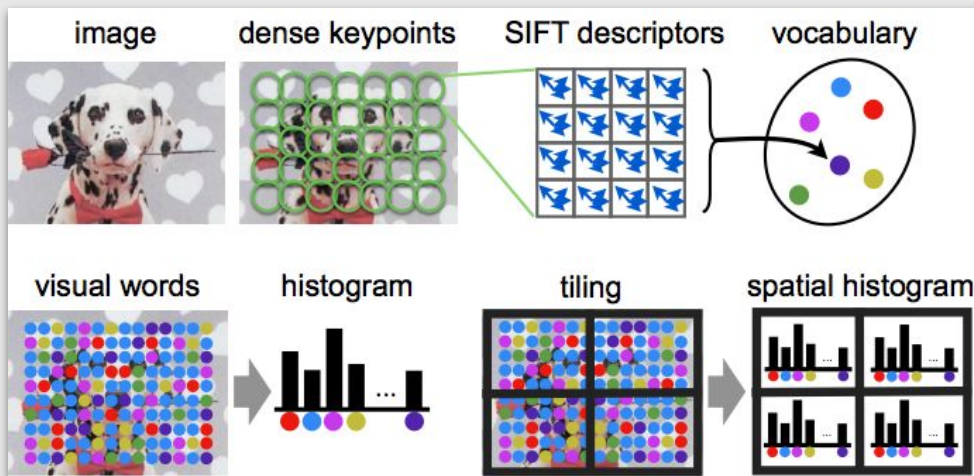


# Maior Dúvida da Aula

1. É possível obtermos melhores resultados com algoritmos não-supervisionados em *dataset* que temos a anotação dos dados? Ou devemos sempre dar preferência ao algoritmo supervisionado?
2. Posso usar um algoritmo de clusterização para realizar classificação de dados?

Bag of visual words

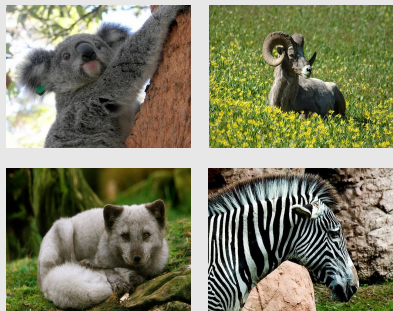


3. Eu entendi sobre o que são os clusters, mas eu perdi sobre como que usamos eles para gerar respostas para nosso sistema, o objetivo é sempre achar algum padrão para dar a resposta, ou os clusters ajudam a ter uma noção de como podemos tratar os dados para aplicação de alguma outra estratégia que ainda vamos ver nas próximas aulas?
4. No método do cotovelo, escolher um número maior de cluster implicaria num overfit?
5. Independentemente da quantidade de dimensões do dataset, é utilizada a distância euclidiana ou existem outras métricas para esse tipo?
6. Existem técnicas de aprendizado não supervisionado que utilizam redes neurais ?

7. Me parece que, diferente dos problemas de aprendizado supervisionado, os problemas de aprendizado não supervisionado, por não terem anotação os dados, demandam mais o envolvimento de especialistas conhecedores das características do sistema/fenômeno/processo dos quais os dados foram obtidos. Essa impressão faz sentido?
8. Pesquisei mais sobre aplicações e vi que os sistemas de recomendação se baseiam nisso, porém não consegui entender muito bem o porquê.
9. Há um certo tempo, vi o termo **self-supervised learning**. Como não é necessário supervisão humana, seria basicamente unsupervised learning? Imagino que as labels teriam que ser construídas de forma similar como você nos mostrou na aula. Se é um método diferente, como este se diferencia de unsupervised learning?

**Self-supervised**  
pretext task training

Dados não-annotados

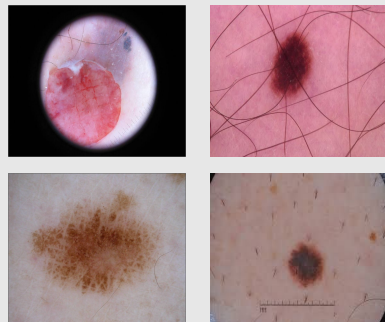


Rede  
Neural

Tarefa  
pretexto

**Supervised**  
downstream task  
training

Dados anotados



Rede  
Neural

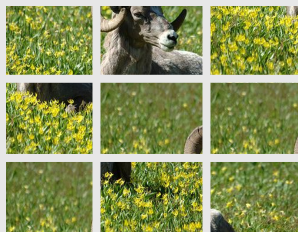
Tarefa  
alvo



Colorização da imagem



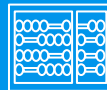
Predição do ângulo de rotação



Montar quebra-cabeça



recod.ai  
reasoning for complex data



# Unsupervised Learning

## Machine Learning

**Prof. Sandra Avila**

Institute of Computing (IC/Unicamp)

MC886/MO444, October 11, 2022

# Today's Agenda

— — —

- Clustering
  - k-Means Variations
  - Hierarchical clustering
  - DBSCAN Clustering
  - Clustering Performance Evaluation

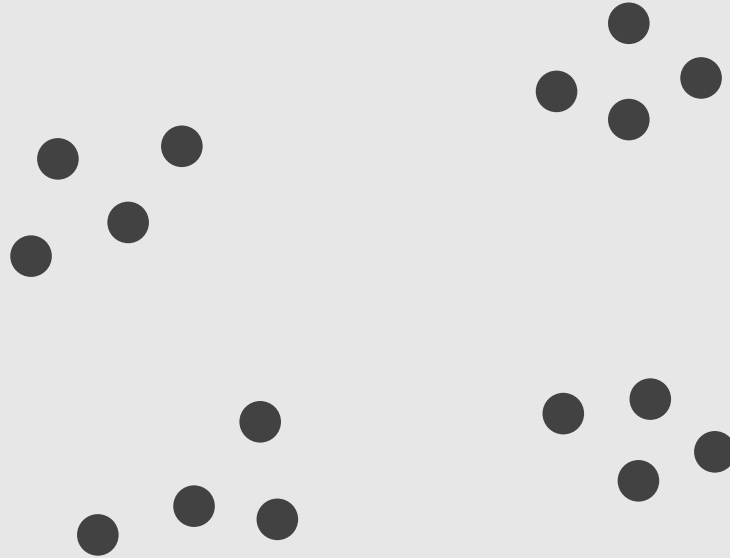


# k-Means Variations

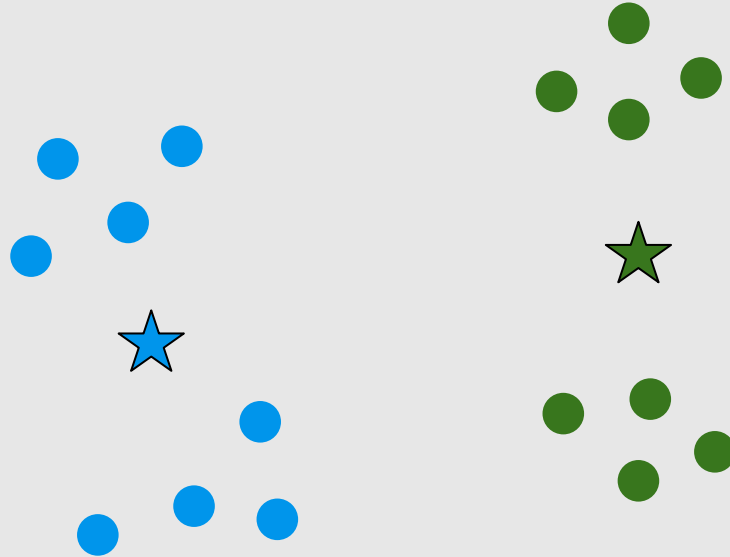
# Bisecting k-Means

- A straightforward extension of the basic k-means.
- To obtain  $k$  clusters:
  - Split the set of all points into two clusters,
  - Select one of these clusters to split,
  - Repeat until  $k$  clusters have been produced.

