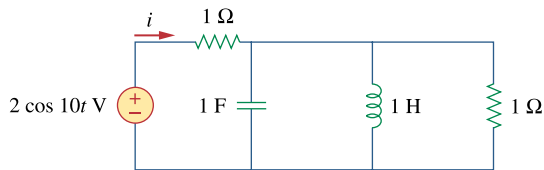


### Chapter 10, Problem 1.

Determine  $i$  in the circuit of Fig. 10.50.



**Figure 10.50**

For Prob. 10.1.

### Chapter 10, Solution 1.

We first determine the input impedance.

$$1 \text{ H} \longrightarrow j\omega L = j1 \times 10 = j10$$

$$1 \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j10 \times 1} = -j0.1$$

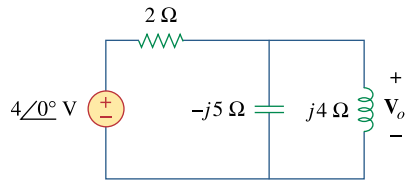
$$Z_{in} = 1 + \left( \frac{1}{j10} + \frac{1}{-j0.1} + \frac{1}{1} \right)^{-1} = 1.0101 - j0.1 = 1.015 \angle -5.653^\circ$$

$$I = \frac{2 \angle 0^\circ}{1.015 \angle -5.653^\circ} = 1.9704 \angle 5.653^\circ$$

$$i(t) = \underline{1.9704 \cos(10t + 5.653^\circ) \text{ A}} = \underline{\underline{1.9704 \cos(10t + 5.65^\circ) \text{ A}}}$$

### Chapter 10, Problem 2.

Solve for  $V_o$  in Fig. 10.51, using nodal analysis.

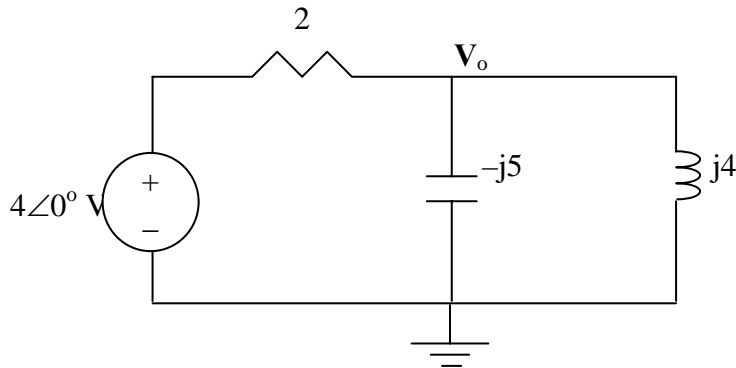


**Figure 10.51**

For Prob. 10.2.

### Chapter 10, Solution 2.

Consider the circuit shown below.



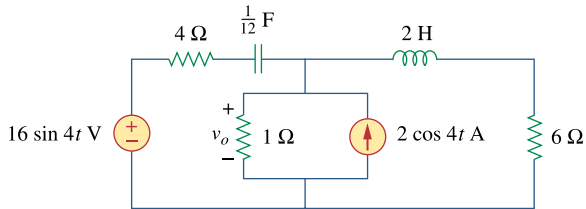
At the main node,

$$\frac{4 - V_o}{2} = \frac{V_o}{-j5} + \frac{V_o}{j4} \quad \longrightarrow \quad 40 = V_o(10 + j)$$

$$V_o = \frac{40}{10 - j} = \underline{3.98 \angle 5.71^\circ \text{ A}}$$

### Chapter 10, Problem 3.

Determine  $v_o$  in the circuit of Fig. 10.52.



**Figure 10.52**

For Prob. 10.3.

### Chapter 10, Solution 3.

$$\omega = 4$$

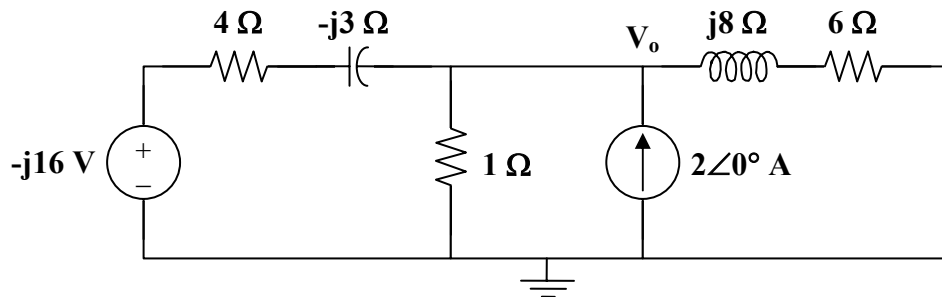
$$2 \cos(4t) \longrightarrow 2 \angle 0^\circ$$

$$16 \sin(4t) \longrightarrow 16 \angle -90^\circ = -j16$$

$$2 \text{ H} \longrightarrow j\omega L = j8$$

$$1/12 \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(4)(1/12)} = -j3$$

The circuit is shown below.



Applying nodal analysis,

$$\frac{-j16 - V_o}{4 - j3} + 2 = \frac{V_o}{1} + \frac{V_o}{6 + j8}$$

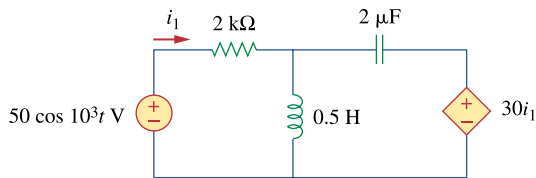
$$\frac{-j16}{4 - j3} + 2 = \left( 1 + \frac{1}{4 - j3} + \frac{1}{6 + j8} \right) V_o$$

$$V_o = \frac{3.92 - j2.56}{1.22 + j0.04} = \frac{4.682 \angle -33.15^\circ}{1.2207 \angle 1.88^\circ} = 3.835 \angle -35.02^\circ$$

Therefore,  $v_o(t) = \underline{\underline{3.835 \cos(4t - 35.02^\circ) \text{ V}}}$

### Chapter 10, Problem 4.

Determine  $i_1$  in the circuit of Fig. 10.53.



**Figure 10.53**

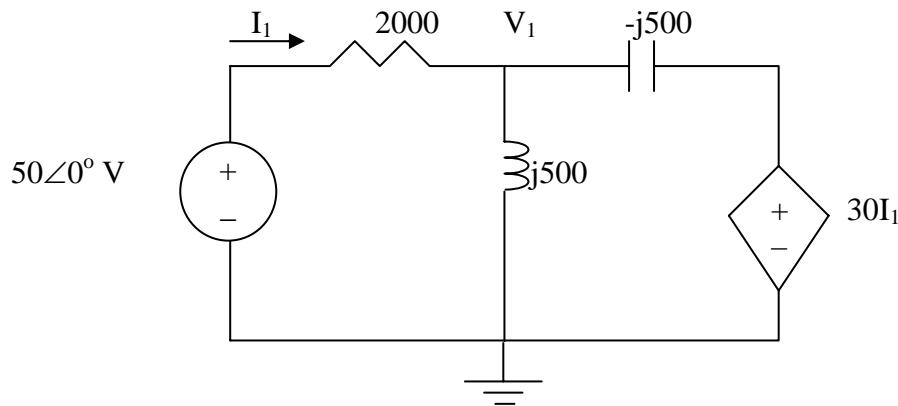
For Prob. 10.4.

### Chapter 10, Solution 4.

$$0.5 H \longrightarrow j\omega L = j0.5 \times 10^3 = j500$$

$$2 \mu F \longrightarrow \frac{1}{j\omega C} = \frac{1}{j10^3 \times 2 \times 10^{-6}} = -j500$$

Consider the circuit as shown below.



At node 1,

$$\frac{50 - V_1}{2000} + \frac{30I_1 - V_1}{-j500} = \frac{V_1}{j500}$$

$$\text{But } I_1 = \frac{50 - V_1}{2000}$$

$$50 - V_1 + j4 \times 30 \left( \frac{50 - V_1}{2000} \right) + j4 V_1 - j4 V_1 = 0 \quad \rightarrow \quad V_1 = 50$$

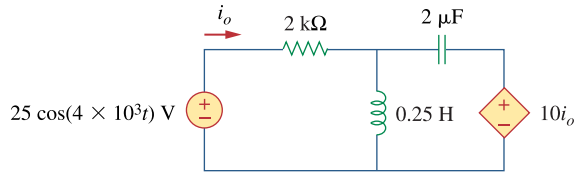
$$I_1 = \frac{50 - V_1}{2000} = 0$$

$$i_1(t) = 0 \text{ A}$$

### Chapter 10, Problem 5.



Find  $i_o$  in the circuit of Fig. 10.54.



**Figure 10.54**

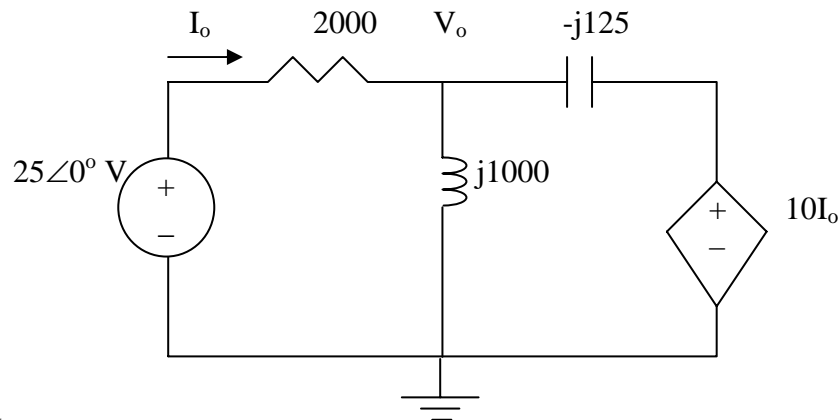
For Prob. 10.5.

### Chapter 10, Solution 5.

$$0.25\text{ H} \longrightarrow j\omega L = j0.25 \times 4 \times 10^3 = j1000$$

$$2\text{ }\mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j4 \times 10^3 \times 2 \times 10^{-6}} = -j125$$

Consider the circuit as shown below.



At node  $V_o$ ,

$$\begin{aligned} \frac{V_o - 25}{2000} + \frac{V_o - 0}{j1000} + \frac{V_o - 10I_o}{-j125} &= 0 \\ V_o - 25 - j2V_o + j16V_o - j160I_o &= 0 \\ (1 + j14)V_o - j160I_o &= 25 \end{aligned}$$

$$\text{But } I_o = (25 - V_o)/2000$$

$$\begin{aligned} (1 + j14)V_o - j2 + j0.08V_o &= 25 \\ V_o &= \frac{25 + j2}{1 + j14.08} = \frac{25.08 \angle 4.57^\circ}{14.115 \angle 58.94^\circ} = 1.7768 \angle -81.37^\circ \end{aligned}$$

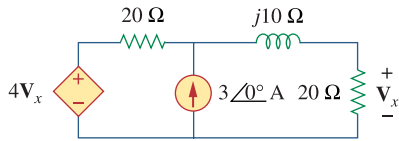
Now to solve for  $i_o$ ,

$$\begin{aligned} I_o &= \frac{25 - V_o}{2000} = \frac{25 - 0.2666 + j1.7567}{2000} = 12.367 + j0.8784 \text{ mA} \\ &= 12.398 \angle 4.06^\circ \end{aligned}$$

$$i_o = \underline{\underline{12.398 \cos(4 \times 10^3 t + 4.06^\circ) \text{ mA}}}$$

### Chapter 10, Problem 6.

Determine  $V_x$  in Fig. 10.55.



**Figure 10.55**  
For Prob. 10.6.

### Chapter 10, Solution 6.

Let  $V_o$  be the voltage across the current source. Using nodal analysis we get:

$$\frac{V_o - 4V_x}{20} - 3 + \frac{V_o}{20 + j10} = 0 \quad \text{where} \quad V_x = \frac{20}{20 + j10} V_o$$

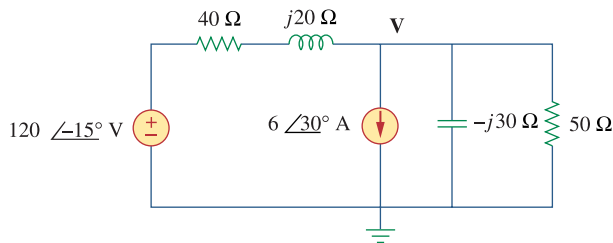
Combining these we get:

$$\frac{V_o}{20} - \frac{4V_o}{20 + j10} - 3 + \frac{V_o}{20 + j10} = 0 \rightarrow (1 + j0.5 - 3)V_o = 60 + j30$$

$$V_o = \frac{60 + j30}{-2 + j0.5} \quad \text{or} \quad V_x = \frac{20(3)}{-2 + j0.5} = \underline{\underline{29.11 \angle -166^\circ \text{ V}}}.$$

### Chapter 10, Problem 7.

Use nodal analysis to find  $V$  in the circuit of Fig. 10.56.



**Figure 10.56**  
For Prob. 10.7.

### Chapter 10, Solution 7.

At the main node,

$$\frac{120\angle -15^\circ - V}{40 + j20} = 6\angle 30^\circ + \frac{V}{-j30} + \frac{V}{50} \longrightarrow \frac{115.91 - j31.058}{40 + j20} - 5.196 - j3 =$$

$$V \left( \frac{1}{40 + j20} + \frac{j}{30} + \frac{1}{50} \right)$$

$$V = \frac{-3.1885 - j4.7805}{0.04 + j0.0233} = \underline{124.08\angle -154^\circ \text{ V}}$$

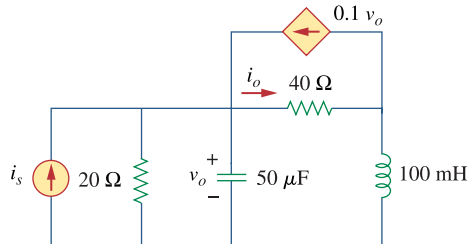


### Chapter 10, Problem 8.



Use nodal analysis to find current  $i_o$  in the circuit of Fig. 10.57. Let

$$i_s = 6 \cos(200t + 15^\circ) \text{ A.}$$



**Figure 10.57**

For Prob. 10.8.

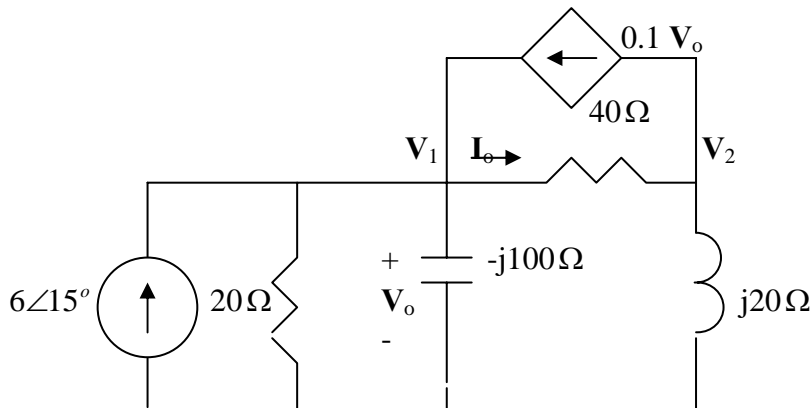
### Chapter 10, Solution 8.

$$\omega = 200,$$

$$100\text{mH} \longrightarrow j\omega L = j200 \times 0.1 = j20$$

$$50\mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j200 \times 50 \times 10^{-6}} = -j100$$

The frequency-domain version of the circuit is shown below.



At node 1,

$$6\angle 15^\circ + 0.1V_1 = \frac{V_1}{20} + \frac{V_1}{-j100} + \frac{V_1 - V_2}{40}$$

$$\text{or} \quad 5.7955 + j1.5529 = (-0.025 + j0.01)V_1 - 0.025V_2 \quad (1)$$

At node 2,

$$\frac{V_1 - V_2}{40} = 0.1V_1 + \frac{V_2}{j20} \quad \longrightarrow \quad 0 = 3V_1 + (1 - j2)V_2 \quad (2)$$

From (1) and (2),

$$\begin{bmatrix} (-0.025 + j0.01) & -0.025 \\ 3 & (1 - j2) \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} (5.7955 + j1.5529) \\ 0 \end{bmatrix} \quad \text{or} \quad \mathbf{AV} = \mathbf{B}$$

Using MATLAB,

$$\mathbf{V} = \text{inv}(\mathbf{A}) * \mathbf{B}$$

leads to  $V_1 = -70.63 - j127.23$ ,  $V_2 = -110.3 + j161.09$

$$I_o = \frac{V_1 - V_2}{40} = 7.276\angle -82.17^\circ$$

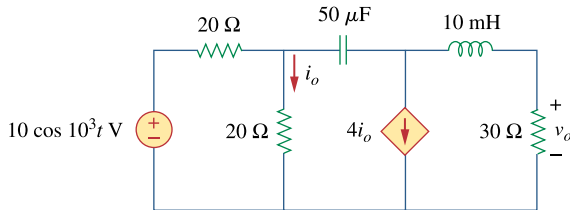
Thus,

$$\underline{i_o(t) = 7.276 \cos(200t - 82.17^\circ) \text{ A}}$$

### Chapter 10, Problem 9.



Use nodal analysis to find  $v_o$  in the circuit of Fig. 10.58.



**Figure 10.58**

For Prob. 10.9.

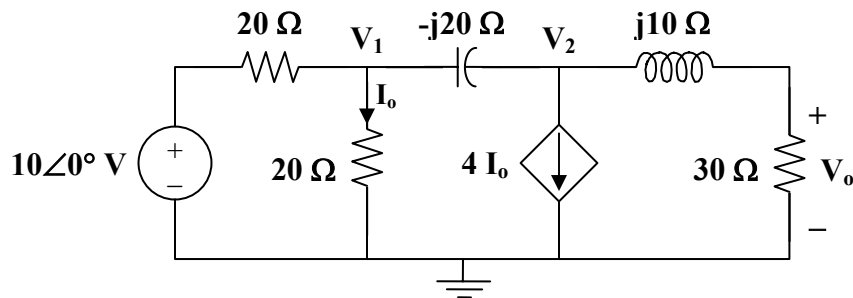
### Chapter 10, Solution 9.

$$10 \cos(10^3 t) \longrightarrow 10 \angle 0^\circ, \quad \omega = 10^3$$

$$10 \text{ mH} \longrightarrow j\omega L = j10$$

$$50 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10^3)(50 \times 10^{-6})} = -j20$$

Consider the circuit shown below.



At node 1,

$$\begin{aligned} \frac{10 - V_1}{20} &= \frac{V_1}{20} + \frac{V_1 - V_2}{-j20} \\ 10 &= (2 + j)V_1 - jV_2 \end{aligned} \quad (1)$$

At node 2,

$$\begin{aligned} \frac{V_1 - V_2}{-j20} &= (4) \frac{V_1}{20} + \frac{V_2}{30 + j10}, \text{ where } I_o = \frac{V_1}{20} \text{ has been substituted.} \\ (-4 + j)V_1 &= (0.6 + j0.8)V_2 \\ V_1 &= \frac{0.6 + j0.8}{-4 + j} V_2 \end{aligned} \quad (2)$$

Substituting (2) into (1)

$$10 = \frac{(2 + j)(0.6 + j0.8)}{-4 + j} V_2 - jV_2$$

or

$$V_2 = \frac{170}{0.6 - j26.2}$$

$$V_o = \frac{30}{30 + j10} V_2 = \frac{3}{3 + j} \cdot \frac{170}{0.6 - j26.2} = 6.154 \angle 70.26^\circ$$

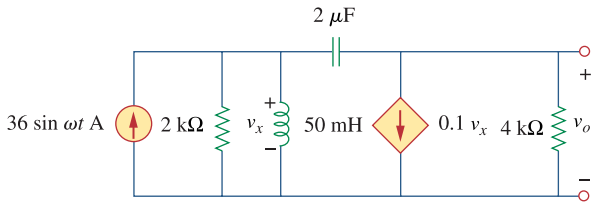
Therefore,

$$v_o(t) = \underline{\underline{6.154 \cos(10^3 t + 70.26^\circ) \text{ V}}}$$

### Chapter 10, Problem 10.



Use nodal analysis to find  $v_o$  in the circuit of Fig. 10.59. Let  $\omega = 2 \text{ krad/s}$ .



**Figure 10.59**

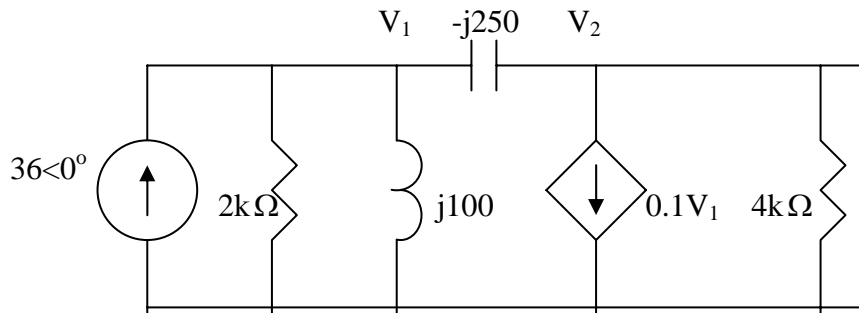
For Prob. 10.10.

### Chapter 10, Solution 10.

$$50 \text{ mH} \longrightarrow j\omega L = j2000 \times 50 \times 10^{-3} = j100, \quad \omega = 2000$$

$$2 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j2000 \times 2 \times 10^{-6}} = -j250$$

Consider the frequency-domain equivalent circuit below.



At node 1,

$$36 = \frac{V_1}{2000} + \frac{V_1}{j100} + \frac{V_1 - V_2}{-j250} \longrightarrow 36 = (0.0005 - j0.006)V_1 - j0.004V_2 \quad (1)$$

At node 2,

$$\frac{V_1 - V_2}{-j250} = 0.1V_1 + \frac{V_2}{4000} \longrightarrow 0 = (0.1 - j0.004)V_1 + (0.00025 + j0.004)V_2 \quad (2)$$

Solving (1) and (2) gives

$$V_o = V_2 = -535.6 + j893.5 = 8951.1 \angle 93.43^\circ$$

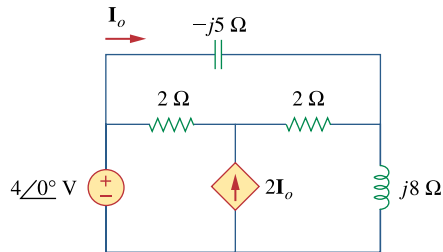
$$v_o(t) = \underline{\underline{8.951 \sin(2000t + 93.43^\circ) \text{ kV}}}$$

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### Chapter 10, Problem 11.



Apply nodal analysis to the circuit in Fig. 10.60 and determine  $\mathbf{I}_o$ .

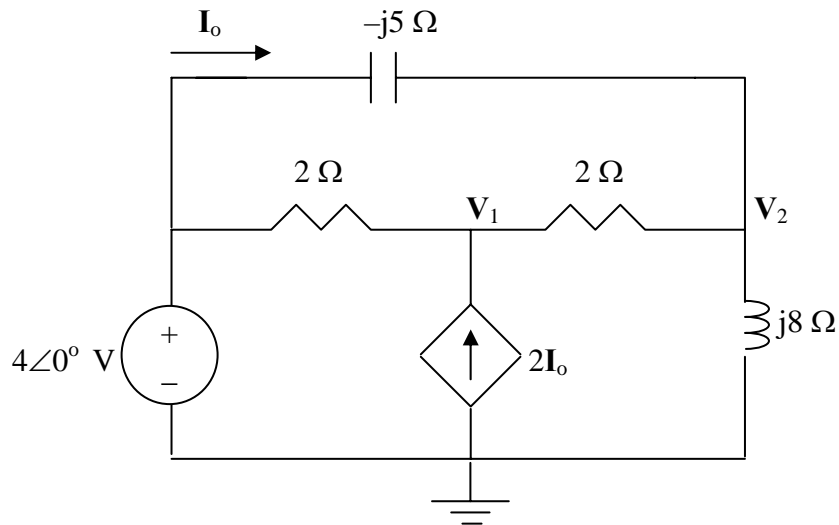


**Figure 10.60**

For Prob. 10.11.

### Chapter 10, Solution 11.

Consider the circuit as shown below.



At node 1,

$$\frac{V_1 - 4}{2} - 2I_o + \frac{V_1 - V_2}{2} = 0$$
$$V_1 - 0.5V_2 - 2I_o = 2$$

$$\text{But, } I_o = (4 - V_2)/(-j5) = -j0.2V_2 + j0.8$$

Now the first node equation becomes,

$$V_1 - 0.5V_2 + j0.4V_2 - j1.6 = 2 \text{ or}$$
$$V_1 + (-0.5 + j0.4)V_2 = 2 + j1.6$$

At node 2,

$$\frac{V_2 - V_1}{2} + \frac{V_2 - 4}{-j5} + \frac{V_2 - 0}{j8} = 0$$
$$-0.5V_1 + (0.5 + j0.075)V_2 = j0.8$$

Using MATLAB to solve this, we get,

$$>> Y = [1, (-0.5 + 0.4i); -0.5, (0.5 + 0.075i)]$$

$$Y =$$

$$\begin{array}{cc} 1.0000 & -0.5000 + 0.4000i \\ -0.5000 & 0.5000 + 0.0750i \end{array}$$

$$>> I = [(2 + 1.6i); 0.8i]$$

$$I =$$

$$\begin{array}{c} 2.0000 + 1.6000i \\ 0 + 0.8000i \end{array}$$

$$>> V = \text{inv}(Y) * I$$

$$V =$$

$$\begin{array}{c} 4.8597 + 0.0543i \\ 4.9955 + 0.9050i \end{array}$$

$$I_o = -j0.2V_2 + j0.8 = -j0.9992 + 0.01086 + j0.8 = 0.01086 - j0.1992$$

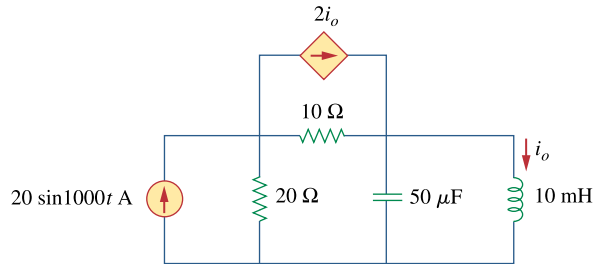
$$= \underline{\underline{199.5 \angle 86.89^\circ \text{ mA}}}.$$

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### Chapter 10, Problem 12.



By nodal analysis, find  $i_o$  in the circuit of Fig. 10.61.



**Figure 10.61**

For Prob. 10.12.

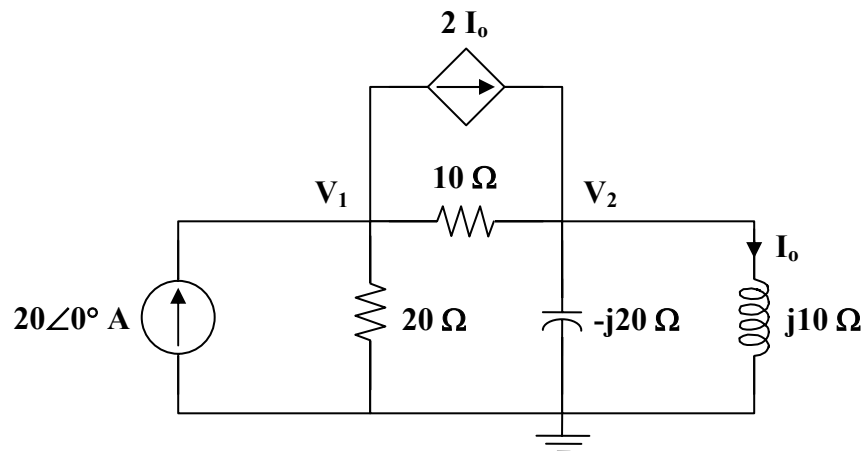
### Chapter 10, Solution 12.

$$20 \sin(1000t) \longrightarrow 20 \angle 0^\circ, \quad \omega = 1000$$

$$10 \text{ mH} \longrightarrow j\omega L = j10$$

$$50 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10^3)(50 \times 10^{-6})} = -j20$$

The frequency-domain equivalent circuit is shown below.





At node 1,

$$20 = 2\mathbf{I}_o + \frac{\mathbf{V}_1}{20} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{10},$$

where

$$\mathbf{I}_o = \frac{\mathbf{V}_2}{j10}$$

$$20 = \frac{2\mathbf{V}_2}{j10} + \frac{\mathbf{V}_1}{20} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{10}$$

$$400 = 3\mathbf{V}_1 - (2 + j4)\mathbf{V}_2 \quad (1)$$

At node 2,

$$\frac{2\mathbf{V}_2}{j10} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{10} = \frac{\mathbf{V}_2}{-j20} + \frac{\mathbf{V}_2}{j10}$$

$$j2\mathbf{V}_1 = (-3 + j2)\mathbf{V}_2$$

or

$$\mathbf{V}_1 = (1 + j1.5)\mathbf{V}_2 \quad (2)$$

Substituting (2) into (1),

$$400 = (3 + j4.5)\mathbf{V}_2 - (2 + j4)\mathbf{V}_2 = (1 + j0.5)\mathbf{V}_2$$

$$\mathbf{V}_2 = \frac{400}{1 + j0.5}$$

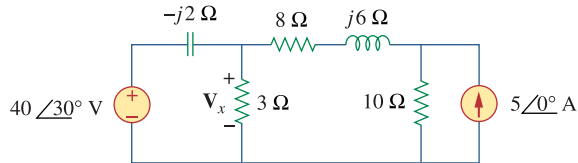
$$\mathbf{I}_o = \frac{\mathbf{V}_2}{j10} = \frac{40}{j(1 + j0.5)} = 35.74 \angle -116.6^\circ$$

Therefore,  $i_o(t) = \underline{\underline{35.74 \sin(1000t - 116.6^\circ) \text{ A}}}$

### Chapter 10, Problem 13.



Determine  $V_x$  in the circuit of Fig. 10.62 using any method of your choice.

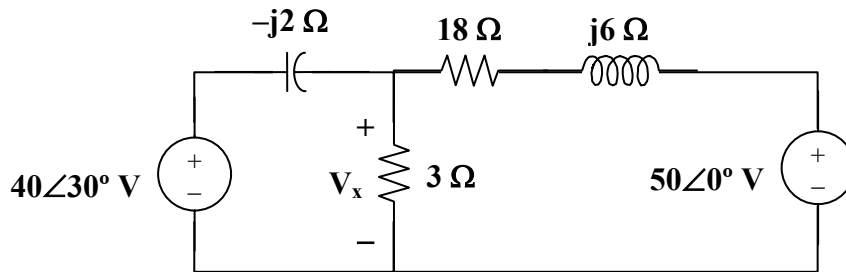


**Figure 10.62**

For Prob. 10.13.

### Chapter 10, Solution 13.

Nodal analysis is the best approach to use on this problem. We can make our work easier by doing a source transformation on the right hand side of the circuit.



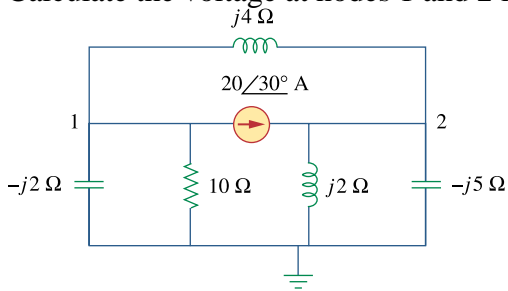
$$\frac{V_x - 40\angle 30^\circ}{-j2} + \frac{V_x}{3} + \frac{V_x - 50}{18 + j6} = 0$$

which leads to  $V_x = \underline{29.36\angle 62.88^\circ \text{ A}}$ .

### Chapter 10, Problem 14.



Calculate the voltage at nodes 1 and 2 in the circuit of Fig. 10.63 using nodal analysis.



**Figure 10.63**

For Prob. 10.14.

### Chapter 10, Solution 14.

At node 1,

$$\begin{aligned} \frac{0 - V_1}{-j2} + \frac{0 - V_1}{10} + \frac{V_2 - V_1}{j4} &= 20 \angle 30^\circ \\ -(1 + j2.5)V_1 - j2.5V_2 &= 173.2 + j100 \end{aligned} \quad (1)$$

At node 2,

$$\begin{aligned} \frac{V_2}{j2} + \frac{V_2}{-j5} + \frac{V_2 - V_1}{j4} &= 20 \angle 30^\circ \\ -j5.5V_2 + j2.5V_1 &= 173.2 + j100 \end{aligned} \quad (2)$$

Equations (1) and (2) can be cast into matrix form as

$$\begin{bmatrix} 1 + j2.5 & j2.5 \\ j2.5 & -j5.5 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} -200 \angle 30^\circ \\ 200 \angle 30^\circ \end{bmatrix}$$

$$\Delta = \begin{vmatrix} 1 + j2.5 & j2.5 \\ j2.5 & -j5.5 \end{vmatrix} = 20 - j5.5 = 20.74 \angle -15.38^\circ$$

$$\Delta_1 = \begin{vmatrix} -200 \angle 30^\circ & j2.5 \\ 200 \angle 30^\circ & -j5.5 \end{vmatrix} = j3(200 \angle 30^\circ) = 600 \angle 120^\circ$$

$$\Delta_2 = \begin{vmatrix} 1 + j2.5 & -200 \angle 30^\circ \\ j2.5 & 200 \angle 30^\circ \end{vmatrix} = (200 \angle 30^\circ)(1 + j5) = 1020 \angle 108.7^\circ$$

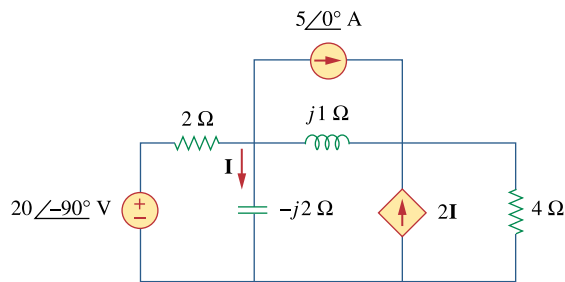
$$V_1 = \frac{\Delta_1}{\Delta} = 28.93 \angle 135.38^\circ$$

$$V_2 = \frac{\Delta_2}{\Delta} = 49.18 \angle 124.08^\circ$$

### Chapter 10, Problem 15.



Solve for the current  $\mathbf{I}$  in the circuit of Fig. 10.64 using nodal analysis.

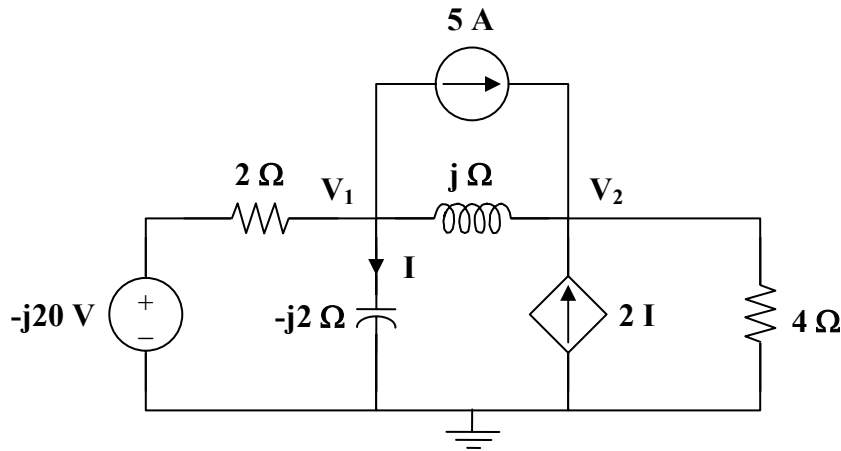


**Figure 10.64**

For Prob. 10.15.

## Chapter 10, Solution 15.

We apply nodal analysis to the circuit shown below.



