b>Aug 1962</b>	706.2524	759.2423	653.2626
<b>Sep 1962</b>	590.4954	638.2882	542.7027
<b>Oct 1962</b>	528.7681	574.2084	483.3279
<b>Nov 1962</b>	450.5242	492.7194	408.3290
<b>Dec 1962</b>	499.0281	535.8450	462.2112

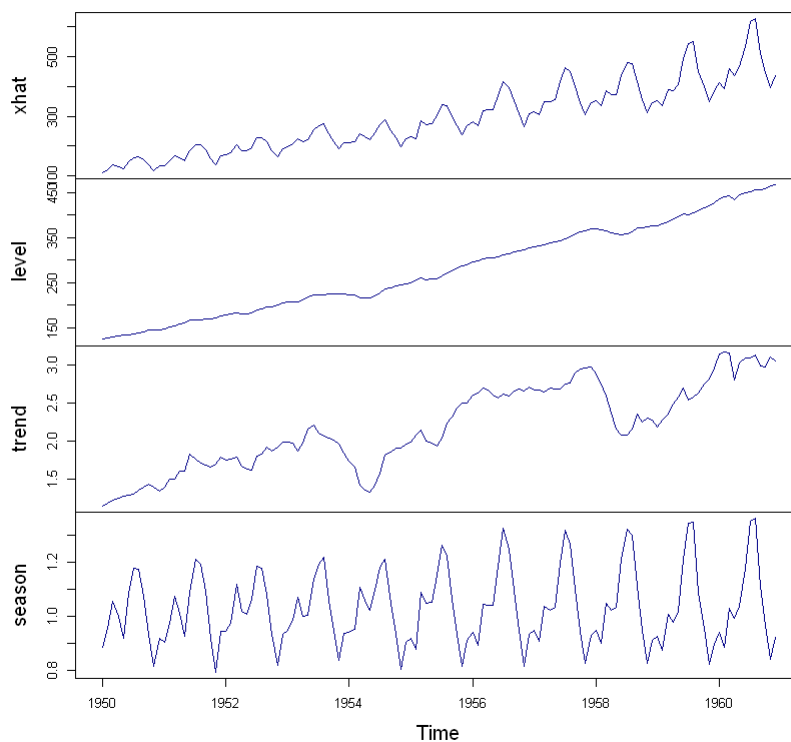
```
In [ ]: plot(model,fore,col="darkred")
```


### Holt-Winters filtering



```
In [ ]: plot(fitted(model), col="darkblue")
```

### fitted(model)



 **Analisis :** Sama seperti percobaan sebelumnya model menangkap dan memvisualisasikan komponen-komponen dengan sangat baik dari data time series,

yaitu level, trend, dan seasonality. Model yang telah di fit menunjukkan bahwa data atau nilai pada 24 periode berikutnya cenderung naik.