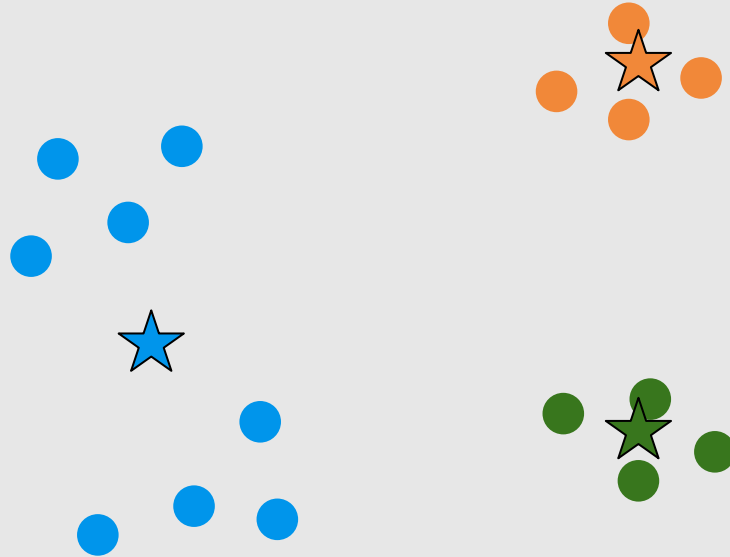
# Bisecting k-Means



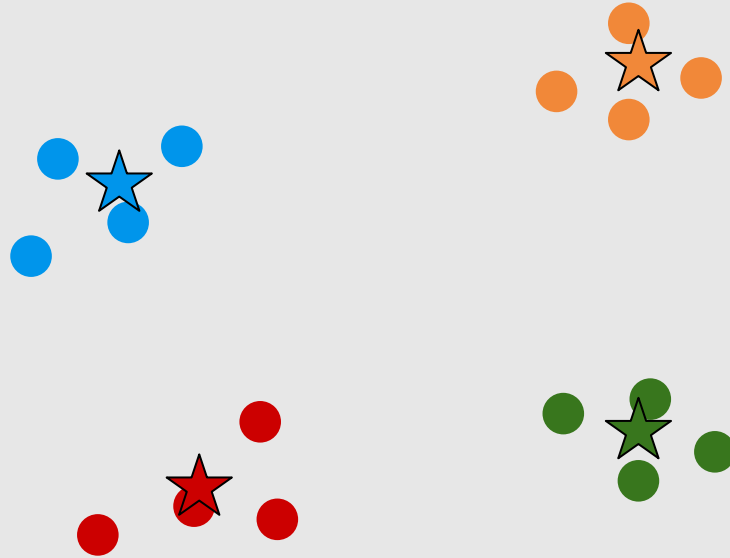
# Bisecting k-Means



# Bisecting k-Means



# Bisecting k-Means



# Mini-batch k-Means

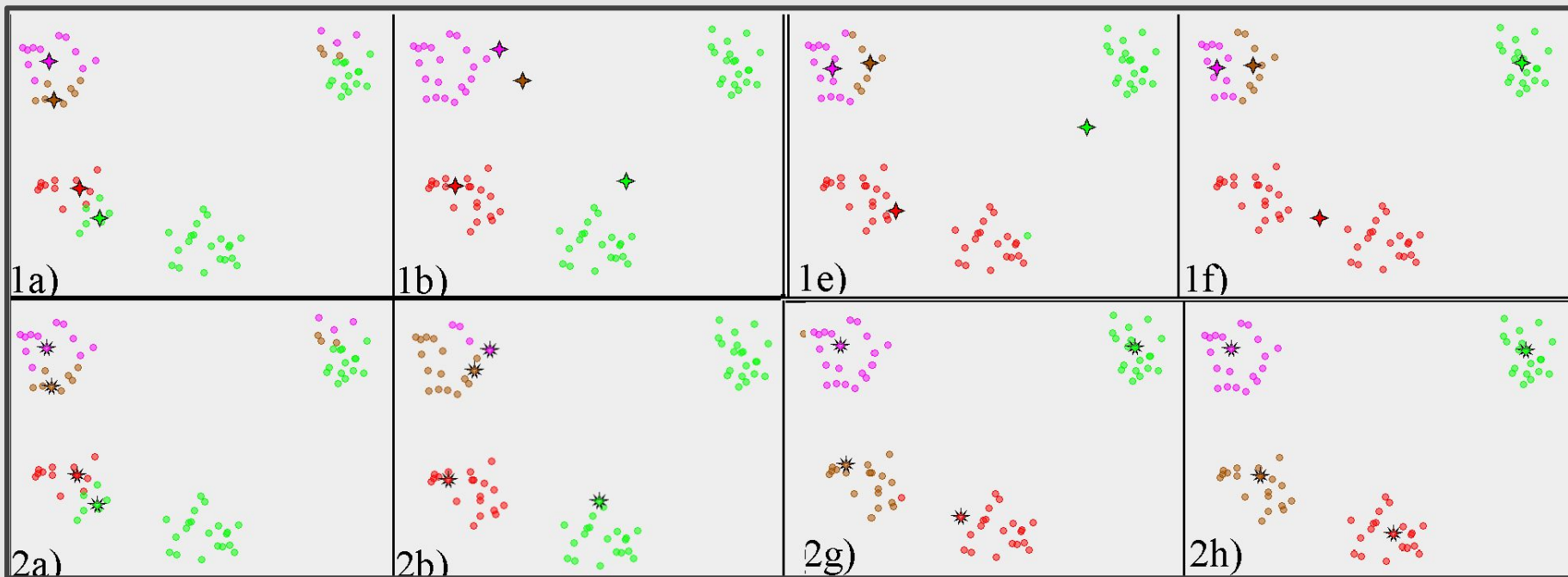
- Uses mini-batches to reduce the computation time, while still attempting to optimize the same objective function.
- Converges faster than k-Means, but the quality of the results is reduced.

# k-Medoids Clustering

- Instead of calculating the mean for each cluster to determine its centroid, one instead **calculates the medoid**.
- Minimizing error over all clusters with respect to the **1-norm distance metric**.
- In contrast to the k-Means, k-Medoids **chooses data points as centroids**.

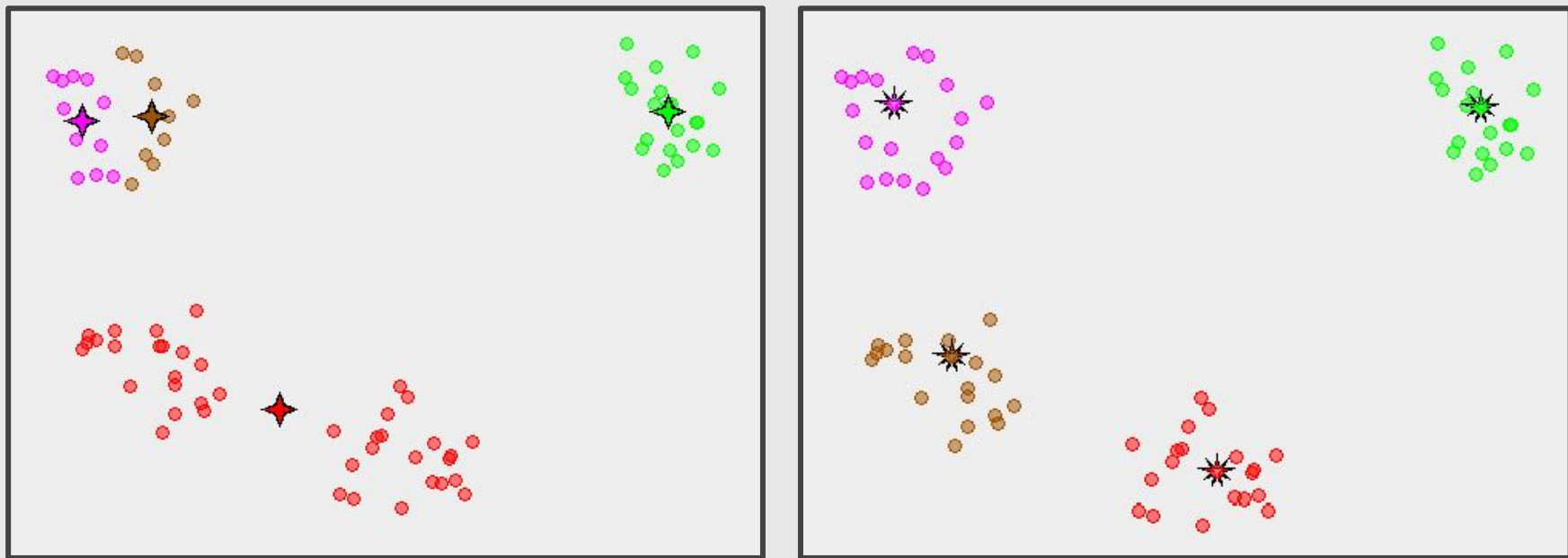


# k-Means (top) vs k-Medoids (bottom)



Credit: [https://commons.wikimedia.org/wiki/File:K-means\\_versus\\_k-medoids.png](https://commons.wikimedia.org/wiki/File:K-means_versus_k-medoids.png)

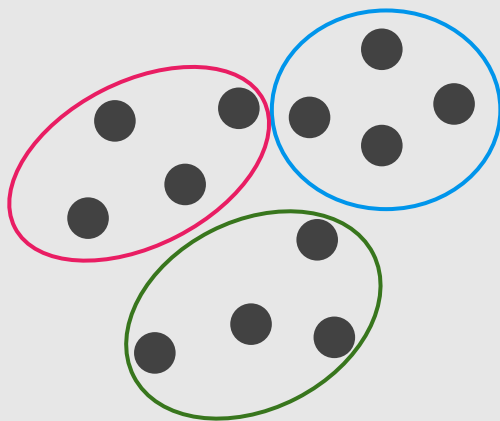
# k-Means (left) vs k-Medoids (right)



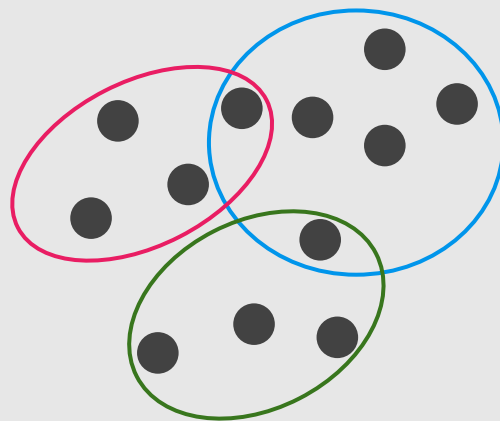
Credit: [https://commons.wikimedia.org/wiki/File:K-means\\_versus\\_k-medoids.png](https://commons.wikimedia.org/wiki/File:K-means_versus_k-medoids.png)

# Fuzzy Clustering (Soft Clustering)

- Each data point can belong to more than one cluster.