At node 1,

$$\frac{-j20 - V_1}{2} = 5 + \frac{V_1}{-j2} + \frac{V_1 - V_2}{j}$$

$$-5 - j10 = (0.5 - j0.5)V_1 + jV_2 \quad (1)$$

At node 2,

$$5 + 2I + \frac{V_1 - V_2}{j} = \frac{V_2}{4},$$

where  $I = \frac{V_1}{-j2}$

$$V_2 = \frac{5}{0.25 - j} V_1 \quad (2)$$

Substituting (2) into (1),

$$-5 - j10 - \frac{j5}{0.25 - j} = 0.5(1 - j)V_1$$

$$(1 - j)V_1 = -10 - j20 - \frac{j40}{1 - j4}$$

$$(\sqrt{2} \angle -45^\circ)V_1 = -10 - j20 + \frac{160}{17} - \frac{j40}{17}$$

$$V_1 = 15.81 \angle 313.5^\circ$$

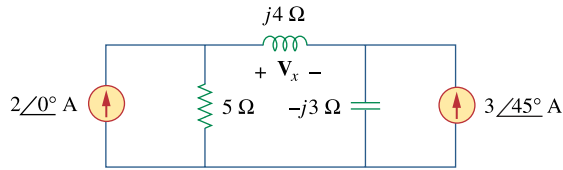
$$I = \frac{V_1}{-j2} = (0.5 \angle 90^\circ)(15.81 \angle 313.5^\circ)$$

$$I = \underline{\underline{7.906 \angle 43.49^\circ \text{ A}}}$$

### Chapter 10, Problem 16.



Use nodal analysis to find  $V_x$  in the circuit shown in Fig. 10.65.

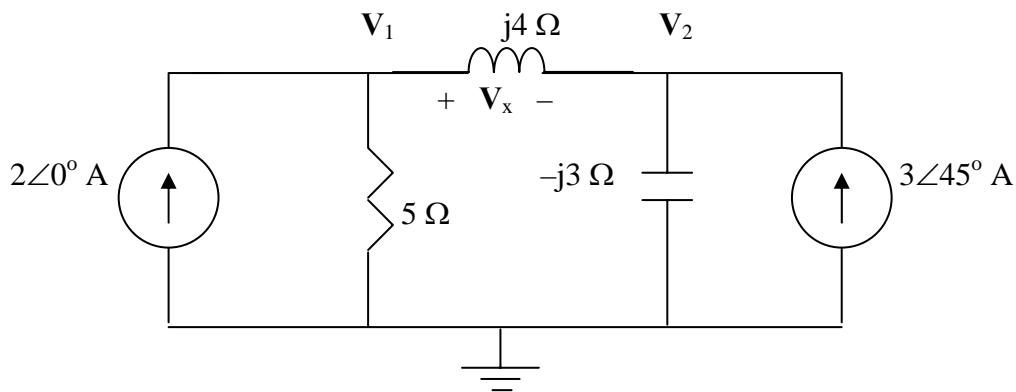


**Figure 10.65**

For Prob. 10.16.

### Chapter 10, Solution 16.

Consider the circuit as shown in the figure below.



At node 1,

$$-2 + \frac{V_1 - 0}{5} + \frac{V_1 - V_2}{j4} = 0 \quad (1)$$

$$(0.2 - j0.25)V_1 + j0.25V_2 = 2$$

At node 2,

$$\frac{V_2 - V_1}{j4} + \frac{V_2 - 0}{-j3} - 3\angle 45^\circ = 0 \quad (2)$$

$$j0.25V_1 + j0.08333V_2 = 2.121 + j2.121$$

In matrix form, (1) and (2) become

$$\begin{bmatrix} 0.2 - j0.25 & j0.25 \\ j0.25 & j0.08333 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} 2 \\ 2.121 + j2.121 \end{bmatrix}$$

Solving this using MATLAB, we get,

```
>> Y=[(0.2-0.25i),0.25i;0.25i,0.08333i]
```

Y =

```
0.2000 - 0.2500i    0 + 0.2500i
0 + 0.2500i    0 + 0.0833i
```

```
>> I=[2;(2.121+2.121i)]
```

I =

```
2.0000
2.1210 + 2.1210i
```

```
>> V=inv(Y)*I
```

V =

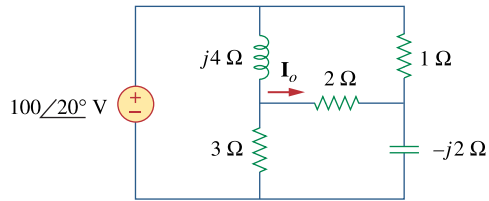
```
5.2793 - 5.4190i
9.6145 - 9.1955i
```

$$V_s = V_1 - V_2 = -4.335 + j3.776 = \underline{\underline{5.749\angle 138.94^\circ \text{ V}}}.$$

### Chapter 10, Problem 17.



By nodal analysis, obtain current  $\mathbf{I}_o$  in the circuit of Fig. 10.66.

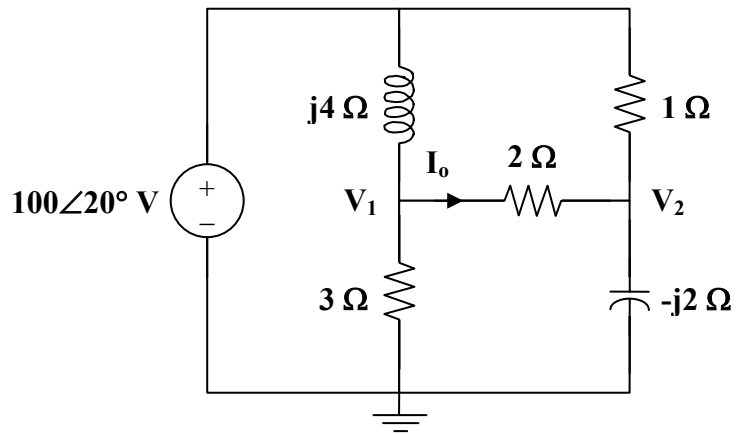


**Figure 10.66**

For Prob. 10.17.

### Chapter 10, Solution 17.

Consider the circuit below.





At node 1,

$$\frac{100\angle 20^\circ - \mathbf{V}_1}{j4} = \frac{\mathbf{V}_1}{3} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{2}$$

$$100\angle 20^\circ = \frac{\mathbf{V}_1}{3}(3 + j10) - j2\mathbf{V}_2$$

(1)

At node 2,

$$\frac{100\angle 20^\circ - \mathbf{V}_2}{1} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{2} = \frac{\mathbf{V}_2}{-j2}$$

$$100\angle 20^\circ = -0.5\mathbf{V}_1 + (1.5 + j0.5)\mathbf{V}_2$$

(2)

From (1) and (2),

$$\begin{bmatrix} 100\angle 20^\circ \\ 100\angle 20^\circ \end{bmatrix} = \begin{bmatrix} -0.5 & 0.5(3 + j) \\ 1 + j10/3 & -j2 \end{bmatrix} \begin{bmatrix} \mathbf{V}_1 \\ \mathbf{V}_2 \end{bmatrix}$$

$$\Delta = \begin{vmatrix} -0.5 & 1.5 + j0.5 \\ 1 + j10/3 & -j2 \end{vmatrix} = 0.1667 - j4.5$$

$$\Delta_1 = \begin{vmatrix} 100\angle 20^\circ & 1.5 + j0.5 \\ 100\angle 20^\circ & -j2 \end{vmatrix} = -55.45 - j286.2$$

$$\Delta_2 = \begin{vmatrix} -0.5 & 100\angle 20^\circ \\ 1 + j10/3 & 100\angle 20^\circ \end{vmatrix} = -26.95 - j364.5$$

$$\mathbf{V}_1 = \frac{\Delta_1}{\Delta} = 64.74\angle -13.08^\circ$$

$$\mathbf{V}_2 = \frac{\Delta_2}{\Delta} = 81.17\angle -6.35^\circ$$

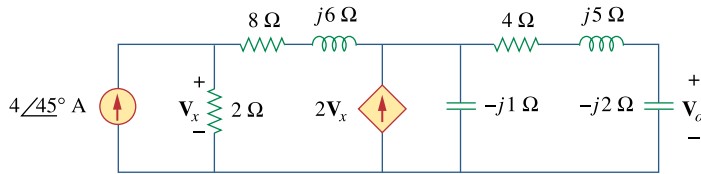
$$\mathbf{I}_o = \frac{\mathbf{V}_1 - \mathbf{V}_2}{2} = \frac{\Delta_1 - \Delta_2}{2\Delta} = \frac{-28.5 + j78.31}{0.3333 - j9}$$

$$\mathbf{I}_o = \underline{\underline{9.25\angle -162.12^\circ \text{ A}}}$$

### Chapter 10, Problem 18.



Use nodal analysis to obtain  $V_o$  in the circuit of Fig. 10.67 below.

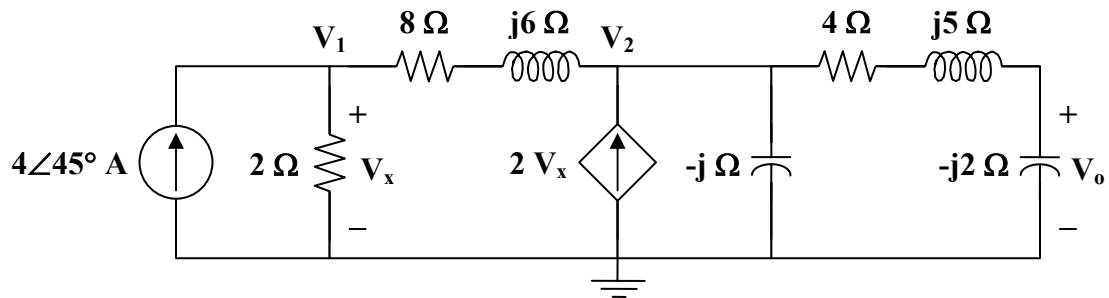


**Figure 10.67**

For Prob. 10.18.

### Chapter 10, Solution 18.

Consider the circuit shown below.



At node 1,

$$4\angle 45^\circ = \frac{\mathbf{V}_1}{2} + \frac{\mathbf{V}_1 - \mathbf{V}_2}{8 + j6}$$

$$200\angle 45^\circ = (29 - j3)\mathbf{V}_1 - (4 - j3)\mathbf{V}_2$$

(1)

At node 2,

$$\frac{\mathbf{V}_1 - \mathbf{V}_2}{8 + j6} + 2\mathbf{V}_x = \frac{\mathbf{V}_2}{-j} + \frac{\mathbf{V}_2}{4 + j5 - j2}, \quad \text{where } \mathbf{V}_x = \mathbf{V}_1$$

$$(104 - j3)\mathbf{V}_1 = (12 + j41)\mathbf{V}_2$$

$$\mathbf{V}_1 = \frac{12 + j41}{104 - j3}\mathbf{V}_2$$

(2)

Substituting (2) into (1),

$$200\angle 45^\circ = (29 - j3)\frac{(12 + j41)}{104 - j3}\mathbf{V}_2 - (4 - j3)\mathbf{V}_2$$

$$200\angle 45^\circ = (14.21\angle 89.17^\circ)\mathbf{V}_2$$

$$\mathbf{V}_2 = \frac{200\angle 45^\circ}{14.21\angle 89.17^\circ}$$

$$\mathbf{V}_o = \frac{-j2}{4 + j5 - j2}\mathbf{V}_2 = \frac{-j2}{4 + j3}\mathbf{V}_2 = \frac{-6 - j8}{25}\mathbf{V}_2$$

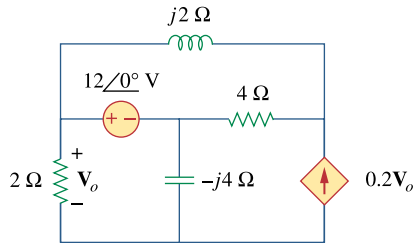
$$\mathbf{V}_o = \frac{10\angle 233.13^\circ}{25} \cdot \frac{200\angle 45^\circ}{14.21\angle 89.17^\circ}$$

$$\mathbf{V}_o = \underline{\underline{5.63\angle 189^\circ \text{ V}}}$$

**Chapter 10, Problem 19.**



Obtain  $V_o$  in Fig. 10.68 using nodal analysis.

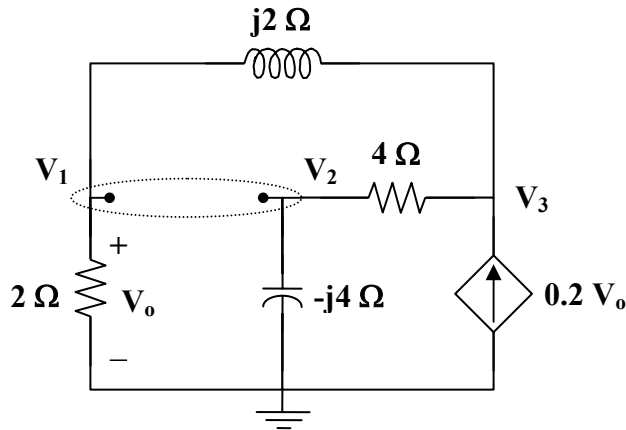


**Figure 10.68**

For Prob. 10.19.

### Chapter 10, Solution 19.

We have a supernode as shown in the circuit below.



Notice that  $V_o = V_1$ .

At the supernode,

$$\begin{aligned} \frac{V_3 - V_2}{4} &= \frac{V_2}{-j4} + \frac{V_1}{2} + \frac{V_1 - V_3}{j2} \\ 0 &= (2 - j2)V_1 + (1 + j)V_2 + (-1 + j2)V_3 \end{aligned} \quad (1)$$

At node 3,

$$\begin{aligned} 0.2V_1 + \frac{V_1 - V_3}{j2} &= \frac{V_3 - V_2}{4} \\ (0.8 - j2)V_1 + V_2 + (-1 + j2)V_3 &= 0 \end{aligned} \quad (2)$$

Subtracting (2) from (1),

$$0 = 1.2V_1 + jV_2 \quad (3)$$

But at the supernode,

$$V_1 = 12\angle 0^\circ + V_2$$

$$\text{or} \quad V_2 = V_1 - 12 \quad (4)$$

Substituting (4) into (3),

$$0 = 1.2V_1 + j(V_1 - 12)$$

$$V_1 = \frac{j12}{1.2 + j} = V_o$$

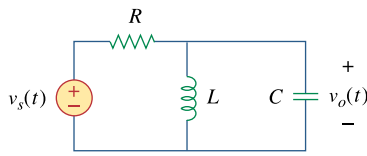
$$V_o = \frac{12\angle 90^\circ}{1.562\angle 39.81^\circ}$$

$$V_o = \underline{7.682\angle 50.19^\circ \text{ V}}$$

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**Chapter 10, Problem 20.**

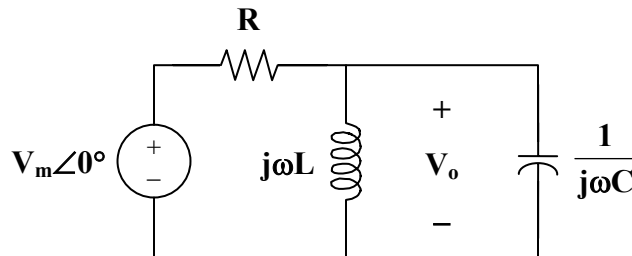
Refer to Fig. 10.69. If  $v_s(t) = V_m \sin \omega t$  and  $v_o(t) = A \sin(\omega t + \phi)$  derive the expressions for  $A$  and  $\phi$

**Figure 10.69**

For Prob. 10.20.

**Chapter 10, Solution 20.**

The circuit is converted to its frequency-domain equivalent circuit as shown below.



$$\text{Let } Z = j\omega L \parallel \frac{1}{j\omega C} = \frac{\frac{L}{C}}{j\omega L + \frac{1}{j\omega C}} = \frac{j\omega L}{1 - \omega^2 LC}$$

$$V_o = \frac{Z}{R + Z} V_m = \frac{\frac{j\omega L}{1 - \omega^2 LC}}{R + \frac{j\omega L}{1 - \omega^2 LC}} V_m = \frac{j\omega L}{R(1 - \omega^2 LC) + j\omega L} V_m$$

$$V_o = \frac{\omega L V_m}{\sqrt{R^2 (1 - \omega^2 LC)^2 + \omega^2 L^2}} \angle \left( 90^\circ - \tan^{-1} \frac{\omega L}{R(1 - \omega^2 LC)} \right)$$

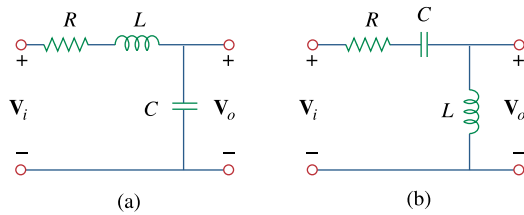
If  $V_o = A \angle \phi$ , then

$$A = \frac{\omega L V_m}{\sqrt{R^2 (1 - \omega^2 LC)^2 + \omega^2 L^2}}$$

$$\text{and } \phi = \underline{\underline{90^\circ - \tan^{-1} \frac{\omega L}{R(1 - \omega^2 LC)}}}$$

### Chapter 10, Problem 21.

For each of the circuits in Fig. 10.70, find  $V_o/V_i$  for  $\omega = 0$ ,  $\omega \rightarrow \infty$ , and  $\omega^2 = 1/LC$ .



**Figure 10.70**

For Prob. 10.21.

### Chapter 10, Solution 21.

$$(a) \quad \frac{V_o}{V_i} = \frac{\frac{1}{j\omega C}}{R + j\omega L + \frac{1}{j\omega C}} = \frac{1}{1 - \omega^2 LC + j\omega RC}$$

At  $\omega = 0$ ,  $\frac{V_o}{V_i} = \frac{1}{1} = \underline{1}$

As  $\omega \rightarrow \infty$ ,  $\frac{V_o}{V_i} = \underline{0}$

At  $\omega = \frac{1}{\sqrt{LC}}$ ,  $\frac{V_o}{V_i} = \frac{1}{jRC \cdot \frac{1}{\sqrt{LC}}} = \underline{\frac{-j}{R} \sqrt{\frac{L}{C}}}$

$$(b) \quad \frac{V_o}{V_i} = \frac{j\omega L}{R + j\omega L + \frac{1}{j\omega C}} = \frac{-\omega^2 LC}{1 - \omega^2 LC + j\omega RC}$$

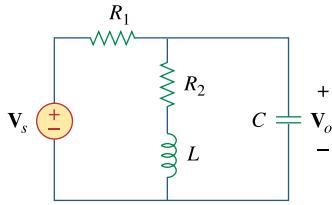
At  $\omega = 0$ ,  $\frac{V_o}{V_i} = \underline{0}$

As  $\omega \rightarrow \infty$ ,  $\frac{V_o}{V_i} = \frac{1}{1} = \underline{1}$

At  $\omega = \frac{1}{\sqrt{LC}}$ ,  $\frac{V_o}{V_i} = \frac{-1}{jRC \cdot \frac{1}{\sqrt{LC}}} = \underline{\frac{j}{R} \sqrt{\frac{L}{C}}}$

### Chapter 10, Problem 22.

For the circuit in Fig. 10.71, determine  $\mathbf{V}_o/\mathbf{V}_s$ .

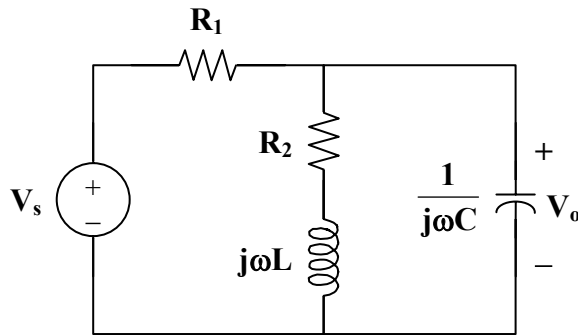


**Figure 10.71**

For Prob. 10.22.

### Chapter 10, Solution 22.

Consider the circuit in the frequency domain as shown below.



$$\text{Let } \mathbf{Z} = (\mathbf{R}_2 + j\omega L) \parallel \frac{1}{j\omega C}$$

$$\mathbf{Z} = \frac{\frac{1}{j\omega C}(\mathbf{R}_2 + j\omega L)}{\mathbf{R}_2 + j\omega L + \frac{1}{j\omega C}} = \frac{\mathbf{R}_2 + j\omega L}{1 + j\omega R_2 - \omega^2 LC}$$

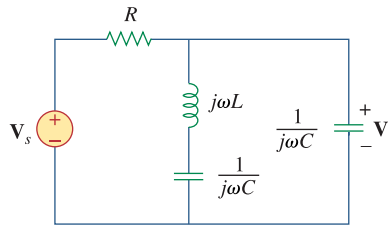
$$\frac{\mathbf{V}_o}{\mathbf{V}_s} = \frac{\mathbf{Z}}{\mathbf{Z} + \mathbf{R}_1} = \frac{\frac{\mathbf{R}_2 + j\omega L}{1 - \omega^2 LC + j\omega R_2 C}}{\mathbf{R}_1 + \frac{\mathbf{R}_2 + j\omega L}{1 - \omega^2 LC + j\omega R_2 C}}$$

$$\frac{\mathbf{V}_o}{\mathbf{V}_s} = \frac{\mathbf{R}_2 + j\omega L}{\mathbf{R}_1 + \mathbf{R}_2 - \omega^2 LCR_1 + j\omega(L + R_1 R_2 C)}$$



### Chapter 10, Problem 23.

Using nodal analysis obtain  $V$  in the circuit of Fig. 10.72.



**Figure 10.72**

For Prob. 10.23.

### Chapter 10, Solution 23.

$$\frac{V - V_s}{R} + \frac{V}{j\omega L + \frac{1}{j\omega C}} + j\omega C V = 0$$

$$V + \frac{j\omega R C V}{- \omega^2 L C + 1} + j\omega R C V = V_s$$

$$\left( \frac{1 - \omega^2 L C + j\omega R C + j\omega R C - j\omega^3 R L C^2}{1 - \omega^2 L C} \right) V = V_s$$

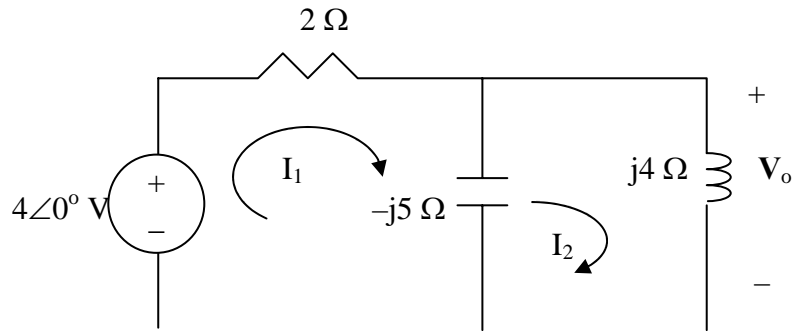
$$V = \frac{(1 - \omega^2 L C) V_s}{1 - \omega^2 L C + j\omega R C (2 - \omega^2 L C)}$$

### Chapter 10, Problem 24.

Use mesh analysis to find  $V_o$  in the circuit of Prob. 10.2.

### Chapter 10, Solution 24.

Consider the circuit as shown below.



For mesh 1,

$$4 = (2 - j5)I_1 + j5I_2 \quad (1)$$

For mesh 2,

$$0 = j5I_1 + (j4 - j5)I_2 \quad \longrightarrow \quad I_1 = \frac{1}{5}I_2 \quad (2)$$

Substituting (2) into (1),

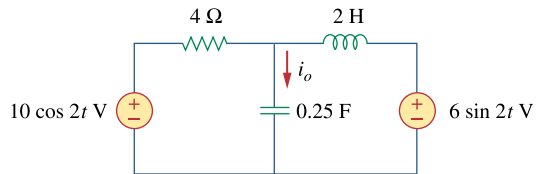
$$4 = (2 - j5)\frac{1}{5}I_2 + j5I_2 \quad \longrightarrow \quad I_2 = \frac{1}{0.1 + j}$$

$$V_o = j4I_2 = \frac{j4}{0.1 + j} = \underline{3.98 \angle 5.71^\circ \text{ V}}$$

**Chapter 10, Problem 25.**



Solve for  $i_o$  in Fig. 10.73 using mesh analysis.



**Figure 10.73**

For Prob. 10.25.

### Chapter 10, Solution 25.

$$\omega = 2$$

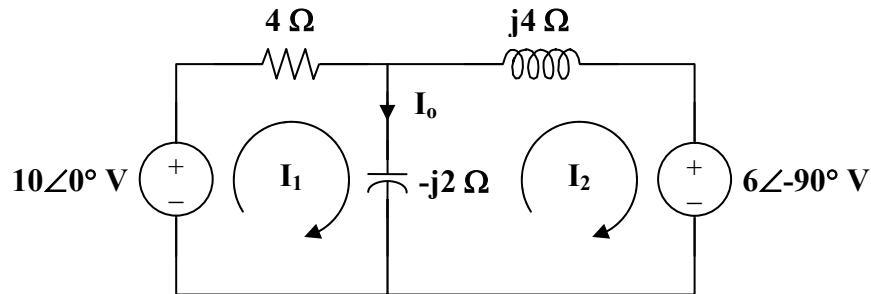
$$10 \cos(2t) \longrightarrow 10 \angle 0^\circ$$

$$6 \sin(2t) \longrightarrow 6 \angle -90^\circ = -j6$$

$$2 \text{ H} \longrightarrow j\omega L = j4$$

$$0.25 \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/4)} = -j2$$

The circuit is shown below.



For loop 1,

$$-10 + (4 - j2)I_1 + j2I_2 = 0$$

$$5 = (2 - j)I_1 + jI_2 \quad (1)$$

For loop 2,

$$j2I_1 + (j4 - j2)I_2 + (-j6) = 0$$

$$I_1 + I_2 = 3 \quad (2)$$

In matrix form (1) and (2) become

$$\begin{bmatrix} 2-j & j \\ 1 & 1 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} 5 \\ 3 \end{bmatrix}$$

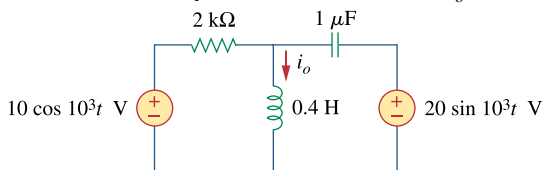
$$\Delta = 2(1-j), \quad \Delta_1 = 5-j3, \quad \Delta_2 = 1-j3$$

$$I_o = I_1 - I_2 = \frac{\Delta_1 - \Delta_2}{\Delta} = \frac{4}{2(1-j)} = 1+j = 1.414 \angle 45^\circ$$

Therefore,  $i_o(t) = \underline{\underline{1.4142 \cos(2t + 45^\circ) \text{ A}}}$

### Chapter 10, Problem 26.

Use mesh analysis to find current  $i_o$  in the circuit of Fig. 10.74.



**Figure 10.74**

For Prob. 10.26.

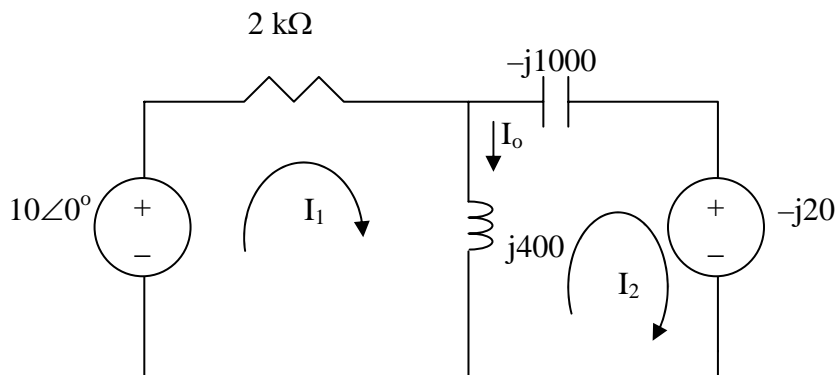
### Chapter 10, Solution 26.

$$0.4 \text{ H} \longrightarrow j\omega L = j10^3 \times 0.4 = j400$$

$$1 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j10^3 \times 10^{-6}} = -j1000$$

$$20 \sin 10^3 t = 20 \cos(10^3 t - 90^\circ) \longrightarrow 20 \angle -90 = -j20$$

The circuit becomes that shown below.



For loop 1,

$$-10 + (12000 + j400)I_1 - j400I_2 = 0 \longrightarrow 1 = (200 + j40)I_1 - j40I_2 \quad (1)$$

For loop 2,

$$-j20 + (j400 - j1000)I_2 - j400I_1 = 0 \longrightarrow -12 = 40I_1 + 60I_2 \quad (2)$$

(2)

In matrix form, (1) and (2) become

$$\begin{bmatrix} 1 \\ -12 \end{bmatrix} = \begin{bmatrix} 200 + j40 & -j40 \\ 40 & 60 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

Solving this leads to

$$I_1 = 0.0025 - j0.0075, \quad I_2 = -0.035 + j0.005$$

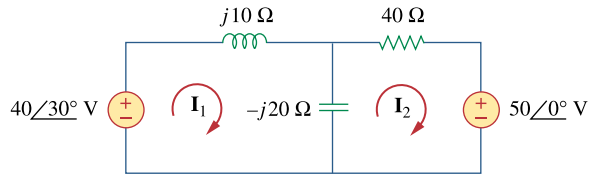
$$I_o = I_1 - I_2 = 0.0375 - j0.0125 = 39.5 \angle -18.43^\circ \text{ mA}$$

$$i_o = 39.5 \cos(10^3 t - 18.43^\circ) \text{ mA}$$

### Chapter 10, Problem 27.



Using mesh analysis, find  $\mathbf{I}_1$  and  $\mathbf{I}_2$  in the circuit of Fig. 10.75.



**Figure 10.75**

For Prob. 10.27.

### Chapter 10, Solution 27.

For mesh 1,

$$\begin{aligned} -40\angle 30^\circ + (j10 - j20)\mathbf{I}_1 + j20\mathbf{I}_2 &= 0 \\ 4\angle 30^\circ &= -j\mathbf{I}_1 + j2\mathbf{I}_2 \end{aligned} \quad (1)$$

For mesh 2,

$$\begin{aligned} 50\angle 0^\circ + (40 - j20)\mathbf{I}_2 + j20\mathbf{I}_1 &= 0 \\ 5 &= -j2\mathbf{I}_1 - (4 - j2)\mathbf{I}_2 \end{aligned} \quad (2)$$

From (1) and (2),

$$\begin{bmatrix} 4\angle 30^\circ \\ 5 \end{bmatrix} = \begin{bmatrix} -j & j2 \\ -j2 & -(4 - j2) \end{bmatrix} \begin{bmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \end{bmatrix}$$

$$\Delta = -2 + 4j = 4.472\angle 116.56^\circ$$

$$\Delta_1 = -(4\angle 30^\circ)(4 - j2) - j10 = 21.01\angle 211.8^\circ$$

$$\Delta_2 = -j5 + 8\angle 120^\circ = 4.44\angle 154.27^\circ$$

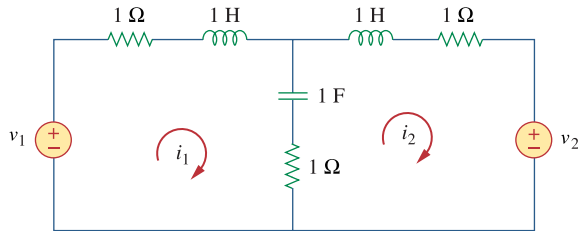
$$\mathbf{I}_1 = \frac{\Delta_1}{\Delta} = \underline{\underline{4.698\angle 95.24^\circ \text{ A}}}$$

$$\mathbf{I}_2 = \frac{\Delta_2}{\Delta} = \underline{\underline{0.9928\angle 37.71^\circ \text{ A}}}$$

**Chapter 10, Problem 28.**



In the circuit of Fig. 10.76, determine the mesh currents  $i_1$  and  $i_2$ . Let  $v_1 = 10 \cos 4t \text{ V}$  and  $v_2 = 20 \cos(4t - 30^\circ) \text{ V}$ .



**Figure 10.76**

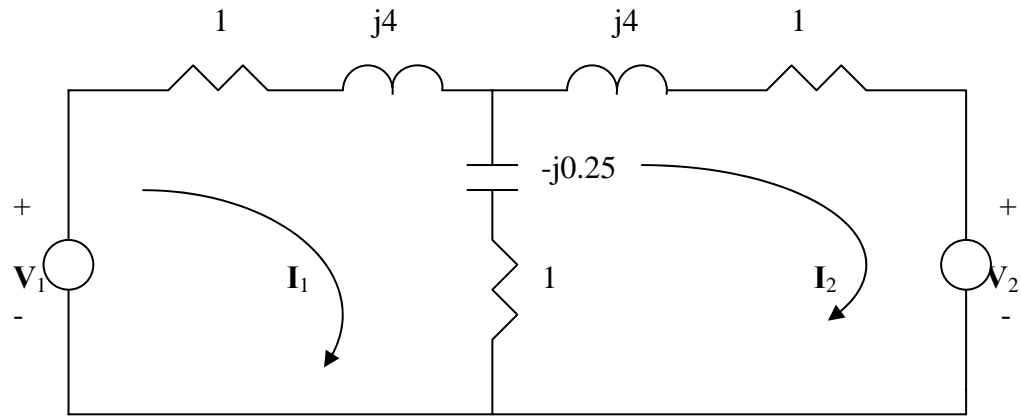
For Prob. 10.28.

**Chapter 10, Solution 28.**

$$1\text{H} \longrightarrow j\omega L = j4, \quad 1\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j1 \times 4} = -j0.25$$

The frequency-domain version of the circuit is shown below, where

$$V_1 = 10\angle 0^\circ, \quad V_2 = 20\angle -30^\circ.$$



$$V_1 = 10\angle 0^\circ, \quad V_2 = 20\angle -30^\circ$$

Applying mesh analysis,

$$10 = (2 + j3.75)I_1 - (1 - j0.25)I_2 \quad (1)$$

$$-20\angle -30^\circ = -(1 - j0.25)I_1 + (2 + j3.75)I_2 \quad (2)$$

From (1) and (2), we obtain

$$\begin{pmatrix} 10 \\ -17.32 + j10 \end{pmatrix} = \begin{pmatrix} 2 + j3.75 & -1 + j0.25 \\ -1 + j0.25 & 2 + j3.75 \end{pmatrix} \begin{pmatrix} I_1 \\ I_2 \end{pmatrix}$$

Solving this leads to

$$I_1 = 2.741\angle -41.07^\circ, \quad I_2 = 4.114\angle 92^\circ$$

Hence,

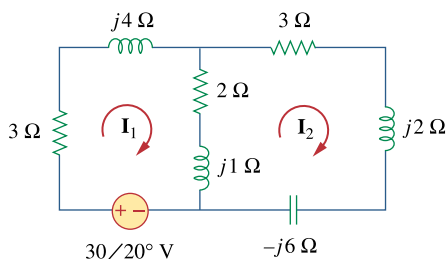
$$i_1(t) = \underline{2.741\cos(4t-41.07^\circ)\text{A}}, \quad i_2(t) = \underline{4.114\cos(4t+92^\circ)\text{A}}.$$



## Chapter 10, Problem 29.



By using mesh analysis, find  $\mathbf{I}_1$  and  $\mathbf{I}_2$  in the circuit depicted in Fig. 10.77.



**Figure 10.77**

For Prob. 10.29.

