

# Programming and Quantitative Skills 2025 Resit Solutions

## Short-Answer Questions (4 points)

### Question 1 (1 point)

Use R to calculate the following:

$$\frac{\frac{2}{3} + \log_2(9)}{\sqrt{2}}$$

Provide both the R command and numeric value in your answer.

**Answer:**

```
(2/3 + log(9, 2)) / sqrt(2)
```

```
[1] 2.71288
```

### Question 2 (1 point)

Write an R command in the box below that generates a sequence of 10 evenly-spaced values starting from 0 and ending in 1.

The first two elements of your sequence should be 0.00000000 and 0.11111111.

Your answer must use a sequence-generating function. It is not permitted to write out the full vector manually.

**Answer:**

```
seq(from = 0, to = 1, length.out = 10)
```

```
[1] 0.0000000 0.1111111 0.2222222 0.3333333 0.4444444 0.5555556 0.6666667  
[8] 0.7777778 0.8888889 1.0000000
```

### Question 3 (1 points)

Consider the following two logical vectors:

```
a <- c(TRUE, TRUE, FALSE, FALSE)
b <- c(TRUE, FALSE, TRUE, FALSE)
```

Write a one-line R command in the box below which returns a new logical vector where the elements are:

- TRUE when the corresponding element of **a** is TRUE *and* **b** is FALSE; and
- FALSE otherwise (i.e. when either **a** is FALSE *or* **b** is TRUE).

Your answer must use the variables **a** and **b** and the appropriate logical operators (a combination of a subset of the operators **&**, **|** and **!**).

*Hint:* The output of your command should be `[1] FALSE TRUE FALSE FALSE`. The reason is because:

- Element 1 is FALSE because **b** is TRUE.
- Element 2 is TRUE because both **a** is TRUE *and* **b** is FALSE.
- Element 3 is FALSE because both **a** is FALSE *and* **b** is TRUE.
- Element 4 is FALSE because **a** is FALSE.

**Answer:**

```
a & !b
```

```
[1] FALSE TRUE FALSE FALSE
```

#### Question 4 (1 point)

Define the vector:

```
x <- c(1, -1, 2, -2, 3, -3)
```

Write an R command in the box below using the **ifelse()** function that returns the absolute value of **x**.

The output of your command should be `[1] 1 1 2 2 3 3`.

Your answer must use the **ifelse()** function. Use of the **abs()** function is not permitted for this question.

**Answer:**

```
ifelse(x > 0, x, -x)
```

```
[1] 1 1 2 2 3 3
```

#### Data Analysis (5 points)

Download the dataset [sales-data-jan-2026.csv](#). The dataset contains information on the total sales of a fictitious firm from January 2026. The firm is a vintage record store chain. The store sells 3 types of products: cassette tapes, compact discs (CDs) and vinyl records. The chain has stores in 4 cities in Noord-Brabant

(Tilburg, Breda, 's-Hertogenbosch and Eindhoven). It charges the same price for each product type in each city: (€4.99 for a tape, €9.99 for a CD and €19.99 for a vinyl record).

The variable descriptions are:

- **product:** The product type (either Tape, CD or Vinyl).
- **city:** The city (either Tilburg, Breda, 's-Hertogenbosch or Eindhoven).
- **price:** The selling price of the product.
- **sales:** The total number of units sold of that product in that city in January 2026.

When reading the dataset into R, assign it to `df`.

### Question 5 (1 point)

What is the median of the variable `sales`?

Provide both the numerical answer and the R command required to obtain the answer (if the dataframe is assigned to `df`).

**Answer:**

```
df <- read.csv("sales-data-jan-2026.csv")
median(df$sales)
```

```
[1] 124.5
```

### Question 6 (2 points)

Part (a): Write an R command in the box below that creates a new variable in `df` called `revenue`, which is price multiplied by sales.

**Answer:**

```
df$revenue <- df$price * df$sales
```

Part (b): Write an R command in the box below that returns the total revenue of the firm from cassette tape sales.