Hard clustering



Soft clustering

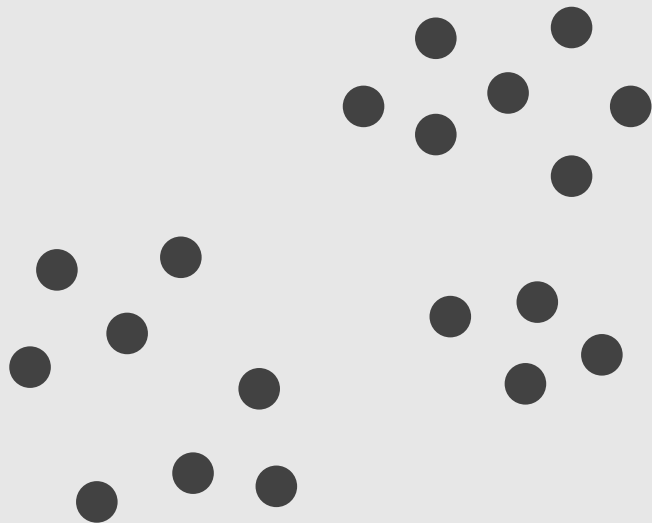
# Today's Agenda

— — —

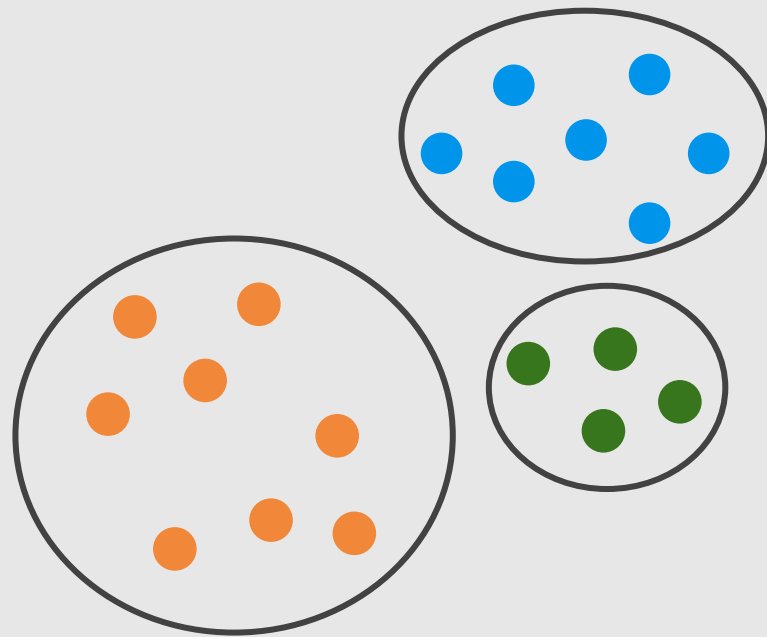
- Clustering
  - k-Means Variations
  - **Hierarchical clustering**
  - DBSCAN Clustering
  - Clustering Performance Evaluation

# Hierarchical Clustering

# Hierarchical versus Partitional

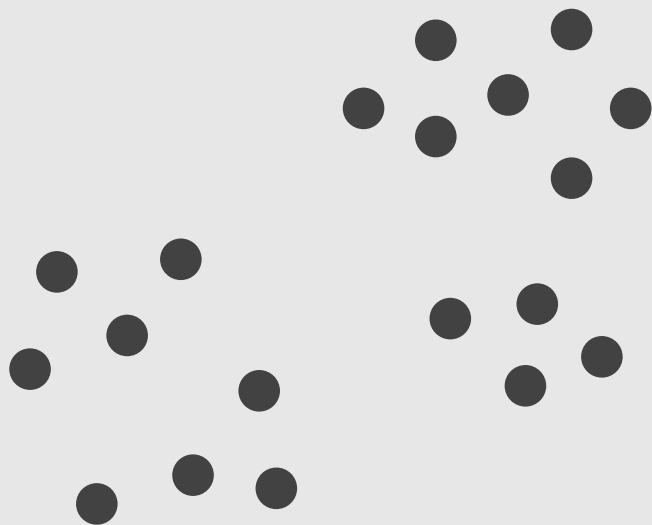


Original data

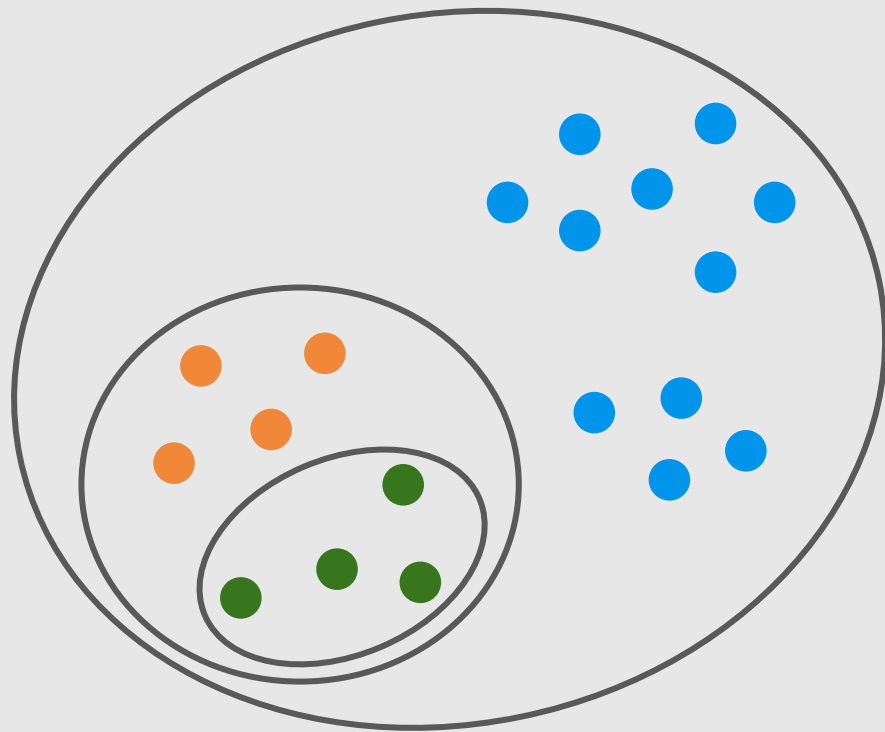


Partitional clustering

# Hierarchical versus Partitional



Original data



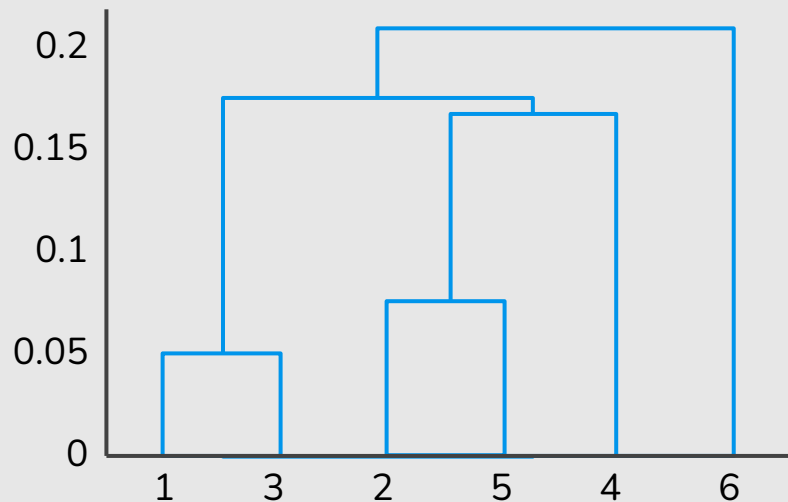
Hierarchical clustering

# Hierarchical Clustering

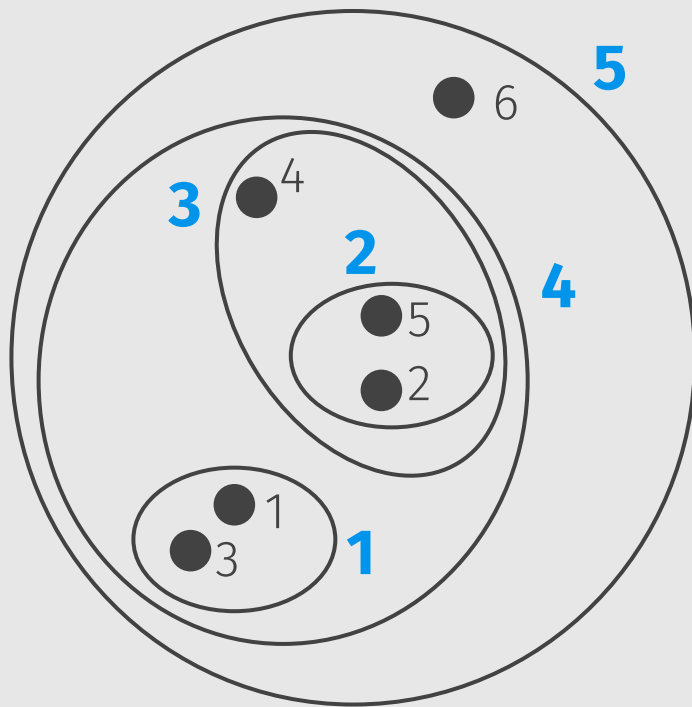
- **Agglomerative** (“bottom up”): each observation **starts in its own cluster**, and pairs of clusters are merged as one moves up the hierarchy.
- **Divisive** (“top down”): all observations **start in one cluster**, and splits are performed recursively as one moves down the hierarchy.



