## Praktikum Pemodelan Statistika terapan

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## Percobaan ke-1: Studi Kasus 1

```
In [ ]: library(readr)
        tissue <- read_csv("breast_tissue.csv") # Checking the structure of adult data
        str(tissue)
       Rows: 106 Columns: 11

    Column specification

       Delimiter: ","
       chr (1): Class
       dbl (10): patient_id, IO, PA500, HFS, DA, Area, A/DA, Max IP, DR, P
       i Use `spec()` to retrieve the full column specification for this data.
       i Specify the column types or set `show_col_types = FALSE` to quiet this message.
       spc_tbl_ [106 x 11] (S3: spec_tbl_df/tbl_df/tbl/data.frame)
        $ patient_id: num [1:106] 1 2 3 4 5 6 7 8 9 10 ...
        $ Class : chr [1:106] "car" "car" "car" "car" ...
        $ I0
                   : num [1:106] 525 330 552 380 363 ...
        $ PA500
                   : num [1:106] 0.187 0.227 0.232 0.241 0.201 ...
        $ HFS
                  : num [1:106] 0.0321 0.2653 0.0635 0.2862 0.2443 ...
        $ DA
                   : num [1:106] 229 121 265 138 125 ...
        $ Area
                   : num [1:106] 6844 3163 11888 5402 3290 ...
        $ A/DA
                  : num [1:106] 29.9 26.1 44.9 39.2 26.3 ...
        $ Max IP : num [1:106] 60.2 69.7 77.8 88.8 69.4 ...
        $ DR
                   : num [1:106] 220.7 99.1 253.8 105.2 103.9 ...
        $ P
                   : num [1:106] 557 400 657 494 425 ...
        - attr(*, "spec")=
         .. cols(
              patient_id = col_double(),
            Class = col_character(),
         . .
         .. I0 = col_double(),
         .. PA500 = col_double(),
             HFS = col double(),
         . .
         .. DA = col_double(),
         .. Area = col double(),
             `A/DA` = col_double(),
             `Max IP` = col_double(),
         . .
            DR = col_double(),
              P = col double()
         . .
         ..)
        - attr(*, "problems")=<externalptr>
In [ ]: tissue <- tissue[, -1]</pre>
        tissue$Class <- as.factor(tissue$Class)</pre>
        levels(tissue$Class)[levels(tissue$Class) %in% c("fad", "gla", "mas")] <-</pre>
        levels(tissue$Class)
      'adi' · 'car' · 'con' · 'other'
```

✓ **Analisis :** Dari dataset BreastTissue, kemudian direduksi kelas dimana fibroadenoma, mastopati, dan glandular dijadikan satu kelas diberi nama 'others'.

```
In [ ]: #Splitting the data using a function from dplyr package
    library(caret)
    library(ggplot2)
```

```
index <- createDataPartition(tissue$Class, p = .70, list = FALSE)</pre>
        train <- tissue[index,]</pre>
        test <- tissue[-index,]</pre>
In [ ]: # Setting the reference
        train$Class <- relevel(train$Class, ref = "adi")</pre>
In [ ]: library(nnet)
        # Training the multinomial model
        multinom_model <- multinom(Class ~ ., data = tissue)</pre>
        # Checking the model
        summary(multinom_model)
       # weights: 44 (30 variable)
       initial value 146.947202
       iter 10 value 107.785951
       iter 20 value 71.796827
       iter 30 value 17.709626
       iter 40 value 11.374947
       iter 50 value 6.775080
       iter 60 value 5.795296
       iter 70 value 5.581882
       iter 80 value 4.879180
       iter 90 value 4.199680
       iter 100 value 4.160692
       final value 4.160692
       stopped after 100 iterations
       Call:
       multinom(formula = Class ~ ., data = tissue)
       Coefficients:
                                        PA500
             (Intercept)
                                10
                                                      HFS
                                                                   DA
                86.45689 -0.92420610 35.426343 -28.995689 -2.7614791 -0.009627356
       car
                65.29309 -0.02131995 3.507425 5.180119 0.3799671 -0.006557466
       con
       other
                94.35136 -0.44817721 -10.573482 45.314817 -0.2506004 -0.011107358
                `A/DA` `Max IP`
                                        DR
             -0.6522402 2.3039134 3.0645844 0.67990594
       car
              1.3401948 0.2354590 -0.1683327 -0.07552706
       con
       other 1.5460282 0.1120201 0.6247094 0.29486854
       Std. Errors:
             (Intercept)
                                10
                                          PA500
                                                        HFS
                                                                   DA
                                                                             Area
             0.03476847 0.1066177 0.0177918233 0.037347078 0.6130240 0.029524661
       car
       con
              0.00246189 0.5774913 0.0003169089 0.002276567 0.3423545 0.005154037
       other 0.03434195 0.1013918 0.0176815177 0.037334873 0.6274376 0.029559302
                `A/DA` `Max IP`
                                      DR
             0.5424341 0.4562191 0.5804292 0.1709975
       car
             0.2034479 0.6789553 0.2860865 0.4041700
       other 0.5335004 0.4787424 0.5696903 0.1633894
       Residual Deviance: 8.321383
       AIC: 68.32138
```