## Chapter 10, Solution 29.

For mesh 1,

$$\begin{aligned}(5 + j5)\mathbf{I}_1 - (2 + j)\mathbf{I}_2 - 30\angle 20^\circ &= 0 \\ 30\angle 20^\circ &= (5 + j5)\mathbf{I}_1 - (2 + j)\mathbf{I}_2 \\ (1)\end{aligned}$$

For mesh 2,

$$\begin{aligned}(5 + j3 - j6)\mathbf{I}_2 - (2 + j)\mathbf{I}_1 &= 0 \\ 0 &= -(2 + j)\mathbf{I}_1 + (5 - j3)\mathbf{I}_2 \\ (2)\end{aligned}$$

From (1) and (2),

$$\begin{bmatrix} 30\angle 20^\circ \\ 0 \end{bmatrix} = \begin{bmatrix} 5 + j5 & -(2 + j) \\ -(2 + j) & 5 - j3 \end{bmatrix} \begin{bmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \end{bmatrix}$$

$$\Delta = 37 + j6 = 37.48\angle 9.21^\circ$$

$$\Delta_1 = (30\angle 20^\circ)(5.831\angle -30.96^\circ) = 175\angle -10.96^\circ$$

$$\Delta_2 = (30\angle 20^\circ)(2.356\angle 26.56^\circ) = 67.08\angle 46.56^\circ$$

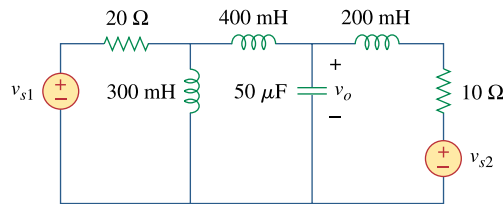
$$\mathbf{I}_1 = \frac{\Delta_1}{\Delta} = \underline{\underline{4.67\angle -20.17^\circ \text{ A}}}$$

$$\mathbf{I}_2 = \frac{\Delta_2}{\Delta} = \underline{\underline{1.79\angle 37.35^\circ \text{ A}}}$$

### Chapter 10, Problem 30.



Use mesh analysis to find  $v_o$  in the circuit of Fig. 10.78. Let  $v_{s1} = 120 \cos(100t + 90^\circ)$  V,  $v_{s2} = 80 \cos 100t$  V.



**Figure 10.78**

For Prob. 10.30.

### Chapter 10, Solution 30.

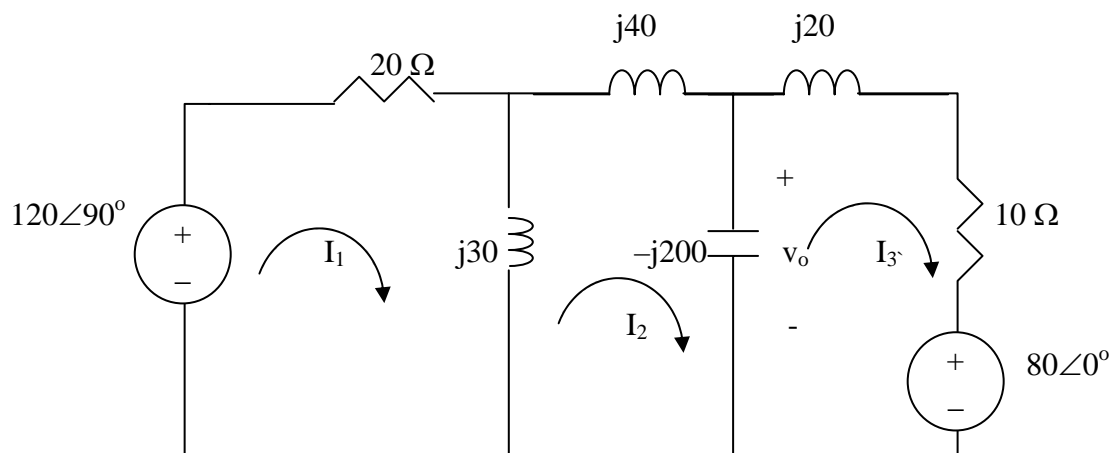
$$300 \text{ mH} \longrightarrow j\omega L = j100 \times 300 \times 10^{-3} = j30$$

$$200 \text{ mH} \longrightarrow j\omega L = j100 \times 200 \times 10^{-3} = j20$$

$$400 \text{ mH} \longrightarrow j\omega L = j100 \times 400 \times 10^{-3} = j40$$

$$50 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j100 \times 50 \times 10^{-6}} = -j200$$

The circuit becomes that shown below.



For mesh 1,

$$-120 \angle 90^\circ + (20 + j30)I_1 - j30I_2 = 0 \longrightarrow j120 = (20 + j30)I_1 - j30I_2 \quad (1)$$

For mesh 2,

$$-j30I_1 + (j30 + j40 - j200)I_2 + j200I_3 = 0 \longrightarrow 0 = -3I_1 - 13I_2 + 20I_3 \quad (2)$$

For mesh 3,

$$80 + j200I_2 + (10 - j180)I_3 = 0 \rightarrow -8 = j20I_2 + (1 - j18)I_3 \quad (3)$$

We put (1) to (3) in matrix form.

$$\begin{bmatrix} 2 + j3 & -j3 & 0 \\ -3 & -13 & 20 \\ 0 & j20 & 1 - j18 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} j12 \\ 0 \\ -8 \end{bmatrix}$$

This is an excellent candidate for MATLAB.

```
>> Z=[(2+3i),-3i,0;-3,-13,20;0,20i,(1-18i)]
```

Z =

```
2.0000 + 3.0000i    0 - 3.0000i    0
-3.0000    -13.0000    20.0000
0    0 + 20.0000i    1.0000 - 18.0000i
```

```
>> V=[12i;0;-8]
```

V =

```
0 + 12.0000i
0
-8.0000
```

```
>> I=inv(Z)*V
```

I =

```
2.0557 + 3.5651i
0.4324 + 2.1946i
0.5894 + 1.9612i
```

$$V_o = -j200(I_2 - I_3) = -j200(-0.157 + j0.2334) = 46.68 + j31.4 = 56.26 \angle 33.93^\circ$$

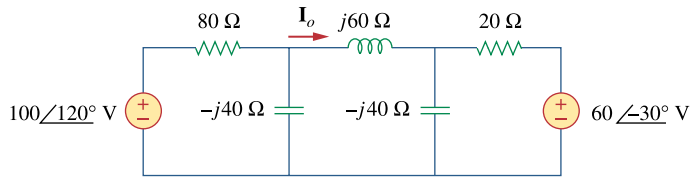
$$v_o = \underline{\underline{56.26 \cos(100t + 33.93^\circ) \text{ V}}}.$$

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### Chapter 10, Problem 31.



Use mesh analysis to determine current  $\mathbf{I}_o$  in the circuit of Fig. 10.79 below.

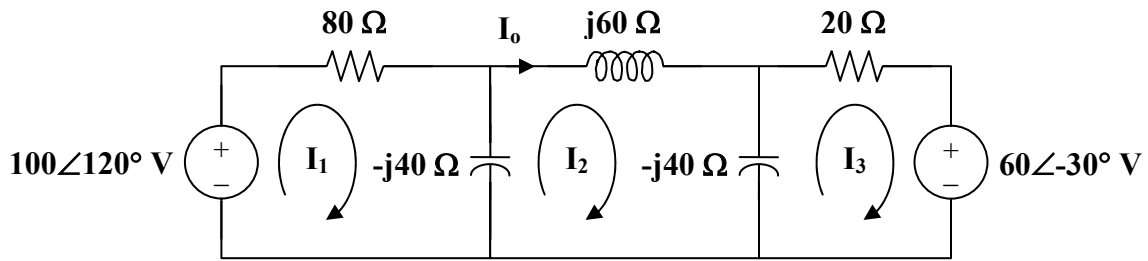


**Figure 10.79**

For Prob. 10.31.

### Chapter 10, Solution 31.

Consider the network shown below.



For loop 1,

$$\begin{aligned} -100\angle 120^\circ + (80 - j40)\mathbf{I}_1 + j40\mathbf{I}_2 &= 0 \\ 10\angle 20^\circ &= 4(2 - j)\mathbf{I}_1 + j4\mathbf{I}_2 \end{aligned} \quad (1)$$

For loop 2,

$$\begin{aligned} j40\mathbf{I}_1 + (j60 - j80)\mathbf{I}_2 + j40\mathbf{I}_3 &= 0 \\ 0 &= 2\mathbf{I}_1 - \mathbf{I}_2 + 2\mathbf{I}_3 \end{aligned} \quad (2)$$

For loop 3,

$$\begin{aligned} 60\angle -30^\circ + (20 - j40)\mathbf{I}_3 + j40\mathbf{I}_2 &= 0 \\ -6\angle -30^\circ &= j4\mathbf{I}_2 + 2(1 - j2)\mathbf{I}_3 \end{aligned} \quad (3)$$

From (2),

$$2\mathbf{I}_3 = \mathbf{I}_2 - 2\mathbf{I}_1$$

Substituting this equation into (3),

$$-6\angle -30^\circ = -2(1 - j2)\mathbf{I}_1 + (1 + j2)\mathbf{I}_2 \quad (4)$$

From (1) and (4),

$$\begin{bmatrix} 10\angle 120^\circ \\ -6\angle -30^\circ \end{bmatrix} = \begin{bmatrix} 4(2 - j) & j4 \\ -2(1 - j2) & 1 + j2 \end{bmatrix} \begin{bmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \end{bmatrix}$$

$$\Delta = \begin{vmatrix} 8 - j4 & -j4 \\ -2 + j4 & 1 + j2 \end{vmatrix} = 32 + j20 = 37.74\angle 32^\circ$$

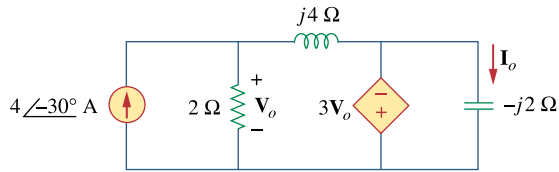
$$\Delta_2 = \begin{vmatrix} 8 - j4 & 10\angle 120^\circ \\ -2 + j4 & -6\angle -30^\circ \end{vmatrix} = -4.928 + j82.11 = 82.25\angle 93.44^\circ$$

$$\mathbf{I}_o = \mathbf{I}_2 = \frac{\Delta_2}{\Delta} = \underline{\underline{2.179\angle 61.44^\circ \text{ A}}}$$

### Chapter 10, Problem 32.



Determine  $V_o$  and  $I_o$  in the circuit of Fig. 10.80 using mesh analysis.

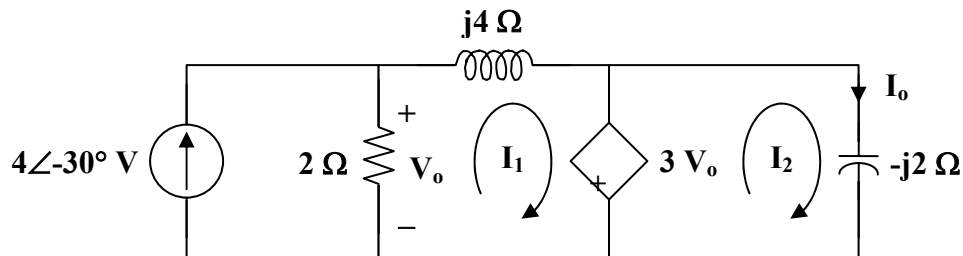


**Figure 10.80**

For Prob. 10.32.

### Chapter 10, Solution 32.

Consider the circuit below.



For mesh 1,

$$(2 + j4)I_1 - 2(4\angle -30^\circ) + 3V_o = 0$$

where

$$V_o = 2(4\angle -30^\circ - I_1)$$

Hence,

$$(2 + j4)I_1 - 8\angle -30^\circ + 6(4\angle -30^\circ - I_1) = 0$$

$$4\angle -30^\circ = (1 - j)I_1$$

or

$$I_1 = 2\sqrt{2}\angle 15^\circ$$

$$I_o = \frac{3V_o}{-j2} = \frac{3}{-j2}(2)(4\angle -30^\circ - I_1)$$

$$I_o = j3(4\angle -30^\circ - 2\sqrt{2}\angle 15^\circ)$$

$$I_o = \underline{8.485\angle 15^\circ \text{ A}}$$

$$V_o = \frac{-j2I_o}{3} = \underline{5.657\angle -75^\circ \text{ V}}$$

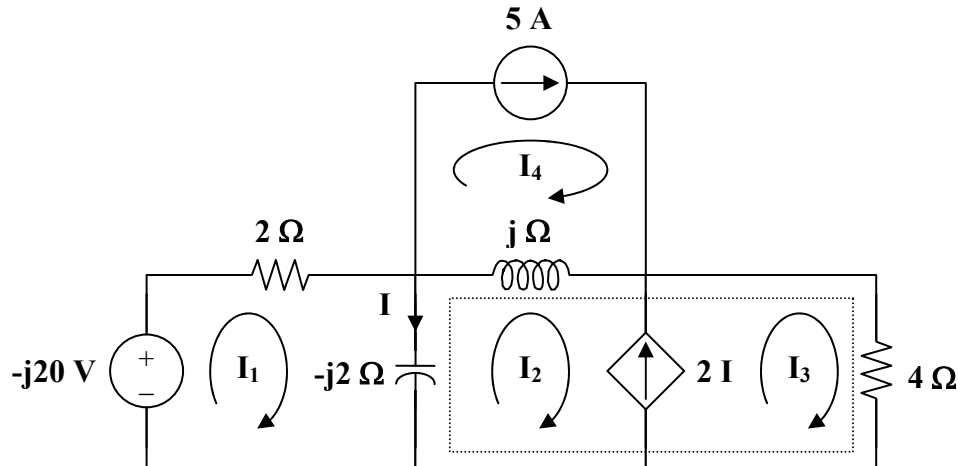
### Chapter 10, Problem 33.



Compute  $\mathbf{I}$  in Prob. 10.15 using mesh analysis.

### Chapter 10, Solution 33.

Consider the circuit shown below.



For mesh 1,

$$\begin{aligned} j20 + (2 - j2)\mathbf{I}_1 + j2\mathbf{I}_2 &= 0 \\ (1 - j)\mathbf{I}_1 + j\mathbf{I}_2 &= -j10 \end{aligned} \quad (1)$$

For the supermesh,

$$(j - j2)\mathbf{I}_2 + j2\mathbf{I}_1 + 4\mathbf{I}_3 - j\mathbf{I}_4 = 0 \quad (2)$$

Also,

$$\begin{aligned} \mathbf{I}_3 - \mathbf{I}_2 &= 2\mathbf{I} = 2(\mathbf{I}_1 - \mathbf{I}_2) \\ \mathbf{I}_3 &= 2\mathbf{I}_1 - \mathbf{I}_2 \end{aligned} \quad (3)$$

For mesh 4,

$$\mathbf{I}_4 = 5 \quad (4)$$

Substituting (3) and (4) into (2),

$$(8 + j2)\mathbf{I}_1 - (-4 + j)\mathbf{I}_2 = j5 \quad (5)$$

Putting (1) and (5) in matrix form,

$$\begin{bmatrix} 1 - j & j \\ 8 + j2 & 4 - j \end{bmatrix} \begin{bmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \end{bmatrix} = \begin{bmatrix} -j10 \\ j5 \end{bmatrix}$$

$$\Delta = -3 - j5, \quad \Delta_1 = -5 + j40, \quad \Delta_2 = -15 + j85$$

$$\mathbf{I} = \mathbf{I}_1 - \mathbf{I}_2 = \frac{\Delta_1 - \Delta_2}{\Delta} = \frac{10 - j45}{-3 - j5} = \underline{\underline{7.906 \angle 43.49^\circ \text{ A}}}$$

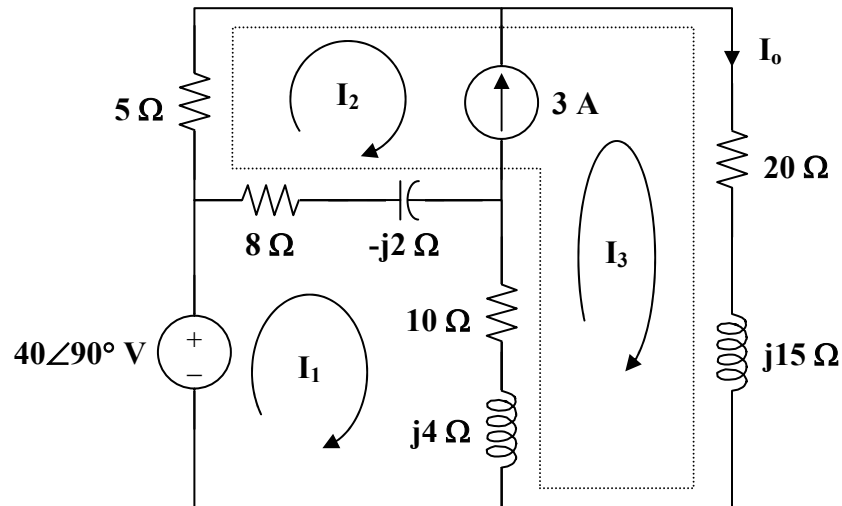
### Chapter 10, Problem 34.



Use mesh analysis to find  $\mathbf{I}_o$  in Fig. 10.28 (for Example 10.10).

### Chapter 10, Solution 34.

The circuit is shown below.



For mesh 1,

$$-j40 + (18 + j2)\mathbf{I}_1 - (8 - j2)\mathbf{I}_2 - (10 + j4)\mathbf{I}_3 = 0 \quad (1)$$

For the supermesh,

$$(13 - j2)\mathbf{I}_2 + (30 + j19)\mathbf{I}_3 - (18 + j2)\mathbf{I}_1 = 0 \quad (2)$$

Also,

$$\mathbf{I}_2 = \mathbf{I}_3 - 3 \quad (3)$$

Adding (1) and (2) and incorporating (3),

$$-j40 + 5(\mathbf{I}_3 - 3) + (20 + j15)\mathbf{I}_3 = 0$$

$$\mathbf{I}_3 = \frac{3 + j8}{5 + j3} = 1.465 \angle 38.48^\circ$$

$$\mathbf{I}_o = \mathbf{I}_3 = \underline{\underline{1.465 \angle 38.48^\circ \text{ A}}}$$



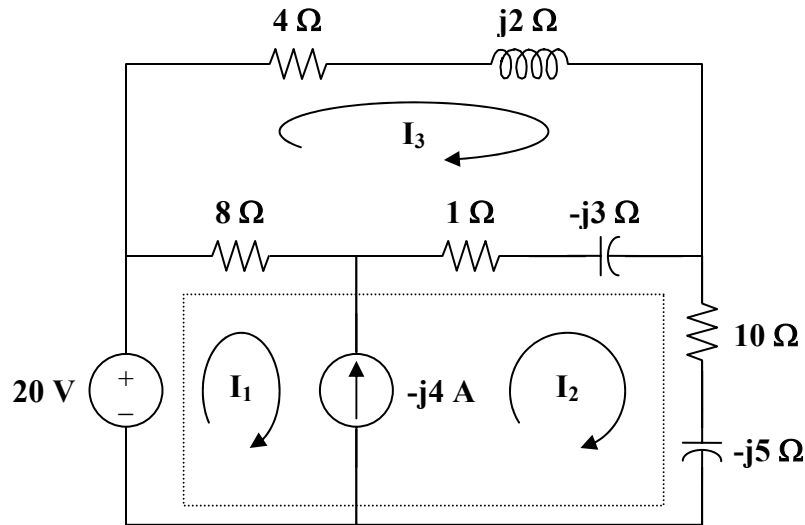
### Chapter 10, Problem 35.



Calculate  $I_o$  in Fig. 10.30 (for Practice Prob. 10.10) using mesh analysis.

### Chapter 10, Solution 35.

Consider the circuit shown below.



For the supermesh,

$$-20 + 8I_1 + (11 - j8)I_2 - (9 - j3)I_3 = 0 \quad (1)$$

Also,

$$I_1 = I_2 + j4 \quad (2)$$

For mesh 3,

$$(13 - j)I_3 - 8I_1 - (1 - j3)I_2 = 0 \quad (3)$$

Substituting (2) into (1),

$$(19 - j8)I_2 - (9 - j3)I_3 = 20 - j32 \quad (4)$$

Substituting (2) into (3),

$$-(9 - j3)I_2 + (13 - j)I_3 = j32 \quad (5)$$

From (4) and (5),

$$\begin{bmatrix} 19 - j8 & -(9 - j3) \\ -(9 - j3) & 13 - j \end{bmatrix} \begin{bmatrix} I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} 20 - j32 \\ j32 \end{bmatrix}$$

$$\Delta = 167 - j69,$$

$$\Delta_2 = 324 - j148$$

$$I_2 = \frac{\Delta_2}{\Delta} = \frac{324 - j148}{167 - j69} = \frac{356.2 \angle -24.55^\circ}{180.69 \angle -22.45^\circ}$$

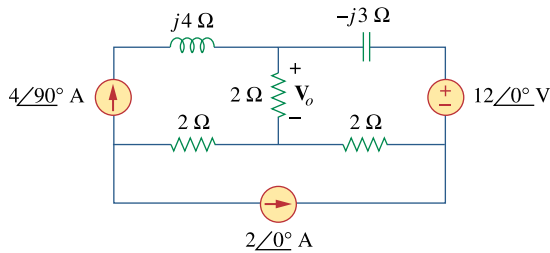
$$I_2 = \underline{\underline{1.971 \angle -2.1^\circ \text{ A}}}$$

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### Chapter 10, Problem 36.



Compute  $V_o$  in the circuit of Fig. 10.81 using mesh analysis.

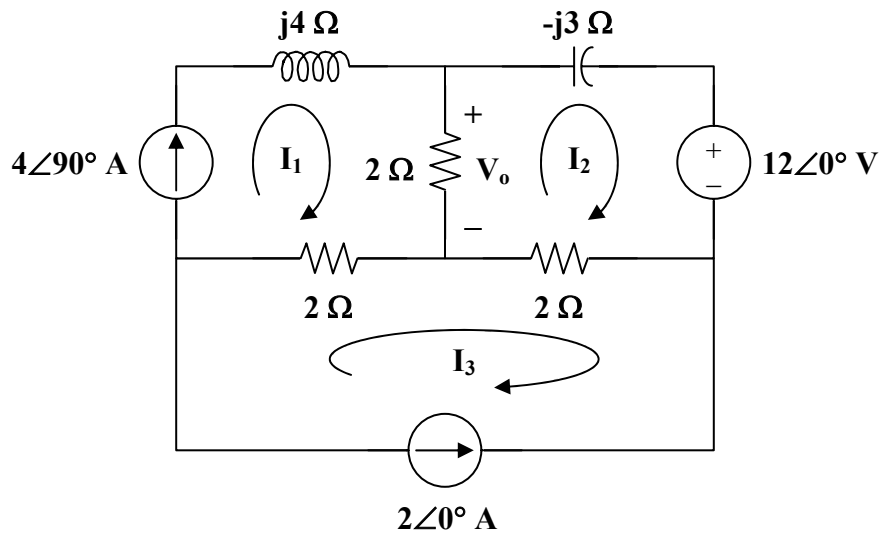


**Figure 10.81**

For Prob. 10.36.

### Chapter 10, Solution 36.

Consider the circuit below.



Clearly,

$$I_1 = 4\angle 90^\circ = j4 \quad \text{and} \quad I_3 = -2$$

For mesh 2,

$$(4 - j3)I_2 - 2I_1 - 2I_3 + 12 = 0$$

$$(4 - j3)I_2 - j8 + 4 + 12 = 0$$

$$I_2 = \frac{-16 + j8}{4 - j3} = -3.52 - j0.64$$

Thus,

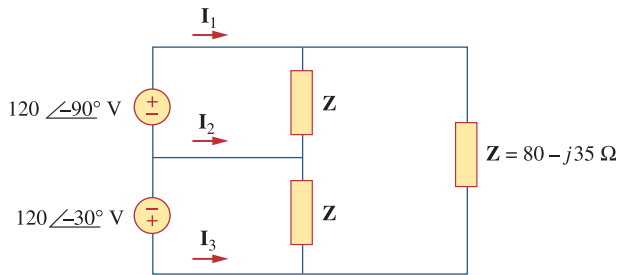
$$V_o = 2(I_1 - I_2) = (2)(3.52 + j4.64) = 7.04 + j9.28$$

$$V_o = \underline{\underline{11.648\angle 52.82^\circ \text{ V}}}$$

**Chapter 10, Problem 37.**



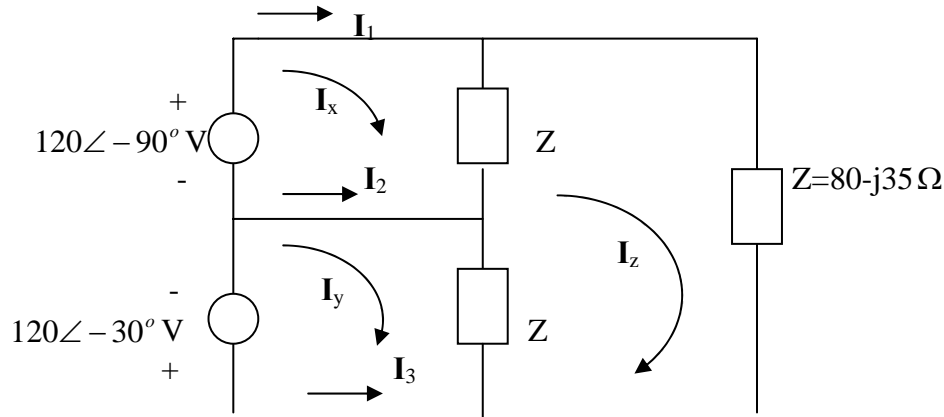
Use mesh analysis to find currents  $\mathbf{I}_1$ ,  $\mathbf{I}_2$ , and  $\mathbf{I}_3$  in the circuit of Fig. 10.82.



**Figure 10.82**

For Prob. 10.37.

**Chapter 10, Solution 37.**



For mesh x,

$$ZI_x - ZI_z = -j120 \quad (1)$$

For mesh y,

$$ZI_y - ZI_z = -120\angle 30^\circ = -103.92 + j60 \quad (2)$$

For mesh z,

$$-ZI_x - ZI_y + 3ZI_z = 0 \quad (3)$$

Putting (1) to (3) together leads to the following matrix equation:

$$\begin{pmatrix} (80 - j35) & 0 & (-80 + j35) \\ 0 & (80 - j35) & (-80 + j35) \\ (-80 + j35) & (-80 + j35) & (240 - j105) \end{pmatrix} \begin{pmatrix} I_x \\ I_y \\ I_z \end{pmatrix} = \begin{pmatrix} -j120 \\ -103.92 + j60 \\ 0 \end{pmatrix} \longrightarrow AI = B$$

Using MATLAB, we obtain

$$I = \text{inv}(A) * B = \begin{pmatrix} -0.2641 - j2.366 \\ -2.181 - j0.954 \\ -0.815 - j1.1066 \end{pmatrix}$$

$$I_1 = I_x = -0.2641 - j2.366 = \underline{2.38\angle -96.37^\circ} \text{ A}$$

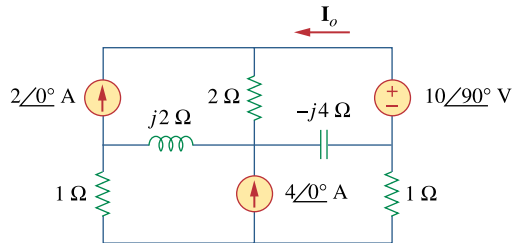
$$I_2 = I_y - I_x = -1.9167 + j1.4116 = \underline{2.38\angle 143.63^\circ} \text{ A}$$

$$I_3 = -I_y = 2.181 + j0.954 = \underline{2.38\angle 23.63^\circ} \text{ A}$$

**Chapter 10, Problem 38.**



Using mesh analysis, obtain  $\mathbf{I}_o$  in the circuit shown in Fig. 10.83.

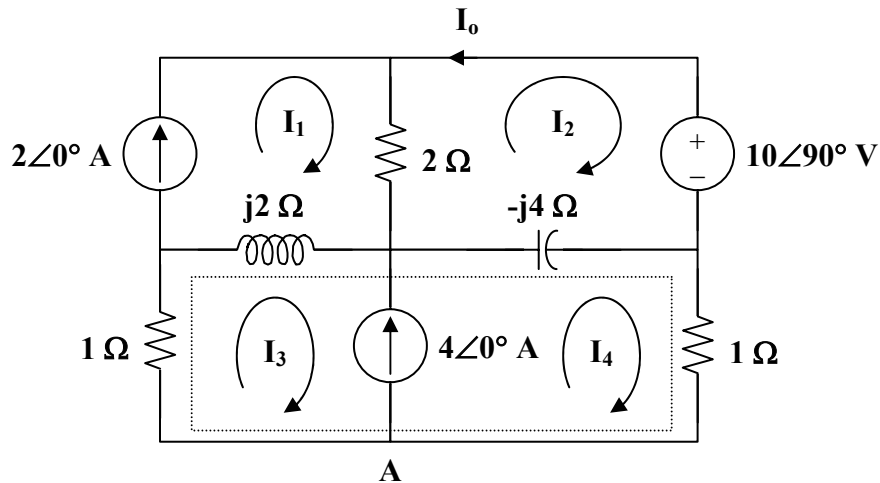


**Figure 10.83**

For Prob. 10.38.

### Chapter 10, Solution 38.

Consider the circuit below.



Clearly,

$$\mathbf{I_1 = 2} \quad (1)$$

For mesh 2,

$$(2 - j4)\mathbf{I_2} - 2\mathbf{I_1} + j4\mathbf{I_4} + 10\angle 90^\circ = 0 \quad (2)$$

Substitute (1) into (2) to get

$$(1 - j2)\mathbf{I_2} + j2\mathbf{I_4} = 2 - j5$$

For the supermesh,

$$\begin{aligned} (1 + j2)\mathbf{I_3} - j2\mathbf{I_1} + (1 - j4)\mathbf{I_4} + j4\mathbf{I_2} &= 0 \\ j4\mathbf{I_2} + (1 + j2)\mathbf{I_3} + (1 - j4)\mathbf{I_4} &= j4 \end{aligned} \quad (3)$$

At node A,

$$\mathbf{I_3 = I_4 - 4} \quad (4)$$

Substituting (4) into (3) gives

$$j2\mathbf{I_2} + (1 - j)\mathbf{I_4} = 2(1 + j3) \quad (5)$$

From (2) and (5),

$$\begin{bmatrix} 1 - j2 & j2 \\ j2 & 1 - j \end{bmatrix} \begin{bmatrix} \mathbf{I_2} \\ \mathbf{I_4} \end{bmatrix} = \begin{bmatrix} 2 - j5 \\ 2 + j6 \end{bmatrix}$$

$$\Delta = 3 - j3, \quad \Delta_1 = 9 - j11$$

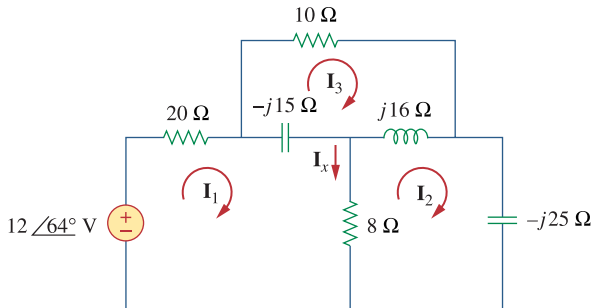
$$\mathbf{I_o = -I_2 = \frac{-\Delta_1}{\Delta} = \frac{-(9 - j11)}{3 - j3} = \frac{1}{3}(-10 + j)}$$

$$\mathbf{I_o = 3.35\angle 174.3^\circ A}$$

### Chapter 10, Problem 39.



Find  $I_1$ ,  $I_2$ ,  $I_3$ , and  $I_x$  in the circuit of Fig. 10.84.



**Figure 10.84**

For Prob. 10.39.

### Chapter 10, Solution 39.

For mesh 1,

$$(28 - j15)I_1 - 8I_2 + j15I_3 = 12\angle 64^\circ \quad (1)$$

For mesh 2,

$$-8I_1 + (8 - j9)I_2 - j16I_3 = 0 \quad (2)$$

For mesh 3,

$$j15I_1 - j16I_2 + (10 + j)I_3 = 0 \quad (3)$$

In matrix form, (1) to (3) can be cast as

$$\begin{pmatrix} (28 - j15) & -8 & j15 \\ -8 & (8 - j9) & -j16 \\ j15 & -j16 & (10 + j) \end{pmatrix} \begin{pmatrix} I_1 \\ I_2 \\ I_3 \end{pmatrix} = \begin{pmatrix} 12\angle 64^\circ \\ 0 \\ 0 \end{pmatrix} \quad \text{or} \quad \mathbf{AI} = \mathbf{B}$$

Using MATLAB,

$$\mathbf{I} = \text{inv}(\mathbf{A}) * \mathbf{B}$$

$$I_1 = -0.128 + j0.3593 = \underline{0.3814\angle 109.6^\circ \text{ A}}$$

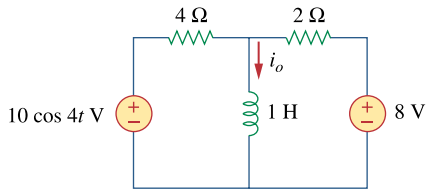
$$I_2 = -0.1946 + j0.2841 = \underline{0.3443\angle 124.4^\circ \text{ A}}$$

$$I_3 = 0.0718 - j0.1265 = \underline{0.1455\angle -60.42^\circ \text{ A}}$$

$$I_x = I_1 - I_2 = 0.0666 + j0.0752 = \underline{0.1005\angle 48.5^\circ \text{ A}}$$

**Chapter 10, Problem 40.**

Find  $i_o$  in the circuit shown in Fig. 10.85 using superposition.

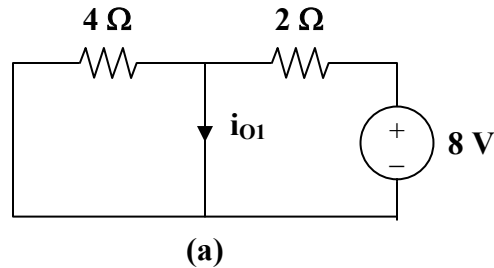


**Figure 10.85**  
For Prob. 10.40.



**Chapter 10, Solution 40.**

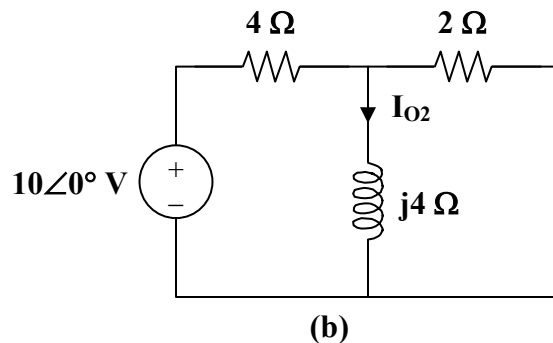
Let  $i_o = i_{o1} + i_{o2}$ , where  $i_{o1}$  is due to the dc source and  $i_{o2}$  is due to the ac source. For  $i_{o1}$ , consider the circuit in Fig. (a).



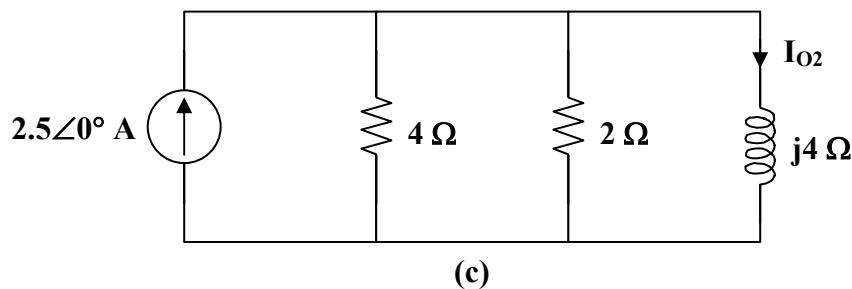
Clearly,

$$i_{o1} = 8/2 = 4 \text{ A}$$

For  $i_{o2}$ , consider the circuit in Fig. (b).



If we transform the voltage source, we have the circuit in Fig. (c), where  $4 \parallel 2 = 4/3 \Omega$ .



By the current division principle,

$$I_{o2} = \frac{4/3}{4/3 + j4} (2.5 \angle 0^\circ)$$

$$I_{o2} = 0.25 - j0.75 = 0.79 \angle -71.56^\circ$$

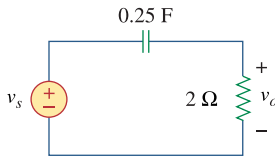
Thus,  $i_{o2} = 0.79 \cos(4t - 71.56^\circ) \text{ A}$

Therefore,

$$i_o = i_{o1} + i_{o2} = \underline{\underline{4 + 0.79 \cos(4t - 71.56^\circ) \text{ A}}}$$

**Chapter 10, Problem 41.**

Find  $v_o$  for the circuit in Fig. 10.86, assuming that  $v_s = 6 \cos 2t + 4 \sin 4t$  V.