**Answer:**

```
sum(df$revenue[df$product == "Tape"])
```

```
[1] 2664.66
```

### Question 7 (1 points)

Write an R command in the box below using the `aggregate()` function that returns the total number of units sold by city.

The output of your command should be:

	city	sales
1	's-Hertogenbosch	414
2	Breda	236
3	Eindhoven	390
4	Tilburg	362

Answer:

```
aggregate(sales ~ city, data = df, FUN = sum)
```

	city	sales
1	's-Hertogenbosch	414
2	Breda	236
3	Eindhoven	390
4	Tilburg	362

### Question 8 (1 points)

Using an appropriate function from the **reshape2** package, write an R command in the box below to reshape the data such that there are 4 rows, one for each city, and the columns are:

- The city.
- The sales of CDs in each city.
- The sales of cassette tapes in each city.
- The sales of vinyl records in each city.

The output should be the following:

	city	CD	Tape	Vinyl
1	's-Hertogenbosch	133	139	142
2	Breda	76	124	36
3	Eindhoven	149	124	117
4	Tilburg	90	147	125

**Hint:** Load the **reshape2** package using the command `library(reshape2)`. You do not need to include loading this package in your answer.

Answer:

```
library(reshape2)
dcast(df, city ~ product, value.var = "sales")
```

	city	CD	Tape	Vinyl
1	's-Hertogenbosch	133	139	142
2	Breda	76	124	36
3	Eindhoven	149	124	117
4	Tilburg	90	147	125

## Data Cleaning (7 points)

Download the following dataset:

[AHOLD DEL\\_historical\\_price.csv](#)

The file was obtained from the website <https://live.euronext.com/>. It contains stock price data for the Dutch-Belgian multinational retail and wholesale holding company Ahold Delhaize, which owns the brands Albert Heijn, Etos, Gall & Gall and Bol.com, as well as several brands in other countries. The data spans the period January 2 to December 31 2025.

In order to analyze the data, some cleaning steps are required.

### Question 9 (5 points)

Perform the data cleaning steps below:

*Note:* The data after each step should match the files below. If you cannot complete a step, you can use these to proceed. For example, if you cannot do part (a), use the file `resit-2025-q9a.csv` to attempt part (b).

- Data after part (a): [resit-2025-q9a.csv](#)
- Data after part (b): [resit-2025-q9b.csv](#)
- Data after part (c): [resit-2025-q9c.csv](#)
- Data after part (d): [resit-2025-q9d.csv](#)

Part (a): Write an R command in the box below to read the dataset into R as `df`. Use the `skip` argument in the `read.csv()` function to skip the lines of metadata at the top of the file, so that the data can be read in properly. The lines of metadata are the following:

```
"Historical Data"  
"From 2025-01-02 to 2025-12-31"  
NL0011794037
```

**Answer:**

```
df <- read.csv("AHOLD DEL_historical_price.csv", skip = 3)
```

Part (b): Write an R command in the box below that will correctly format the `Date` variable to an R date.

**Answer:**

```
df$date <- as.Date(df$date, format = "%d/%m/%Y")
```

Part (c): Write an R command in the box below that will sort the data by date ascending. That is, January 2 should be first and December 31 should be last.

**Answer:**

```
df <- df[order(df$Date), ]
```

Part (d): Write an R command in the box below that creates a variable called **spread** which is the **High** variable minus the **Low** variable. This variable measures the volatility of the stock in a day.

**Answer:**

```
df$spread <- df$High - df$Low
```

Part (e): Write an R command in the box below that will convert all the variable names to lower case.

