

1. Finite Differences

Show that the central difference is exact for polynomials of degree 3, i.e. $D_0 p(x) = p'(x)$ for quadratic polynomials p .

Hint: Repeat the error analysis of the lecture but use an explicit formula for the remainder of the Taylor expansion.