

Gram-Schmidt Procedure (3D) - Data Set 1

	x	y	z
u1	1	2	5
u2	0	4	11
u3	0	2	4

V1 = u1	1	2	5
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V2 = u2 - A	-2.1	-0.2	0.5
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V2 = u3 - B - C	-0.085106383	0.468085	-0.170213
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V1   =	5.477225575		
e1 = V1/  V1   =	0.182574186	0.365148	0.912871

V2   =	2.167948339		
e2 = V2/  V2   =	-0.968657768	-0.092253	0.230633

V3   =	0.505291153		
e3 = V3/  V3   =	-0.168430384	0.926367	-0.336861

V1 on V2	0	This is not an Orthogonal set
V2 on V3	1.94289E-16	
V1 on V3	0	

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u2·V1 =	63		
V1·V1 =	30		
u2·V1/V1·V1 =	2.1		
A = (u2·V1/V1·V1)*V1 =	2.1	4.2	10.5

u3·V1 =	24		
u3·V1/V1·V1 =	0.8		
B = (u3·V1/V1·V1)*V1 =	0.8	1.6	4

u3·V2 =	1.6		
u3·V2/V2·V2 =	0.340426		
C = (u3·V2/V2·V2)*V2 =	-0.714894	-0.068085	0.170213

Norms	
1	Orthonormal

1	Orthonormal
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1	Orthonormal
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Gram-Schmidt Procedure (3D) - Data Set 2

Walter Manger

	x	y	z
u1	5	0	0
u2	5	1	0
u3	5	5	4

V1 = u1	5	0	0
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V2 = u2 - A	0	1	0
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V2 = u3 - B - C	0	0	4
-----------------	---	---	---

V1   =	5
e1 = V1/  V1   =	100

V2   =	1
e2 = V2/  V2   =	010

V3   =	4
e3 = V3/  V3   =	001

V1 on V2	0
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V2 on V3	0
----------	---

V1 on V3	0
----------	---

This is an Orthogonal set

u2·V1 =	25
V1·V1 =	25
u2·V1/V1·V1 =	1
A = (u2·V1/V1·V1)*V1 =	500

u3·V1 =	25
u3·V1/V1·V1 =	1
B = (u3·V1/V1·V1)*V1 =	500

u3·V2 =	5
u3·V2/V2·V2 =	5
C = (u3·V2/V2·V2)*V2 =	050

Norms	
1	Orthonormal

1	Orthonormal
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1	Orthonormal
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Gram-Schmidt Procedure (3D) - Data Set 3

	x	y	z
u1	1	2	5
u2	2	4	10
u3	0	2	4

V1 = u1	1	2	5
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V2 = u2 - A	0	0	0
-------------	---	---	---

V2 = u3 - B - C	-0.8	0.4	0
-----------------	------	-----	---

V1   =	5.477225575
e1 = V1/  V1   =	0.1825741860.3651480.9128709

V2   =	0
e2 = V2/  V2   =	

V3   =	0.894427191
e3 = V3/  V3   =	-0.8944271910.4472140

V1 on V2	#VALUE!	#VALUE!
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V2 on V3	#VALUE!
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V1 on V3	-5.55112E-17
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Walter Manger

u2·V1 =	60
V1·V1 =	30
u2·V1/V1·V1 =	2
A = (u2·V1/V1·V1)*V1 =	2410

u3·V1 =	24
u3·V1/V1·V1 =	0.8
B = (u3·V1/V1·V1)*V1 =	0.81.64

u3·V2 =	0
u3·V2/V2·V2 =	
C = (u3·V2/V2·V2)*V2 =	000

Norms
1Orthonormal

#VALUE!	#VALUE!
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1Orthonormal
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Gram-Schmidt Procedure (3D) - Data Set 4

Walter Manger

	x	y	z
u1	1	0	2
u2	2	4	0
u3	3	2	9

V1 = u1	1	0	2
---------	---	---	---

V2 = u2 - A	1.6	4	-0.8
-------------	-----	---	------

V2 = u3 - B - C	-1.66667	0.833333	0.833333
-----------------	----------	----------	----------