**Answer:**

```
names(df) <- tolower(names(df))
```

### Question 10 (1 point)

If you performed the data cleaning steps from the previous exercise correctly, your final dataset should match the following file: [ahold-delhaize-2025.csv](#)

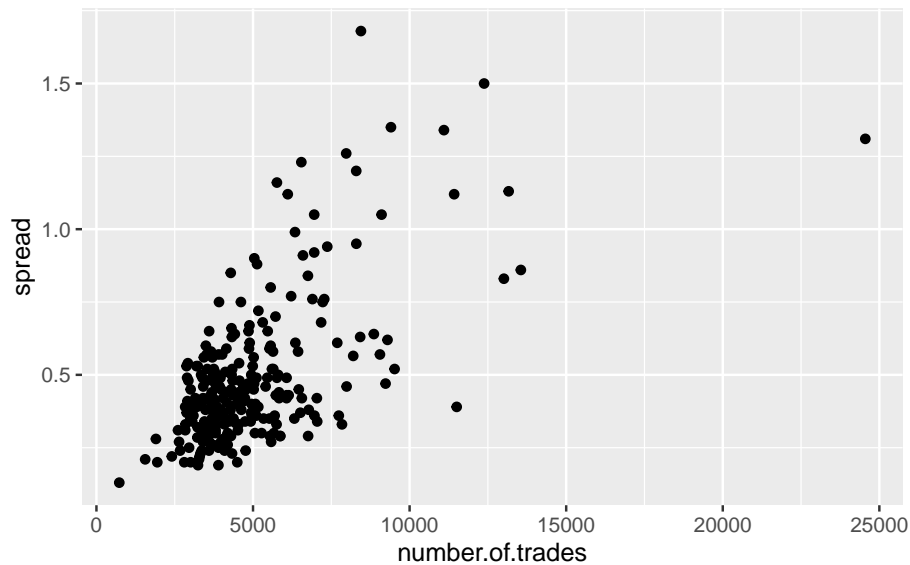
Using either your cleaned data or the data from the file above, create a scatter plot with **number.of.trades** on the horizontal axis and **spread** on the vertical axis.

Choose the answer below which best interprets what you see in the plot.

- When **number.of.trades** is high, **spread** is usually low.
- When **number.of.trades** is high, **spread** is usually also high.
- There does not appear to be any relationship between the variables **number.of.trades** and **spread**.
- When **number.of.trades** is at its highest or lowest, **spread** is at its highest, but for values of **number.of.trades** near the median, **spread** is at its lowest.

**Answer:**

```
library(ggplot2)  
ggplot(df, aes(number.of.trades, spread)) + geom_point()
```



```
# When `number.of.trades` is high, `spread` is usually also high.
```

### Question 11 (1 point)

Using the cleaned data, plot the variable `close` across time. In which quarter of the year was the variable `close` at its highest?

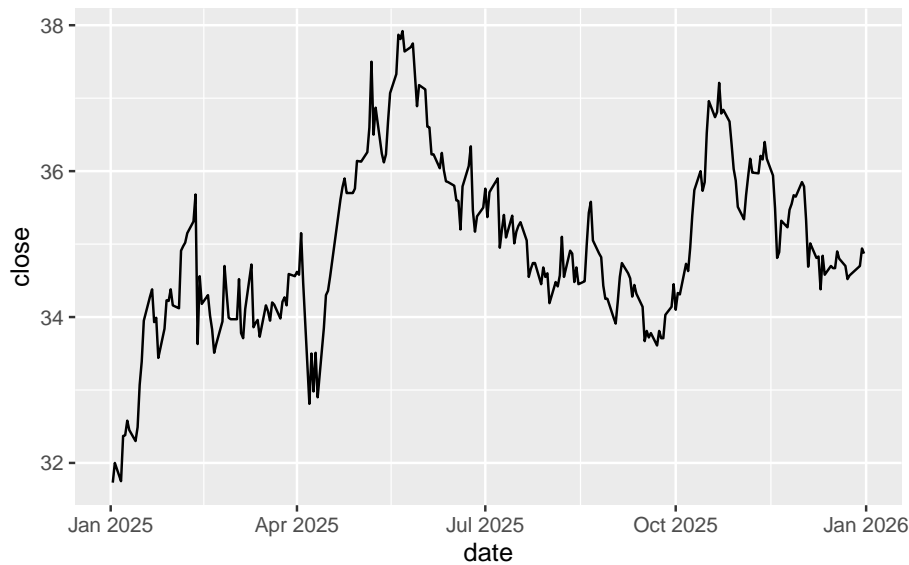
Type the quarter number in the box below, where:

- Quarter 1 is January-March.
- Quarter 2 is April-June.
- Quarter 3 is July-September.
- Quarter 4 is October-December.

