

## Unit-4 Recursion

Definition: - The process on which a function calls itself directly or indirectly 48 called recursion. It 19 a powerful technique of writing a complicated algorithm in an easy way. According to this technique a problem is defined in terms of itself. The problem is solved by dividing it into smaller problems, which are similar in nature to the original problem. These smaller problems are solved and their solutions are applied to get the final solution of our original problem.

A function will be recursive, if it contains following features;

i) Function should call atself.

PP) Function should have a stopping condition (base criteria).

Using recursive algorithm, certain problems can be solved quite easily. Examples of such problems are Towers of Hanos (TOH), Inorder/Preorder/ Postorder tree traversals, DFS of Graph etc.

Recursive vs. I ferative algorithm:

		TI Line
Property	Recursion	Iteration
Definition	Function calls etself	A set of instructions repeatedly executed.
Application	It is used for functions	It 18 used for loops.
Termination.	It will terminate at base case, where there will be no	It will terminate when the condition for eteration is satisfied.
	function call.	1 1 0 1 1
ry Usage	The 98 used when code size needs to be small, and time complexity is not an issuse.	- 111 - 0
y Code Size	It has smaller code size	ve>It has larger code saze.
VP Teme Complexity	It has very high (generally exponential) time complexity.	It has relatively lower time complexity (generally polynomial or logarithmic).

Tail recursion (Definition & Example):
A recursive function is tail recursive when recursive call is the last thing executed by the function. So, when nothing is left to do after comming back from the recurive call.

Example (Using (++);

# include < iostream>
using namespace std;

Void print N (int n) & if (n20) & return;

94 (n20) ?

seturn;

cout < < n < < " ";

print N(n-1);

3

ant main () {

pant N(10);

}

Output: 10 9 8 7 6 5 4 3 2 1 0

# The tast recursion as better than non-tast recursion. As there as no task left after the recursive call, at will be easier for the compiler to organize optimize the code.

# A non-tail recursive function can be written as tail-recursive to optimize 9t. Consider the following function to calculate factorial of n.

Yong fact (ent n) { of (n/=1)

return 1;

n\*fact (n-1);

This function is a non-tail recursive function because the value returned by fact (n-1) is used in fact (n), so the call to fact (n-1) is not the last thing done by fact n. The above function can be withten as tail recursive function by adding some other parameters as follows:
long fact (long n, long a) & ef(n = 0)

return a;
return fact (n-1, a\*n);

@Examples of Recursive Algorithms: 1) Factorial: Factorial of any number n +8 denoted as n! and 18 equal to; n! = n x (n-1) x (n-2) x ... x 3 x 2 x 1. for e.g.; Factorial of 5 18; 5!= 5×4×3×2×1 Recursive Algorithm for calculation of factorial of given integer; Step1: Start Step2: Read number n Step3: call factorial (n) Step4: Print factorial f function to call Steps: Stop. and factorial (n) Step1: of n==1 then othern 1. 5 tep2: else,

f=n\*factorial (n-1) Step3: returnf; # Now we can eaisly write C or C++ program on the basis of this algorithm. 2) Fibonacci Sequence: Fibonacci series are the numbers in the sequence 0, 1, 1, 2, 3, 5, 8, 13, 21, ... By the definition, the first two numbers are 0 and 1. each subsequent numbers on the series 18 equal to the sun of the previous two numbers. Recursive Algorithm for Abonacci Sequence: Step 1: Start Step 2: Read number n Step3: Call frb(m). Step4: Print fib(n)

Int fib (int n)

Step 1: if (n=1 || n==2)

return 1;

Step 2: else, fib(n) = fib(n-1) + fib(n-2)

Step 3: return fib(n);

3) Greatest Common Divisor (GCD): [Imp]

GCD or Greatest Common Divisor of two or more integers
is the largest positive integer that can divide both the
number without leaving any remainder.

Example: - GCD of 20 and 8 18 4.

## Recursive Algorithm for GCD:

Step 1: Start

Step 2: Read Loo numbers a and b.

Step3: Call gcd (a,b)