V1   =	2.236068		
e1 = V1/  V1   =	0.447214	0	0.894427

V2   =	4.38178		
e2 = V2/  V2   =	0.365148	0.912871	-0.18257

V3   =	2.041241		
e3 = V3/  V3   =	-0.8165	0.408248	0.408248

u2·V1 =	2		
V1·V1 =	5		
u2·V1/V1·V1 =	0.4		
A = (u2·V1/V1·V1)*V1 =	0.4	0	0.8

u3·V1 =	21		
u3·V1/V1·V1 =	4.2		
B = (u3·V1/V1·V1)*V1 =	4.2	0	8.4

u3·V2 =	5.6		
u3·V2/V2·V2 =	0.291667		
C = (u3·V2/V2·V2)*V2 =	0.466667	1.166667	-0.23333

Norms	
1	Orthonormal

1	Orthonormal
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1	Orthonormal
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V1 on V2	0	This is an Orthogonal set
V2 on V3	0	
V1 on V3	0	

Gram-Schmidt Procedure (4D) - Data Set 1

	x	y	z	t
u1	2	0	0	0
u2	4	8	0	0
u3	3	6	9	0
u4	0	0	0	8

V1 = u1	2	0	0	0
---------	---	---	---	---

V2 = u2 - A	0	8	0	0
-------------	---	---	---	---

V3 = u3 - B - C	0	0	9	0
-----------------	---	---	---	---

V4 = u4 - D - E - F	0	0	0	8
---------------------	---	---	---	---

V1·V1 =	4
V2·V2 =	64
V3·V3 =	81
V4·V4 =	64

$  V1   =$	2				
$e1 = V1/  V1   =$	<table><tr><td>1</td><td>0</td><td>0</td><td>0</td></tr></table>	1	0	0	0
1	0	0	0		

$$||V_2|| = 8$$

$$e_2 = V_2 / ||V_2|| =$$

0	1	0	0
---	---	---	---

$  V3   =$	9			
$e3 = V3/  V3   =$	0	0	1	0

$  V4   =$	8				
$e3 = V3/  V3   =$	<table><tr><td>0</td><td>0</td><td>0</td><td>1</td></tr></table>	0	0	0	1
0	0	0	1		

Walter Manger

u2·V1 =	8				
u2·V1/V1·V1 =	2				
A = (u2·V1/V1·V1)*V1 =	<table><tr><td>4</td><td>0</td><td>0</td><td>0</td></tr></table>	4	0	0	0
4	0	0	0		

u3·V1 =	6				
u3·V1/V1·V1 =	1.5				
B = (u3·V1/V1·V1)*V1 =	<table><tr><td>3</td><td>0</td><td>0</td><td>0</td></tr></table>	3	0	0	0
3	0	0	0		

u3·V2 =	48			
u3·V2/V2·V2 =	0.75			
C = (u3·V2/V2·V2)*V2 =	0	6	0	0

u4·V1 =	0			
u4·V1/V1·V1 =	0			
D = (u4·V1/V1·V1)*V1 =	0	0	0	0

u4·V2 =	0				
u4·V2/V2·V2 =	0				
E = (u4·V2/V2·V2)*V2 =	<table><tr><td>0</td><td>0</td><td>0</td><td>0</td></tr></table>	0	0	0	0
0	0	0	0		

u4·V3 =	0				
u4·V3/V3·V3 =	0				
F = (u4·V3/V3·V3)*V3 =	<table><tr><td>0</td><td>0</td><td>0</td><td>0</td></tr></table>	0	0	0	0
0	0	0	0		

Norms	
1	Orthonormal

1	Orthonormal
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1	Orthonormal
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1	Orthonormal
---	-------------

V1 on V2	0	This is an Orthogonal set
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V1 on V3	0
----------	---

