

$$s_{\text{orig}} = \text{rand}(1:20)$$

$$p_{\text{orig}} = 1/20$$

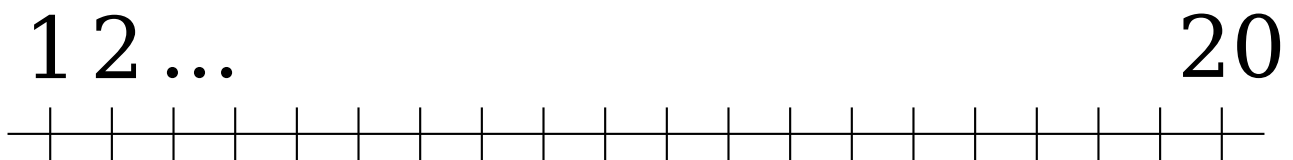
$$s_{\text{dest}} = \text{rand}(1:20)$$

$$p_{\text{dest}} = 1/20$$

We only look at travelers in one direction:

$$s_{\text{dest}} > s_{\text{orig}}$$

Let us draw the train line:



$$\begin{aligned} p_{s1} &= P(s_{\text{orig}} \leq 1 \wedge s_{\text{dest}} > 1) \\ &= P(s_{\text{orig}} \leq 1) P(s_{\text{dest}} > 1) \\ &= 1/20 \cdot 19/20 \\ &= 19/400 \end{aligned}$$

In the general case:

$$\begin{aligned} p_{si} &= P(s_{\text{orig}} \leq i) P(s_{\text{dest}} > i) \\ &= i/20 \cdot (1 - i/20) \\ &= i/20 - i^2/400 \end{aligned}$$