✓ Analisis: Dalam regresi logistik multinomial memakai library nnet, menghasilkan model training yang mengiterasi optimisasi train model. Optimisasi tersebut bertujual untuk meminimalkan fungsi objektivitas untuk menemukan model parameter yang optimal. Optimisasi terhenti setelah mencapai kriteria convergence, saat dimana improvisasi objek sudah kecil dan maksimum iterasi tercapai. Nilai AIC yang cenderung rendah menunjukkan bahwa model memiliki kualitas yang baik.

In [ ]: exp(coef(multinom\_model))

A matrix: 3	} ×	10	of	type	dbl
-------------	-----	----	----	------	-----

	(Intercept)	10	PA500	HFS	DA	Area	`A
ca	<b>r</b> 3.529816e+37	0.3968464	2.429210e+15	2.554656e-13	0.06319822	0.9904188	0.520
cor	1 2.272107e+28	0.9789057	3.336224e+01	1.777040e+02	1.46223641	0.9934640	3.819
othe	<b>r</b> 9.468380e+40	0.6387915	2.558557e-05	4.786024e+19	0.77833332	0.9889541	4.692
4							•

In [ ]: head(round(fitted(multinom\_model), 2),20)

A matrix:  $20 \times 4$  of type dbl

	adi	car	con	other
1	0	0.97	0	0.03
2	0	1.00	0	0.00
3	0	1.00	0	0.00
4	0	1.00	0	0.00
5	0	1.00	0	0.00
6	0	0.96	0	0.04
7	0	0.77	0	0.23
8	0	0.53	0	0.47
9	0	1.00	0	0.00
10	0	1.00	0	0.00
11	0	1.00	0	0.00
12	0	1.00	0	0.00
13	0	0.91	0	0.09
14	0	1.00	0	0.00
15	0	1.00	0	0.00
16	0	1.00	0	0.00
17	0	1.00	0	0.00
18	0	0.55	0	0.45
19	0	1.00	0	0.00
20	0	0.96	0	0.04

In [ ]: tail(round(fitted(multinom\_model), 2),20)

A matrix:  $20 \times 4$  of type dbl

			7.	
	adi	car	con	other
87	1	0	0	0
88	1	0	0	0
89	1	0	0	0
90	1	0	0	0
91	1	0	0	0
92	1	0	0	0
93	1	0	0	0
94	1	0	0	0
95	1	0	0	0
96	1	0	0	0
97	1	0	0	0
98	1	0	0	0
99	1	0	0	0
100	1	0	0	0
101	1	0	0	0
102	1	0	0	0
103	1	0	0	0
104	1	0	0	0
105	1	0	0	0
106	1	0	0	0