V1 on V4	0
----------	---

V2 on V3	0
----------	---

V2 on V4	0
----------	---

V3 on V4	0
----------	---

Gram-Schmidt Procedure (4D) - Data Set 2

	x	y	z	t
u1	4	0	0	0
u2	4	8	0	0
u3	4	8	9	0
u4	4	8	9	8

V1 = u1	4	0	0	0
---------	---	---	---	---

V2 = u2 - A	0	8	0	0
-------------	---	---	---	---

V3 = u3 - B - C	0	0	9	0
-----------------	---	---	---	---

V4 = u4 -D - E - F	0	-8	-9	0
--------------------	---	----	----	---

V1·V1 =	16
V2·V2 =	64
V3·V3 =	81
V4·V4 =	145

$$||V1|| = 4$$

$$e1 = V1/||V1|| =$$

1	0	0	0
---	---	---	---

$$||V_2|| = 8$$

$$e_2 = V_2 / ||V_2|| =$$

0	1	0	0
---	---	---	---

$$||V_3|| = 9$$

$$e_3 = V_3 / ||V_3|| =$$

0	0	1	0
---	---	---	---

$  V4   =$	12.04159			
$e3 = V3/  V3   =$	0	-0.66436	-0.74741	0

V1 on V2	0	This is not an Orthogonal set
V1 on V3	0	
V1 on V4	0	
V2 on V3	0	
V2 on V4	-0.66436	
V3 on V4	-0.74741	

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u2·V1 =	16				
u2·V1/V1·V1 =	1				
A = (u2·V1/V1·V1)*V1 =	<table><tr><td>4</td><td>0</td><td>0</td><td>0</td></tr></table>	4	0	0	0
4	0	0	0		

u3·V1 =	16				
u3·V1/V1·V1 =	1				
B = (u3·V1/V1·V1)*V1 =	<table><tr><td>4</td><td>0</td><td>0</td><td>0</td></tr></table>	4	0	0	0
4	0	0	0		

u3·V2 =	64				
u3·V2/V2·V2 =	1				
C = (u3·V2/V2·V2)*V2 =	<table><tr><td>0</td><td>8</td><td>0</td><td>0</td></tr></table>	0	8	0	0
0	8	0	0		

u4·V1 =	16				
u4·V1/V1·V1 =	1				
D = (u4·V1/V1·V1)*V1 =	<table><tr><td>4</td><td>8</td><td>9</td><td>8</td></tr></table>	4	8	9	8
4	8	9	8		

u4·V2 =	64				
u4·V2/V2·V2 =	1				
E = (u4·V2/V2·V2)*V2 =	<table><tr><td>0</td><td>8</td><td>0</td><td>0</td></tr></table>	0	8	0	0
0	8	0	0		

u4·V3 =	81				
u4·V3/V3·V3 =	1				
F = (u4·V3/V3·V3)*V3 =	<table border="1"><tr><td>0</td><td>0</td><td>9</td><td>0</td></tr></table>	0	0	9	0
0	0	9	0		

Norms	
1	Orthonormal

1	Orthonormal
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1	Orthonormal
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1	Orthonormal
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Gram-Schmidt Procedure (4D) - Data Set 3

	x	y	z	t
u1	4	0	0	0
u2	6	8	8	8
u3	4	0	9	5
u4	8	8	9	8

V1 = u1	4	0	0	8
---------	---	---	---	---

V2 = u2 - A	1.6	8	8	-0.8
-------------	-----	---	---	------

V3 = u3 - B - C	0.292683	-4.53659	4.463415	-0.14634
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V4 = u4 - D - E - F	-3.37297	-9.71892	-11.0378	-0.71351
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V1·V1 =	80
V2·V2 =	131.2
V3·V3 =	40.60976
V4·V4 =	228.1773

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u2·V1 =	88
u2·V1/V1·V1 =	1.1
A = (u2·V1/V1·V1)*V1 =	4.4008

u3·V1 =	56
u3·V1/V1·V1 =	0.7
B = (u3·V1/V1·V1)*V1 =	2.8000

u3·V2 =	74.4
u3·V2/V2·V2 =	0.567073
C = (u3·V2/V2·V2)*V2 =	0.9073174.5365854.536585-0.45366

u4·V1 =	96
u4·V1/V1·V1 =	1.2
D = (u4·V1/V1·V1)*V1 =	9.69.610.89.6

u4·V2 =	142.4
u4·V2/V2·V2 =	1.085366
E = (u4·V2/V2·V2)*V2 =	1.7365858.6829278.682927-0.86829

u4·V3 =	5.04878
u4·V3/V3·V3 =	0.124324
F = (u4·V3/V3·V3)*V3 =	0.036388-0.564010.554911-0.01819