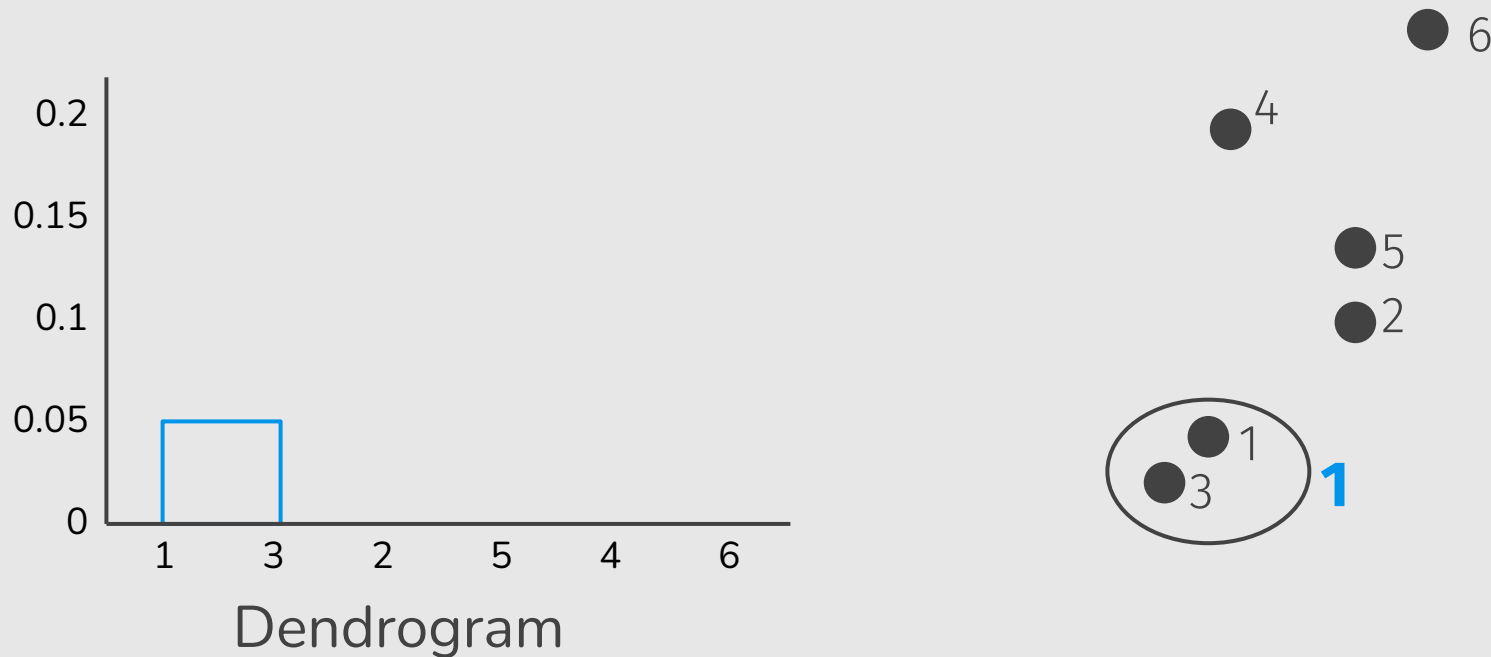
# Agglomerative Hierarchical Clustering



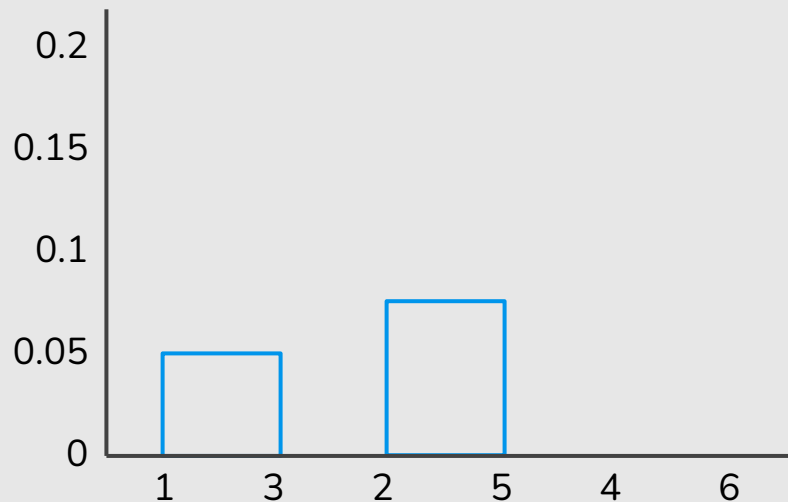
Dendrogram



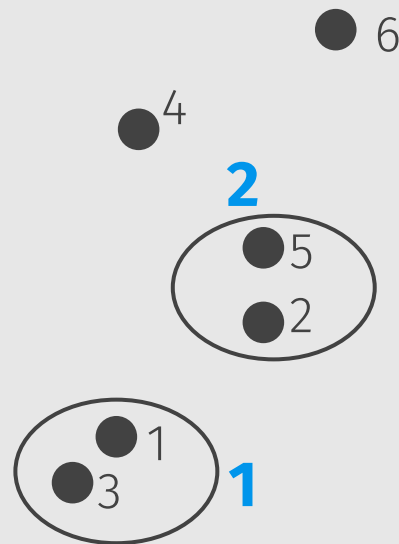
# Agglomerative Hierarchical Clustering



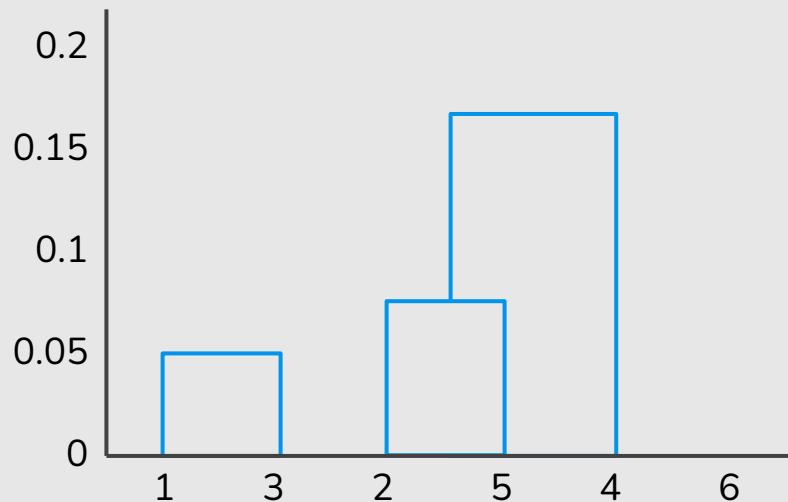
# Agglomerative Hierarchical Clustering



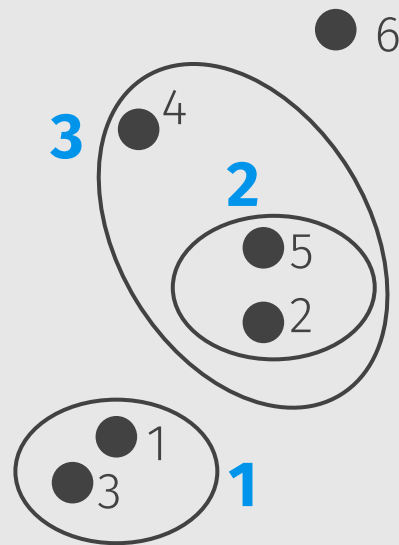
Dendrogram



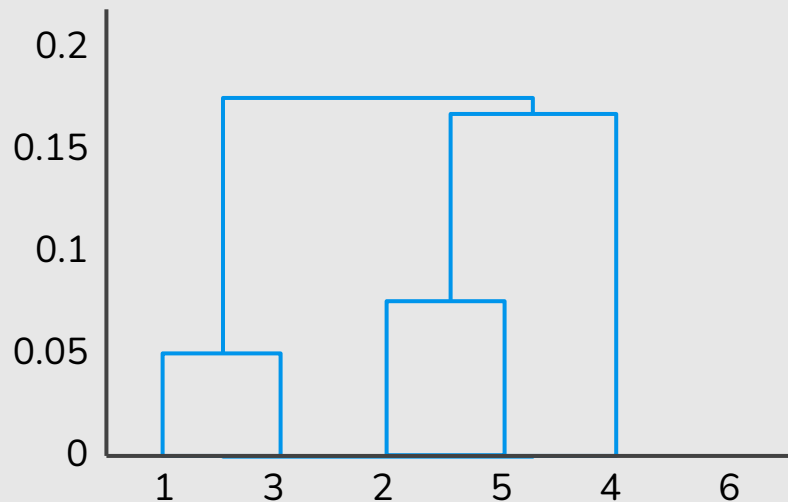
# Agglomerative Hierarchical Clustering



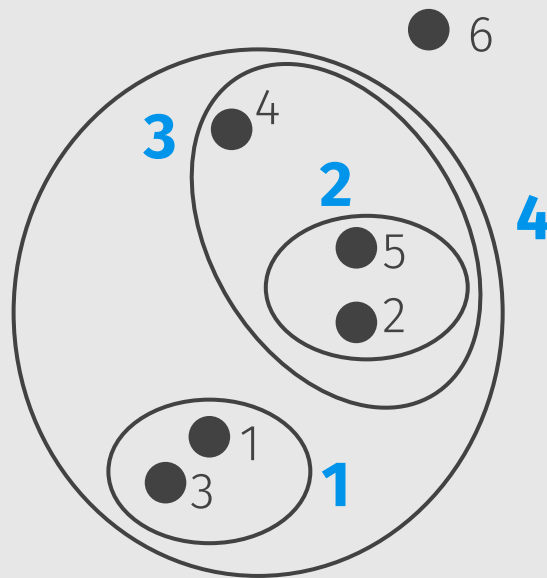
Dendrogram



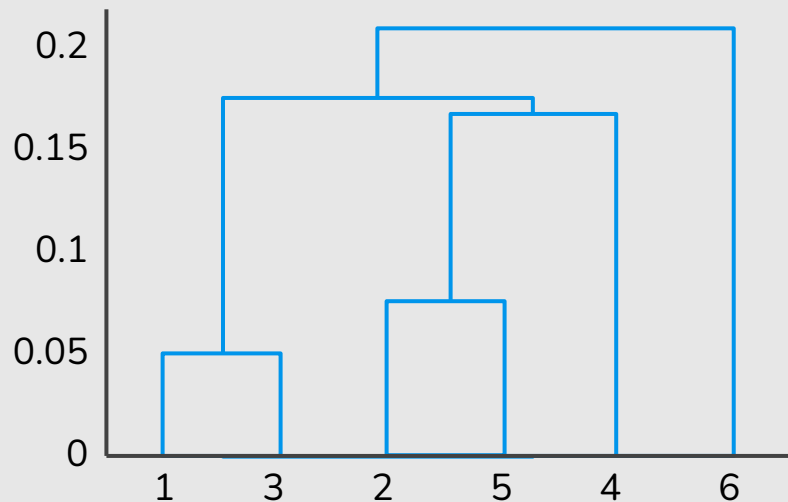
# Agglomerative Hierarchical Clustering



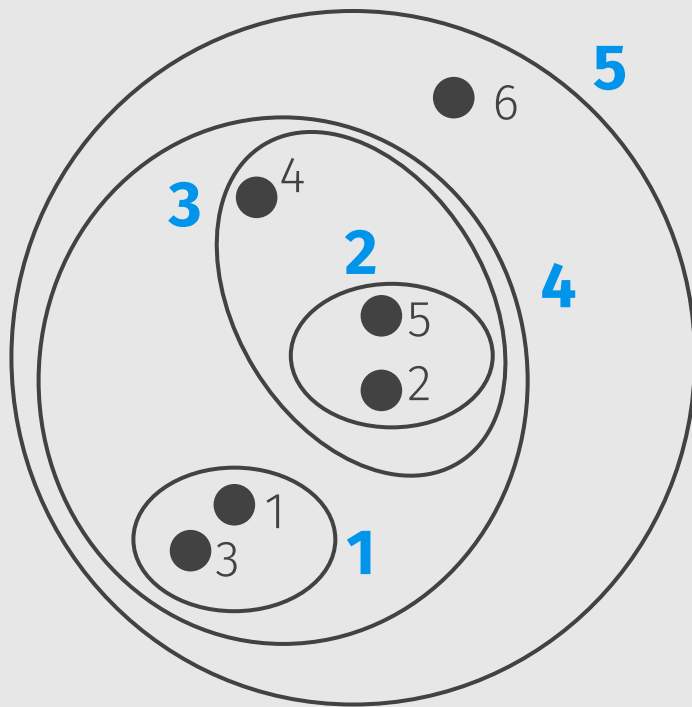
Dendrogram