✓ Analisis: Regresi multinomial memprediksi probabilitas pengamatan tertentu untuk menjadi bagian dari kelas tertentu. Kolom mewakili tingkat klasifikasi dan baris mewakili pengamatan. 20 baris pertama terklasifikasi sebagai carsinoma dan 20 baris terakhir tergolong sebagai adipose

```
In []: # Predicting the values for train dataset
    train$ClassPredicted <- predict(multinom_model, newdata = train, "class")
    # Building classification table
    tab <- table(train$Class, train$ClassPredicted)
    # Calculating accuracy - sum of diagonal elements divided by total obs
    round((sum(diag(tab)))/sum(tab))*100,2)</pre>
```

```
In []: # Predicting the class for test dataset
    test$ClassPredicted <- predict(multinom_model, newdata = test, "class")
    # Building classification table
    tab <- table(test$Class, test$ClassPredicted)
    tab</pre>
```

```
      adi
      car
      con other

      adi
      6
      0
      0
      0

      car
      0
      6
      0
      0
      0

      con
      0
      0
      4
      0

      other
      0
      0
      0
      14
```

✓ Analisis: Didapat untuk akurasi skor dari tiap tiap konfigurasi dan semua plot yang. Didapat bahwa akurasinya sangat tinggi yaitu 98.68%. Disimpulkan bahwa model bagus dan stabil.

## Percobaan ke-3: Studi Kasus 3

Analisis: Kode di atas digunakan untuk membuat dataset klasifikasi sintetis dengan 1000 sampel, 10 fitur, dan 3 kelas. Dan distribusi kelas terbagi menjadi 334 untuk tiap kelas. Disini kita dapat memahami struktur dataset klasifikasi dan distribusi kelasnya.

```
In [ ]: # define the multinomial logistic regression model
    from sklearn.linear_model import LogisticRegression
    model = LogisticRegression(multi_class='multinomial', solver='lbfgs')
```

✓ **Analisis**: Memanggil fungsi multinomial logistic regression kemudian di fit menggunakan cross-entropy loss dan akan dipredict nilainya untuk tiap label kelasnya.

```
In [ ]: # evaluate multinomial logistic regression model
        from numpy import mean
        from numpy import std
        from sklearn.datasets import make_classification
        from sklearn.model_selection import cross_val_score
        from sklearn.model selection import RepeatedStratifiedKFold
        from sklearn.linear_model import LogisticRegression
        # define dataset
        X, y = make_classification(n_samples=1000, n_features=10, n_informative=5,
                                   n redundant=5, n classes=3, random state=1)
        # define the multinomial logistic regression model
        model = LogisticRegression(multi class='multinomial', solver='lbfgs')
        # define the model evaluation procedure
        cv = RepeatedStratifiedKFold(n splits=10, n repeats=3, random state=1)
        # evaluate the model and collect the scores
        n_scores = cross_val_score(model, X, y, scoring='accuracy', cv=cv, n_jobs=-1)
        # report the model performance
        print('Mean Accuracy: %.3f (%.3f)' % (mean(n_scores), std(n_scores)))
```

Mean Accuracy: 0.681 (0.042)

Analisis: Dalam kasus ini kita bisa melihat multinomial logistic regression model dengan penalty default dan didapat dengan mean classification akurasi sekitar 68.1% dari dataset klasifikasi sintetis. Dengan 3 kali perulangan dengan 10 folds, dimana nilai ini adalah nilai default dari repeated stratified k-fold crossvalidation, kita bisa mengevaluasi model menggunakan klasifikasi.

```
In []: # make a prediction with a multinomial logistic regression model
    from sklearn.datasets import make_classification
    from sklearn.linear_model import LogisticRegression
    # define dataset
    X, y = make_classification(n_samples=1000, n_features=10, n_informative=5, n_red
    # define the multinomial logistic regression model
    model = LogisticRegression(multi_class='multinomial', solver='lbfgs')
    # fit the model on the whole dataset
    model.fit(X, y)
    # define a single row of input data
    row = [1.89149379, -0.39847585, 1.63856893, 0.01647165, 1.51892395, -3.52651223,
    # predict the class label
    yhat = model.predict([row])
    # summarize the predicted class
    print('Predicted Class: %d' % yhat[0])
```

Predicted Class: 1

```
In []: # predict probabilities with a multinomial logistic regression model
    from sklearn.datasets import make_classification
    from sklearn.linear_model import LogisticRegression
    # define dataset
    X, y = make_classification(n_samples=1000, n_features=10, n_informative=5, n_red
    # define the multinomial logistic regression model
    model = LogisticRegression(multi_class='multinomial', solver='lbfgs')
    # fit the model on the whole dataset
    model.fit(X, y)
    # define a single row of input data
    row = [1.89149379, -0.39847585, 1.63856893, 0.01647165, 1.51892395, -3.52651223,
    # predict a multinomial probability distribution
    yhat = model.predict_proba([row])
    # summarize the predicted probabilities
    print('Predicted Probabilities: %s' % yhat[0])
```