V1   =	8.944272
e1 = V1/  V1   =	0.447214000.894427

Norms	
1	Orthonormal

V2   =	11.45426
e2 = V2/  V2   =	0.1396860.698430.69843-0.06984

1	Orthonormal
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V3   =	6.372578
e3 = V3/  V3   =	0.045928-0.711890.70041-0.02296

1	Orthonormal
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V4   =	15.10554
e3 = V3/  V3   =	-0.22329-0.6434-0.73071-0.04724

1	Orthonormal
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V1 on V2	-6.2E-17	This is not an Orthogonal set
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V1 on V3	1.28E-16
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V1 on V4	-0.14211
----------	----------

V2 on V3	9.15E-17
----------	----------

V2 on V4	-0.98762
----------	----------

V3 on V4	-0.06294
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Gram-Schmidt Procedure (4D) - Data Set 4

	x	y	z	t
u1	1	0	0	9
u2	0	8	4	2
u3	4	0	9	5
u4	0	8	0	1
V1 = u1	1	0	0	4
V2 = u2 - A	-0.47059	8	4	0.117647
V3 = u3 - B - C	2.791789	-3.46041	7.269795	-0.69795
V4 = u4 - D - E - F	1.459892	-1.61872	-0.37418	0.399733
V1·V1 =	17			
V2·V2 =	80.23529			
V3·V3 =	73.10557			
V4·V4 =	5.051352			

V1   =	4.123106			
e1 = V1/  V1   =	0.242536	0	0	0.970143
V2   =	8.957416			
e2 = V2/  V2   =	-0.05254	0.893115	0.446557	0.013134
V3   =	8.55018			
e3 = V3/  V3   =	0.326518	-0.40472	0.850251	-0.08163
V4   =	2.247521			
e3 = V3/  V3   =	0.649556	-0.72023	-0.16649	0.177855

V1 on V2	0	This is not an Orthogonal set
V1 on V3	0	
V1 on V4	0.330085	
V2 on V3	9.54E-18	
V2 on V4	-0.74938	
V3 on V4	0.347507	

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u2·V1 =	8			
u2·V1/V1·V1 =	0.470588			
A = (u2·V1/V1·V1)*V1 =	0.470588	0	0	1.882353
u3·V1 =	24			
u3·V1/V1·V1 =	1.411765			
B = (u3·V1/V1·V1)*V1 =	1.411765	0	0	5.647059
u3·V2 =	34.70588			
u3·V2/V2·V2 =	0.432551			
C = (u3·V2/V2·V2)*V2 =	-0.20355	3.460411	1.730205	0.050888
u4·V1 =	4			
u4·V1/V1·V1 =	0.235294			
D = (u4·V1/V1·V1)*V1 =	0	1.882353	0	0.235294
u4·V2 =	64.11765			
u4·V2/V2·V2 =	0.79912			
E = (u4·V2/V2·V2)*V2 =	-0.37606	6.392962	3.196481	0.094014
u4·V3 =	-28.3812			
u4·V3/V3·V3 =	-0.38822			
F = (u4·V3/V3·V3)*V3 =	-1.08384	1.343409	-2.8223	0.270959

Norms	
1	Orthonormal
1	Orthonormal
1	Orthonormal
1	Orthonormal



Least Square Forecasting - Data Set 1

Walter Manger

x	y	xy	x²	y²	y^
1	8	8	1	64	5.38
2	6	12	4	36	6.59
3	10	30	9	100	7.79
4	6	24	16	36	8.99
5	10	50	25	100	10.2
6	13	78	36	169	11.4
7	9	63	49	81	12.6
8	11	88	64	121	13.8
9	15	135	81	225	15.01
10	17	170	100	289	16.21
11	18	198	121	324	17.41
12	21	252	144	441	18.62
15	Forcasted at x ----->				22.22
20	Forcasted at x ----->				28.24
25	Forcasted at x ----->				34.25