# Agglomerative Hierarchical Clustering

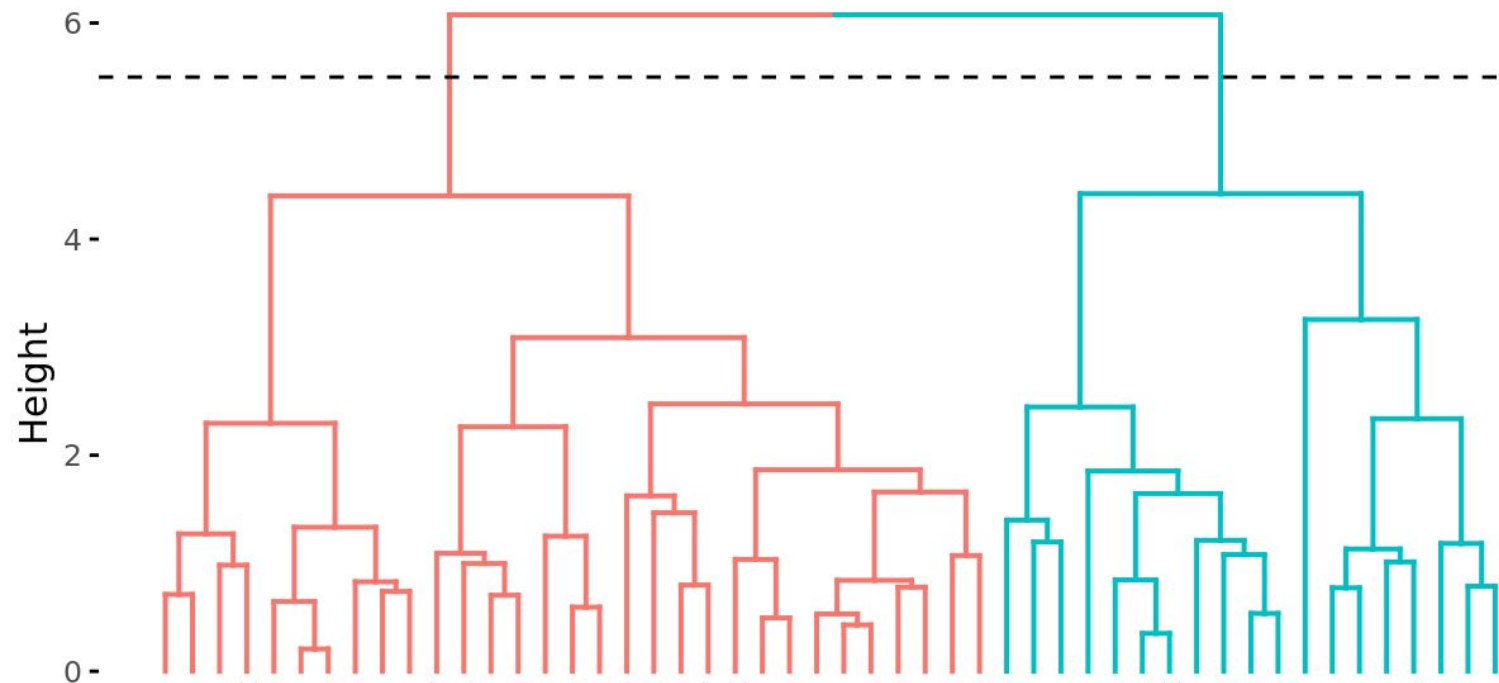


Dendrogram



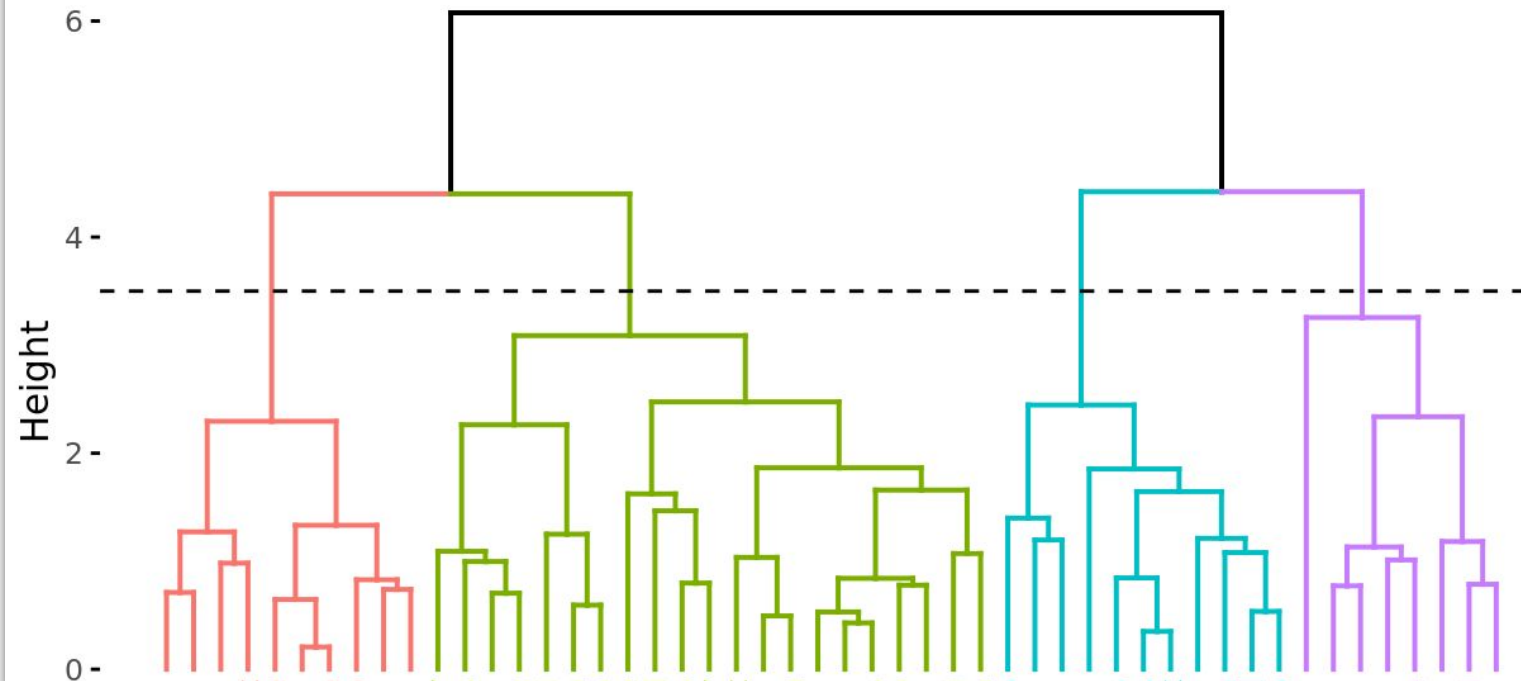
# Herarchical clustering

Distancia euclídea, Linkage complete, K=2



# Herarchical clustering

Distancia euclídea, Linkage complete, K=4

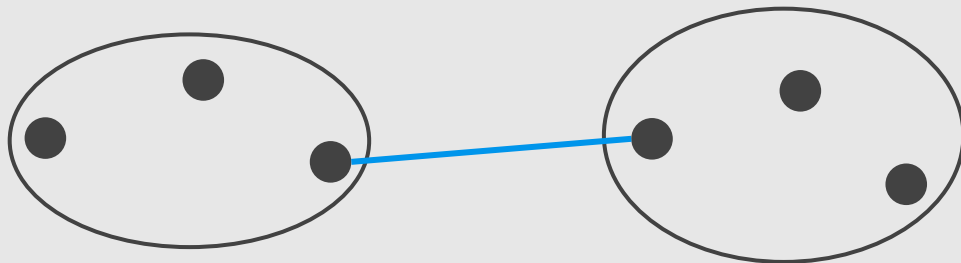




# Agglomerative Hierarchical Clustering

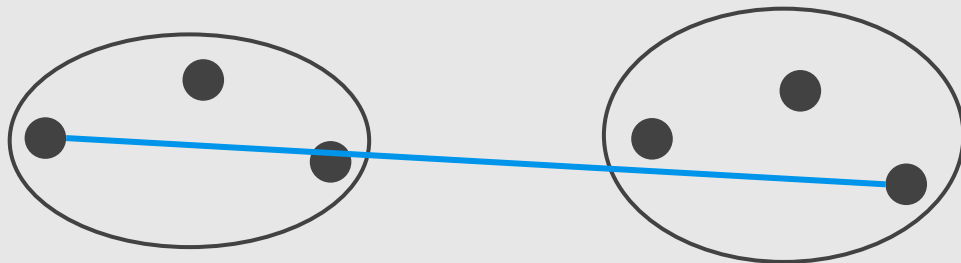
- 1: compute the **proximity matrix**, if necessary.
- 2: **repeat**
- 3:     merge the closest two clusters.
- 4:     update the proximity matrix to reflect the proximity between the new cluster and the original clusters.
- 5: **until** only one cluster remains.