Predicted Probabilities: [0.16470456 0.50297138 0.33232406]

✓ Analisis: Disini kemudian memasukkan sebuah satu baris data dummy dengan variable row yang kemudian dilakukan prediksi, didapat bahwa dalam baris tersebut merupakan kelas pertama. Beserta probrabilitas untuk tiap tiap kelasnya.

```
In []: # define the multinomial logistic regression model with a default penalty
    LogisticRegression(multi_class='multinomial', solver='lbfgs', penalty='12', C=1.
Out[]:    LogisticRegression
    LogisticRegression(multi_class='multinomial')
```

✓ Analisis: Selanjutnya dari dataset kemudian dilakukan prediksi dengan solver Limited-memory Broyden-Fletcher-Goldfarb-Shanno untuk optimisasinya.

✓ **Analisis :** Mari kita lihat dari L2 penalti dengan berat value dari range 0.0001 hingga 1.0. Dengan perhitungan komplex dari multinomial logistic regression di bawah ini.

```
In [ ]: # tune regularization for multinomial logistic regression
        from numpy import mean
        from numpy import std
        from sklearn.datasets import make_classification
        from sklearn.model_selection import cross_val_score
        from sklearn.model_selection import RepeatedStratifiedKFold
        from sklearn.linear_model import LogisticRegression
        from matplotlib import pyplot
        # get the dataset
        def get_dataset():
                X, y = make_classification(n_samples=1000, n_features=20, n_informative=
                                     n_redundant=5, random_state=1, n_classes=3)
                return X, y
In [ ]: # get a list of models to evaluate
        def get_models():
                models = dict()
                for p in [0.0, 0.0001, 0.001, 0.01, 0.1, 1.0]:
                        # create name for model
                        key = '%.4f' % p
                        # turn off penalty in some cases
                        if p == 0.0:
                                 # no penalty in this case
                                 models[key] = LogisticRegression(multi_class='multinomia
                        else:
                                 models[key] = LogisticRegression(multi_class='multinomia
                return models
        # evaluate a give model using cross-validation
        def evaluate_model(model, X, y):
                # define the evaluation procedure
                cv = RepeatedStratifiedKFold(n_splits=10, n_repeats=3, random_state=1)
                # evaluate the model
                scores = cross val score(model, X, y, scoring='accuracy', cv=cv, n jobs=
                return scores
In [ ]: # define dataset
        X, y = get dataset()
        # get the models to evaluate
        models = get models()
        # evaluate the models and store results
        results, names = list(), list()
        for name, model in models.items():
                # evaluate the model and collect the scores
                scores = evaluate model(model, X, y)
```

```
# store the results
         results.append(scores)
         names.append(name)
         # summarize progress along the way
         print('>%s %.3f (%.3f)' % (name, mean(scores), std(scores)))
 # plot model performance for comparison
 pyplot.boxplot(results, labels=names, showmeans=True)
 pyplot.show()
>0.0000 0.777 (0.037)
>0.0001 0.683 (0.049)
>0.0010 0.762 (0.044)
>0.0100 0.775 (0.040)
>0.1000 0.774 (0.038)
>1.0000 0.777 (0.037)
0.85
0.80
0.75
0.70
                                   0
0.65
0.60
        0.0000
                    0.0001
                                0.0010
                                            0.0100
                                                        0.1000
                                                                   1.0000
```

Box and Whisker Plots of L2 Penalty Configuration vs. Accuracy for Multinomial Logistic Regression

Analisis: Kode di atas memungkinkan ntuk membandingkan kinerja model regresi logistik dengan berbagai tingkat regularisasi. Dari gambar box plot di atas untuk akurasi skor dari tiap tiap konfigurasi dan kita dapat memahami bagaimana performa model berubah dengan perubahan parameter regularisasi. Dalam kasus ini C Value dari 0.1 memiliki skor terbaik dengan sekitar 77.7%. Yang skornya sama dengan yang tanpa penalti.