**Answer:**

```
[1] "LC_CTYPE=C;LC_NUMERIC=C;LC_TIME=C;LC_COLLATE=C;LC_MONETARY=C;LC_MESSAGES=ga_IE.UTF-8;LC_
```

```
library(ggplot2)
ggplot(df, aes(date, close)) + geom_line()
```



```
# The close variable is at its highest in Q2
```

### Optimization (2 points)

The following 2 questions will involve working with the following mathematical function defined over all real numbers  $x$ :

$$f(x) = -10 - 4x + 2x^2$$

#### Question 12 (1 point)

Plot the function between the  $x$  values  $-3$  and  $+5$ . Add the correct options in the boxes below that best describe the plot.

Part (a): The shape of the function is a *straight line* / *flat* / *U-shaped* / *inverse U-shaped*.

Part (b): When  $f(x) = -10$ , the corresponding values of  $x$  are \_\_\_\_ and \_\_\_\_.

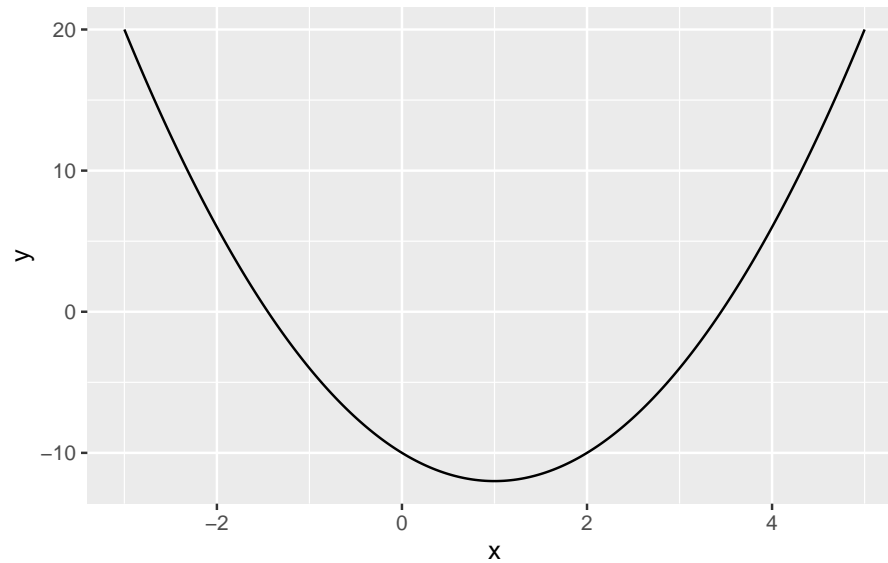
Part (c): At  $x = 4$ , the function is *downward-sloping* / *flat* / *upward-sloping*.

**Answer:**

```
f <- function(x) {
  y <- -10 - 4*x + 2 * x^2
  return(y)
}
library(ggplot2)
x <- seq(-3, 5, length.out = 2000)
```



```
y <- f(x)
df <- data.frame(x, y)
ggplot(df, aes(x, y)) + geom_line()
```



```
# Part (a) The shape of the function is U-shaped.
# Part (b) The values of x when f(x)=-10 are 0 and 2.
# Part (c) At x=4, the function is upward-sloping.
```

### Question 13 (1 point)

Use R to find the value of  $x$  at an extreme point of this function.

Part (a) Type this value of  $x$  in the box below.

**Answer:**

```
f_min <- optimize(f, c(-100, 100), maximum = FALSE)
f_min$minimum
```

```
[1] 1
```

Part (b): What value does the function take at the extreme point?

**Answer:**

```
f_min$objective
```

```
[1] -12
```

```
# or alternatively:  
f(f_min$minimum)
```

```
[1] -12
```