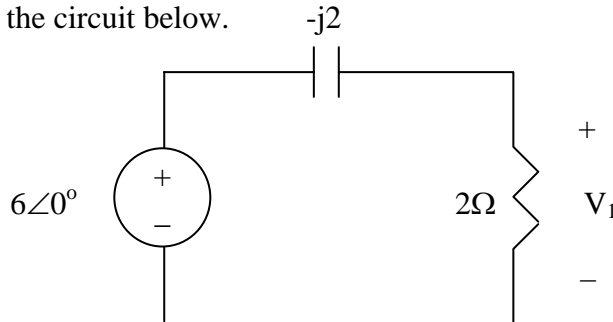
**Figure 10.86**  
For Prob. 10.41.

### Chapter 10, Solution 41.

We apply superposition principle. We let

$$v_o = v_1 + v_2$$

where  $v_1$  and  $v_2$  are due to the sources  $6\cos 2t$  and  $4\sin 4t$  respectively. To find  $v_1$ , consider the circuit below.



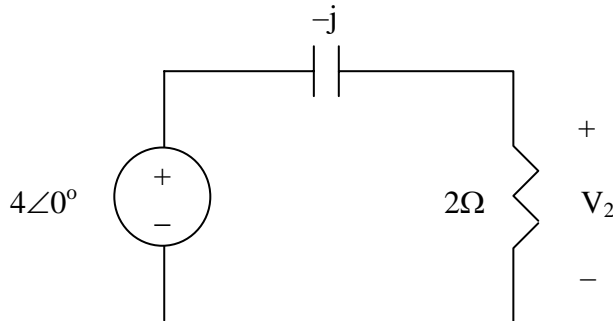
$$1/4F \longrightarrow \frac{1}{j\omega C} = \frac{1}{j2 \times 1/4} = -j2$$

$$V_1 = \frac{2}{2-j2}(6) = 3 + j3 = 4.2426 \angle 45^\circ$$

Thus,

$$v_1 = 4.2426 \cos(2t + 45^\circ)$$

To get  $v_2$ , consider the circuit below



$$1/4F \longrightarrow \frac{1}{j\omega C} = \frac{1}{j4 \times 1/4} = -j1$$

$$V_2 = \frac{2}{2-j}(4) = 3.2 + j1.6 = 3.578 \angle 26.56^\circ$$

$$v_2 = 3.578 \sin(4t + 26.56^\circ)$$

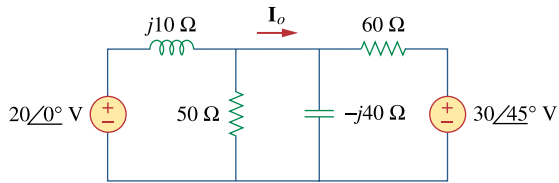
Hence,

$$v_o = \underline{\underline{4.243\cos(2t + 45^\circ) + 3.578\sin(4t + 25.56^\circ) \text{ V}}}$$

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### Chapter 10, Problem 42.

Solve for  $I_o$  in the circuit of Fig. 10.87.



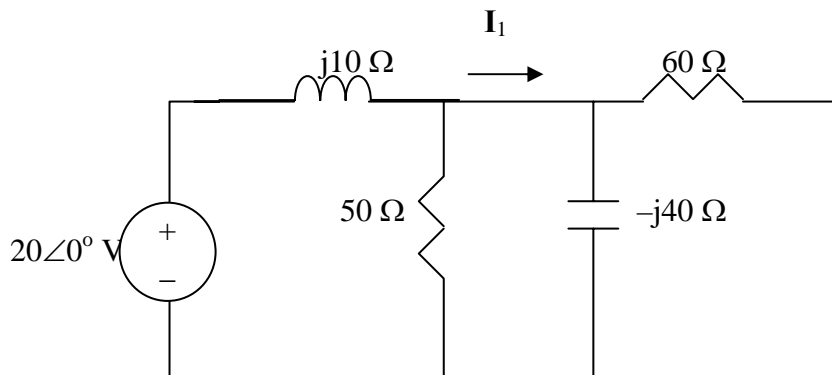
**Figure 10.87**

For Prob. 10.42.

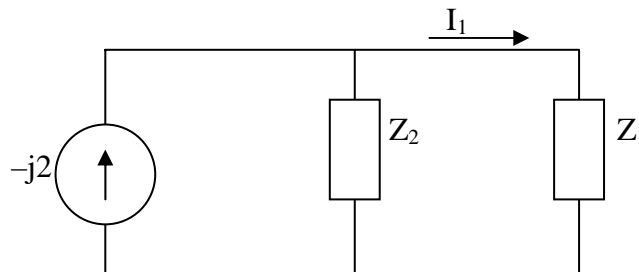
### Chapter 10, Solution 42.

$$\text{Let } I_o = I_1 + I_2$$

where  $I_1$  and  $I_2$  are due to  $20\angle 0^\circ$  and  $30\angle 45^\circ$  sources respectively. To get  $I_1$ , we use the circuit below.



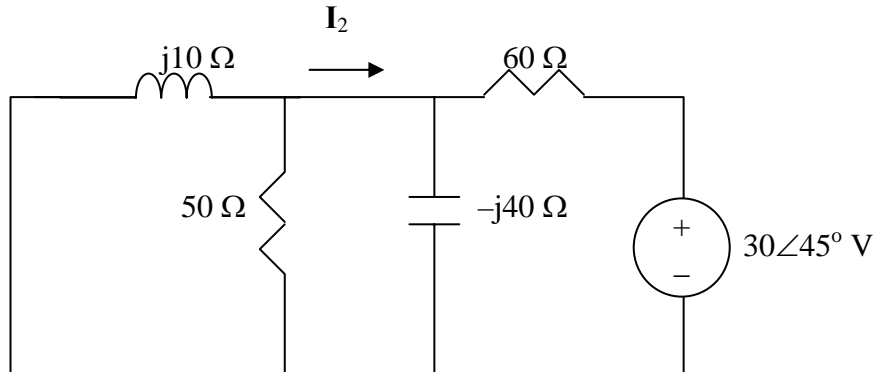
Let  $Z_1 = -j40//60 = 18.4615 - j27.6927$ ,  $Z_2 = j10//50 = 1.9231 + j9.615$   
Transforming the voltage source to a current source leads to the circuit below.



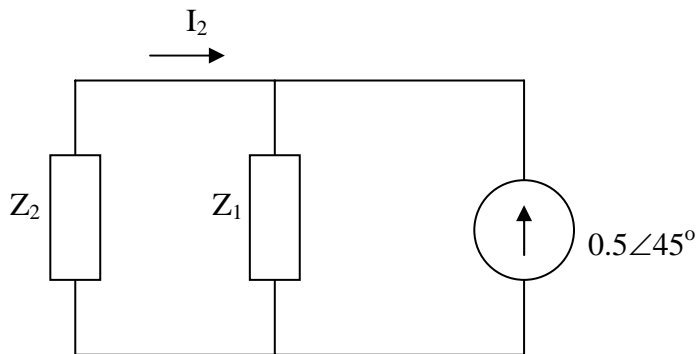
Using current division,

$$I_1 = \frac{Z_2}{Z_1 + Z_2}(-j2) = 0.6217 + j0.3626$$

To get  $I_2$ , we use the circuit below.



After transforming the voltage source, we obtain the circuit below.



Using current division,

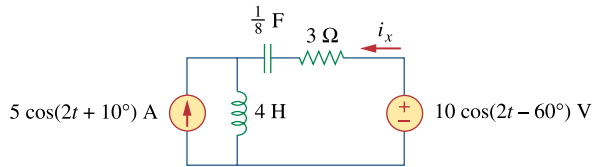
$$I_2 = \frac{-Z_1}{Z_1 + Z_2}(0.5\angle 45^\circ) = -0.5275 - j0.3077$$

Hence,

$$I_o = I_1 + I_2 = 0.0942 + j0.0509 = \underline{0.109\angle 30^\circ \text{ A}}$$

**Chapter 10, Problem 43.**

Using the superposition principle, find  $i_x$  in the circuit of Fig. 10.88.



**Figure 10.88**

For Prob. 10.43.

### Chapter 10, Solution 43.

Let  $\mathbf{I}_x = \mathbf{I}_1 + \mathbf{I}_2$ , where  $\mathbf{I}_1$  is due to the voltage source and  $\mathbf{I}_2$  is due to the current source.

$$\omega = 2$$

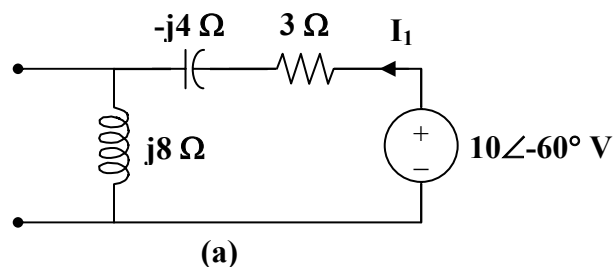
$$5 \cos(2t + 10^\circ) \longrightarrow 5 \angle 10^\circ$$

$$10 \cos(2t - 60^\circ) \longrightarrow 10 \angle -60^\circ$$

$$4 \text{ H} \longrightarrow j\omega L = j8$$

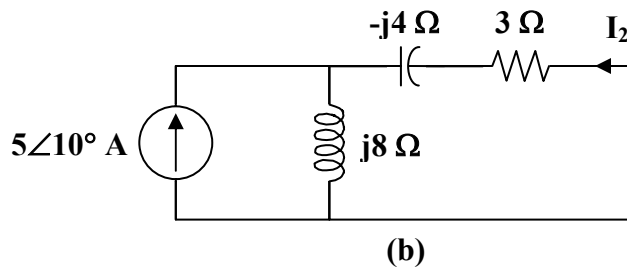
$$\frac{1}{8} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/8)} = -j4$$

For  $\mathbf{I}_1$ , consider the circuit in Fig. (a).



$$\mathbf{I}_1 = \frac{10 \angle -60^\circ}{3 + j8 - j4} = \frac{10 \angle -60^\circ}{3 + j4}$$

For  $\mathbf{I}_2$ , consider the circuit in Fig. (b).



$$\mathbf{I}_2 = \frac{-j8}{3 + j8 - j4} (5 \angle 10^\circ) = \frac{-j40 \angle 10^\circ}{3 + j4}$$

$$\mathbf{I}_x = \mathbf{I}_1 + \mathbf{I}_2 = \frac{1}{3 + j4} (10 \angle -60^\circ - j40 \angle 10^\circ)$$

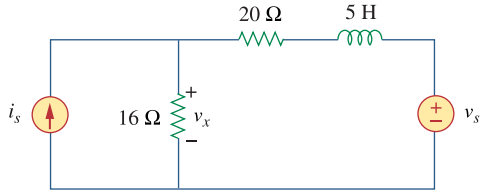
$$\mathbf{I}_x = \frac{49.51 \angle -76.04^\circ}{5 \angle 53.13^\circ} = 9.902 \angle -129.17^\circ$$

Therefore,  $i_x = \underline{\underline{9.902 \cos(2t - 129.17^\circ) \text{ A}}}$

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### Chapter 10, Problem 44.

Use the superposition principle to obtain  $v_x$  in the circuit of Fig. 10.89. Let  $v_s = 50 \sin 2t$  V and  $i_s = 12 \cos(6t + 10^\circ)$  A.



**Figure 10.89**

For Prob. 10.44.

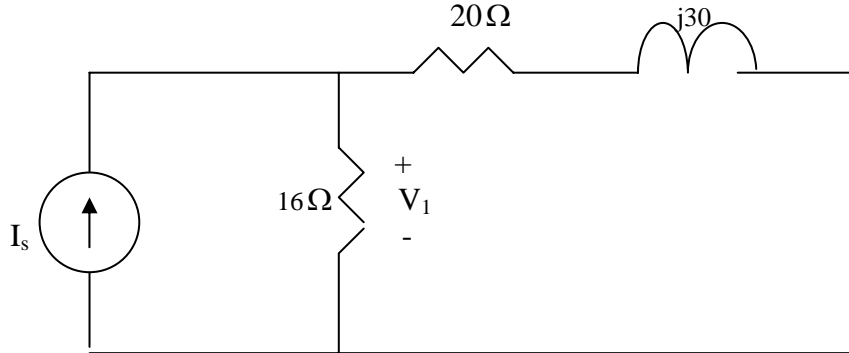


**Chapter 10, Solution 44.**

Let  $v_x = v_1 + v_2$ , where  $v_1$  and  $v_2$  are due to the current source and voltage source respectively.

For  $v_1$ ,  $\omega = 6$ ,  $5 \text{ H} \longrightarrow j\omega L = j30$

The frequency-domain circuit is shown below.

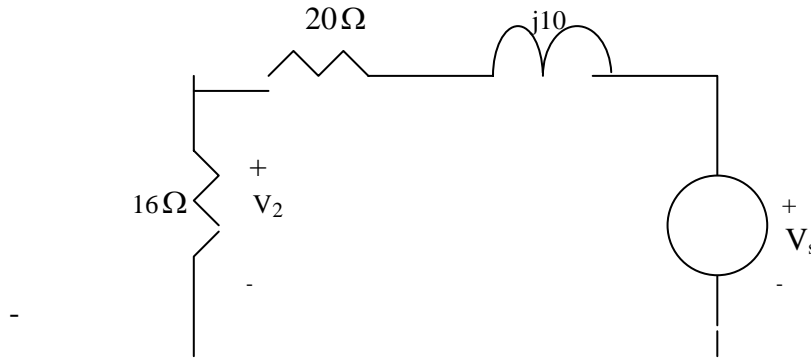


$$\text{Let } Z = 16 \parallel (20 + j30) = \frac{16(20 + j30)}{36 + j30} = 11.8 + j3.497 = 12.31 \angle 16.5^\circ$$

$$V_1 = I_s Z = (12 \angle 10^\circ)(12.31 \angle 16.5^\circ) = 147.7 \angle 26.5^\circ \longrightarrow v_1 = 147.7 \cos(6t + 26.5^\circ) \text{ V}$$

For  $v_2$ ,  $\omega = 2$ ,  $5 \text{ H} \longrightarrow j\omega L = j10$

The frequency-domain circuit is shown below.



Using voltage division,

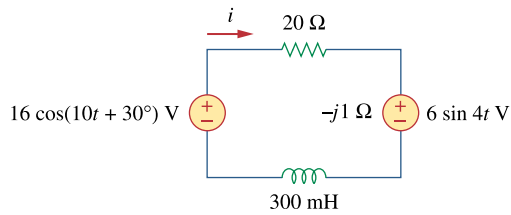
$$V_2 = \frac{16}{16 + 20 + j10} V_s = \frac{16(50 \angle 0^\circ)}{36 + j10} = 21.41 \angle -15.52^\circ \longrightarrow v_2 = 21.41 \sin(2t - 15.52^\circ) \text{ V}$$

Thus,

$$v_x = 147.7 \cos(6t + 26.5^\circ) + 21.41 \sin(2t - 15.52^\circ) \text{ V}$$

### Chapter 10, Problem 45.

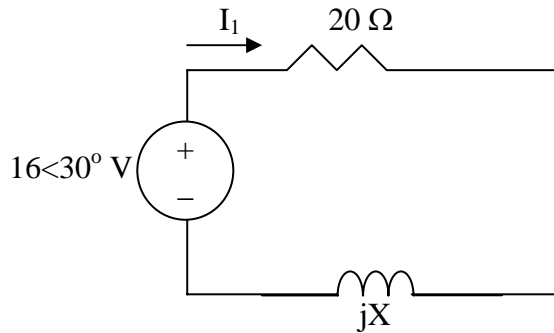
Use superposition to find  $i(t)$  in the circuit of Fig. 10.90.



**Figure 10.90**  
For Prob. 10.45.

### Chapter 10, Solution 45.

Let  $i = i_1 + i_2$ , where  $i_1$  and  $i_2$  are due to  $16\cos(10t + 30^\circ)$  and  $6\sin 4t$  sources respectively. To find  $i_1$ , consider the circuit below.

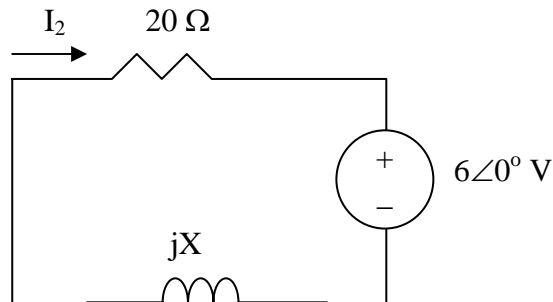


$$X = \omega L = 10 \times 300 \times 10^{-3} = 3$$

$$I_1 = \frac{16 \angle 30^\circ}{20 + j3} = 0.7911$$

$$i_1 = 0.7911 \cos(10t + 21.47^\circ) \text{ A}$$

To find  $i_2$ , consider the circuit below.



$$X = \omega L = 4 \times 300 \times 10^{-3} = 1.2$$

$$I_2 = -\frac{6 \angle 0^\circ}{20 + j1.2} = 0.2995 \angle 176.6^\circ$$

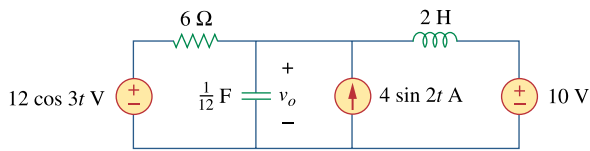
$$i_2 = 0.2995 \sin(4t + 176.6^\circ) \text{ A}$$

Thus,

$$\begin{aligned} i &= i_1 + i_2 = 0.7911 \cos(10t + 21.47^\circ) + 0.2995 \sin(4t + 176.6^\circ) \text{ A} \\ &= \underline{\underline{791.1 \cos(10t + 21.47^\circ) + 299.5 \sin(4t + 176.6^\circ) \text{ mA}}} \end{aligned}$$

### Chapter 10, Problem 46.

Solve for  $v_o(t)$  in the circuit of Fig. 10.91 using the superposition principle.

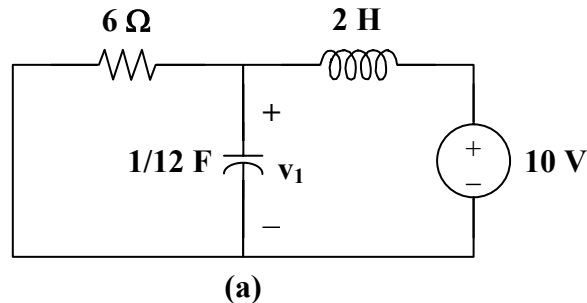


**Figure 10.91**

For Prob. 10.46.

### Chapter 10, Solution 46.

Let  $v_o = v_1 + v_2 + v_3$ , where  $v_1$ ,  $v_2$ , and  $v_3$  are respectively due to the 10-V dc source, the ac current source, and the ac voltage source. For  $v_1$  consider the circuit in Fig. (a).



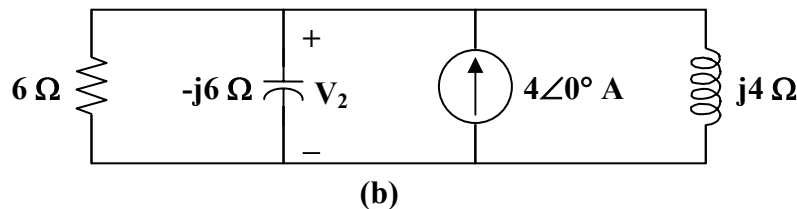
The capacitor is open to dc, while the inductor is a short circuit. Hence,  
 $v_1 = 10 \text{ V}$

For  $v_2$ , consider the circuit in Fig. (b).

$$\omega = 2$$

$$2 \text{ H} \longrightarrow j\omega L = j4$$

$$\frac{1}{12} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/12)} = -j6$$



Applying nodal analysis,

$$4 = \frac{\mathbf{V}_2}{6} + \frac{\mathbf{V}_2}{-j6} + \frac{\mathbf{V}_2}{j4} = \left( \frac{1}{6} + \frac{j}{6} - \frac{j}{4} \right) \mathbf{V}_2$$

$$\mathbf{V}_2 = \frac{24}{1 - j0.5} = 21.45 \angle 26.56^\circ$$

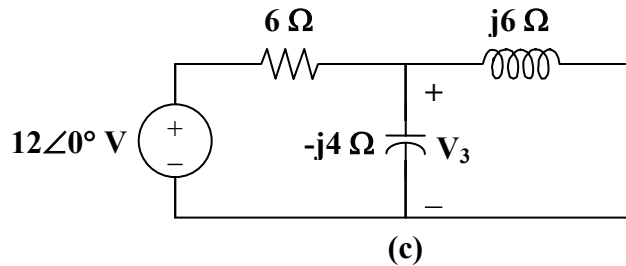
Hence,  $v_2 = 21.45 \sin(2t + 26.56^\circ) \text{ V}$

For  $v_3$ , consider the circuit in Fig. (c).

$$\omega = 3$$

$$2 \text{ H} \longrightarrow j\omega L = j6$$

$$\frac{1}{12} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(3)(1/12)} = -j4$$



At the non-reference node,

$$\frac{12 - \mathbf{V}_3}{6} = \frac{\mathbf{V}_3}{-j4} + \frac{\mathbf{V}_3}{j6}$$

$$\mathbf{V}_3 = \frac{12}{1 + j0.5} = 10.73 \angle -26.56^\circ$$

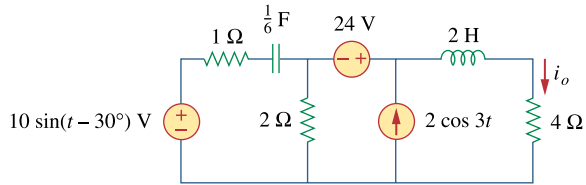
Hence,  $v_3 = 10.73 \cos(3t - 26.56^\circ) \text{ V}$

Therefore,  $v_o = \underline{\underline{10 + 21.45 \sin(2t + 26.56^\circ) + 10.73 \cos(3t - 26.56^\circ) \text{ V}}}$

**Chapter 10, Problem 47.**



Determine  $i_o$  in the circuit of Fig. 10.92, using the superposition principle.

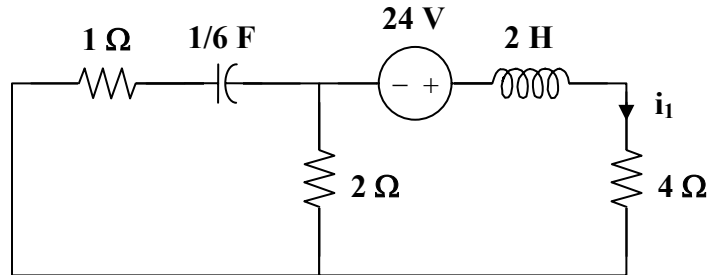


**Figure 10.92**

For Prob. 10.47.

### Chapter 10, Solution 47.

Let  $i_o = i_1 + i_2 + i_3$ , where  $i_1$ ,  $i_2$ , and  $i_3$  are respectively due to the 24-V dc source, the ac voltage source, and the ac current source. For  $i_1$ , consider the circuit in Fig. (a).



Since the capacitor is an open circuit to dc,

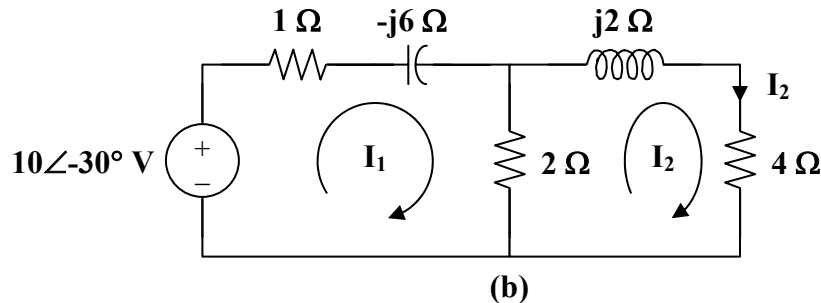
$$i_1 = \frac{24}{4+2} = 4 \text{ A}$$

For  $i_2$ , consider the circuit in Fig. (b).

$$\omega = 1$$

$$2 \text{ H} \longrightarrow j\omega L = j2$$

$$\frac{1}{6} \text{ F} \longrightarrow \frac{1}{j\omega C} = -j6$$



For mesh 1,

$$\begin{aligned} -10\angle -30^\circ + (3 - j6)I_1 - 2I_2 &= 0 \\ 10\angle -30^\circ &= 3(1 - 2j)I_1 - 2I_2 \end{aligned} \quad (1)$$

For mesh 2,

$$\begin{aligned} 0 &= -2I_1 + (6 + j2)I_2 \\ I_1 &= (3 + j)I_2 \end{aligned} \quad (2)$$

Substituting (2) into (1)

$$10 \angle -30^\circ = 13 - j15 \mathbf{I}_2$$

$$\mathbf{I}_2 = 0.504 \angle 19.1^\circ$$

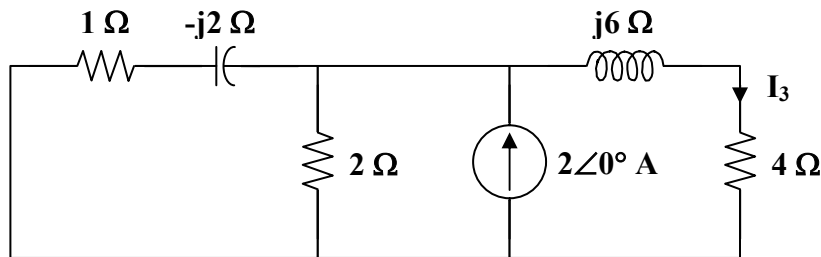
Hence,  $i_2 = 0.504 \sin(t + 19.1^\circ) \text{ A}$

For  $i_3$ , consider the circuit in Fig. (c).

$$\omega = 3$$

$$2 \text{ H} \longrightarrow j\omega L = j6$$

$$\frac{1}{6} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(3)(1/6)} = -j2$$



(c)

$$2 \parallel (1 - j2) = \frac{2(1 - j2)}{3 - j2}$$

Using current division,

$$\mathbf{I}_3 = \frac{\frac{2(1 - j2)}{3 - j2} \cdot (2 \angle 0^\circ)}{4 + j6 + \frac{2(1 - j2)}{3 - j2}} = \frac{2(1 - j2)}{13 + j3}$$

$$\mathbf{I}_3 = 0.3352 \angle -76.43^\circ$$

Hence  $i_3 = 0.3352 \cos(3t - 76.43^\circ) \text{ A}$

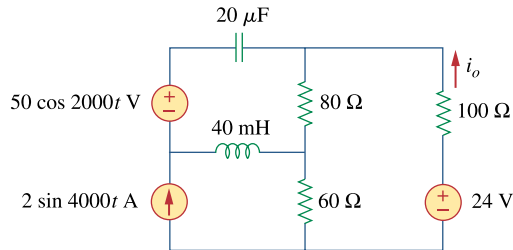
Therefore,  $i_o = \underline{4 + 0.504 \sin(t + 19.1^\circ) + 0.3352 \cos(3t - 76.43^\circ) \text{ A}}$



### Chapter 10, Problem 48.



Find  $i_o$  in the circuit of Fig. 10.93 using superposition.



**Figure 10.93**

For Prob. 10.48.

### Chapter 10, Solution 48.

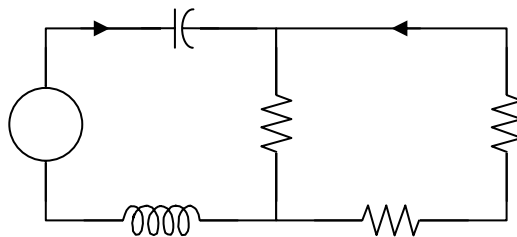
Let  $i_o = i_{o1} + i_{o2} + i_{o3}$ , where  $i_{o1}$  is due to the ac voltage source,  $i_{o2}$  is due to the dc voltage source, and  $i_{o3}$  is due to the ac current source. For  $i_{o1}$ , consider the circuit in Fig. (a).

$$\omega = 2000$$

$$50 \cos(2000t) \longrightarrow 50 \angle 0^\circ$$

$$40 \text{ mH} \longrightarrow j\omega L = j(2000)(40 \times 10^{-3}) = j80$$

$$20 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2000)(20 \times 10^{-6})} = -j25$$



$$80 \parallel (60 + 100) = 160/3$$

$$\mathbf{I} = \frac{50}{160/3 + j80 - j25} = \frac{30}{32 + j33}$$

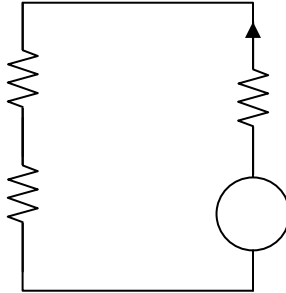
Using current division,

$$\mathbf{I}_{O1} = \frac{-80\mathbf{I}}{80+160} = \frac{-1}{3}\mathbf{I} = \frac{10\angle 180^\circ}{46\angle 45.9^\circ}$$

$$\mathbf{I}_{O1} = 0.217\angle 134.1^\circ$$

Hence,  $i_{O1} = 0.217 \cos(2000t + 134.1^\circ) \text{ A}$

For  $i_{O2}$ , consider the circuit in Fig. (b).



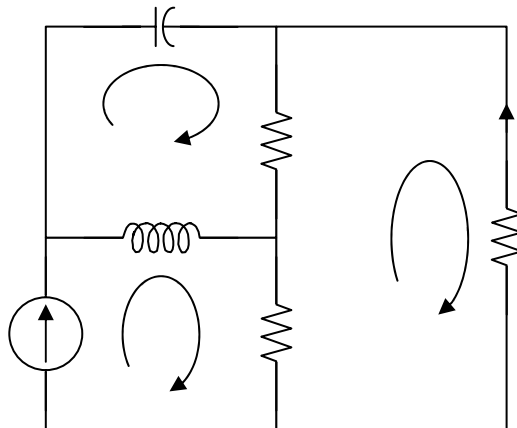
$$i_{O2} = \frac{24}{80+60+100} = 0.1 \text{ A}$$

For  $i_{O3}$ , consider the circuit in Fig. (c).

$$\omega = 4000$$

$$2 \cos(4000t) \longrightarrow 2\angle 0^\circ$$

$$40 \text{ mH} \longrightarrow j\omega L = j(4000)(40 \times 10^{-3}) = j160$$



$$20 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(4000)(20 \times 10^{-6})} = -j12.5$$

For mesh 1,

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$$\mathbf{I}_1 = 2 \quad (1)$$

For mesh 2,

$$(80 + j160 - j12.5)\mathbf{I}_2 - j160\mathbf{I}_1 - 80\mathbf{I}_3 = 0$$

Simplifying and substituting (1) into this equation yields

$$(8 + j14.75)\mathbf{I}_2 - 8\mathbf{I}_3 = j32 \quad (2)$$

For mesh 3,

$$240\mathbf{I}_3 - 60\mathbf{I}_1 - 80\mathbf{I}_2 = 0$$

Simplifying and substituting (1) into this equation yields

$$\mathbf{I}_2 = 3\mathbf{I}_3 - 1.5 \quad (3)$$

Substituting (3) into (2) yields

$$(16 + j44.25)\mathbf{I}_3 = 12 + j54.125$$

$$\mathbf{I}_3 = \frac{12 + j54.125}{16 + j44.25} = 1.1782 \angle 7.38^\circ$$

$$\mathbf{I}_{O3} = -\mathbf{I}_3 = -1.1782 \angle 7.38^\circ$$

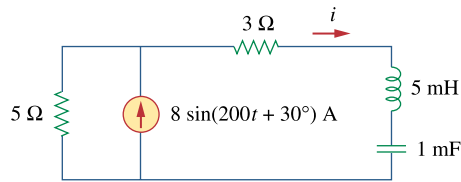
Hence,  $i_{O3} = -1.1782 \sin(4000t + 7.38^\circ) \text{ A}$

Therefore,  $i_O = \underline{\underline{0.1 + 0.217 \cos(2000t + 134.1^\circ) - 1.1782 \sin(4000t + 7.38^\circ) \text{ A}}}$

### Chapter 10, Problem 49.

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Using source transformation, find  $i$  in the circuit of Fig. 10.94.



**Figure 10.94**

For Prob. 10.49.

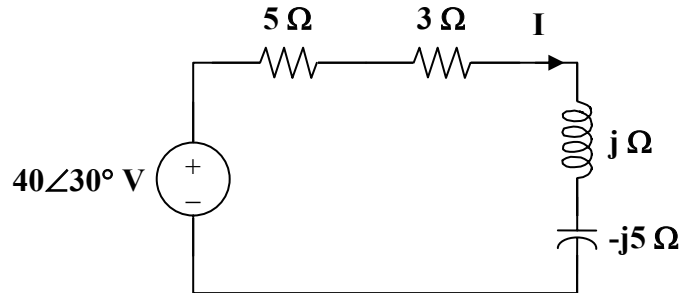
### Chapter 10, Solution 49.

$$8 \sin(200t + 30^\circ) \longrightarrow 8 \angle 30^\circ, \quad \omega = 200$$

$$5 \text{ mH} \longrightarrow j\omega L = j(200)(5 \times 10^{-3}) = j$$

$$1 \text{ mF} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(200)(1 \times 10^{-3})} = -j5$$

After transforming the current source, the circuit becomes that shown in the figure below.



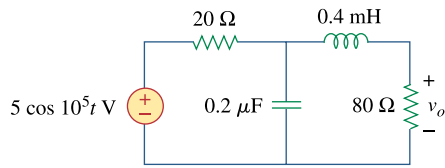
$$I = \frac{40 \angle 30^\circ}{5 + 3 + j - j5} = \frac{40 \angle 30^\circ}{8 - j4} = 4.472 \angle 56.56^\circ$$

$$i = \underline{\underline{4.472 \sin(200t + 56.56^\circ) \text{ A}}}$$

### Chapter 10, Problem 50.

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Use source transformation to find  $v_o$  in the circuit of Fig. 10.95.



**Figure 10.95**  
For Prob. 10.50.

### Chapter 10, Solution 50.

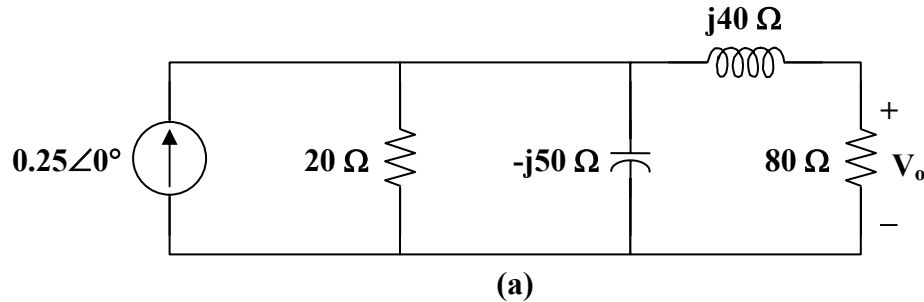
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$$5 \cos(10^5 t) \longrightarrow 5 \angle 0^\circ, \quad \omega = 10^5$$

$$0.4 \text{ mH} \longrightarrow j\omega L = j(10^5)(0.4 \times 10^{-3}) = j40$$

$$0.2 \text{ } \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10^5)(0.2 \times 10^{-6})} = -j50$$

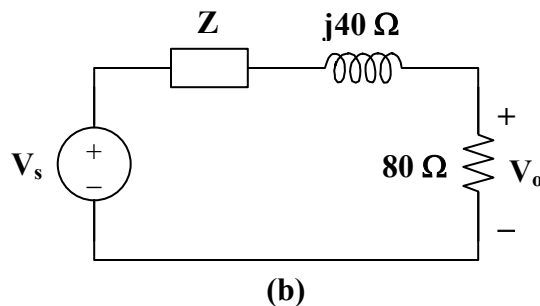
After transforming the voltage source, we get the circuit in Fig. (a).



$$\text{Let } Z = 20 \parallel -j50 = \frac{-j100}{2 - j5}$$

$$\text{and } V_s = (0.25 \angle 0^\circ) Z = \frac{-j25}{2 - j5}$$

With these, the current source is transformed to obtain the circuit in Fig.(b).