# Defining Proximity between Clusters



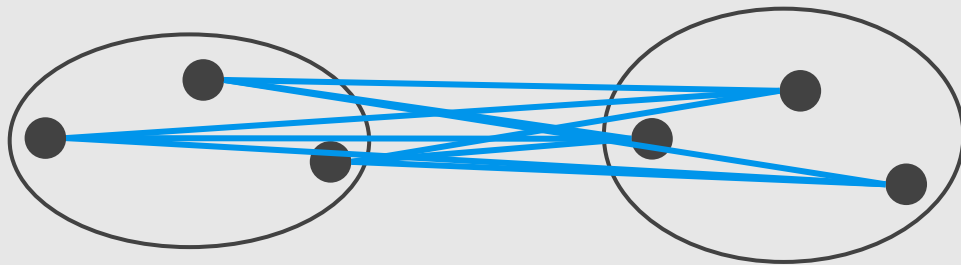
**Single link** or **MIN**: defines cluster proximity as the **proximity** between the closest two points that are in different clusters.

# Defining Proximity between Clusters



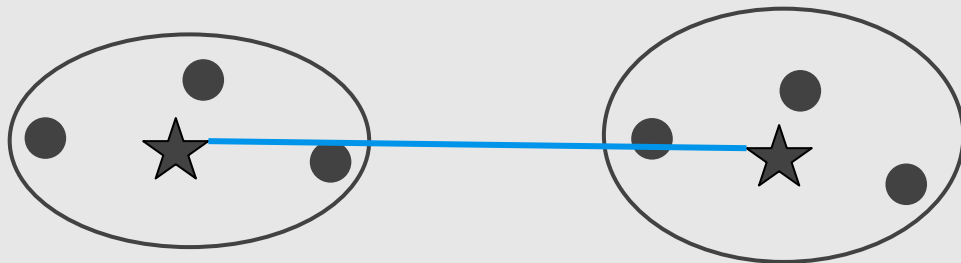
**Complete link** or **MAX**: takes the proximity between the **farthest** two points in different clusters to be the cluster proximity.

# Defining Proximity between Clusters



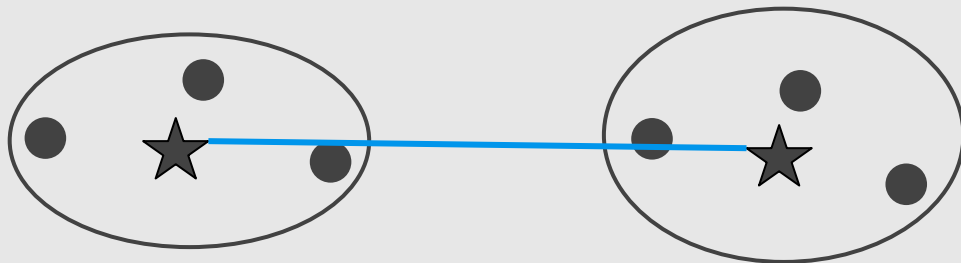
**Average:** defines cluster proximity to be the **average pairwise** proximities of all pairs of points from different clusters.

# Defining Proximity between Clusters



**Centroids:** the cluster proximity is commonly defined as the proximity between cluster centroids.

# Defining Proximity between Clusters



**Ward's:** measures the proximity between two clusters in terms of the increase in the SSE that results from merging the two cluster.

# Agglomerative Hierarchical Clustering

1: compute the **proximity matrix**, if necessary.

2: **repeat**

3:     merge the closest two clusters.

4:     update the proximity matrix to reflect the proximity  
      between the new cluster and the original clusters.

5: **until** only one cluster remains.

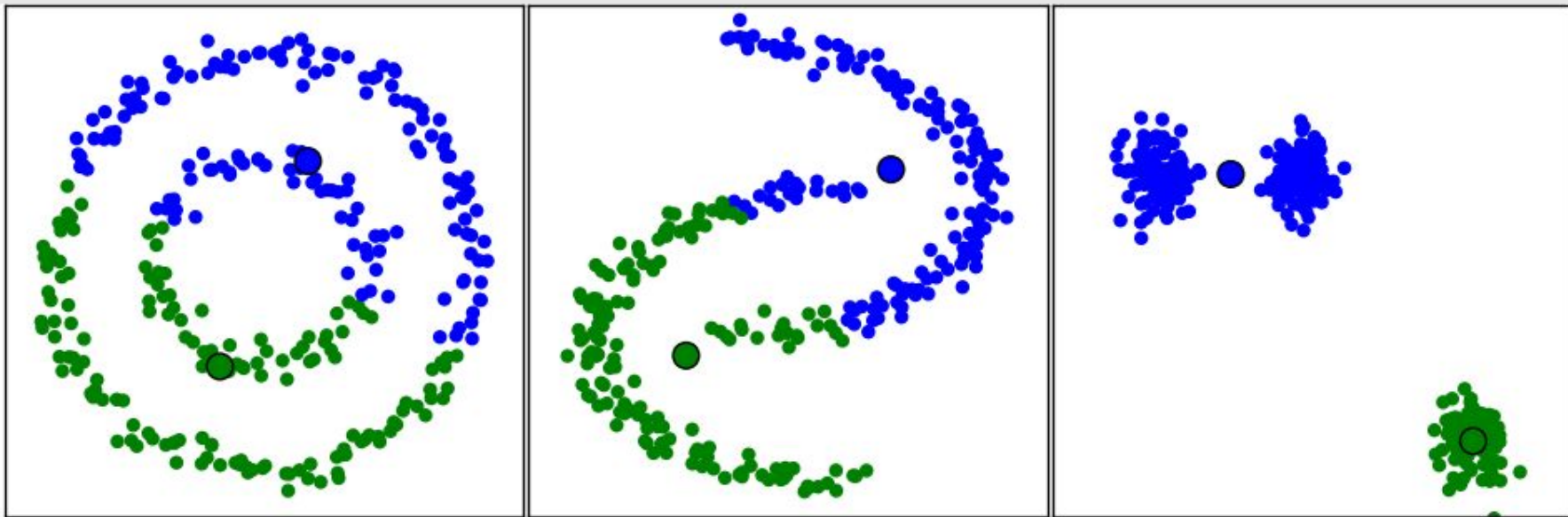
# Today's Agenda

— — —

- Clustering
  - k-Means Variations
  - Hierarchical clustering
  - **DBSCAN Clustering**
  - Clustering Performance Evaluation