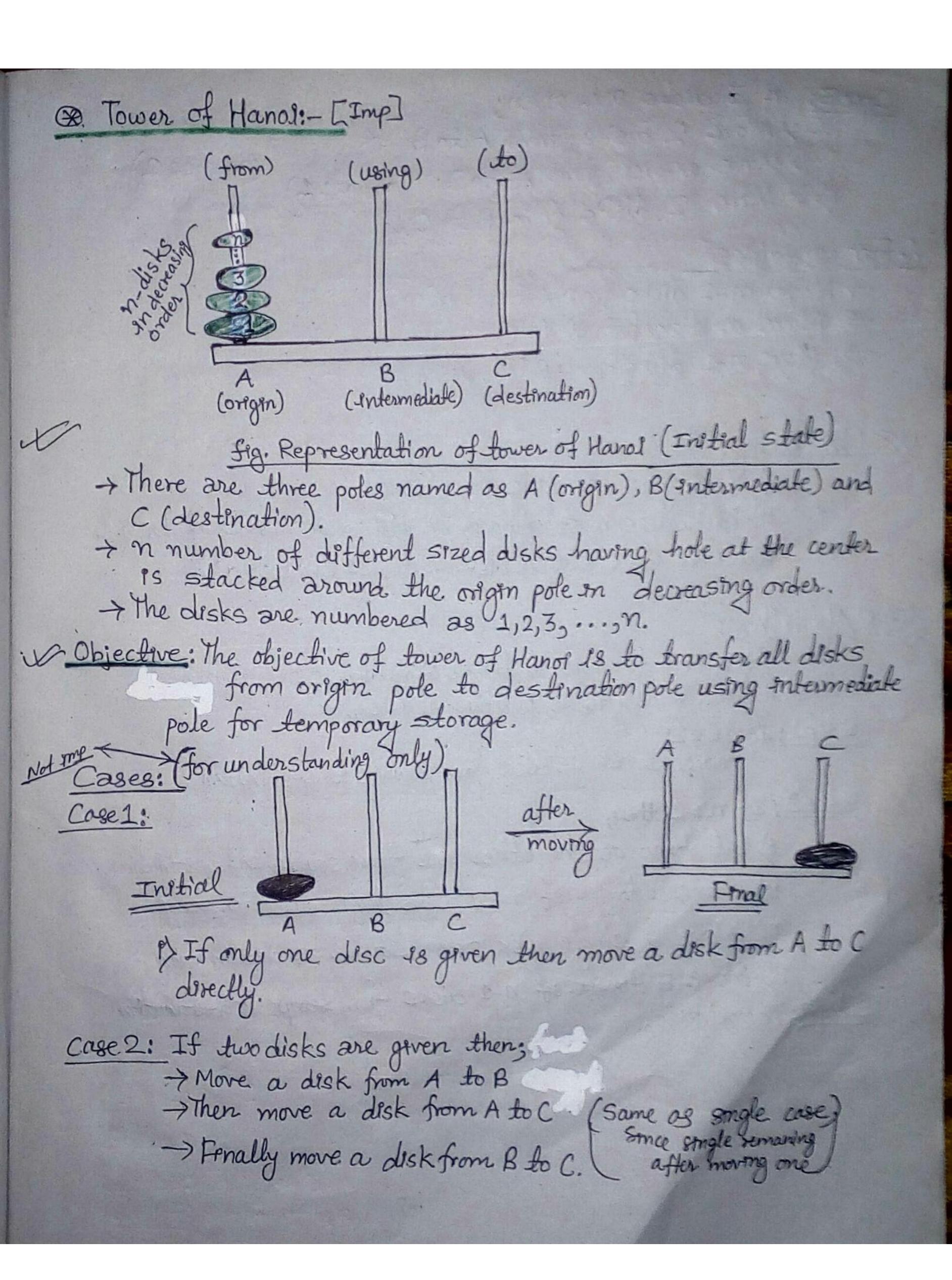
Step 4: Print gcd.
Step 5: Step.

ent gcd (enta, entb)

Step 1: if (b==0) return a;

5/2 : else, gcd = gcd(b, a %b);

Sdep3: return gcd;



Case 3: 4f 3 disks are given; -> Move 2 disks from A to B \* (as cose 2) -> Move a disk from A. to C (as. Case 1) -> Move 2 disks from B to C. 4

... For n-disks

→ Move n-1 disks from A to B. using C. → Move a disk from A to C

-> Move n-1 desks from B tol using A

W Conditions:

Move only one disk at a time.

PP Fach disk must always be placed around one of the pole.

PP Never place larger disk on top of smaller disk.

Algorithm:
Algorithm to move a tower of n disks from source to destination. (where n is positive integer).

Stepl: If n==1; move a single disk from source to destination.

Step 2: If n>1;

1) Let temp be the other pole than source and destination.
11) Move a tower of (n-1) disks from source to temp. move a single disk from source to destination. nove a tower of (n-1) disks from temp to destination. 5lep3: Terminate.

Dimplementation of tower of Hanci using C; #include. 4 staio. h> # include (conio.h) vord TOH (ant, char, char, char); // function prototype. void main () § Printf ("Enter number of disks"); scanf ("/d", dn); TOH (n, '0', 'D', 'I'); // function call void TOH (ant n, char A, char B, char C) { If (n>0) {
TOH (n-1, A, C, B); Printf ("Move disk %d from /c to /c \n, m, A, B); TOH (n-1, C, B, A); @ Applications of Recursion: 1) The most important data structure 'Tree' does not exist without recursion. We can solve that in iterative way also but that will be a very tough task. All puzzle games leke Chess, Candy Crush etc broadly uses recursion. 98 the backbone of AI. my Many of the well known sorting algorithms (take Quick, Merge etc.) v) It is the backbone for searching,

D. Advantages of Recursion:

1) The code becomes much earser to write.

recursive such as tower of Hanos.

18th Reduces unnecessary calling of functions.

@. Disadvantages of Recursion:

Recursive functions are generally slower than non-recursive functions.

The may require a lot of memory to hold intermediate results on the system stack.

1117) It is It is difficult to think recursively so one must be very careful when writing recursive functions.