By voltage division,

$$V_o = \frac{80}{Z + 80 + j40} V_s = \frac{80}{\frac{-j100}{2 - j5} + 80 + j40} \cdot \frac{-j25}{2 - j5}$$

$$V_o = \frac{8(-j25)}{36 - j42} = 3.615 \angle -40.6^\circ$$

$$\text{Therefore, } v_o = \underline{\underline{3.615 \cos(10^5 t - 40.6^\circ) \text{ V}}}$$

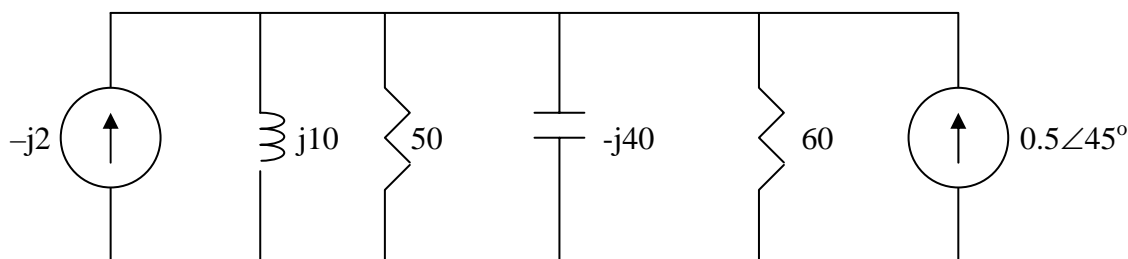
### Chapter 10, Problem 51.

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Use source transformation to find  $I_o$  in the circuit of Prob. 10.42.

### Chapter 10, Solution 51.

Transforming the voltage sources into current sources, we have the circuit as shown below.



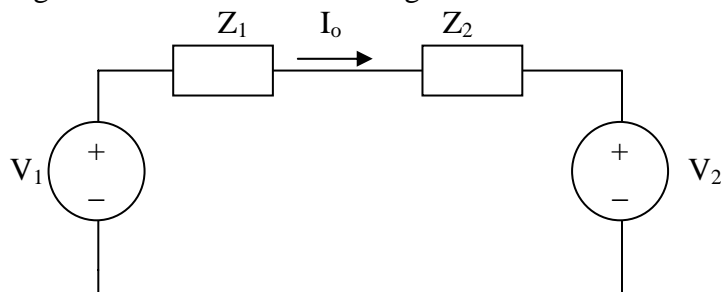
$$\text{Let } Z_1 = j10 // 50 = \frac{j10 \times 50}{50 + j10} = 1.9231 + j9.615$$

$$V_1 = -j2Z_1 = 19.231 - j3.846$$

$$\text{Let } Z_2 = -j40 // 60 = \frac{-j40 \times 60}{60 - j40} = 18.4615 - j27.6923$$

$$V_2 = Z_2 \times 0.5 \angle 45^\circ = 16.315 - 3.263$$

Transforming the current sources to voltage sources leads to the circuit below.



Applying KVL to the loop gives

$$-V_1 + I_o(Z_1 + Z_2) + V_2 = 0 \quad \longrightarrow \quad I_o = \frac{V_1 - V_2}{Z_1 + Z_2}$$

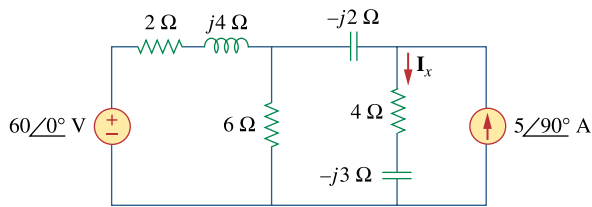
$$I_o = \frac{19.231 - j3.846 - 16.315 + j3.263}{1.9231 + j9.615 + 18.4615 - j27.6923} = \underline{0.1093 \angle 30^\circ \text{ A}} = \underline{\underline{109.3 \angle 30^\circ \text{ mA}}}$$

### Chapter 10, Problem 52.

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Use the method of source transformation to find  $\mathbf{I}_x$  in the circuit of Fig. 10.96.



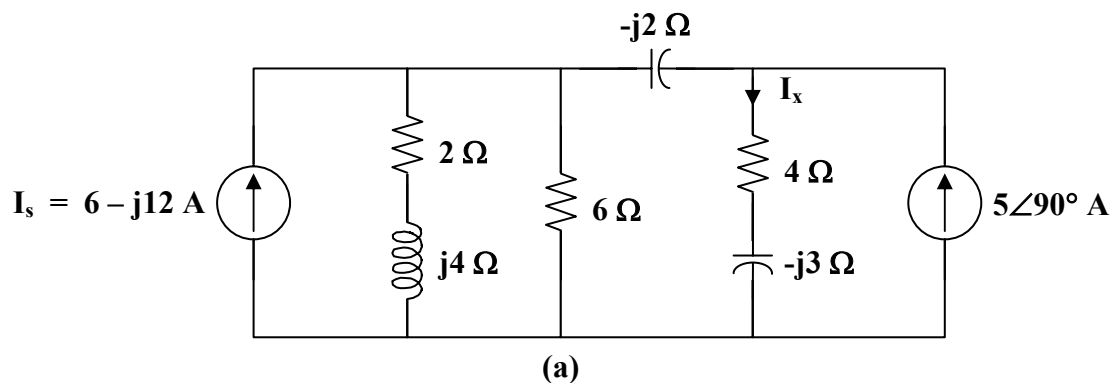
**Figure 10.96**  
For Prob. 10.52.

### Chapter 10, Solution 52.

We transform the voltage source to a current source.

$$\mathbf{I}_s = \frac{60\angle 0^\circ}{2 + j4} = 6 - j12$$

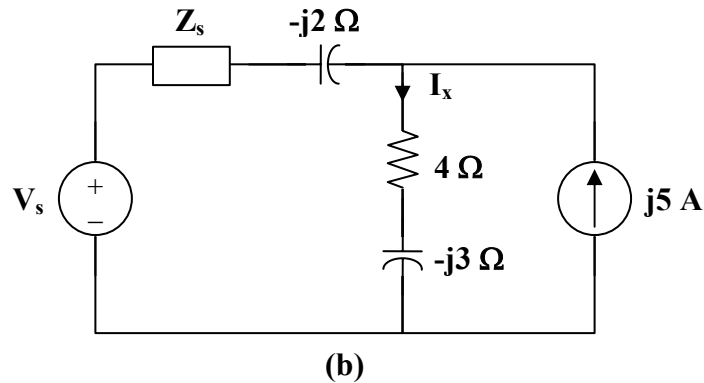
The new circuit is shown in Fig. (a).



$$\begin{aligned} \text{Let } \mathbf{Z}_s &= 6 \parallel (2 + j4) = \frac{6(2 + j4)}{8 + j4} = 2.4 + j1.8 \\ \mathbf{V}_s &= \mathbf{I}_s \mathbf{Z}_s = (6 - j12)(2.4 + j1.8) = 36 - j18 = 18(2 - j) \end{aligned}$$



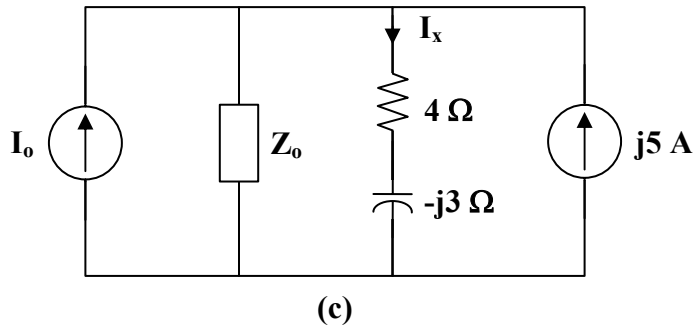
With these, we transform the current source on the left hand side of the circuit to a voltage source. We obtain the circuit in Fig. (b).



Let  $Z_o = Z_s - j2 = 2.4 - j0.2 = 0.2(12 - j)$

$$I_o = \frac{V_s}{Z_o} = \frac{18(2 - j)}{0.2(12 - j)} = 15.517 - j6.207$$

With these, we transform the voltage source in Fig. (b) to a current source. We obtain the circuit in Fig. (c).



Using current division,

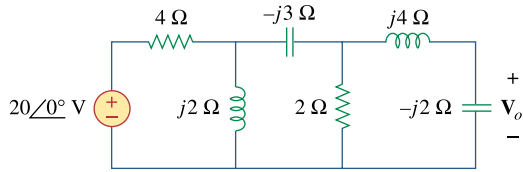
$$I_x = \frac{Z_o}{Z_o + 4 - j3} (I_o + j5) = \frac{2.4 - j0.2}{6.4 - j3.2} (15.517 - j1.207)$$

$$I_x = 5 + j1.5625 = \underline{\underline{5.238 \angle 17.35^\circ \text{ A}}}$$

### Chapter 10, Problem 53.



Use the concept of source transformation to find  $V_o$  in the circuit of Fig. 10.97.

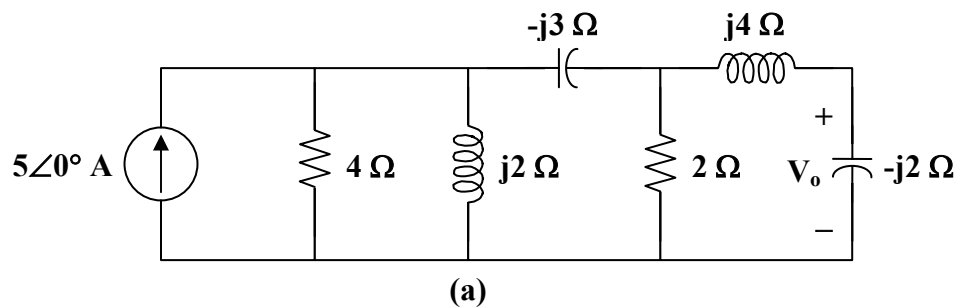


**Figure 10.97**

For Prob. 10.53.

### Chapter 10, Solution 53.

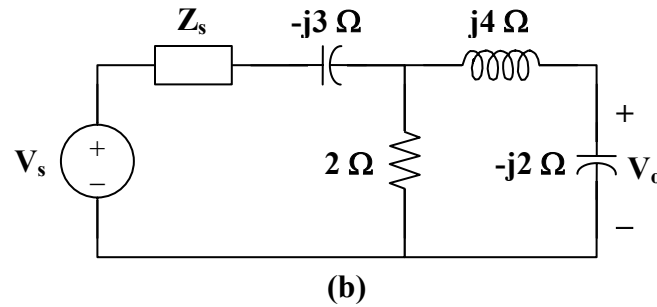
We transform the voltage source to a current source to obtain the circuit in Fig. (a).



$$\text{Let } \mathbf{Z}_s = 4 \parallel j2 = \frac{j8}{4 + j2} = 0.8 + j1.6$$

$$\mathbf{V}_s = (5\angle 0^\circ) \mathbf{Z}_s = (5)(0.8 + j1.6) = 4 + j8$$

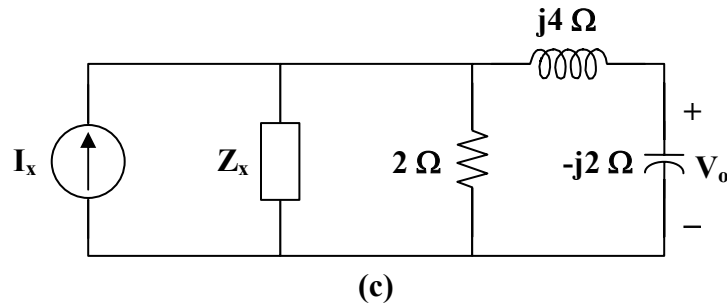
With these, the current source is transformed so that the circuit becomes that shown in Fig. (b).



Let  $\mathbf{Z}_x = \mathbf{Z}_s - j3 = 0.8 - j1.4$

$$\mathbf{I}_x = \frac{\mathbf{V}_s}{\mathbf{Z}_s} = \frac{4 + j8}{0.8 - j1.4} = -3.0769 + j4.6154$$

With these, we transform the voltage source in Fig. (b) to obtain the circuit in Fig. (c).

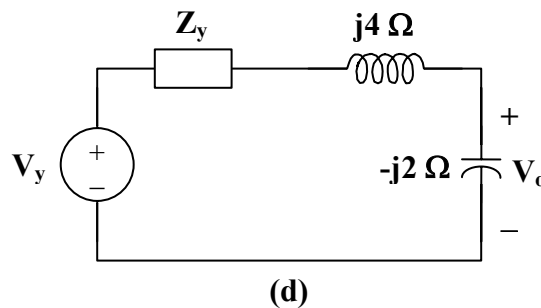


Let  $\mathbf{Z}_y = 2 \parallel \mathbf{Z}_x = \frac{1.6 - j2.8}{2.8 - j1.4} = 0.8571 - j0.5714$

$$\mathbf{V}_y = \mathbf{I}_x \mathbf{Z}_y = (-3.0769 + j4.6154) \cdot (0.8571 - j0.5714) = j5.7143$$

With these, we transform the current source to obtain the circuit in Fig. (d).

Using current division,



$$\mathbf{V}_o = \frac{-j2}{\mathbf{Z}_y + j4 - j2} \mathbf{V}_y = \frac{-j2(j5.7143)}{0.8571 - j0.5714 + j4 - j2} = \underline{\underline{(3.529 - j5.883) \text{ V}}}$$

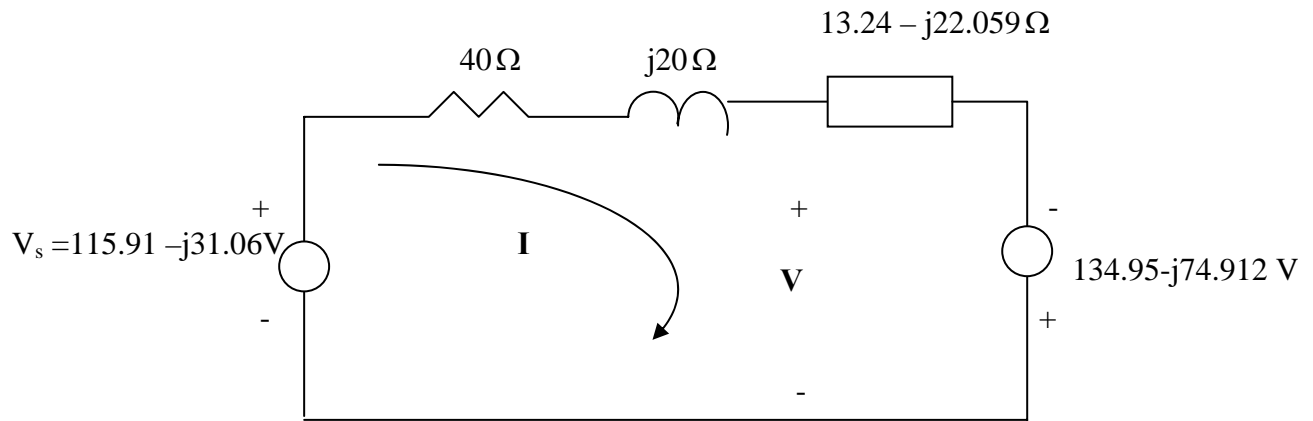
### Chapter 10, Problem 54.

Rework Prob. 10.7 using source transformation.

### Chapter 10, Solution 54.

$$50 \parallel (-j30) = \frac{50(-j30)}{50 - j30} = 13.24 - j22.059$$

We convert the current source to voltage source and obtain the circuit below.



Applying KVL gives

$$-115.91 + j31.058 + (53.24 - j2.059)I - 134.95 + j74.912 = 0$$

$$\text{or } I = \frac{-250.86 + j105.97}{53.24 - j2.059} = -4.7817 + j1.8055$$

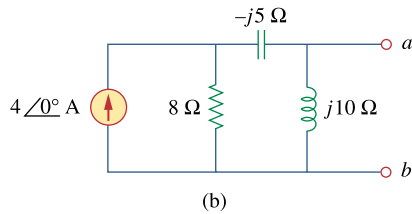
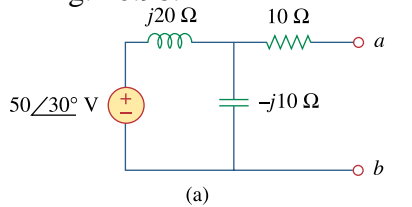
$$\text{But } -V_s + (40 + j20)I + V = 0 \quad \longrightarrow \quad V = V_s - (40 + j20)I$$

$$V = 115.91 - j31.05 - (40 + j20)(-4.7817 + j1.8055) = \underline{124.06 \angle -154^\circ \text{ V}}$$

which agrees with the result in Prob. 10.7.

**Chapter 10, Problem 55.**

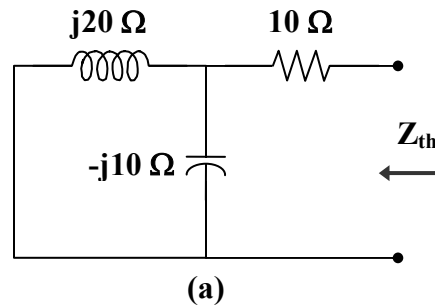
Find the Thevenin and Norton equivalent circuits at terminals  $a$ - $b$  for each of the circuits in Fig. 10.98.

**Figure 10.98**

For Prob. 10.55.

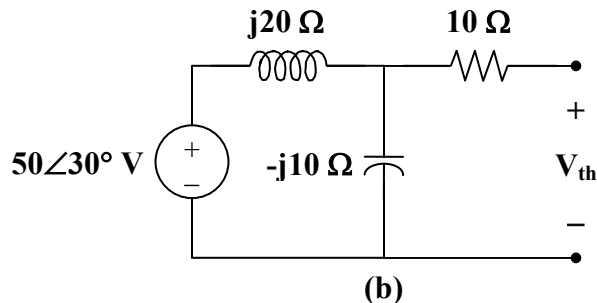
**Chapter 10, Solution 55.**

(a) To find  $\mathbf{Z}_{th}$ , consider the circuit in Fig. (a).



$$\begin{aligned}\mathbf{Z}_N = \mathbf{Z}_{th} &= 10 + j20 \parallel (-j10) = 10 + \frac{(j20)(-j10)}{j20 - j10} \\ &= 10 - j20 = \underline{\underline{22.36\angle -63.43^\circ \Omega}}\end{aligned}$$

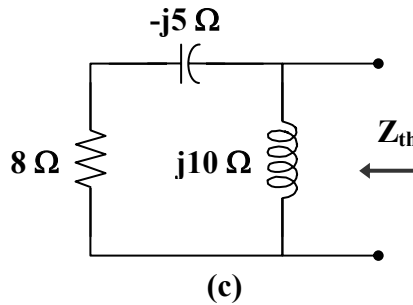
To find  $\mathbf{V}_{th}$ , consider the circuit in Fig. (b).



$$\mathbf{V}_{th} = \frac{-j10}{j20 - j10} (50 \angle 30^\circ) = \underline{\underline{-50 \angle 30^\circ \text{ V}}}$$

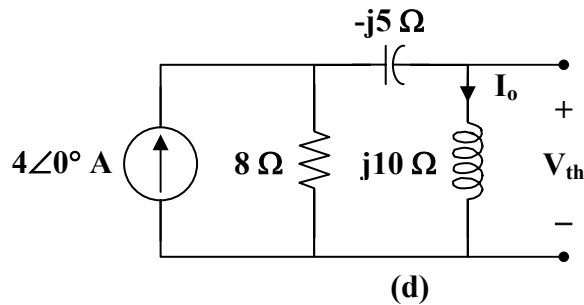
$$\mathbf{I}_N = \frac{\mathbf{V}_{th}}{\mathbf{Z}_{th}} = \frac{-50 \angle 30^\circ}{22.36 \angle -63.43^\circ} = \underline{\underline{2.236 \angle 273.4^\circ \text{ A}}}$$

(b) To find  $\mathbf{Z}_{th}$ , consider the circuit in Fig. (c).



$$\mathbf{Z}_N = \mathbf{Z}_{th} = j10 \parallel (8 - j5) = \frac{(j10)(8 - j5)}{j10 + 8 - j5} = \underline{\underline{10 \angle 26^\circ \Omega}}$$

To obtain  $\mathbf{V}_{th}$ , consider the circuit in Fig. (d).



By current division,

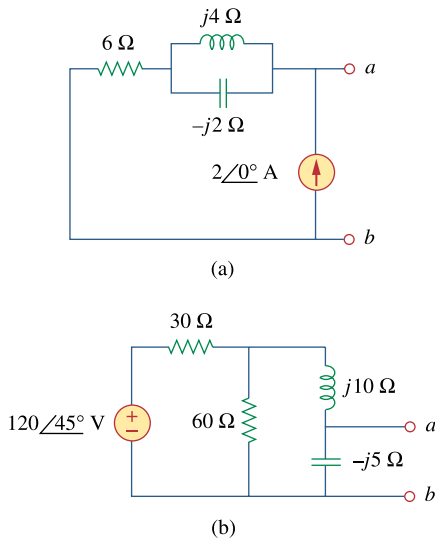
$$\mathbf{I}_o = \frac{8}{8 + j10 - j5} (4 \angle 0^\circ) = \frac{32}{8 + j5}$$

$$\mathbf{V}_{th} = j10 \mathbf{I}_o = \frac{j320}{8 + j5} = \underline{\underline{33.92 \angle 58^\circ \text{ V}}}$$

$$\mathbf{I}_N = \frac{\mathbf{V}_{th}}{\mathbf{Z}_{th}} = \frac{33.92 \angle 58^\circ}{10 \angle 26^\circ} = \underline{\underline{3.392 \angle 32^\circ \text{ A}}}$$

### Chapter 10, Problem 56.

For each of the circuits in Fig. 10.99, obtain Thevenin and Norton equivalent circuits at terminals  $a$ - $b$ .

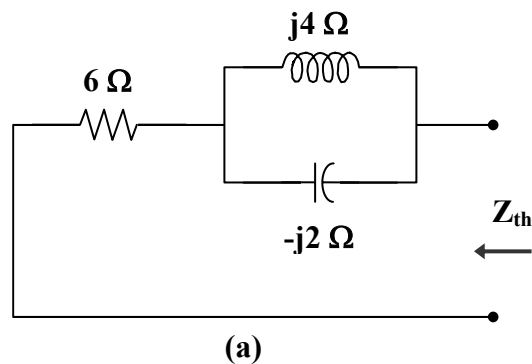


**Figure 10.99**

For Prob. 10.56.

### Chapter 10, Solution 56.

(a) To find  $\mathbf{Z}_{th}$ , consider the circuit in Fig. (a).



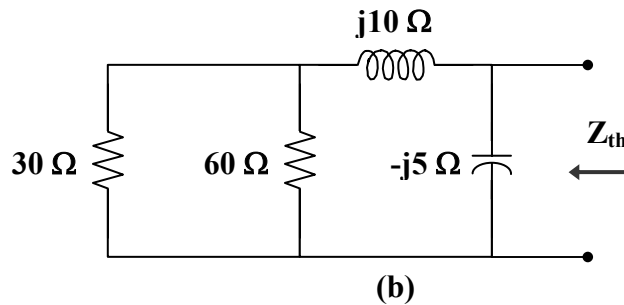
$$\begin{aligned}\mathbf{Z}_N = \mathbf{Z}_{th} &= 6 + j4 \parallel (-j2) = 6 + \frac{(j4)(-j2)}{j4 - j2} = 6 - j4 \\ &= \underline{\underline{7.211 \angle -33.69^\circ \Omega}}\end{aligned}$$

By placing short circuit at terminals  $a$ - $b$ , we obtain,

$$\mathbf{I}_N = \underline{\underline{2 \angle 0^\circ \text{ A}}}$$

$$\mathbf{V}_{th} = \mathbf{Z}_{th} \mathbf{I}_{th} = (7.211 \angle -33.69^\circ)(2 \angle 0^\circ) = \underline{\underline{14.422 \angle -33.69^\circ \text{ V}}}$$

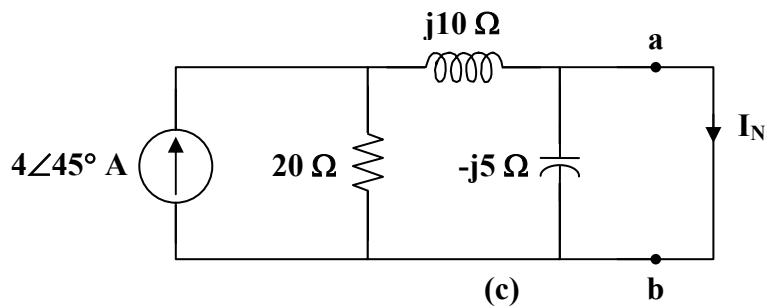
- (b) To find  $\mathbf{Z}_{th}$ , consider the circuit in Fig. (b).



$$30 \parallel 60 = 20$$

$$\begin{aligned}\mathbf{Z}_N = \mathbf{Z}_{th} &= -j5 \parallel (20 + j10) = \frac{(-j5)(20 + j10)}{20 + j5} \\ &= \underline{\underline{5.423 \angle -77.47^\circ \Omega}}\end{aligned}$$

To find  $\mathbf{V}_{th}$  and  $\mathbf{I}_N$ , we transform the voltage source and combine the  $30 \Omega$  and  $60 \Omega$  resistors. The result is shown in Fig. (c).



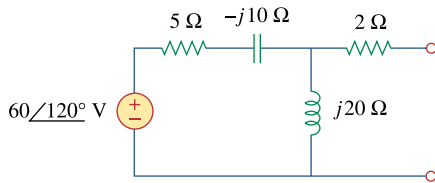
$$\begin{aligned}\mathbf{I}_N &= \frac{20}{20 + j10} (4 \angle 45^\circ) = \frac{2}{5} (2 - j)(4 \angle 45^\circ) \\ &= \underline{\underline{3.578 \angle 18.43^\circ \text{ A}}}\end{aligned}$$

$$\begin{aligned}\mathbf{V}_{th} = \mathbf{Z}_{th} \mathbf{I}_N &= (5.423 \angle -77.47^\circ) (3.578 \angle 18.43^\circ) \\ &= \underline{\underline{19.4 \angle -59^\circ \text{ V}}}\end{aligned}$$



### Chapter 10, Problem 57.

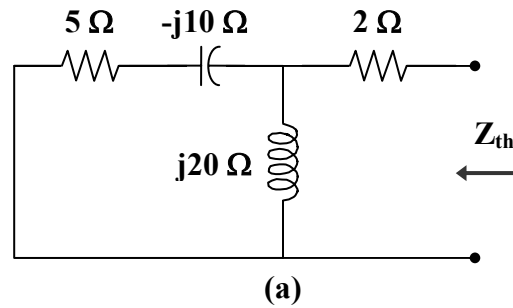
Find the Thevenin and Norton equivalent circuits for the circuit shown in Fig. 10.100.



**Figure 10.100**  
For Prob. 10.57.

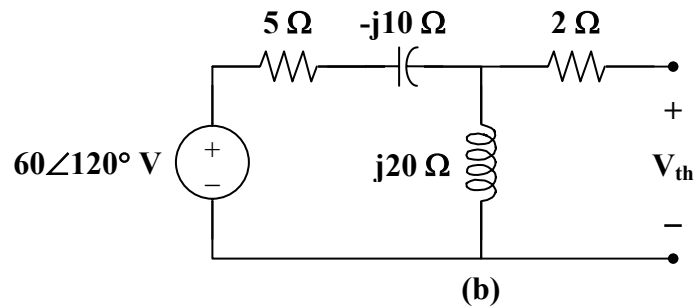
**Chapter 10, Solution 57.**

To find  $\mathbf{Z}_{th}$ , consider the circuit in Fig. (a).



$$\begin{aligned}\mathbf{Z}_N = \mathbf{Z}_{th} &= 2 + j20 \parallel (5 - j10) = 2 + \frac{(j20)(5 - j10)}{5 + j10} \\ &= 18 - j12 = \mathbf{21.63\angle -33.7^\circ \Omega}\end{aligned}$$

To find  $\mathbf{V}_{th}$ , consider the circuit in Fig. (b).

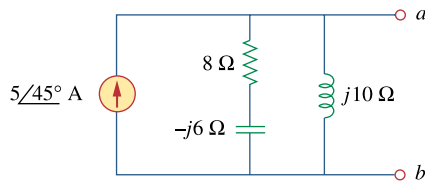


$$\begin{aligned}\mathbf{V}_{th} &= \frac{j20}{5 - j10 + j20} (60\angle 120^\circ) = \frac{j4}{1 + j2} (60\angle 120^\circ) \\ &= \mathbf{107.3\angle 146.56^\circ \text{ V}}\end{aligned}$$

$$\mathbf{I}_N = \frac{\mathbf{V}_{th}}{\mathbf{Z}_{th}} = \frac{107.3\angle 146.56^\circ}{21.633\angle -33.7^\circ} = \mathbf{4.961\angle -179.7^\circ \text{ A}}$$

### Chapter 10, Problem 58.

For the circuit depicted in Fig. 10.101, find the Thevenin equivalent circuit at terminals  $a$ - $b$ .

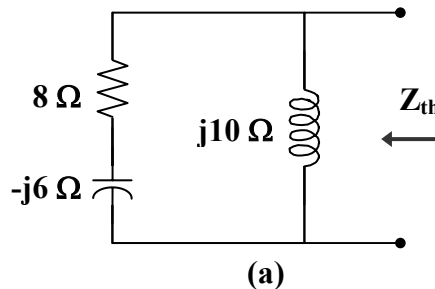


**Figure 10.101**

For Prob. 10.58.

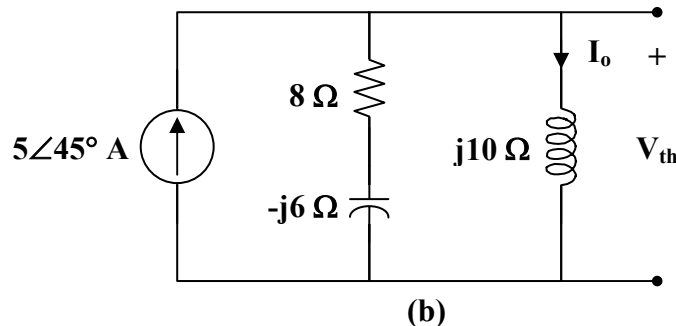
### Chapter 10, Solution 58.

Consider the circuit in Fig. (a) to find  $\mathbf{Z}_{th}$ .



$$\begin{aligned}\mathbf{Z}_{th} &= j10 \parallel (8 - j6) = \frac{(j10)(8 - j6)}{8 + j4} = 5(2 + j) \\ &= \underline{\underline{11.18\angle 26.56^\circ\ \Omega}}\end{aligned}$$

Consider the circuit in Fig. (b) to find  $\mathbf{V}_{th}$ .

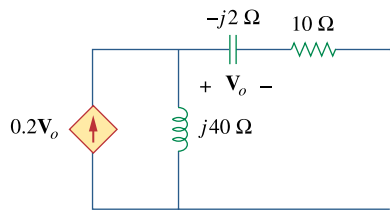


$$\mathbf{I}_o = \frac{8 - j6}{8 - j6 + j10} (5\angle 45^\circ) = \frac{4 - j3}{4 + j2} (5\angle 45^\circ)$$

$$\mathbf{V}_{th} = j10\mathbf{I}_o = \frac{(j10)(4 - j3)(5\angle 45^\circ)}{(2)(2 + j)} = \underline{\underline{55.9\angle 71.56^\circ\ \text{V}}}$$

### Chapter 10, Problem 59.

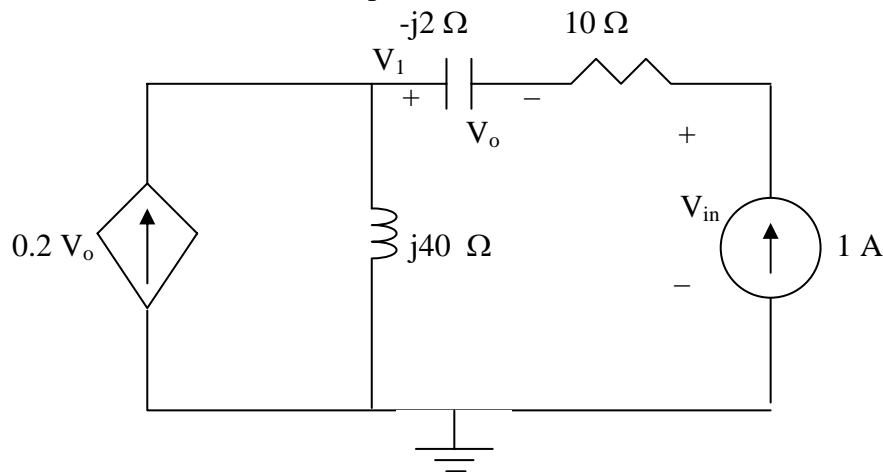
Calculate the output impedance of the circuit shown in Fig. 10.102.



**Figure 10.102**  
For Prob. 10.59.

### Chapter 10, Solution 59.

Insert a 1-A current source at the output as shown below.



$$0.2 v_o + 1 = \frac{V_1}{j40}$$

But  $v_o = -1(-j2) = j2$

$$j2 \times 0.2 + 1 = \frac{V_1}{j40} \quad \longrightarrow \quad V_1 = -16 + j40$$

$$V_{in} = V_1 - V_o + 10 = -6 + j38 = 1 \times Z_{in}$$

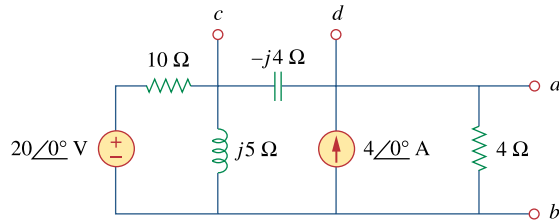
$$Z_{in} = \underline{\underline{-6 + j38 \, \Omega.}}$$

### Chapter 10, Problem 60.



Find the Thevenin equivalent of the circuit in Fig. 10.103 as seen from:

- (a) terminals  $a$ - $b$       (b) terminals  $c$ - $d$

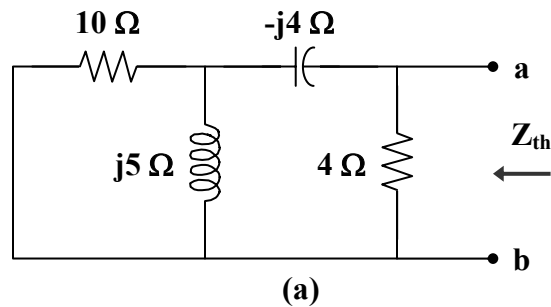


**Figure 10.103**

For Prob. 10.60.

### Chapter 10, Solution 60.

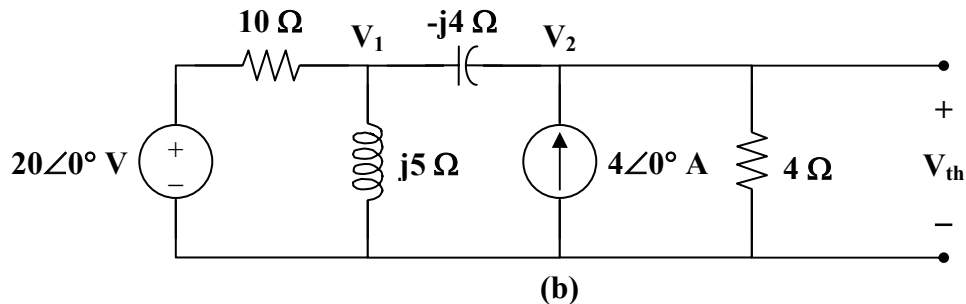
- (a) To find  $Z_{th}$ , consider the circuit in Fig. (a).



$$Z_{th} = 4 \parallel (-j4 + 10 \parallel j5) = 4 \parallel (-j4 + 2 + j4)$$

$$Z_{th} = 4 \parallel 2 = \underline{1.333 \Omega}$$

- To find  $V_{th}$ , consider the circuit in Fig. (b).