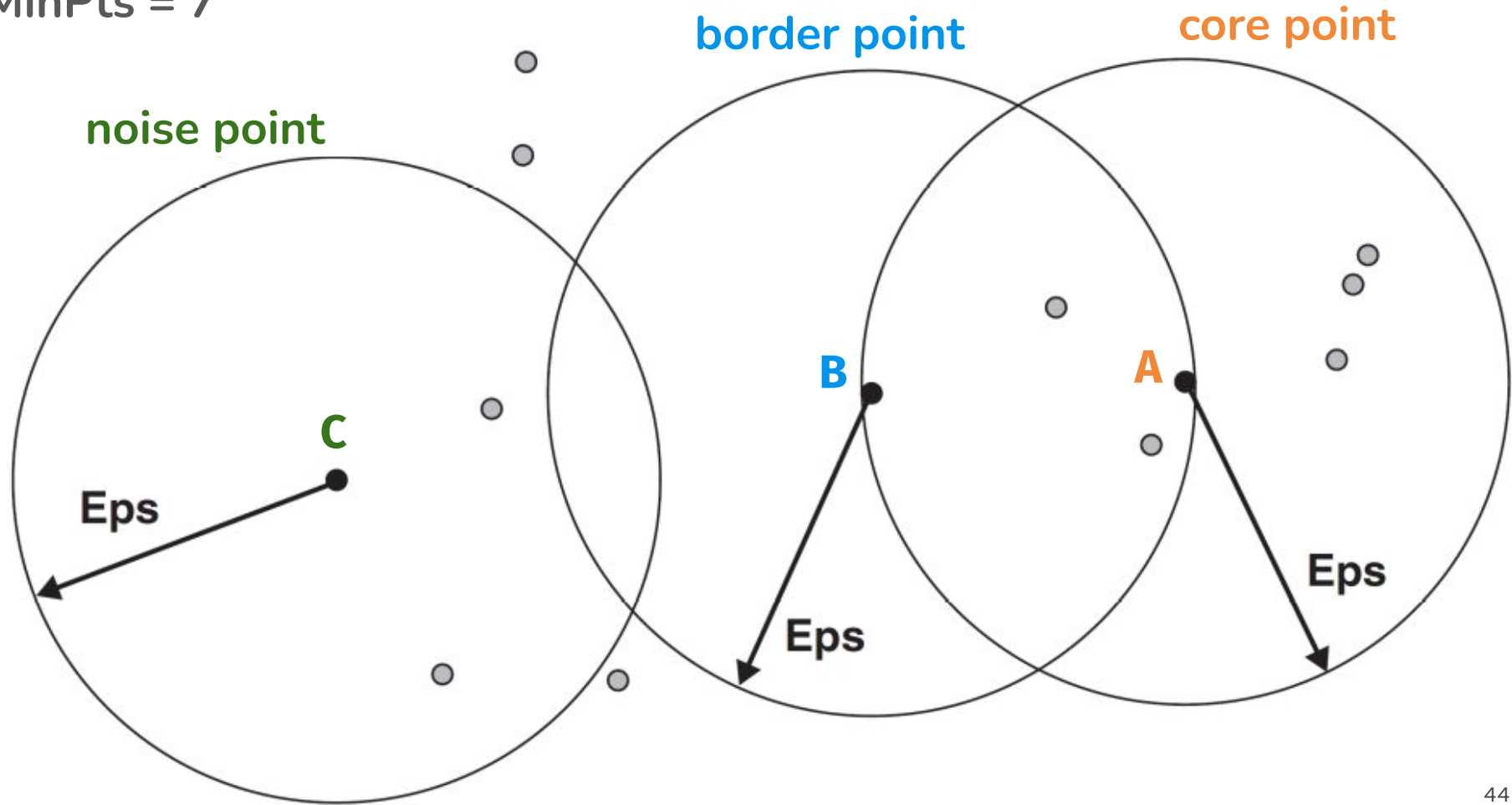
# DBSCAN



# DBSCAN Clustering

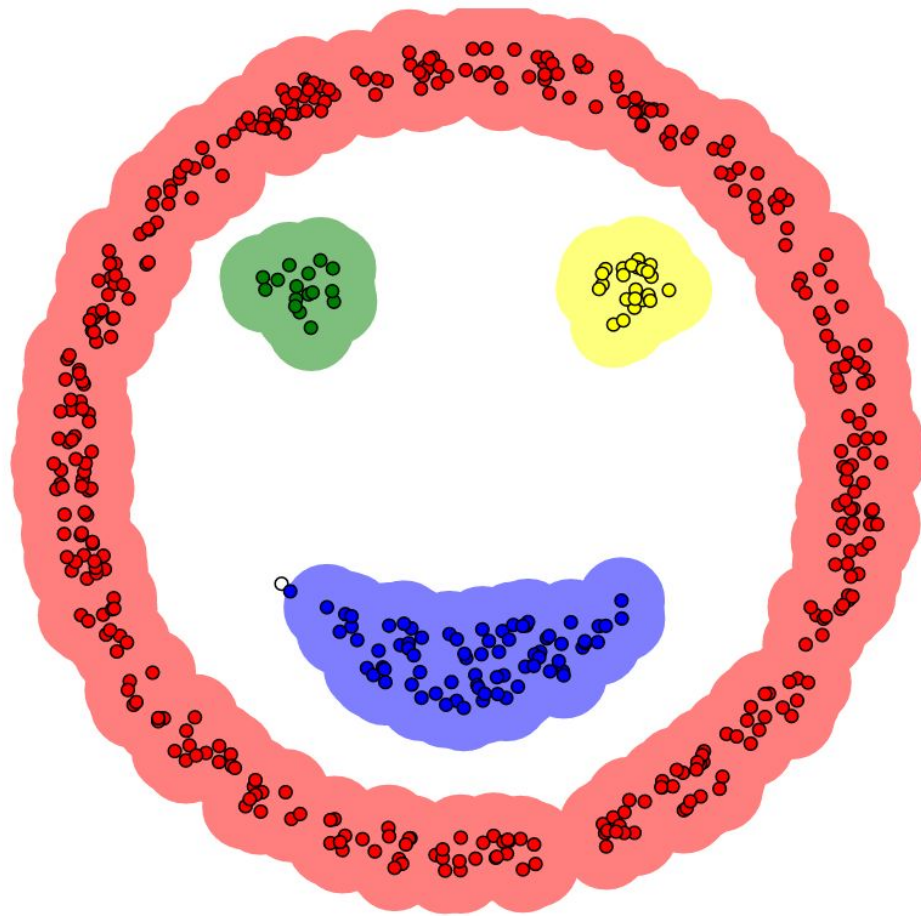
- Density-Based Spatial Clustering of Applications with Noise
- Given a set of points in some space, **it groups together points that are closely packed together** (points with many nearby neighbors), marking as outliers points that lie alone in low-density regions.

MinPts = 7



# DBSCAN Clustering

- **Core points**: A point is a core point if there are at least  $MinPts$  within a distance of  $Eps$ , where  $MinPts$  and  $Eps$  are user-specified parameters.
- **Border points**: A border point is not a core point, but falls within the neighborhood of a core point.
- **Noise points**: A noise point is any point that is neither a core point nor a border point.



epsilon = 1.00  
minPoints = 4

Restart

# DBSCAN Algorithm

1. Start with an **arbitrary** point which has not been visited and its neighborhood information is retrieved from the *Eps* parameter.
2. If this point contains *MinPts* within *Eps* neighborhood, cluster formation starts.

Otherwise the point\* is labeled as **noise**.

\* This point can be later found within the *Eps* neighborhood of a different point and, thus can be made a part of the cluster.

# DBSCAN Algorithm

3. If a point is found to be a **core** point then the points within the *Eps* neighborhood is also part of the cluster. So all the points found within *Eps* neighborhood are added, along with their own *Eps* neighborhood, if they are also **core** points.
4. The process restarts with a new point which can be a part of a new cluster or labeled as **noise**.



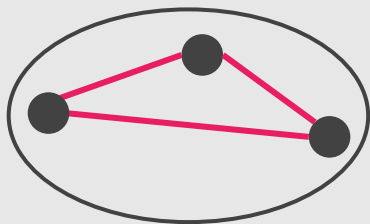
# Clustering Performance Evaluation

# Clustering Evaluation

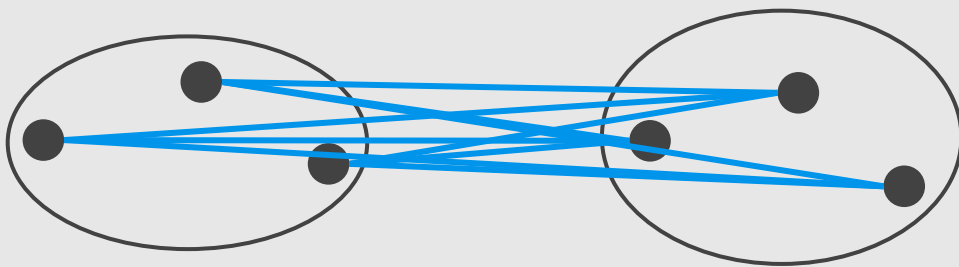
- Evaluating the performance of a clustering algorithm **is not as trivial** as counting the number of errors or the precision and recall of a supervised classification algorithm.
- Adjusted Rand index
- Mutual Information based scores
- Homogeneity, completeness and V-measure
- **Silhouette Coefficient**

# Silhouette Coefficient

- The silhouette value is a measure of how similar a sample is to its own cluster (**cohesion**) compared to other clusters (**separation**).



Cohesion



Separation

# Silhouette Coefficient

- The silhouette value is a measure of how similar a sample is to its own cluster (**cohesion**) compared to other clusters (**separation**).
- The silhouette ranges from  $-1$  to  $+1$ .
  - High value = the clustering configuration is appropriate.
  - Low value = the clustering configuration may have too many or too few clusters.

# Silhouette Coefficient

- The Silhouette Coefficient is defined **for each sample** and is composed of two scores:
  - ***a***: The mean distance between a sample and all other points **in the same cluster**.
  - ***b***: The mean distance between a sample and all other points **in the next nearest cluster**.

# Silhouette Coefficient

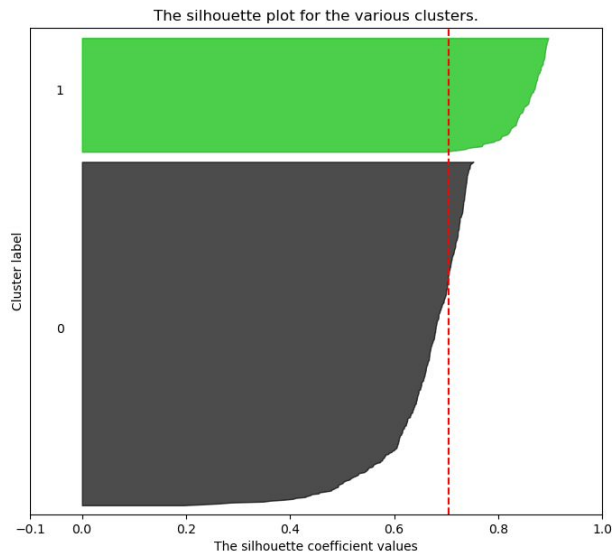
- The Silhouette Coefficient  $s$  for **a single sample** is given as:

$$s = \frac{b - a}{\max(a, b)}$$

- The score is bounded between -1 for incorrect clustering and +1 for highly dense clustering ( $a \ll b$ ). Scores around zero indicate overlapping clusters.

