

R-4.2

Algorithm mergeSort(S, C)

Input sequence S with n elements, comparator C

Output sequence S sorted according to C

if S.size() > 1 then

$(S_1, S_2) \leftarrow \text{partition}(S, n/2)$

 mergeSort(S_1 , C)

 mergeSort(S_2 , C)

$S \leftarrow \text{merge}(S_1, S_2, C)$

Algorithm merge(A, B, C)

Input sequences A and B with $n/2$ elements each, comparator C

Output sorted sequence of A and B

$S \leftarrow$ empty sequence

while $\neg A.\text{isEmpty}() \wedge \neg B.\text{isEmpty}()$ do

 if C.isLessThan(B.first().element(), A.first().element()) then

$S.\text{insertLast}(B.\text{remove}(B.\text{first}()))$

 else

$S.\text{insertLast}(A.\text{remove}(A.\text{first}()))$

while $\neg A.\text{isEmpty}()$ do

$S.\text{insertLast}(A.\text{remove}(A.\text{first}()))$

While $\neg B.\text{isEmpty}()$ do

$S.\text{insertLast}(B.\text{remove}(B.\text{first}()))$

return S

R-4.5

Algorithm specialMerge(A, B, C)

Input sequences A and B with $n/2$ elements each, comparator C

Output sorted sequence of A and B

$S \leftarrow$ empty sequence

while $\neg A.isEmpty() \wedge \neg B.isEmpty()$ do

 if C.isLessThan(B.first().element(), A.first().element()) then

 S.insertLast(B.remove(B.first()))

 Else if C.isEqual(B.first().element(), A.first().element()) then

 S.insertLast(B.remove(B.first()))

 A.remove(A.first())

 else

 S.insertLast(A.remove(A.first()))

while $\neg A.isEmpty()$ do

 S.insertLast(A.remove(A.first()))

While $\neg B.isEmpty()$ do

 S.insertLast(B.remove(B.first()))

return removeRepeated(s)

Algorithm removeRepeated(s)

For $i \leftarrow 0$ to s.size()-2 do

 If s.elemAtRank(i) = s.elemAtRank(i+1) then

 s.removeAtRank(i)

$i \leftarrow i-1$

return s

R-4.9

Since the list is already sorted then best running time will be the case, which is $O(n \log(n))$

C-4.10

1. Sort the sequence S using Heap-Sort. The running time should be $O(n \log n)$
2. Initialize two variables `currentCount` and `maxCount`
3. Iterate on the sorted sequence, and increment the `currentCount` until the ID changes, then compare `currentCount` with `maxCount`. If `currentCount` is greater than set `maxCount` as `currentCount`. The running time for the operation is $O(n)$

The total running time is $O(n \log n)$