At node 1,

$$\frac{20 - V_1}{10} = \frac{V_1}{j5} + \frac{V_1 - V_2}{-j4}$$

$$(1 + j0.5)V_1 - j2.5V_2 = 20 \quad (1)$$

At node 2,

$$4 + \frac{V_1 - V_2}{-j4} = \frac{V_2}{4}$$

$$V_1 = (1 - j)V_2 + j16 \quad (2)$$

Substituting (2) into (1) leads to

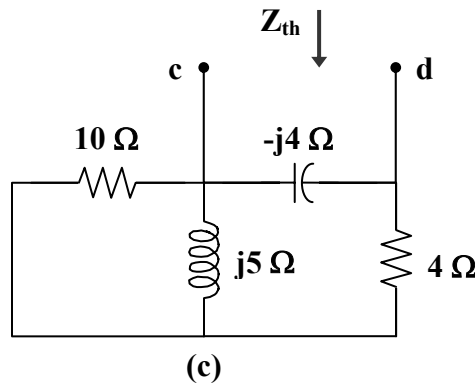
$$28 - j16 = (1.5 - j3)V_2$$

$$V_2 = \frac{28 - j16}{1.5 - j3} = 8 + j5.333$$

Therefore,

$$V_{th} = V_2 = \underline{\underline{9.615 \angle 33.69^\circ \text{ V}}}$$

(b) To find  $Z_{th}$ , consider the circuit in Fig. (c).



$$Z_{th} = -j4 \parallel (4 + 10 \parallel j5) = -j4 \parallel \left(4 + \frac{j10}{2 + j}\right)$$

$$Z_{th} = -j4 \parallel (6 + j4) = \frac{-j4}{6} (6 + j4) = \underline{\underline{2.667 - j4 \Omega}}$$

To find  $V_{th}$ , we will make use of the result in part (a).

$$V_2 = 8 + j5.333 = (8/3)(3 + j2)$$

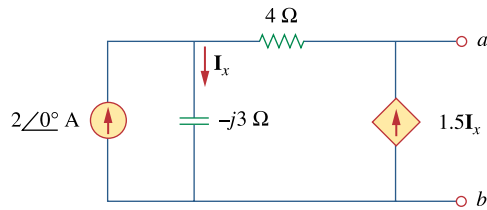
$$V_1 = (1 - j)V_2 + j16 = j16 + (8/3)(5 - j)$$

$$V_{th} = V_1 - V_2 = 16/3 + j8 = \underline{\underline{9.614 \angle 56.31^\circ \text{ V}}}$$

**Chapter 10, Problem 61.**



Find the Thevenin equivalent at terminals  $a$ - $b$  of the circuit in Fig. 10.104.

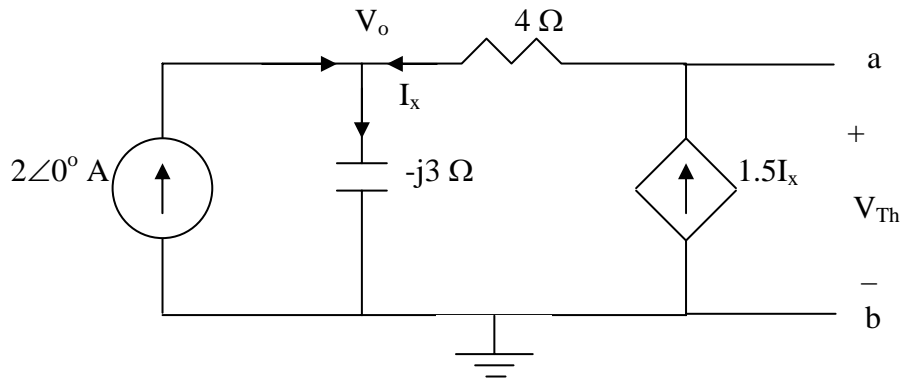


**Figure 10.104**

For Prob. 10.61.

### Chapter 10, Solution 61.

To find  $V_{Th}$ , consider the circuit below

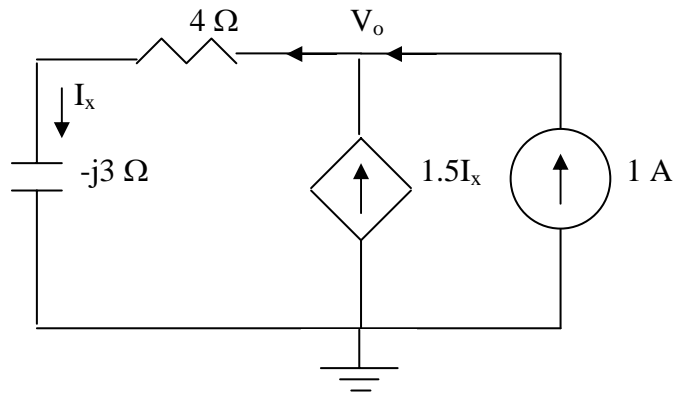


$$2 + 1.5I_x = I_x \longrightarrow I_x = -4$$

$$\text{But } V_o = -j3I_x = j12$$

$$V_{Th} = V_o + 6I_x = \underline{j12 - 24 \text{ V}}$$

To find  $Z_{Th}$ , consider the circuit shown below.



$$1 + 1.5I_x = I_x \Rightarrow I_x = -2$$

$$-V_o + I_x(4 - j3) = 0 \longrightarrow V_o = -8 + j6$$

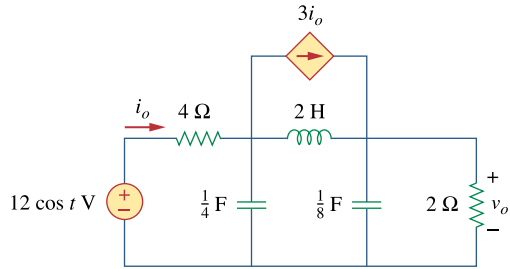
$$Z_{Th} = \frac{V_o}{1} = \underline{-8 + j6 \Omega}$$



**Chapter 10, Problem 62.**



Using Thevenin's theorem, find  $v_o$  in the circuit of Fig. 10.105.



**Figure 10.105**

For Prob. 10.62.

### Chapter 10, Solution 62.

First, we transform the circuit to the frequency domain.

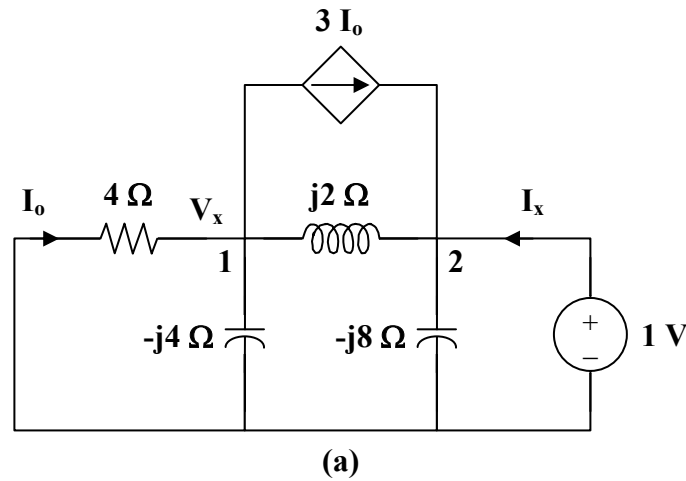
$$12 \cos(t) \longrightarrow 12 \angle 0^\circ, \quad \omega = 1$$

$$2 \text{ H} \longrightarrow j\omega L = j2$$

$$\frac{1}{4} \text{ F} \longrightarrow \frac{1}{j\omega C} = -j4$$

$$\frac{1}{8} \text{ F} \longrightarrow \frac{1}{j\omega C} = -j8$$

To find  $Z_{th}$ , consider the circuit in Fig. (a).



At node 1,

$$\frac{V_x}{4} + \frac{V_x}{-j4} + 3I_o = \frac{1 - V_x}{j2}, \quad \text{where } I_o = \frac{-V_x}{4}$$

Thus, 
$$\frac{V_x}{-j4} - \frac{2V_x}{4} = \frac{1 - V_x}{j2}$$

$$V_x = 0.4 + j0.8$$

At node 2,

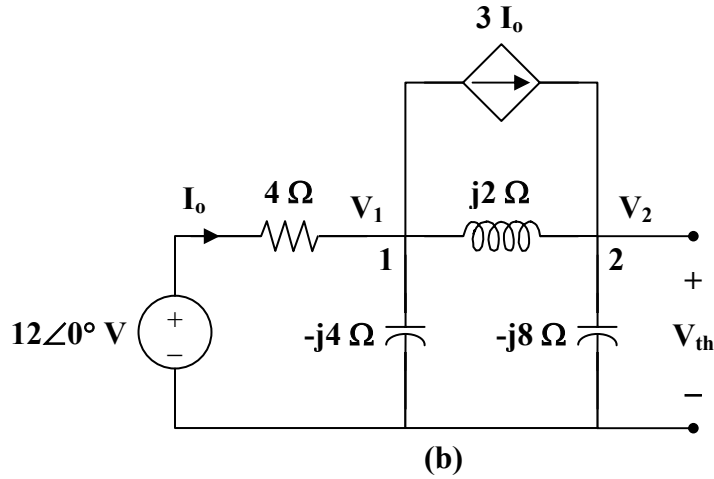
$$I_x + 3I_o = \frac{1}{-j8} + \frac{1 - V_x}{j2}$$

$$I_x = (0.75 + j0.5)V_x - j\frac{3}{8}$$

$$I_x = -0.1 + j0.425$$

$$Z_{th} = \frac{1}{I_x} = -0.5246 - j2.229 = 2.29 \angle -103.24^\circ \Omega$$

To find  $V_{th}$ , consider the circuit in Fig. (b).



At node 1,

$$\frac{12 - V_1}{4} = 3I_o + \frac{V_1}{-j4} + \frac{V_1 - V_2}{j2}, \quad \text{where } I_o = \frac{12 - V_1}{4}$$

$$24 = (2 + j)V_1 - j2V_2 \quad (1)$$

At node 2,

$$\frac{V_1 - V_2}{j2} + 3I_o = \frac{V_2}{-j8}$$

$$72 = (6 + j4)V_1 - j3V_2 \quad (2)$$

From (1) and (2),

$$\begin{bmatrix} 24 \\ 72 \end{bmatrix} = \begin{bmatrix} 2 + j & -j2 \\ 6 + j4 & -j3 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$

$$\Delta = -5 + j6,$$

$$\Delta_2 = -j24$$

$$V_{th} = V_2 = \frac{\Delta_2}{\Delta} = 3.073 \angle -219.8^\circ$$

Thus,

$$V_o = \frac{2}{2 + Z_{th}} V_{th} = \frac{(2)(3.073 \angle -219.8^\circ)}{1.4754 - j2.229}$$

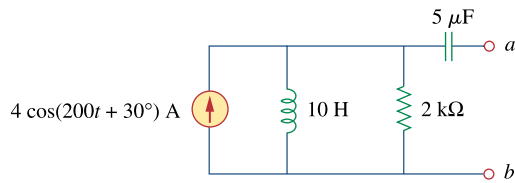
$$V_o = \frac{6.146 \angle -219.8^\circ}{2.673 \angle -56.5^\circ} = 2.3 \angle -163.3^\circ$$

Therefore,  $v_o = \underline{2.3 \cos(t - 163.3^\circ) \text{ V}}$

### Chapter 10, Problem 63.



Obtain the Norton equivalent of the circuit depicted in Fig. 10.106 at terminals  $a$ - $b$ .



**Figure 10.106**

For Prob. 10.63.

**Chapter 10, Solution 63.**

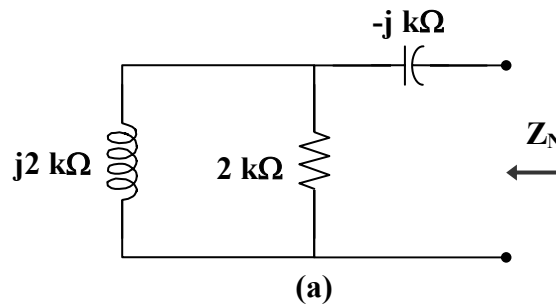
Transform the circuit to the frequency domain.

$$4 \cos(200t + 30^\circ) \longrightarrow 4 \angle 30^\circ, \quad \omega = 200$$

$$10 \text{ H} \longrightarrow j\omega L = j(200)(10) = j2 \text{ k}\Omega$$

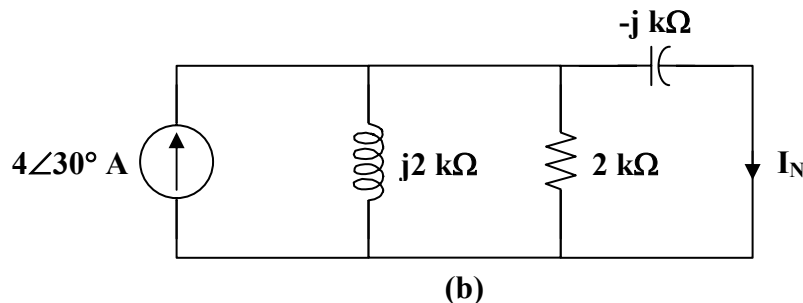
$$5 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(200)(5 \times 10^{-6})} = -j \text{ k}\Omega$$

$Z_N$  is found using the circuit in Fig. (a).



$$Z_N = -j + 2 \parallel j2 = -j + 1 + j = 1 \text{ k}\Omega$$

We find  $I_N$  using the circuit in Fig. (b).



$$j2 \parallel 2 = 1 + j$$

By the current division principle,

$$I_N = \frac{1 + j}{1 + j - j} (4 \angle 30^\circ) = 5.657 \angle 75^\circ$$

Therefore,

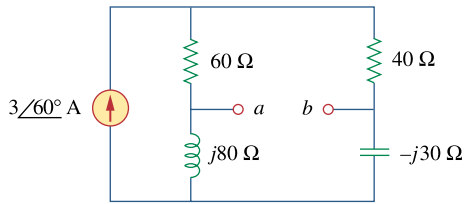
$$i_N = \underline{\underline{5.657 \cos(200t + 75^\circ) \text{ A}}}$$

$$Z_N = \underline{\underline{1 \text{ k}\Omega}}$$

### Chapter 10, Problem 64.



For the circuit shown in Fig. 10.107, find the Norton equivalent circuit at terminals  $a$ - $b$ .

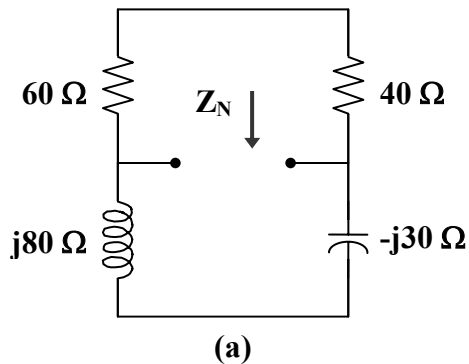


**Figure 10.107**

For Prob. 10.64.

**Chapter 10, Solution 64.**

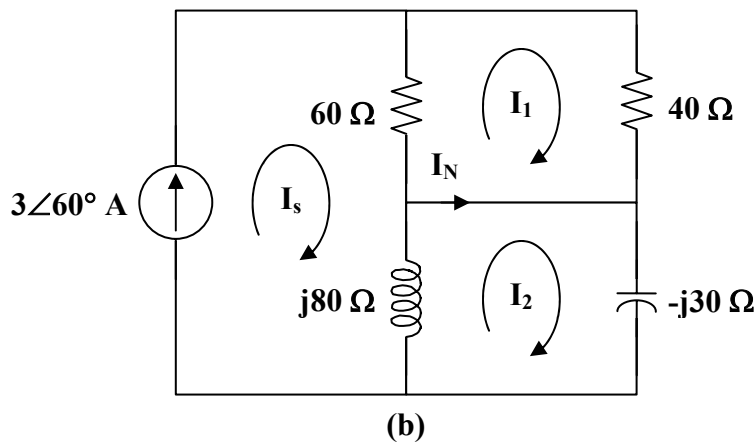
$Z_N$  is obtained from the circuit in Fig. (a).



$$Z_N = (60 + 40) \parallel (j80 - j30) = 100 \parallel j50 = \frac{(100)(j50)}{100 + j50}$$

$$Z_N = 20 + j40 = \underline{\underline{44.72\angle 63.43^\circ \Omega}}$$

To find  $I_N$ , consider the circuit in Fig. (b).



$$I_s = 3\angle 60^\circ$$

For mesh 1,

$$100I_1 - 60I_s = 0$$

$$I_1 = 1.8\angle 60^\circ$$

For mesh 2,

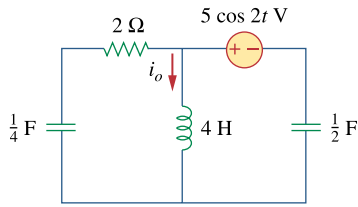
$$(j80 - j30)I_2 - j80I_s = 0$$

$$I_2 = 4.8\angle 60^\circ$$

$$I_N = I_2 - I_1 = \underline{\underline{3\angle 60^\circ \text{ A}}}$$

### Chapter 10, Problem 65.

Compute  $i_o$  in Fig. 10.108 using Norton's theorem.



**Figure 10.108**  
For Prob. 10.65.

### Chapter 10, Solution 65.

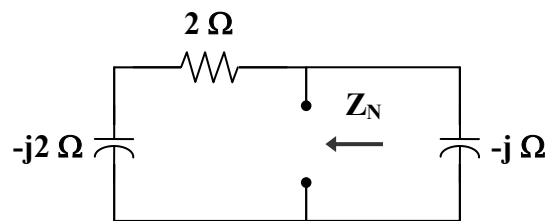
$$5 \cos(2t) \longrightarrow 5 \angle 0^\circ, \quad \omega = 2$$

$$4 \text{ H} \longrightarrow j\omega L = j(2)(4) = j8$$

$$\frac{1}{4} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/4)} = -j2$$

$$\frac{1}{2} \text{ F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(2)(1/2)} = -j$$

To find  $\mathbf{Z}_N$ , consider the circuit in Fig. (a).

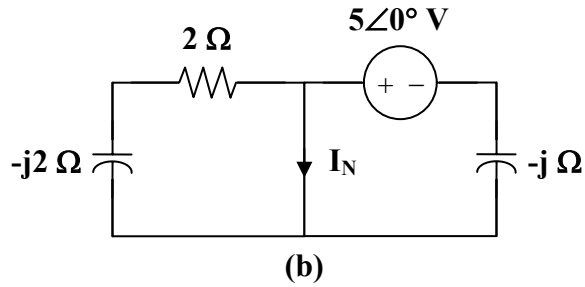


(a)

$$\mathbf{Z}_N = -j \parallel (2 - j2) = \frac{-j(2 - j2)}{2 - j3} = \frac{1}{13}(2 - j10)$$

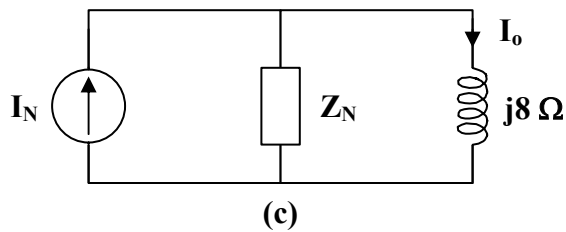


To find  $\mathbf{I}_N$ , consider the circuit in Fig. (b).



$$\mathbf{I}_N = \frac{5\angle 0^\circ}{-j} = j5$$

The Norton equivalent of the circuit is shown in Fig. (c).



Using current division,

$$\mathbf{I}_o = \frac{\mathbf{Z}_N}{\mathbf{Z}_N + j8} \mathbf{I}_N = \frac{(1/13)(2 - j10)(j5)}{(1/13)(2 - j10) + j8} = \frac{50 + j10}{2 + j94}$$

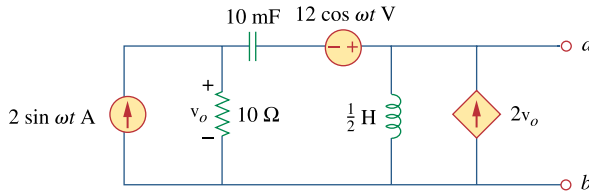
$$\mathbf{I}_o = 0.1176 - j0.5294 = 0.542 \angle -77.47^\circ$$

Therefore,  $i_o = \underline{\underline{542 \cos(2t - 77.47^\circ) \text{ mA}}}$

### Chapter 10, Problem 66.



At terminals  $a$ - $b$ , obtain Thevenin and Norton equivalent circuits for the network depicted in Fig. 10.109. Take  $\omega = 10$  rad/s.



**Figure 10.109**

For Prob. 10.66.

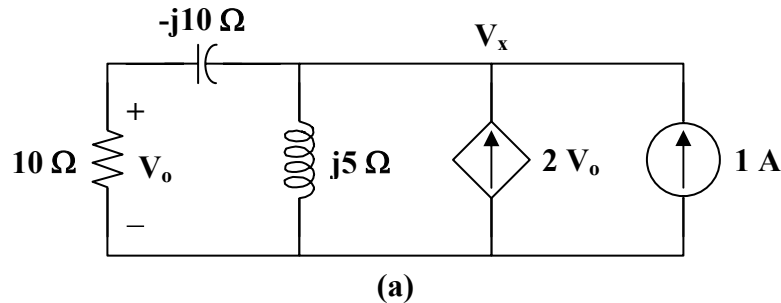
### Chapter 10, Solution 66.

$$\omega = 10$$

$$0.5 \text{ H} \longrightarrow j\omega L = j(10)(0.5) = j5$$

$$10 \text{ mF} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10)(10 \times 10^{-3})} = -j10$$

To find  $Z_{th}$ , consider the circuit in Fig. (a).

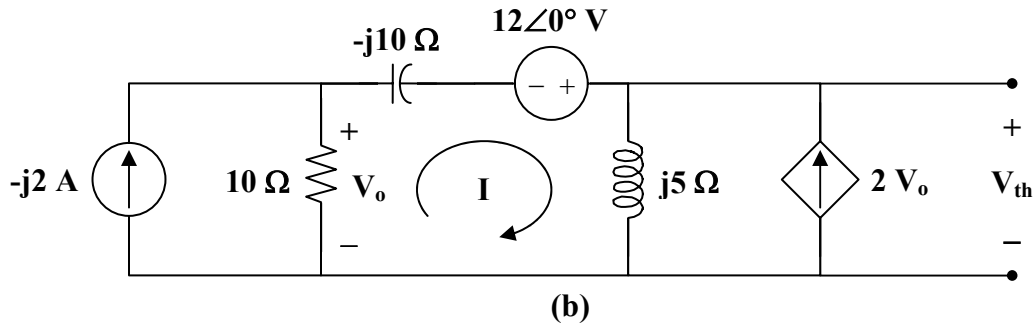


$$1 + 2V_o = \frac{V_x}{j5} + \frac{V_x}{10 - j10}, \quad \text{where } V_o = \frac{10V_x}{10 - j10}$$

$$1 + \frac{19V_x}{10 - j10} = \frac{V_x}{j5} \longrightarrow V_x = \frac{-10 + j10}{21 + j2}$$

$$Z_N = Z_{th} = \frac{V_x}{1} = \frac{14.142 \angle 135^\circ}{21.095 \angle 5.44^\circ} = \underline{\underline{0.67 \angle 129.56^\circ \Omega}}$$

To find  $V_{th}$  and  $I_N$ , consider the circuit in Fig. (b).



$$(10 - j10 + j5)I - (10)(-j2) + j5(2V_o) - 12 = 0$$

where  $V_o = (10)(-j2 - I)$

Thus,

$$(10 - j105)I = -188 - j20$$

$$I = \frac{188 + j20}{-10 + j105}$$

$$V_{th} = j5(I + 2V_o) = j5(-19I - j40) = -j95I + 200$$

$$V_{th} = \frac{-j95(188 + j20)}{-10 + j105} + 200 = 29.73 + j1.8723$$

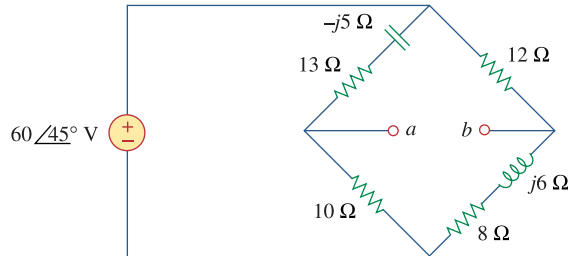
$$V_{th} = \underline{\underline{29.79\angle 3.6^\circ \text{ V}}}$$

$$I_N = \frac{V_{th}}{Z_{th}} = \frac{29.79\angle 3.6^\circ}{0.67\angle 129.56^\circ} = \underline{\underline{44.46\angle -125.96^\circ \text{ A}}}$$

### Chapter 10, Problem 67.



Find the Thevenin and Norton equivalent circuits at terminals  $a$ - $b$  in the circuit of Fig. 10.110.



**Figure 10.110**  
For Prob. 10.67.

### Chapter 10, Solution 67.

$$Z_N = Z_{Th} = 10 \parallel (13 - j5) + 12 \parallel (8 + j6) = \frac{10(13 - j5)}{23 - j5} + \frac{12(8 + j6)}{20 + j6} = \underline{11.243 + j1.079 \Omega}$$

$$V_a = \frac{10}{23 - j5} (60 \angle 45^\circ) = 13.78 + j21.44, \quad V_b = \frac{(8 + j6)}{20 + j6} (60 \angle 45^\circ) = 12.069 + j26.08 \Omega$$

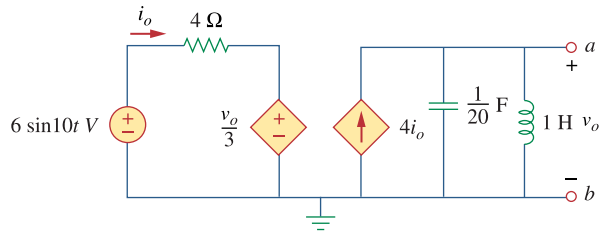
$$V_{Th} = V_a - V_b = 1.711 - j4.64 = \underline{4.945 \angle -69.76^\circ \text{ V}},$$

$$I_N = \frac{V_{Th}}{Z_{Th}} = \frac{4.945 \angle -69.76^\circ}{11.295 \angle 5.48^\circ} = \underline{0.4378 \angle -75.24^\circ \text{ A}}$$

### Chapter 10, Problem 68.



Find the Thevenin equivalent at terminals  $a-b$  in the circuit of Fig. 10.111.



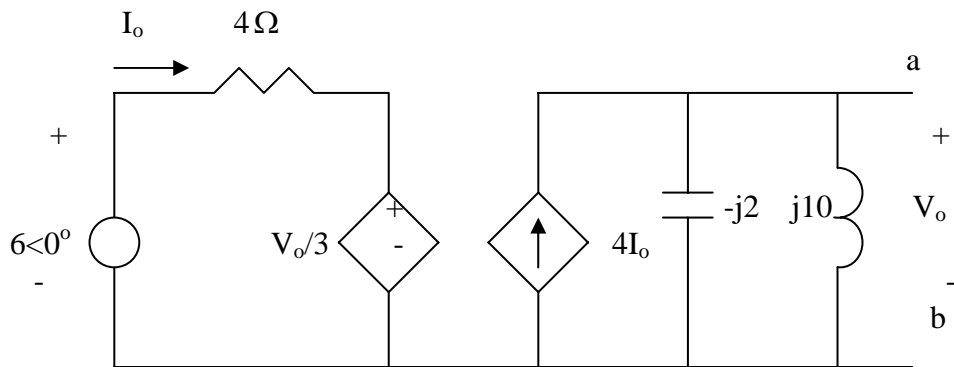
**Figure 10.111**

For Prob. 10.68.

### Chapter 10, Solution 68.

$$\begin{aligned} 1\text{ H} &\longrightarrow j\omega L = j10 \times 1 = j10 \\ \frac{1}{20}\text{ F} &\longrightarrow \frac{1}{j\omega C} = \frac{1}{j10 \times \frac{1}{20}} = -j2 \end{aligned}$$

We obtain  $V_{Th}$  using the circuit below.



$$j10 // (-j2) = \frac{j10(-j2)}{j10 - j2} = -j2.5$$

$$V_o = 4I_o \times (-j2.5) = -j10I_o \quad (1)$$

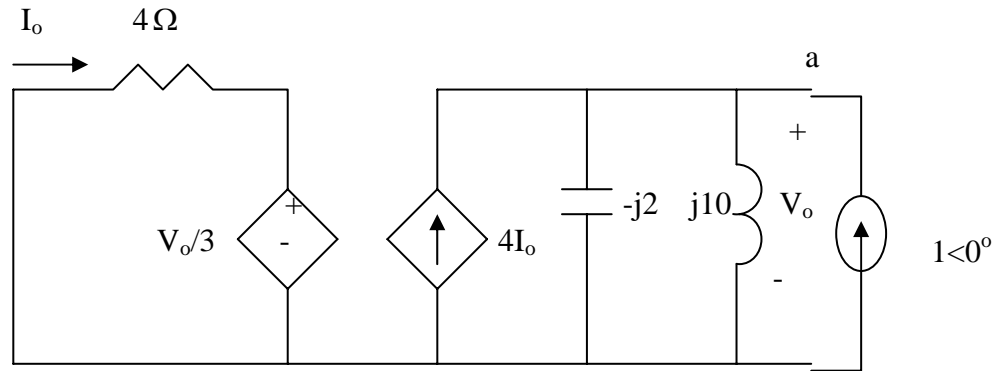
$$-6 + 4I_o + \frac{1}{3}V_o = 0 \quad (2)$$

Combining (1) and (2) gives

$$I_o = \frac{6}{4 - j10/3}, \quad V_{Th} = V_o = -j10I_o = \frac{-j60}{4 - j10/3} = 11.52 \angle -50.19^\circ$$

$$\underline{v_{Th} = 11.52 \sin(10t - 50.19^\circ)}$$

To find  $R_{Th}$ , we insert a 1-A source at terminals a-b, as shown below.



$$4I_o + \frac{1}{3}V_o = 0 \quad \longrightarrow \quad I_o = -\frac{V_o}{12}$$

$$1 + 4I_o = \frac{V_o}{-j2} + \frac{V_o}{j10}$$

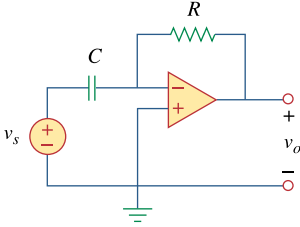
Combining the two equations leads to

$$V_o = \frac{1}{0.333 + j0.4} = 1.2293 - j1.4766$$

$$Z_{Th} = \frac{V_o}{1} = \underline{1.2293 - j1.477 \Omega}$$

### Chapter 10, Problem 69.

For the differentiator shown in Fig. 10.112, obtain  $\mathbf{V}_o/\mathbf{V}_s$ . Find  $v_o(t)$  when  $v_s(t) = V_m \sin \omega t$  and  $\omega = 1/RC$ .



**Figure 10.112**  
For Prob. 10.69.

### Chapter 10, Solution 69.

This is an inverting op amp so that

$$\frac{\mathbf{V}_o}{\mathbf{V}_s} = \frac{-\mathbf{Z}_f}{\mathbf{Z}_i} = \frac{-R}{1/j\omega C} = \underline{-j\omega RC}$$

When  $\mathbf{V}_s = V_m$  and  $\omega = 1/RC$ ,

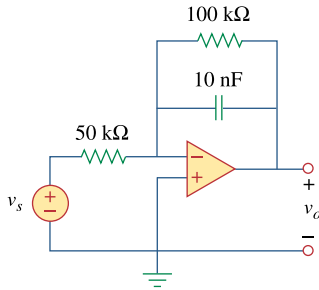
$$\mathbf{V}_o = -j \cdot \frac{1}{RC} \cdot RC \cdot V_m = -jV_m = V_m \angle -90^\circ$$

Therefore,

$$v_o(t) = V_m \sin(\omega t - 90^\circ) = \underline{-V_m \cos(\omega t)}$$

### Chapter 10, Problem 70.

The circuit in Fig. 10.113 is an integrator with a feedback resistor. Calculate  $v_o(t)$  if  $v_s = 2 \cos 4 \times 10^4 t$  V.



**Figure 10.113**  
For Prob. 10.70.

### Chapter 10, Solution 70.

This may also be regarded as an inverting amplifier.

$$2 \cos(4 \times 10^4 t) \longrightarrow 2 \angle 0^\circ, \quad \omega = 4 \times 10^4$$

$$10 \text{ nF} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(4 \times 10^4)(10 \times 10^{-9})} = -j2.5 \text{ k}\Omega$$

$$\frac{V_o}{V_s} = \frac{-Z_f}{Z_i}$$

$$\text{where } Z_i = 50 \text{ k}\Omega \text{ and } Z_f = 100 \text{ k} \parallel (-j2.5 \text{ k}) = \frac{-j100}{40 - j} \text{ k}\Omega.$$

$$\text{Thus, } \frac{V_o}{V_s} = \frac{j2}{40 - j}$$

$$\text{If } V_s = 2 \angle 0^\circ,$$

$$V_o = \frac{j4}{40 - j} = \frac{4 \angle 90^\circ}{40.01 \angle -1.43^\circ} = 0.1 \angle 91.43^\circ$$

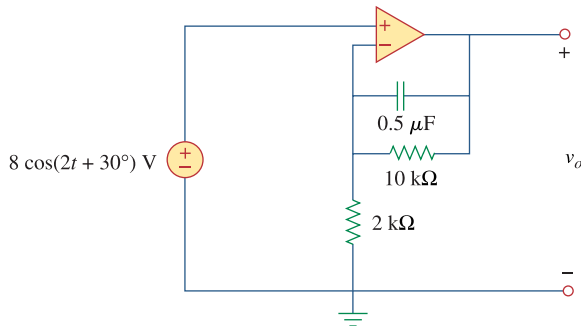
Therefore,

$$v_o(t) = \underline{\underline{0.1 \cos(4 \times 10^4 t + 91.43^\circ) \text{ V}}}$$



### Chapter 10, Problem 71.

Find  $v_o$  in the op amp circuit of Fig. 10.114.



**Figure 10.114**  
For Prob. 10.71.

### Chapter 10, Solution 71.

$$8 \cos(2t + 30^\circ) \longrightarrow 8 \angle 30^\circ$$

$$0.5 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j2 \times 0.5 \times 10^{-6}} = -j1 \text{ M}\Omega$$

At the inverting terminal,

$$\frac{V_o - 8 \angle 30^\circ}{-j1000\text{k}} + \frac{V_o - 8 \angle 30^\circ}{10\text{k}} = \frac{8 \angle 30^\circ}{2\text{k}} \longrightarrow$$

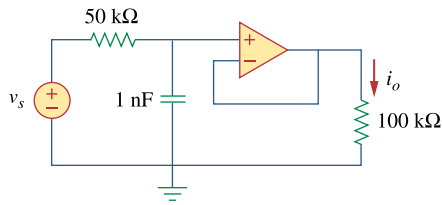
$$V_o(1 - j100) = 8 \angle 30^\circ + 800 \angle -60^\circ + 4000 \angle -60^\circ$$

$$V_o = \frac{6.928 + j4 + 2400 - j4157}{1 - j100} = \frac{4800 \angle -59.9^\circ}{100 \angle -89.43^\circ} = 48 \angle 29.53^\circ$$

$$v_o(t) = \underline{\underline{48 \cos(2t + 29.53^\circ) \text{ V}}}$$

### Chapter 10, Problem 72.

Compute  $i_o(t)$  in the op amp circuit in Fig. 10.115 if  $v_s = 4\cos 10^4 t$  V.



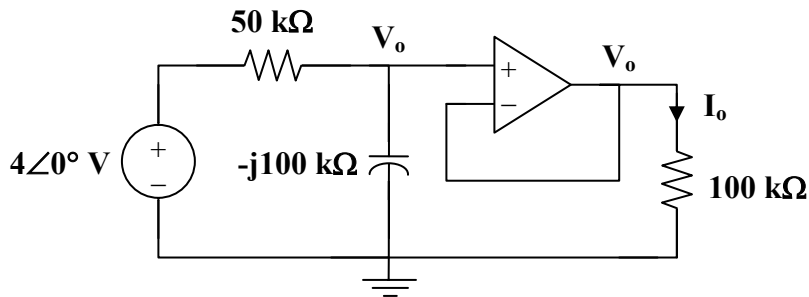
**Figure 10.115**  
For Prob. 10.72.