# Silhouette Coefficient

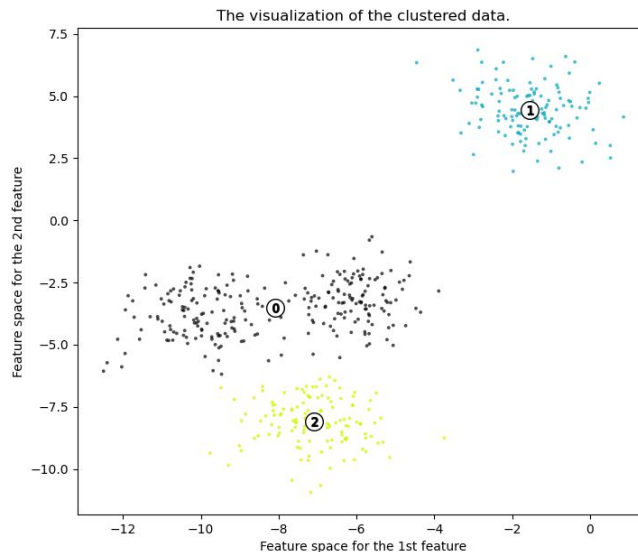
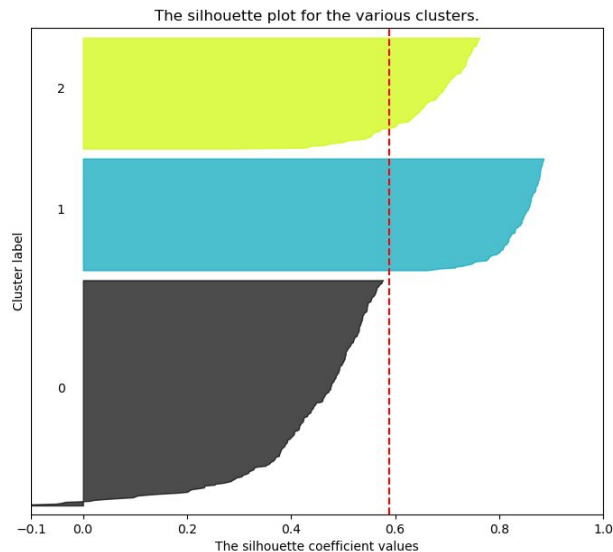
**Silhouette analysis for KMeans clustering on sample data with  $n\_clusters = 2$**



[https://scikit-learn.org/stable/auto\\_examples/cluster/plot\\_kmeans\\_silhouette\\_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py](https://scikit-learn.org/stable/auto_examples/cluster/plot_kmeans_silhouette_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py)

# Silhouette Coefficient

**Silhouette analysis for KMeans clustering on sample data with `n_clusters = 3`**

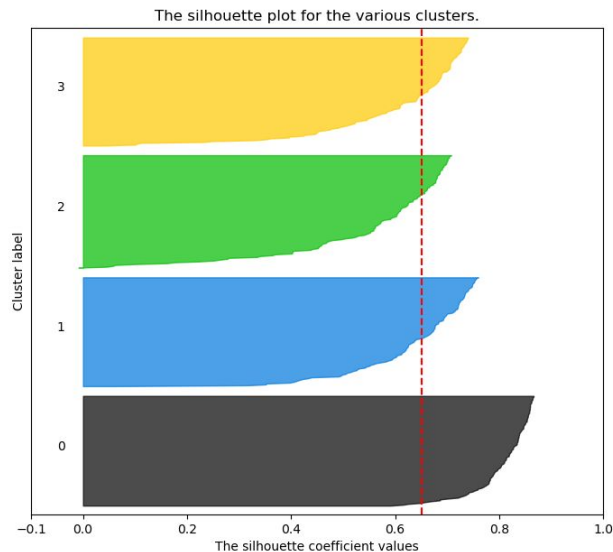


[https://scikit-learn.org/stable/auto\\_examples/cluster/plot\\_kmeans\\_silhouette\\_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py](https://scikit-learn.org/stable/auto_examples/cluster/plot_kmeans_silhouette_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py)



# Silhouette Coefficient

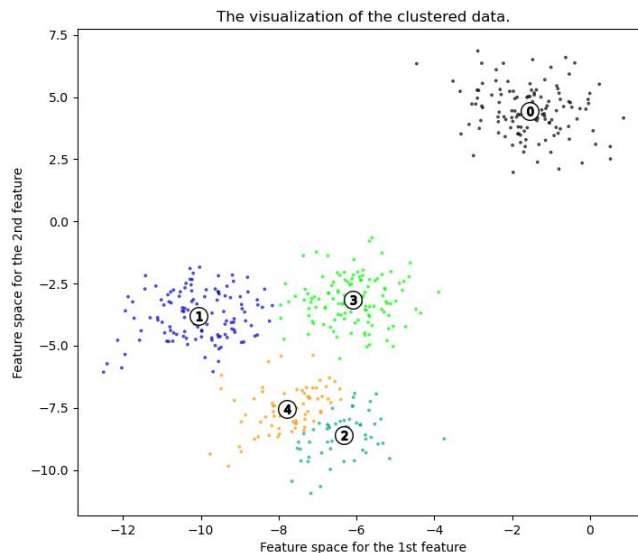
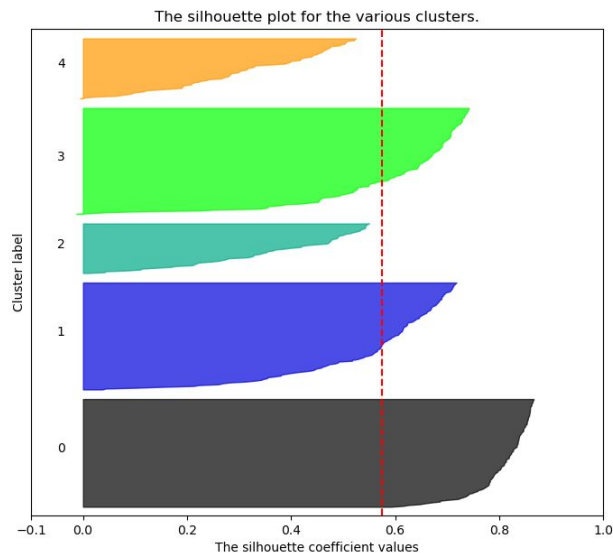
**Silhouette analysis for KMeans clustering on sample data with  $n\_clusters = 4$**



[https://scikit-learn.org/stable/auto\\_examples/cluster/plot\\_kmeans\\_silhouette\\_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py](https://scikit-learn.org/stable/auto_examples/cluster/plot_kmeans_silhouette_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py)

# Silhouette Coefficient

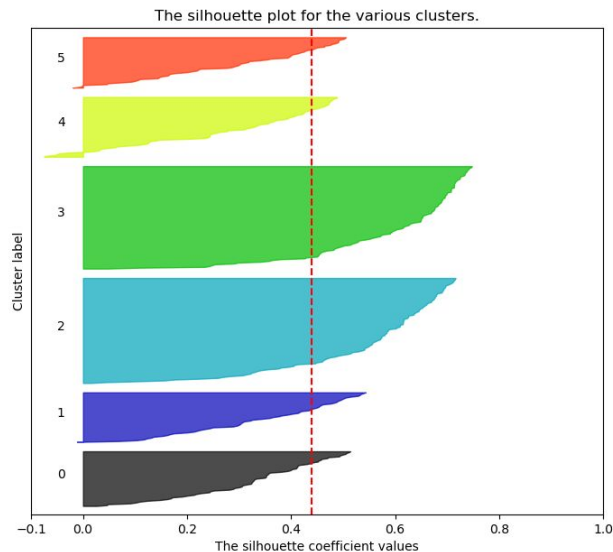
**Silhouette analysis for KMeans clustering on sample data with  $n\_clusters = 5$**



[https://scikit-learn.org/stable/auto\\_examples/cluster/plot\\_kmeans\\_silhouette\\_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py](https://scikit-learn.org/stable/auto_examples/cluster/plot_kmeans_silhouette_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py)

# Silhouette Coefficient

Silhouette analysis for KMeans clustering on sample data with `n_clusters = 6`



[https://scikit-learn.org/stable/auto\\_examples/cluster/plot\\_kmeans\\_silhouette\\_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py](https://scikit-learn.org/stable/auto_examples/cluster/plot_kmeans_silhouette_analysis.html#sphx-qlr-auto-examples-cluster-plot-kmeans-silhouette-analysis-py)



## 2.3. Clustering

### 2.3.1. Overview of clustering methods

#### 2.3.2. K-means

- 2.3.2.1. Mini Batch K-Means

#### 2.3.3. Affinity Propagation

#### 2.3.4. Mean Shift

#### 2.3.5. Spectral clustering

- 2.3.5.1. Different label assignment strategies

#### 2.3.6. Hierarchical clustering

- 2.3.6.1. Different linkage type: Ward, complete and average linkage

- 2.3.6.2. Adding connectivity constraints

- 2.3.6.3. Varying the metric

#### 2.3.7. DBSCAN

#### 2.3.8. Birch

#### 2.3.9. Clustering performance

## 2.3. Clustering

Clustering of unlabeled data can be performed with the module `sklearn.cluster`.

Each clustering algorithm comes in two variants: a class, that implements the `fit` method to learn the clusters on train data, and a function, that, given train data, returns an array of integer labels corresponding to the different clusters. For the class, the labels over the training data can be found in the `labels_` attribute.

### Input data

One important thing to note is that the algorithms implemented in this module can take different kinds of matrix as input. All the methods accept standard data matrices of shape `[n_samples, n_features]`. These can be obtained from the classes in the `sklearn.feature_extraction` module. For `AffinityPropagation`, `SpectralClustering` and `DBSCAN` one can also input similarity matrices of shape `[n_samples, n_samples]`. These can be obtained from the functions in the `sklearn.metrics.pairwise` module.

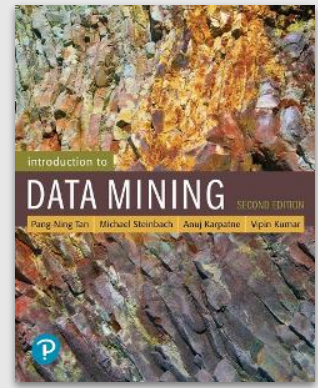
### 2.3.1. Overview of clustering methods

MiniBatchKMeans AffinityPropagation MeanShift SpectralClustering Ward AgglomerativeClustering DBSCAN Birch GaussianMixture



# References

— — —



## Machine Learning Books

- Pattern Recognition and Machine Learning, Chap. 9 “Mixture Models and EM”
- Pattern Classification, Chap. 10 “Unsupervised Learning and Clustering”
- Introduction to Data Mining, Chap. 7 “Cluster Analysis: Basic Concepts and Algorithms” [https://www-users.cs.umn.edu/~kumar001/dmbook/ch7\\_clustering.pdf](https://www-users.cs.umn.edu/~kumar001/dmbook/ch7_clustering.pdf)

## Machine Learning Courses

- <https://www.coursera.org/learn/machine-learning>, Week 8