Points	Σx	Σy	Σxy	Σx²	Σy²
12	78	144	1108	650	1986

$\bar{X} = \frac{78}{12} = 6.5$

$\bar{Y} = \frac{144}{12} = 12$

b =

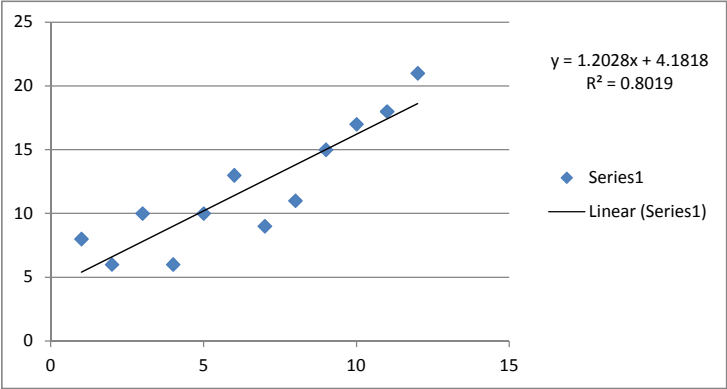
12	1108	-	78	144
12	650	-	78	78

=

1.202797

a = ybar - xbar\*b =

4.181818



Least Square Forecasting - Data Set 2

Walter Manger

x	y	xy	x²	y²	y^
1	254	254	1	64516	250.22
2	257	514	4	66049	255.01
3	249	747	9	62001	259.81
4	253	1012	16	64009	264.6
5	275	1375	25	75625	269.39
6	273	1638	36	74529	274.19
7	287	2009	49	82369	278.98
8	295	2360	64	87025	283.77
9	289	2601	81	83521	288.57
10	297	2970	100	88209	293.36
11	301	3311	121	90601	298.16
12	289	3468	144	83521	302.95
15	Forecasted at x ----->				317.33
20	Forecasted at x ----->				341.3
25	Forecasted at x ----->				365.27

Points	Σx	Σy	Σxy	Σx²	Σy²
12	78	3319	22259	650	921975

$\bar{X} = \frac{78}{12} = 6.5$

$\bar{Y} = \frac{3319}{12} = 276.5833$

b =

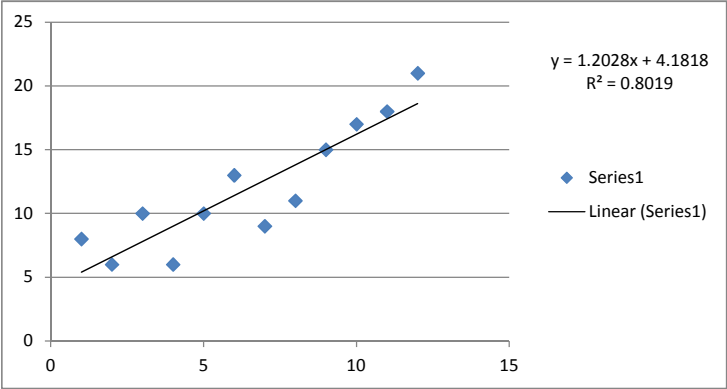
12	22259	-	78	3319
12	650	-	78	78

=

4.793706

a = ybar - xbar\*b =

245.4242



Least Square Forecasting - Data Set 3

x	y	xy	x <sup>2</sup>	y <sup>2</sup>	y <sup>^</sup>
1	3.25	3.25	1	10.5625	3.62
2	3.46	6.92	4	11.9716	3.59
3	3.57	10.71	9	12.7449	3.57
4	3.63	14.52	16	13.1769	3.55
5	3.84	19.2	25	14.7456	3.52
6	3.91	23.46	36	15.2881	3.5
7	3.68	25.76	49	13.5424	3.47
8	3.36	26.88	64	11.2896	3.45
9	3.28	29.52	81	10.7584	3.43
10	3.33	33.3	100	11.0889	3.4
11	3.26	35.86	121	10.6276	3.38
12	3.27	39.24	144	10.6929	3.36
15	Forcasted at x ----->				3.29
20	Forcasted at x ----->				3.17
25	Forcasted at x ----->				3.05

Points	Σx	Σy	Σxy	Σx <sup>2</sup>	Σy <sup>2</sup>
12	78	41.84	268.62	650	146.4894

$\bar{X} = \frac{78}{12} = 6.5$

$\bar{Y} = \frac{41.84}{12} = 3.486667$

b =

12	268.62	-	78	41.84
12	650	-	78	78

=

-0.02336

a = ybar - xbar\*b =

3.638485

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