### Chapter 10, Solution 72.

$$4\cos(10^4 t) \longrightarrow 4\angle 0^\circ, \quad \omega = 10^4$$

$$1 \text{ nF} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(10^4)(10^{-9})} = -j100 \text{ k}\Omega$$

Consider the circuit as shown below.



At the noninverting node,

$$\frac{4 - V_o}{50} = \frac{V_o}{-j100} \longrightarrow V_o = \frac{4}{1 + j0.5}$$

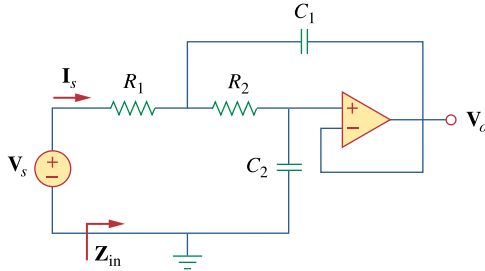
$$I_o = \frac{V_o}{100\text{k}} = \frac{4}{(100)(1 + j0.5)} \text{ mA} = 35.78\angle -26.56^\circ \mu\text{A}$$

Therefore,

$$i_o(t) = \underline{\underline{35.78 \cos(10^4 t - 26.56^\circ) \mu\text{A}}}$$

### Chapter 10, Problem 73.

If the input impedance is defined as  $Z_{in} = V_s / I_s$  find the input impedance of the op amp circuit in Fig. 10.116 when  $R_1 = 10 \text{ k}\Omega$ ,  $R_2 = 20 \text{ k}\Omega$ ,  $C_1 = 10 \text{ nF}$ , and  $\omega = 5000 \text{ rad/s}$ .



**Figure 10.116**  
For Prob. 10.73.

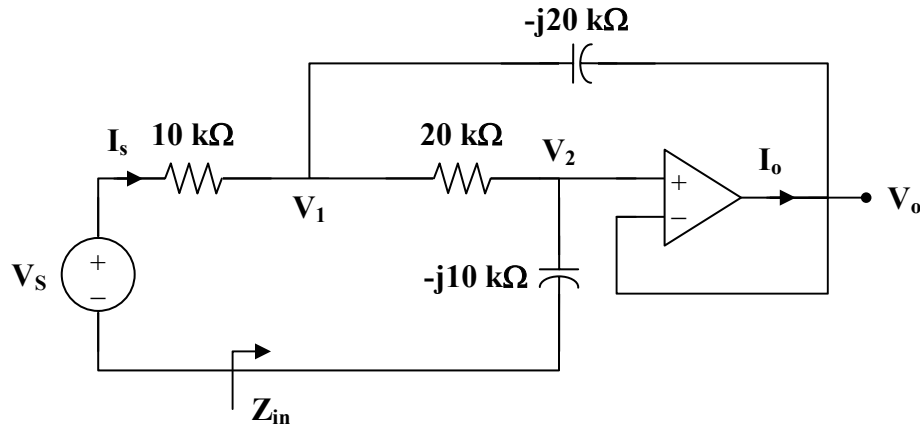
### Chapter 10, Solution 73.

As a voltage follower,  $V_2 = V_o$ .

$$C_1 = 10 \text{ nF} \longrightarrow \frac{1}{j\omega C_1} = \frac{1}{j(5 \times 10^3)(10 \times 10^{-9})} = -j20 \text{ k}\Omega$$

$$C_2 = 20 \text{ nF} \longrightarrow \frac{1}{j\omega C_2} = \frac{1}{j(5 \times 10^3)(20 \times 10^{-9})} = -j10 \text{ k}\Omega$$

Consider the circuit in the frequency domain as shown below.



At node 1,

$$\begin{aligned}\frac{V_s - V_1}{10} &= \frac{V_1 - V_o}{-j20} + \frac{V_1 - V_o}{20} \\ 2V_s &= (3 + j)V_1 - (1 + j)V_o\end{aligned}\quad (1)$$

At node 2,

$$\begin{aligned}\frac{V_1 - V_o}{20} &= \frac{V_o - 0}{-j10} \\ V_1 &= (1 + j2)V_o\end{aligned}\quad (2)$$

Substituting (2) into (1) gives

$$2V_s = j6V_o \quad \text{or} \quad V_o = -j\frac{1}{3}V_s$$

$$V_1 = (1 + j2)V_o = \left(\frac{2}{3} - j\frac{1}{3}\right)V_s$$

$$I_s = \frac{V_s - V_1}{10k} = \frac{(1/3)(1 + j)}{10k} V_s$$

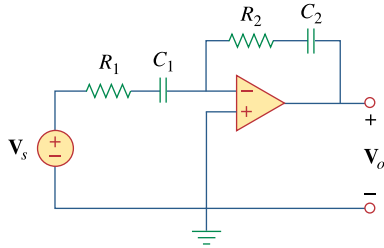
$$\frac{I_s}{V_s} = \frac{1 + j}{30k}$$

$$Z_{in} = \frac{V_s}{I_s} = \frac{30k}{1 + j} = 15(1 - j)k$$

$$Z_{in} = \underline{\underline{21.21\angle -45^\circ \text{ k}\Omega}}$$

### Chapter 10, Problem 74.

Evaluate the voltage gain  $A_v = V_o/V_s$  in the op amp circuit of Fig. 10.117. Find  $A_v$  at  $\omega = 0$ ,  $\omega \rightarrow \infty$ ,  $\omega = 1/R_1C_1$ , and  $\omega = 1/R_2C_2$ .



**Figure 10.117**  
For Prob. 10.74.

### Chapter 10, Solution 74.

$$Z_i = R_1 + \frac{1}{j\omega C_1},$$

$$Z_f = R_2 + \frac{1}{j\omega C_2}$$

$$A_v = \frac{V_o}{V_s} = \frac{-Z_f}{Z_i} = -\frac{R_2 + \frac{1}{j\omega C_2}}{R_1 + \frac{1}{j\omega C_1}} = -\left(\frac{C_1}{C_2}\right) \left( \frac{1 + j\omega R_2 C_2}{1 + j\omega R_1 C_1} \right)$$

$$\text{At } \omega = 0, \quad A_v = -\frac{C_1}{C_2}$$

$$\text{As } \omega \rightarrow \infty, \quad A_v = -\frac{R_2}{R_1}$$

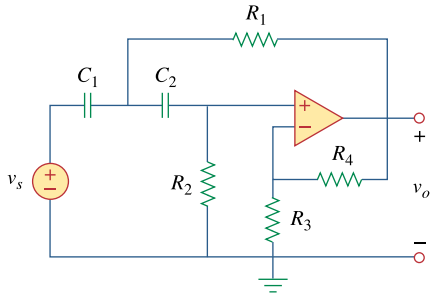
$$\text{At } \omega = \frac{1}{R_1 C_1}, \quad A_v = -\left(\frac{C_1}{C_2}\right) \left( \frac{1 + j R_2 C_2 / R_1 C_1}{1 + j} \right)$$

$$\text{At } \omega = \frac{1}{R_2 C_2}, \quad A_v = -\left(\frac{C_1}{C_2}\right) \left( \frac{1 + j}{1 + j R_1 C_1 / R_2 C_2} \right)$$

**Chapter 10, Problem 75.**



In the op amp circuit of Fig. 10.118, find the closed-loop gain and phase shift of the output voltage with respect to the input voltage if  $C_1 = C_2 = 1 \text{ nF}$ ,  $R_1 = R_2 = 100 \text{ k}\Omega$ ,  $R_3 = 20 \text{ k}\Omega$ ,  $R_4 = 40 \text{ k}\Omega$ , and  $\omega = 2000 \text{ rad/s}$ .



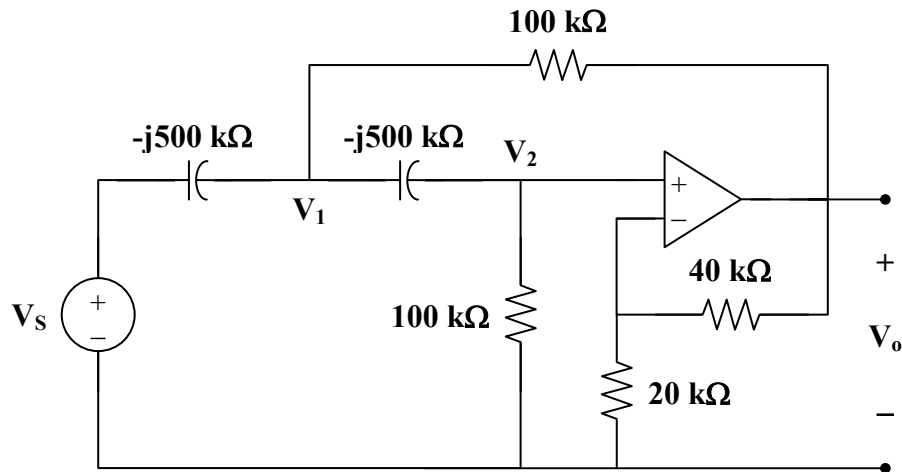
**Figure 10.118**  
For Prob. 10.75.

### Chapter 10, Solution 75.

$$\omega = 2 \times 10^3$$

$$C_1 = C_2 = 1 \text{ nF} \longrightarrow \frac{1}{j\omega C_1} = \frac{1}{j(2 \times 10^3)(1 \times 10^{-9})} = -j500 \text{ k}\Omega$$

Consider the circuit shown below.



Let  $V_s = 10\text{V}$ .

At node 1,

$$\begin{aligned} &[(V_1 - 10)/(-j500\text{k})] + [(V_1 - V_o)/10^5] + [(V_1 - V_2)/(-j500\text{k})] = 0 \\ &\text{or } (1 + j0.4)V_1 - j0.2V_2 - V_o = j2 \end{aligned} \quad (1)$$

At node 2,

$$\begin{aligned} &[(V_2 - V_1)/(-j5)] + (V_2 - 0) = 0 \\ &\text{or } -j0.2V_1 + (1 + j0.2)V_2 = 0 \text{ or } V_1 = (1 - j5)V_2 \end{aligned} \quad (2)$$

But

$$V_2 = \frac{R_3}{R_3 + R_4} V_o = \frac{V_o}{3} \quad (3)$$

From (2) and (3),

$$V_1 = (0.3333 - j1.6667)V_o \quad (4)$$

Substituting (3) and (4) into (1),

$$(1+j0.4)(0.3333-j1.6667)V_o - j0.06667V_o - V_o = j2$$

$$(1.077\angle 21.8^\circ)(1.6997\angle -78.69^\circ) = 1.8306\angle -56.89^\circ = 1 - j1.5334$$

Thus,

$$(1-j1.5334)V_o - j0.06667V_o - V_o = j2$$

$$\text{and, } V_o = j2/(-j1.6601) = -1.2499 = 1.2499\angle 180^\circ \text{ V}$$

Since  $V_s = 10$ ,

$$V_o/V_s = \underline{\underline{0.12499\angle 180^\circ}}.$$

Checking with MATLAB.

```
>> Y=[1+0.4i,-0.2i,-1;1,-1+5i,0;0,-3,1]
```

Y =

```
1.0000 + 0.4000i    0 - 0.2000i -1.0000
1.0000    -1.0000 + 5.0000i    0
0    -3.0000    1.0000
```

```
>> I=[2i;0;0]
```

I =

```
0 + 2.0000i
0
0
```

```
>> V=inv(Y)*I
```

V =

```
-0.4167 + 2.0833i
-0.4167
-1.2500 + 0.0000i (this last term is v_o)
```

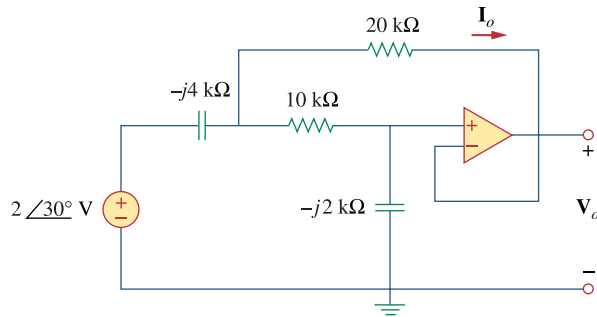
and, the answer checks.



**Chapter 10, Problem 76.**



Determine  $V_o$  and  $I_o$  in the op amp circuit of Fig. 10.119.



**Figure 10.119**  
For Prob. 10.76.

### Chapter 10, Solution 76.

Let the voltage between the  $-j4\text{k}\Omega$  capacitor and the  $10\text{k}\Omega$  resistor be  $V_1$ .

$$\begin{aligned}\frac{2\angle 30^\circ - V_1}{-j4\text{k}} &= \frac{V_1 - V_o}{10\text{k}} + \frac{V_1 - V_o}{20\text{k}} \longrightarrow \\ 2\angle 30^\circ &= (1 - j0.6)V_1 + j0.6V_o \\ &= 1.7321 + j1\end{aligned}\quad (1)$$

Also,

$$\frac{V_1 - V_o}{10\text{k}} = \frac{V_o}{-j2\text{k}} \longrightarrow V_1 = (1 + j5)V_o \quad (2)$$

Solving (2) into (1) yields

$$\begin{aligned}2\angle 30^\circ &= (1 - j0.6)(1 + j5)V_o + j0.6V_o = (1 + 3 - j0.6 + j5 + j6)V_o \\ &= (4 + j5)V_o \\ V_o &= \frac{2\angle 30^\circ}{6.403\angle 51.34^\circ} = \underline{0.3124\angle -21.34^\circ \text{ V}}\end{aligned}$$

```
>> Y=[1-0.6i,0.6i;1,-1-0.5i]
```

Y =

$$\begin{bmatrix} 1.0000 - 0.6000i & 0 + 0.6000i \\ 1.0000 & -1.0000 - 5.0000i \end{bmatrix}$$

```
>> I=[1.7321+1i;0]
```

I =

$$\begin{bmatrix} 1.7321 + 1.0000i \\ 0 \end{bmatrix}$$

```
>> V=inv(Y)*I
```

V =

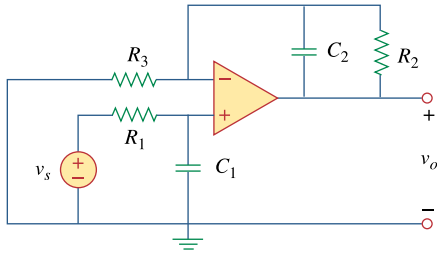
$$\begin{bmatrix} 0.8593 + 1.3410i \\ 0.2909 - 0.1137i \end{bmatrix} = V_o = 0.3123\angle -21.35^\circ \text{ V. Answer checks.}$$

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**Chapter 10, Problem 77.**



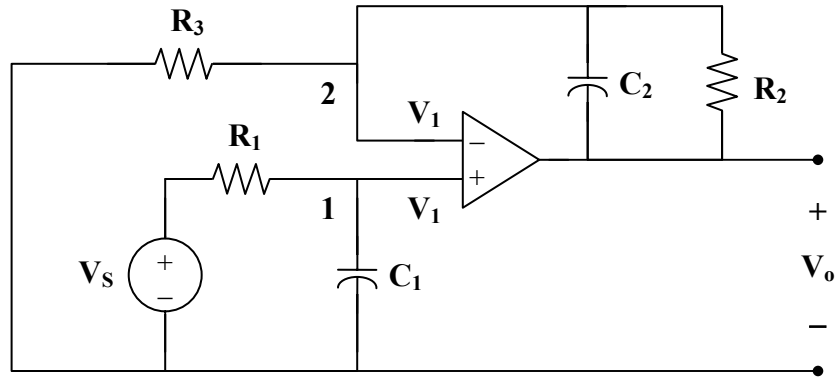
Compute the closed-loop gain  $V_o/V_s$  for the op amp circuit of Fig. 10.120.



**Figure 10.120**  
For Prob. 10.77.

## Chapter 10, Solution 77.

Consider the circuit below.



At node 1,

$$\begin{aligned}\frac{V_s - V_1}{R_1} &= j\omega C_1 V_1 \\ V_s &= (1 + j\omega R_1 C_1) V_1\end{aligned}\quad (1)$$

At node 2,

$$\begin{aligned}\frac{0 - V_1}{R_3} &= \frac{V_1 - V_o}{R_2} + j\omega C_2 (V_1 - V_o) \\ V_1 &= (V_o - V_1) \left( \frac{R_3}{R_2} + j\omega C_2 R_3 \right) \\ V_o &= \left( 1 + \frac{1}{(R_3/R_2) + j\omega C_2 R_3} \right) V_1\end{aligned}\quad (2)$$

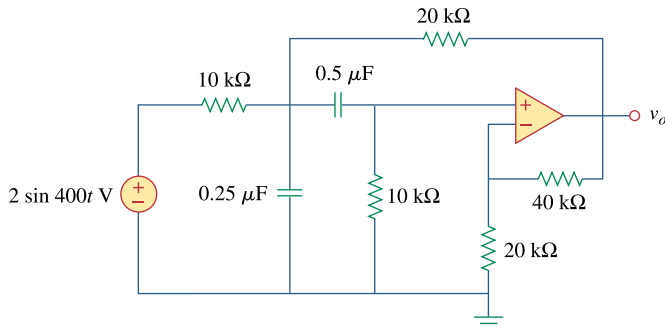
From (1) and (2),

$$\begin{aligned}V_o &= \frac{V_s}{1 + j\omega R_1 C_1} \left( 1 + \frac{R_2}{R_3 + j\omega C_2 R_2 R_3} \right) \\ \frac{V_o}{V_s} &= \frac{R_2 + R_3 + j\omega C_2 R_2 R_3}{(1 + j\omega R_1 C_1)(R_3 + j\omega C_2 R_2 R_3)}\end{aligned}$$

**Chapter 10, Problem 78.**



Determine  $v_o(t)$  in the op amp circuit in Fig. 10.121 below.



**Figure 10.121**

For Prob. 10.78.

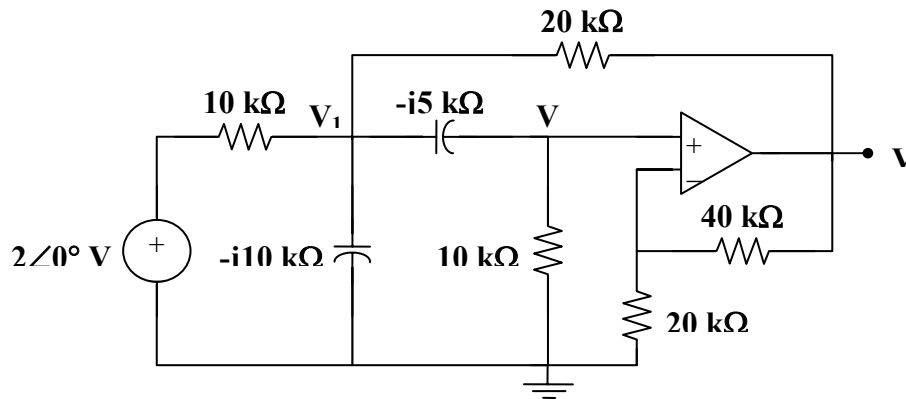
**Chapter 10, Solution 78.**

$$2 \sin(400t) \longrightarrow 2 \angle 0^\circ, \quad \omega = 400$$

$$0.5 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(400)(0.5 \times 10^{-6})} = -j5 \text{ k}\Omega$$

$$0.25 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(400)(0.25 \times 10^{-6})} = -j10 \text{ k}\Omega$$

Consider the circuit as shown below.



At node 1,

$$\frac{2 - V_1}{10} = \frac{V_1}{-j10} + \frac{V_1 - V_2}{-j5} + \frac{V_1 - V_o}{20}$$

$$4 = (3 + j6)V_1 - j4V_2 - V_o \quad (1)$$

At node 2,

$$\frac{V_1 - V_2}{-j5} = \frac{V_2}{10}$$

$$V_1 = (1 - j0.5)V_2 \quad (2)$$

But

$$V_2 = \frac{20}{20 + 40} V_o = \frac{1}{3} V_o \quad (3)$$

From (2) and (3),

$$V_1 = \frac{1}{3} \cdot (1 - j0.5) V_o \quad (4)$$

Substituting (3) and (4) into (1) gives

$$4 = (3 + j6) \cdot \frac{1}{3} \cdot (1 - j0.5) V_o - j\frac{4}{3} V_o - V_o = \left(1 + j\frac{1}{6}\right) V_o$$

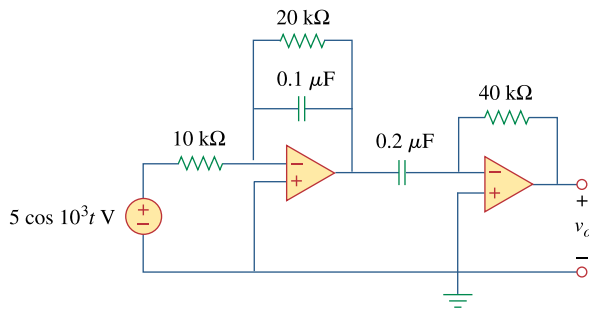
$$V_o = \frac{24}{6 + j} = 3.945 \angle -9.46^\circ$$

Therefore,

$$v_o(t) = \underline{\underline{3.945 \sin(400t - 9.46^\circ) \text{ V}}}$$

### Chapter 10, Problem 79.

For the op amp circuit in Fig. 10.122, obtain  $v_o(t)$ .



**Figure 10.122**  
For Prob. 10.79.

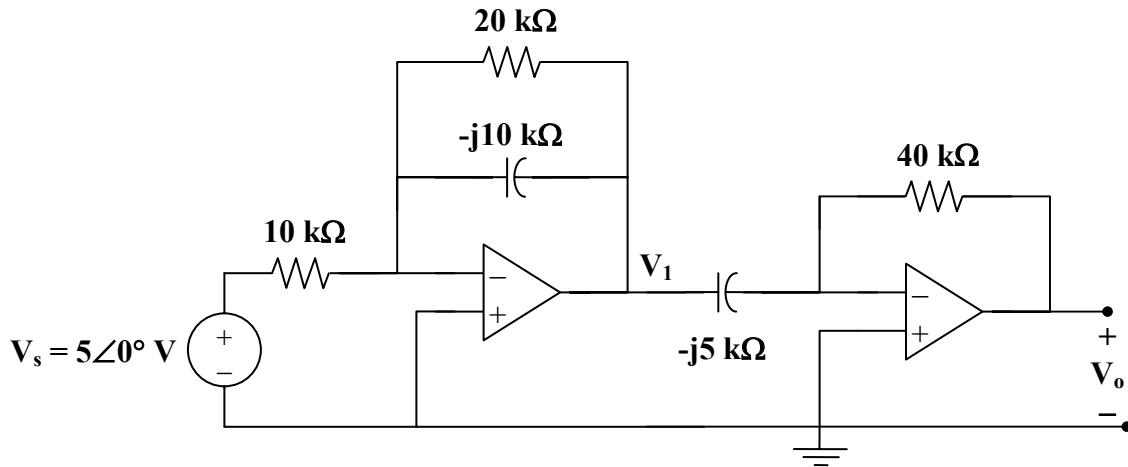
**Chapter 10, Solution 79.**

$$5 \cos(1000t) \longrightarrow 5 \angle 0^\circ, \quad \omega = 1000$$

$$0.1 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(1000)(0.1 \times 10^{-6})} = -j10 \text{ k}\Omega$$

$$0.2 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(1000)(0.2 \times 10^{-6})} = -j5 \text{ k}\Omega$$

Consider the circuit shown below.



Since each stage is an inverter, we apply  $V_o = \frac{-Z_f}{Z_i} V_i$  to each stage.

$$V_o = \frac{-40}{-j5} V_1 \quad (1)$$

and

$$V_1 = \frac{-20 \parallel (-j10)}{10} V_s \quad (2)$$

From (1) and (2),

$$V_o = \left( \frac{-j8}{10} \right) \left( \frac{-(20)(-j10)}{20 - j10} \right) 5 \angle 0^\circ$$

$$V_o = 16(2 + j) = 35.78 \angle 26.56^\circ$$

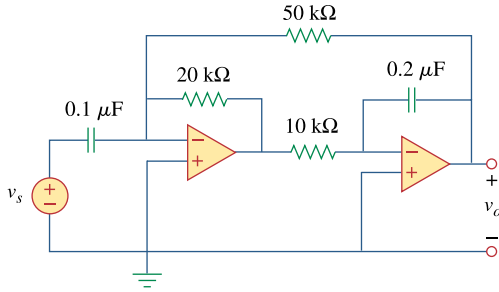
Therefore,  $v_o(t) = \underline{\underline{35.78 \cos(1000t + 26.56^\circ) \text{ V}}}$



### Chapter 10, Problem 80.



Obtain  $v_o(t)$  for the op amp circuit in Fig. 10.123 if  $v_s = 4\cos(1000t - 60^\circ)$  V.



**Figure 10.123**

For Prob. 10.80.

### Chapter 10, Solution 80.

$$4\cos(1000t - 60^\circ) \longrightarrow 4\angle -60^\circ, \quad \omega = 1000$$

$$0.1 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(1000)(0.1 \times 10^{-6})} = -j10 \text{ k}\Omega$$

$$0.2 \mu\text{F} \longrightarrow \frac{1}{j\omega C} = \frac{1}{j(1000)(0.2 \times 10^{-6})} = -j5 \text{ k}\Omega$$

The two stages are inverters so that

$$\mathbf{V}_o = \left( \frac{20}{-j10} \cdot (4\angle -60^\circ) + \frac{20}{50} \mathbf{V}_o \right) \left( \frac{-j5}{10} \right)$$

$$= \frac{-j}{2} \cdot (j2) \cdot (4\angle -60^\circ) + \frac{-j}{2} \cdot \frac{2}{5} \mathbf{V}_o$$

$$(1 + j/5) \mathbf{V}_o = 4\angle -60^\circ$$

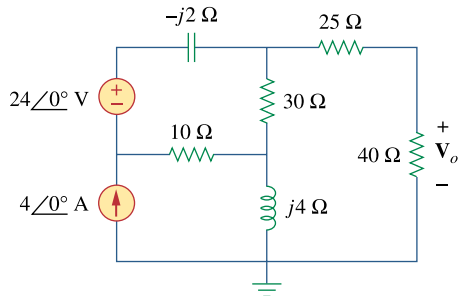
$$\mathbf{V}_o = \frac{4\angle -60^\circ}{1 + j/5} = 3.922\angle -71.31^\circ$$

Therefore,  $v_o(t) = \underline{\underline{3.922 \cos(1000t - 71.31^\circ) \text{ V}}}$

### Chapter 10, Problem 81.



Use *PSpice* to determine  $V_o$  in the circuit of Fig. 10.124. Assume  $\omega = 1$  rad/s.



**Figure 10.124**

For Prob. 10.81.

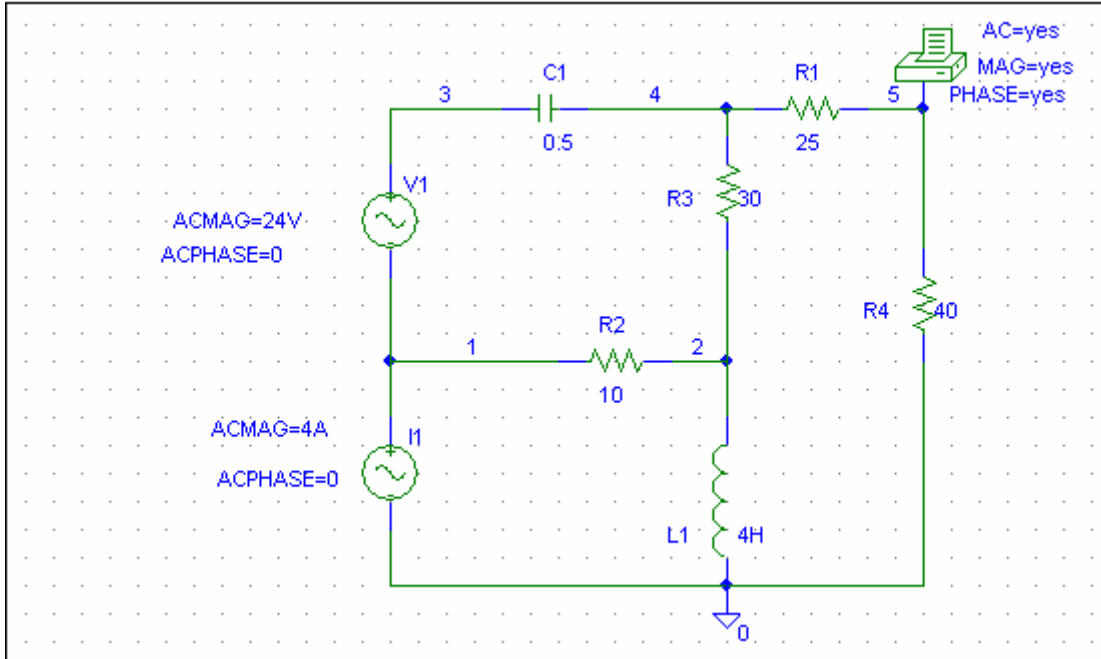
## Chapter 10, Solution 81.

We need to get the capacitance and inductance corresponding to  $-j2\ \Omega$  and  $j4\ \Omega$ .

$$-j2 \longrightarrow C = \frac{1}{\omega X_c} = \frac{1}{1 \times 2} = 0.5\text{ F}$$

$$j4 \longrightarrow L = \frac{X_L}{\omega} = 4\text{ H}$$

The schematic is shown below.



When the circuit is simulated, we obtain the following from the output file.

FREQ	VM(5)	VP(5)
1.592E-01	1.127E+01	-1.281E+02

From this, we obtain

$$V_o = \underline{11.27 \angle 128.1^\circ \text{ V.}}$$

## Chapter 10, Problem 82.

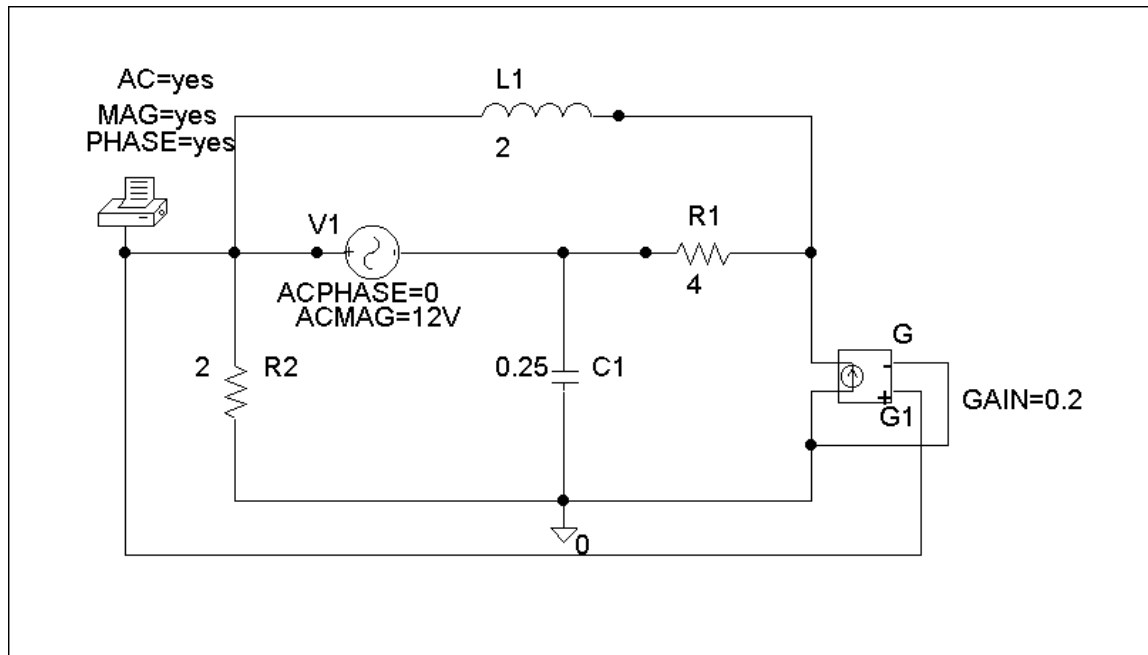
Solve Prob. 10.19 using *PSpice*.

## Chapter 10, Solution 82.

The schematic is shown below. We insert PRINT to print  $V_o$  in the output file. For AC Sweep, we set Total Pts = 1, Start Freq = 0.1592, and End Freq = 0.1592. After simulation, we print out the output file which includes:

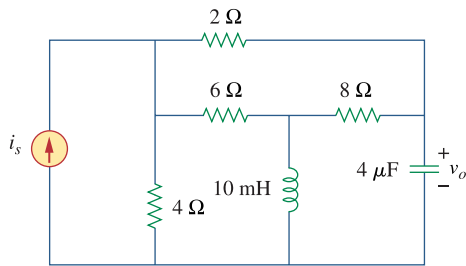
FREQ	VM(\$N_0001)	VP(\$N_0001)
1.592 E-01	7.684 E+00	5.019 E+01

which means that  $V_o = \underline{7.684 \angle 50.19^\circ \text{ V}}$



### Chapter 10, Problem 83.

Use *PSpice* to find  $v_o(t)$  in the circuit of Fig. 10.125. Let  $i_s = 2 \cos(10_3 t)$  A.

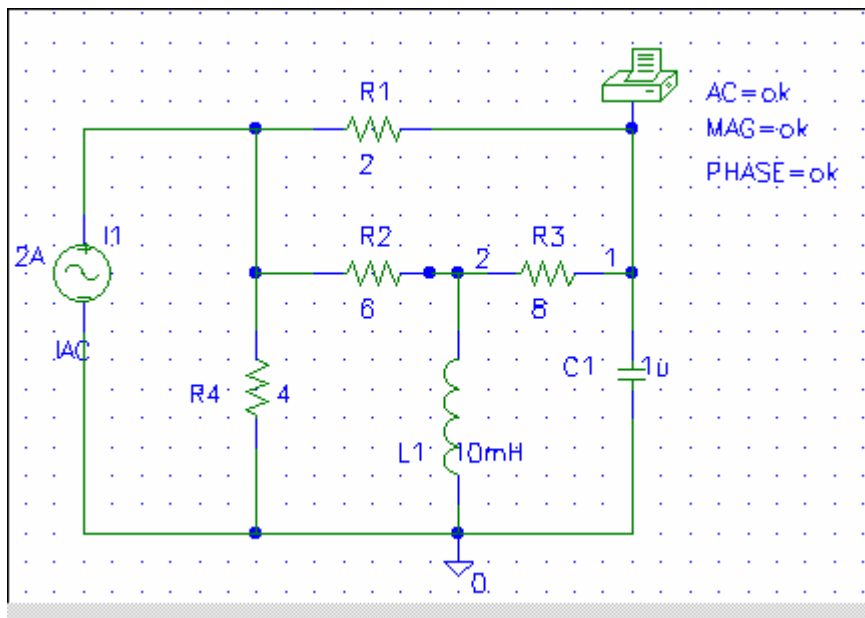


**Figure 10.125**

For Prob. 10.83.

### Chapter 10, Solution 83.

The schematic is shown below. The frequency is  $f = \omega / 2\pi = \frac{1000}{2\pi} = 159.15$



When the circuit is saved and simulated, we obtain from the output file

FREQ	VM(1)	VP(1)
1.592E+02	6.611E+00	-1.592E+02

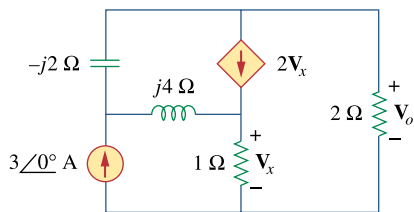
Thus,

$$v_o = \underline{\underline{6.611 \cos(1000t - 159.2^\circ) \text{ V}}}$$

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### Chapter 10, Problem 84.

Obtain  $V_o$  in the circuit of Fig. 10.126 using *PSpice*.



**Figure 10.126**

For Prob. 10.84.

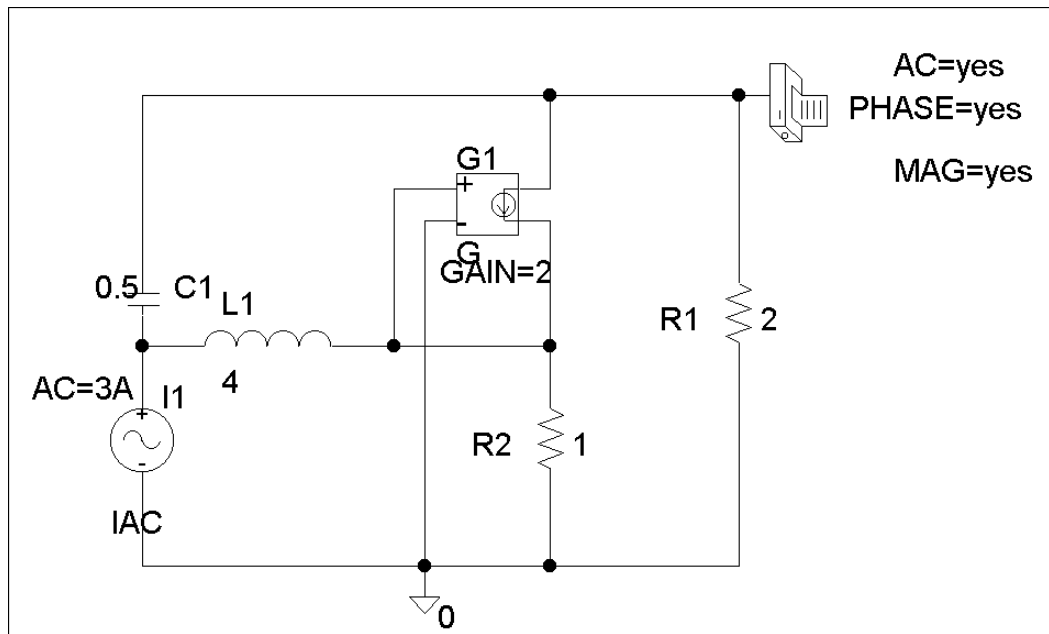
### Chapter 10, Solution 84.

The schematic is shown below. We set PRINT to print  $V_o$  in the output file. In AC Sweep box, we set Total Pts = 1, Start Freq = 0.1592, and End Freq = 0.1592. After simulation, we obtain the output file which includes:

VP(\$N_0003)	FREQ	VM(\$N_0003)	
	1.592 E-01	1.664 E+00	-1.646
E+02			

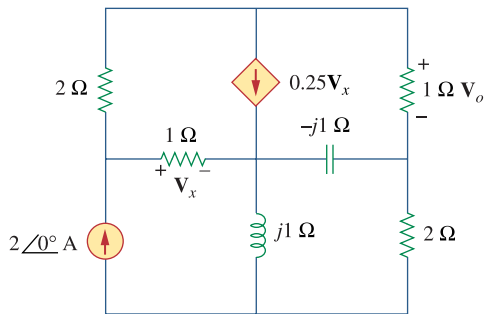
Namely,

$$V_o = \underline{1.664 \angle -146.4^\circ \text{ V}}$$



### Chapter 10, Problem 85.

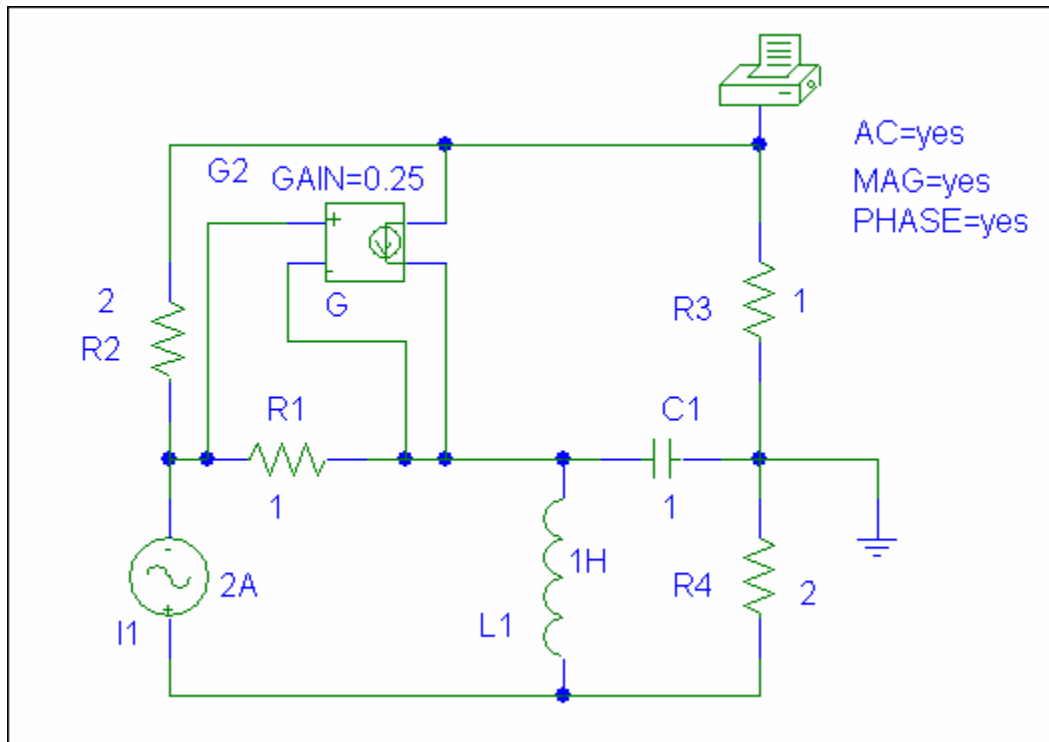
Use *PSpice* to find  $V_o$  in the circuit of Fig. 10.127.



**Figure 10.127**  
For Prob. 10.85.

### Chapter 10, Solution 85.

The schematic is shown below. We let  $\omega = 1$  rad/s so that  $L=1$ H and  $C=1$ F.



When the circuit is saved and simulated, we obtain from the output file

```
FREQ      VM($N_0001) VP($N_0001)
1.592E-01  4.471E-01  1.437E+01
```

From this, we conclude that

$$V_o = \underline{447.1 \angle 14.37^\circ \text{ mV}}$$

Checking using MATLAB and nodal analysis we get,

```
>> Y=[1.5,-0.25,-0.25,0;0,1.25,-1.25,1i;-0.5,-1,1.5,0;0,1i,0,0.5-1i]
```

Y =

```
1.5000    -0.2500    -0.2500         0
         0     1.2500    -1.2500    0 + 1.0000i
-0.5000    -1.0000     1.5000         0
         0     0 + 1.0000i         0    0.5000 - 1.0000i
```

```
>> I=[0;0;2;-2]
```

I =

```
0
0
2
-2
```

```
>> V=inv(Y)*I
```

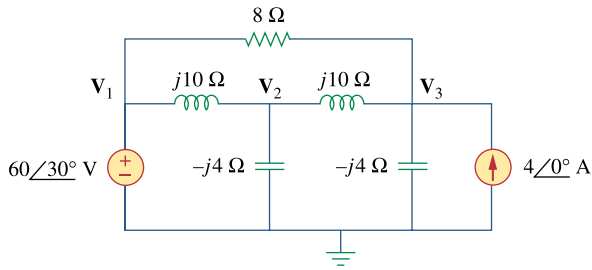
V =

```
0.4331 + 0.1110i = V_o = 0.4471 ∠ 14.38°, answer checks.
0.6724 + 0.3775i
1.9260 + 0.2887i
-0.1110 - 1.5669i
```



**Chapter 10, Problem 86.**

Use *PSpice* to find  $V_1$ ,  $V_2$ , and  $V_3$  in the network of Fig. 10.128.



**Figure 10.128**  
For Prob. 10.86.

### Chapter 10, Solution 86.

The schematic is shown below. We insert three pseudocomponent PRINTs at nodes 1, 2, and 3 to print  $V_1$ ,  $V_2$ , and  $V_3$ , into the output file. Assume that  $w = 1$ , we set Total Pts = 1, Start Freq = 0.1592, and End Freq = 0.1592. After saving and simulating the circuit, we obtain the output file which includes:

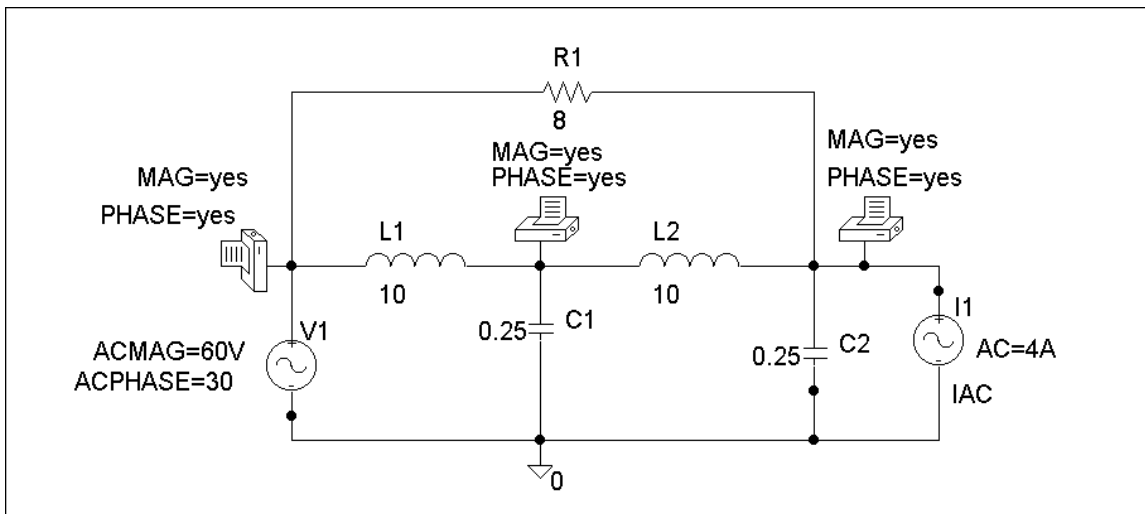
	FREQ	VM(\$N_0002)	
VP(\$N_0002)	1.592 E-01	6.000 E+01	3.000
E+01			

	FREQ	VM(\$N_0003)	
VP(\$N_0003)	1.592 E-01	2.367 E+02	-8.483
E+01			

	FREQ	VM(\$N_0001)	
VP(\$N_0001)	1.592 E-01	1.082 E+02	1.254
E+02			

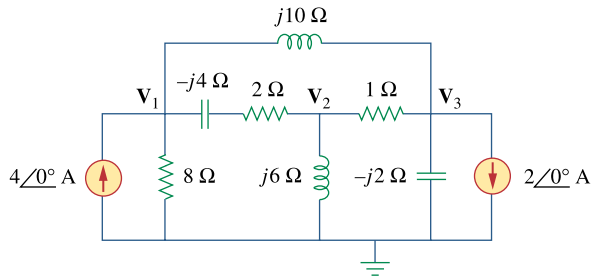
Therefore,

$$V_1 = \underline{60\angle 30^\circ \text{ V}} \quad V_2 = \underline{236.7\angle -84.83^\circ \text{ V}} \quad V_3 = \underline{108.2\angle 125.4^\circ \text{ V}}$$



### Chapter 10, Problem 87.

Determine  $V_1$ ,  $V_2$ , and  $V_3$  in the circuit of Fig. 10.129 using *PSpice*.



**Figure 10.129**  
For Prob. 10.87.

### Chapter 10, Solution 87.

The schematic is shown below. We insert three PRINTs at nodes 1, 2, and 3. We set Total Pts = 1, Start Freq = 0.1592, End Freq = 0.1592 in the AC Sweep box. After simulation, the output file includes:

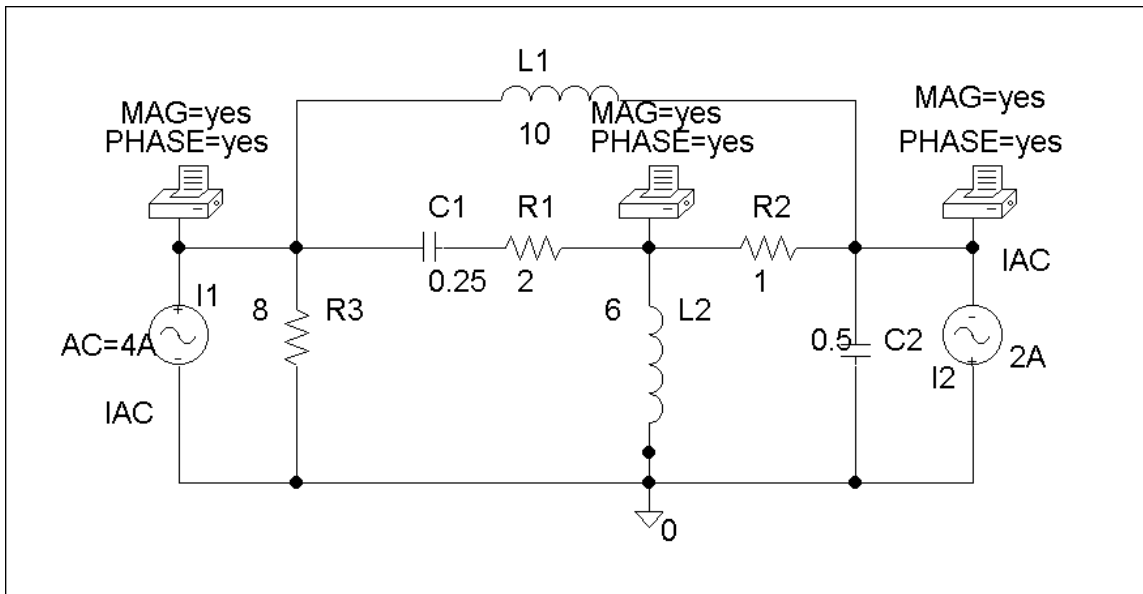
	FREQ	VM(\$N_0004)	
VP(\$N_0004)	1.592 E-01	1.591 E+01	1.696
E+02			

	FREQ	VM(\$N_0001)	
VP(\$N_0001)	1.592 E-01	5.172 E+00	-1.386
E+02			

	FREQ	VM(\$N_0003)	
VP(\$N_0003)	1.592 E-01	2.270 E+00	-1.524
E+02			

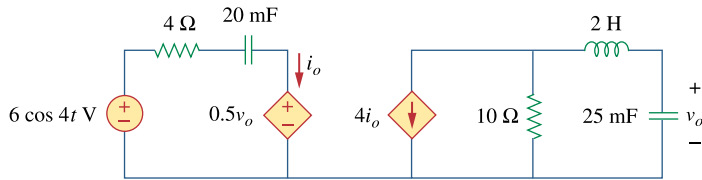
Therefore,

$$V_1 = \underline{15.91\angle 169.6^\circ \text{ V}} \quad V_2 = \underline{5.172\angle -138.6^\circ \text{ V}} \quad V_3 = \underline{2.27\angle -152.4^\circ \text{ V}}$$



### Chapter 10, Problem 88.

Use *PSpice* to find  $v_o$  and  $i_o$  in the circuit of Fig. 10.130 below.



**Figure 10.130**  
For Prob. 10.88.

### Chapter 10, Solution 88.

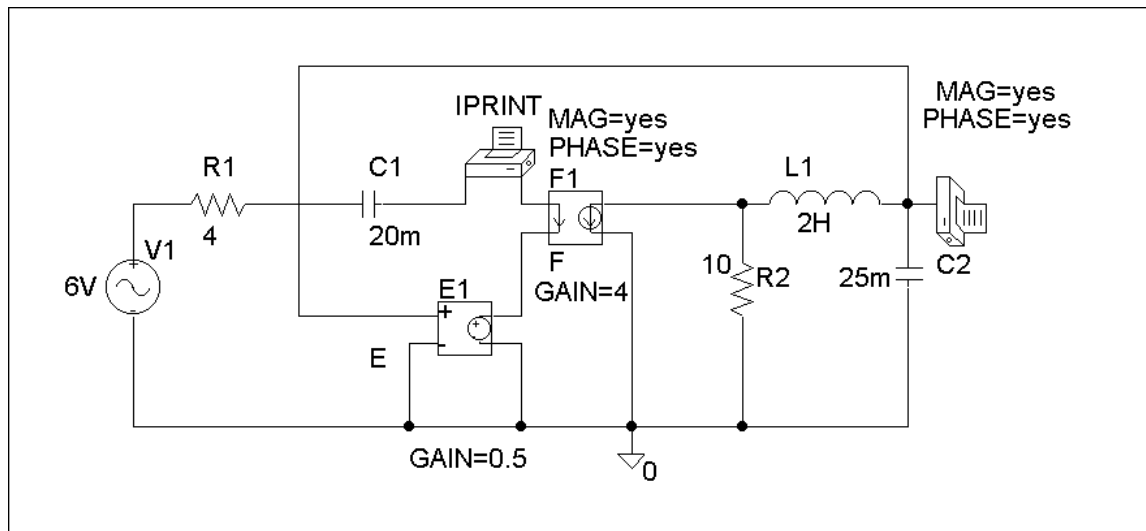
The schematic is shown below. We insert IPRINT and PRINT to print  $I_o$  and  $V_o$  in the output file. Since  $\omega = 4$ ,  $f = \omega/2\pi = 0.6366$ , we set Total Pts = 1, Start Freq = 0.6366, and End Freq = 0.6366 in the AC Sweep box. After simulation, the output file includes:

VP(\$N_0002)	FREQ	VM(\$N_0002)	
	6.366 E-01	3.496 E+01	1.261
E+01			

(V_PRINT2)	FREQ	IM(V_PRINT2)	IP
	6.366 E-01	8.912 E-01	
-8.870 E+01			

Therefore,  $V_o = 34.96\angle 12.6^\circ \text{ V}$ ,  $I_o = 0.8912\angle -88.7^\circ \text{ A}$

$$v_o = \underline{34.96 \cos(4t + 12.6^\circ) \text{ V}}, \quad i_o = \underline{0.8912 \cos(4t - 88.7^\circ) \text{ A}}$$



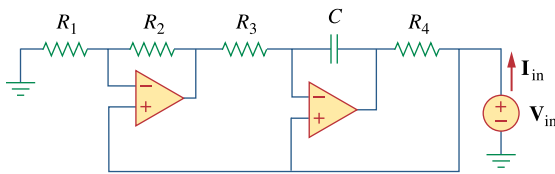
### Chapter 10, Problem 89.

The op amp circuit in Fig. 10.131 is called an *inductance simulator*. Show that the input impedance is given by

$$Z_{\text{in}} = \frac{V_{\text{in}}}{I_{\text{in}}} = j\omega L_{\text{eq}}$$

where

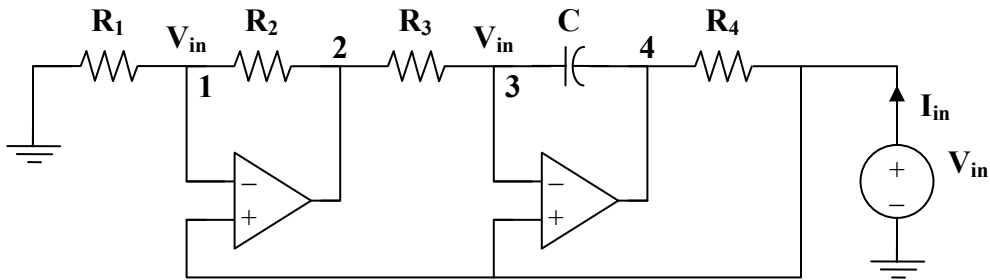
$$L_{\text{eq}} = \frac{R_1 R_3 R_4}{R_2} C$$



**Figure 10.131**  
For Prob. 10.89.

## Chapter 10, Solution 89.

Consider the circuit below.



At node 1,

$$\begin{aligned}\frac{0 - V_{in}}{R_1} &= \frac{V_{in} - V_2}{R_2} \\ -V_{in} + V_2 &= \frac{R_2}{R_1} V_{in}\end{aligned}\quad (1)$$

At node 3,

$$\begin{aligned}\frac{V_2 - V_{in}}{R_3} &= \frac{V_{in} - V_4}{1/j\omega C} \\ -V_{in} + V_4 &= \frac{V_{in} - V_2}{j\omega C R_3}\end{aligned}\quad (2)$$

From (1) and (2),

$$-V_{in} + V_4 = \frac{-R_2}{j\omega C R_3 R_1} V_{in}$$

Thus,

$$I_{in} = \frac{V_{in} - V_4}{R_4} = \frac{R_2}{j\omega C R_3 R_1 R_4} V_{in}$$

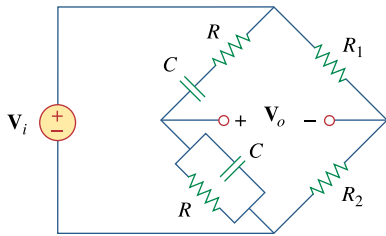
$$Z_{in} = \frac{V_{in}}{I_{in}} = \frac{j\omega C R_1 R_3 R_4}{R_2} = j\omega L_{eq}$$

$$\text{where } L_{eq} = \frac{R_1 R_3 R_4 C}{R_2}$$



### Chapter 10, Problem 90.

Figure 10.132 shows a Wien-bridge network. Show that the frequency at which the phase shift between the input and output signals is zero is  $f = \frac{1}{2\pi RC}$ , and that the necessary gain is  $A_v = V_o/V_i = 3$  at that frequency.



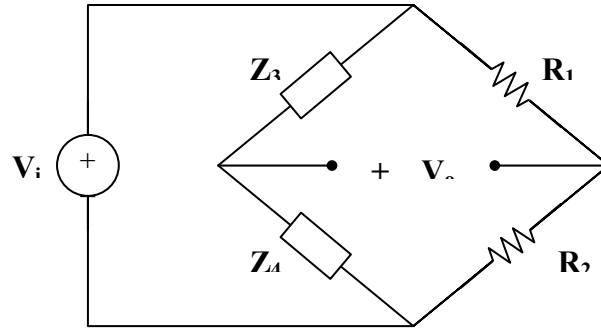
**Figure 10.132**  
For Prob. 10.90.

### Chapter 10, Solution 90.

Let 
$$\mathbf{Z}_4 = R \parallel \frac{1}{j\omega C} = \frac{R}{1 + j\omega RC}$$

$$\mathbf{Z}_3 = R + \frac{1}{j\omega C} = \frac{1 + j\omega RC}{j\omega C}$$

Consider the circuit shown below.



$$\mathbf{V}_o = \frac{\mathbf{Z}_4}{\mathbf{Z}_3 + \mathbf{Z}_4} \mathbf{V}_i - \frac{R_2}{R_1 + R_2} \mathbf{V}_i$$

$$\begin{aligned} \frac{\mathbf{V}_o}{\mathbf{V}_i} &= \frac{\frac{R}{1 + j\omega C}}{\frac{R}{1 + j\omega C} + \frac{1 + j\omega RC}{j\omega C}} - \frac{R_2}{R_1 + R_2} \\ &= \frac{j\omega RC}{j\omega RC + (1 + j\omega RC)^2} - \frac{R_2}{R_1 + R_2} \end{aligned}$$

$$\frac{\mathbf{V}_o}{\mathbf{V}_i} = \frac{j\omega RC}{1 - \omega^2 R^2 C^2 + j3\omega RC} - \frac{R_2}{R_1 + R_2}$$

For  $\mathbf{V}_o$  and  $\mathbf{V}_i$  to be in phase,  $\frac{\mathbf{V}_o}{\mathbf{V}_i}$  must be purely real. This happens when

$$1 - \omega^2 R^2 C^2 = 0$$

$$\omega = \frac{1}{RC} = 2\pi f$$

or 
$$f = \frac{1}{2\pi RC}$$

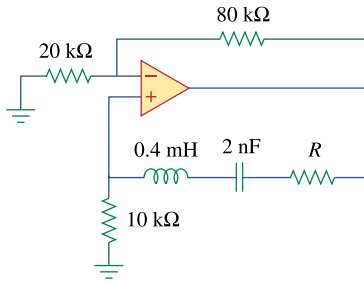
At this frequency, 
$$\mathbf{A}_v = \frac{\mathbf{V}_o}{\mathbf{V}_i} = \frac{1}{3} - \frac{R_2}{R_1 + R_2}$$

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### Chapter 10, Problem 91.

Consider the oscillator in Fig. 10.133.

- (a) Determine the oscillation frequency.
- (b) Obtain the minimum value of  $R$  for which oscillation takes place.



**Figure 10.133**  
For Prob. 10.91.

**Chapter 10, Solution 91.**

- (a) Let  $V_2$  = voltage at the noninverting terminal of the op amp  
 $V_o$  = output voltage of the op amp  
 $Z_p = 10 \text{ k}\Omega = R_o$   
 $Z_s = R + j\omega L + \frac{1}{j\omega C}$

As in Section 10.9,

$$\frac{V_2}{V_o} = \frac{Z_p}{Z_s + Z_p} = \frac{R_o}{R + R_o + j\omega L - \frac{j}{\omega C}}$$

$$\frac{V_2}{V_o} = \frac{\omega C R_o}{\omega C (R + R_o) + j(\omega^2 LC - 1)}$$

For this to be purely real,

$$\omega_o^2 LC - 1 = 0 \longrightarrow \omega_o = \frac{1}{\sqrt{LC}}$$

$$f_o = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{(0.4 \times 10^{-3})(2 \times 10^{-9})}}$$

$$f_o = \underline{\underline{180 \text{ kHz}}}$$

- (b) At oscillation,

$$\frac{V_2}{V_o} = \frac{\omega_o C R_o}{\omega_o C (R + R_o)} = \frac{R_o}{R + R_o}$$

This must be compensated for by

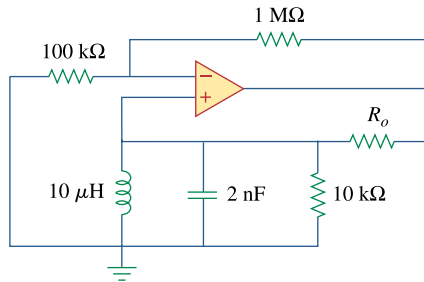
$$A_v = \frac{V_o}{V_2} = 1 + \frac{80}{20} = 5$$

$$\frac{R_o}{R + R_o} = \frac{1}{5} \longrightarrow R = 4R_o = \underline{\underline{40 \text{ k}\Omega}}$$

### Chapter 10, Problem 92.

The oscillator circuit in Fig. 10.134 uses an ideal op amp.

- (a) Calculate the minimum value of  $R_o$  that will cause oscillation to occur.
- (b) Find the frequency of oscillation.



**Figure 10.134**  
For Prob. 10.92.

## Chapter 10, Solution 92.

Let  $V_2$  = voltage at the noninverting terminal of the op amp

$V_o$  = output voltage of the op amp

$$Z_s = R_o$$

$$Z_p = j\omega L \parallel \frac{1}{j\omega C} \parallel R = \frac{1}{\frac{1}{R} + j\omega C + \frac{1}{j\omega L}} = \frac{\omega RL}{\omega L + jR(\omega^2 LC - 1)}$$

As in Section 10.9,

$$\frac{V_2}{V_o} = \frac{Z_p}{Z_s + Z_p} = \frac{\frac{\omega RL}{\omega L + jR(\omega^2 LC - 1)}}{R_o + \frac{\omega RL}{\omega L + jR(\omega^2 LC - 1)}}$$

$$\frac{V_2}{V_o} = \frac{\omega RL}{\omega RL + \omega R_o L + jR_o R(\omega^2 LC - 1)}$$

For this to be purely real,

$$\omega_o^2 LC = 1 \longrightarrow f_o = \frac{1}{2\pi\sqrt{LC}}$$

(a) At  $\omega = \omega_o$ ,

$$\frac{V_2}{V_o} = \frac{\omega_o RL}{\omega_o RL + \omega_o R_o L} = \frac{R}{R + R_o}$$

This must be compensated for by

$$A_v = \frac{V_o}{V_2} = 1 + \frac{R_f}{R_o} = 1 + \frac{1000k}{100k} = 11$$

Hence,

$$\frac{R}{R + R_o} = \frac{1}{11} \longrightarrow R_o = 10R = \underline{\underline{100 \text{ k}\Omega}}$$

$$(b) \quad f_o = \frac{1}{2\pi\sqrt{(10 \times 10^{-6})(2 \times 10^{-9})}}$$

$$f_o = \underline{\underline{1.125 \text{ MHz}}}$$

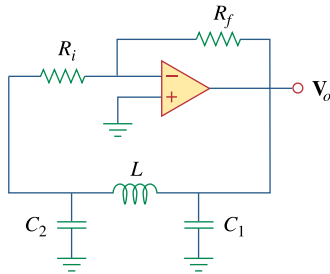
### Chapter 10, Problem 93.

**end**

Figure 10.135 shows a *Colpitts oscillator*. Show that the oscillation frequency is

$$f_o = \frac{1}{2\pi\sqrt{LC_T}}$$

where  $C_T = C_1 C_2 / (C_1 + C_2)$ . Assume  $R_i \gg X_{C_2}$



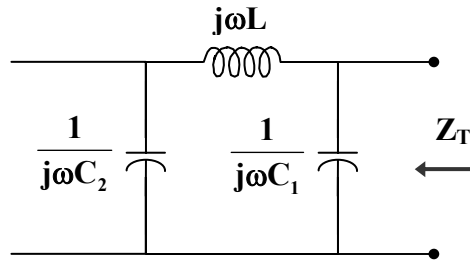
**Figure 10.135**

A Colpitts oscillator; for Prob. 10.93.

(Hint: Set the imaginary part of the impedance in the feedback circuit equal to zero.)

### Chapter 10, Solution 93.

As shown below, the impedance of the feedback is



$$Z_T = \frac{1}{j\omega C_1} \parallel \left( j\omega L + \frac{1}{j\omega C_2} \right)$$

$$Z_T = \frac{\frac{-j}{\omega C_1} \left( j\omega L + \frac{-j}{\omega C_2} \right)}{\frac{-j}{\omega C_1} + j\omega L + \frac{-j}{\omega C_2}} = \frac{\frac{1}{\omega} - \omega L C_2}{j(C_1 + C_2 - \omega^2 L C_1 C_2)}$$

In order for  $Z_T$  to be real, the imaginary term must be zero; i.e.

$$C_1 + C_2 - \omega_0^2 L C_1 C_2 = 0$$

$$\omega_0^2 = \frac{C_1 + C_2}{L C_1 C_2} = \frac{1}{L C_T}$$

$$f_0 = \frac{1}{2\pi\sqrt{L C_T}}$$



### Chapter 10, Problem 94.



Design a Colpitts oscillator that will operate at 50 kHz.

### Chapter 10, Solution 94.

If we select  $C_1 = C_2 = 20 \text{ nF}$

$$C_T = \frac{C_1 C_2}{C_1 + C_2} = \frac{C_1}{2} = 10 \text{ nF}$$

Since  $f_o = \frac{1}{2\pi\sqrt{LC_T}}$ ,

$$L = \frac{1}{(2\pi f)^2 C_T} = \frac{1}{(4\pi^2)(2500 \times 10^6)(10 \times 10^{-9})} = 10.13 \text{ mH}$$

$$X_c = \frac{1}{\omega C_2} = \frac{1}{(2\pi)(50 \times 10^3)(20 \times 10^{-9})} = 159 \Omega$$

We may select  $R_i = 20 \text{ k}\Omega$  and  $R_f \geq R_i$ , say  $R_f = 20 \text{ k}\Omega$ .

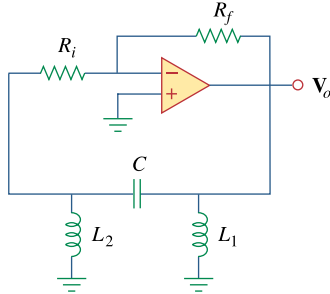
Thus,

$$C_1 = C_2 = \underline{20 \text{ nF}}, \quad L = \underline{10.13 \text{ mH}} \quad R_f = R_i = \underline{20 \text{ k}\Omega}$$

### Chapter 10, Problem 95.

Figure 10.136 shows a *Hartley oscillator*. Show that the frequency of oscillation is

$$f_o = \frac{1}{2\pi\sqrt{C(L_1 + L_2)}}$$



**Figure 10.136**

A Hartley oscillator; For Prob. 10.95.

### Chapter 10, Solution 95.

First, we find the feedback impedance.

$$Z_T = j\omega L_1 \parallel \left( j\omega L_2 + \frac{1}{j\omega C} \right)$$

$$Z_T = \frac{j\omega L_1 \left( j\omega L_2 - \frac{j}{\omega C} \right)}{j\omega L_1 + j\omega L_2 - \frac{j}{\omega C}} = \frac{\omega^2 L_1 C (1 - \omega L_2)}{j(\omega^2 C (L_1 + L_2) - 1)}$$

In order for  $Z_T$  to be real, the imaginary term must be zero; i.e.

$$\omega_o^2 C (L_1 + L_2) - 1 = 0$$

$$\omega_o = 2\pi f_o = \frac{1}{C(L_1 + L_2)}$$

$$f_o = \frac{1}{2\pi\sqrt{C(L_1 + L_2)}}$$

### Chapter 10, Problem 96.

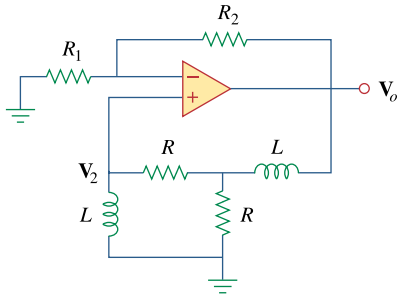
Refer to the oscillator in Fig. 10.137.

(a) Show that

$$\frac{V_2}{V_o} = \frac{1}{3 + j(\omega L/R - R/\omega L)}$$

(b) Determine the oscillation frequency  $f_o$ .

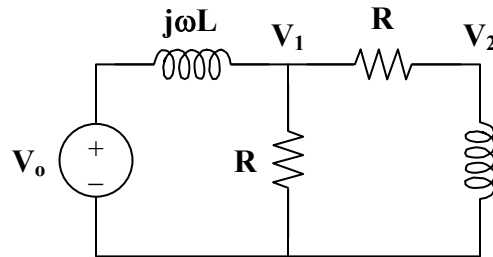
(c) Obtain the relationship between  $R_1$  and  $R_2$  in order for oscillation to occur.



**Figure 10.137**  
For Prob. 10.96.

## Chapter 10, Solution 96.

- (a) Consider the feedback portion of the circuit, as shown below.



$$V_2 = \frac{j\omega L}{R + j\omega L} V_1 \longrightarrow V_1 = \frac{R + j\omega L}{j\omega L} V_2 \quad (1)$$

Applying KCL at node 1,

$$\frac{V_o - V_1}{j\omega L} = \frac{V_1}{R} + \frac{V_1}{R + j\omega L}$$

$$V_o - V_1 = j\omega L V_1 \left( \frac{1}{R} + \frac{1}{R + j\omega L} \right)$$

$$V_o = V_1 \left( 1 + \frac{j2\omega RL - \omega^2 L^2}{R(R + j\omega L)} \right)$$

(2)

From (1) and (2),

$$V_o = \left( \frac{R + j\omega L}{j\omega L} \right) \left( 1 + \frac{j2\omega RL - \omega^2 L^2}{R(R + j\omega L)} \right) V_2$$

$$\frac{V_o}{V_2} = \frac{R^2 + j\omega RL + j2\omega RL - \omega^2 L^2}{j\omega RL}$$

$$\frac{V_2}{V_o} = \frac{1}{3 + \frac{R^2 - \omega^2 L^2}{j\omega RL}}$$

$$\frac{V_2}{V_o} = \frac{1}{3 + j(\omega L/R - R/\omega L)}$$

(b) Since the ratio  $\frac{V_2}{V_o}$  must be real,

$$\frac{\omega_o L}{R} - \frac{R}{\omega_o L} = 0$$

$$\omega_o L = \frac{R^2}{\omega_o L}$$

$$\omega_o = 2\pi f_o = \frac{R}{L}$$

$$\underline{f_o = \frac{R}{2\pi L}}$$

(c) When  $\omega = \omega_o$

$$\frac{V_2}{V_o} = \frac{1}{3}$$

This must be compensated for by  $A_v = 3$ . But

$$A_v = 1 + \frac{R_2}{R_1} = 3$$

$$\underline{R_2 = 2R_1}$$