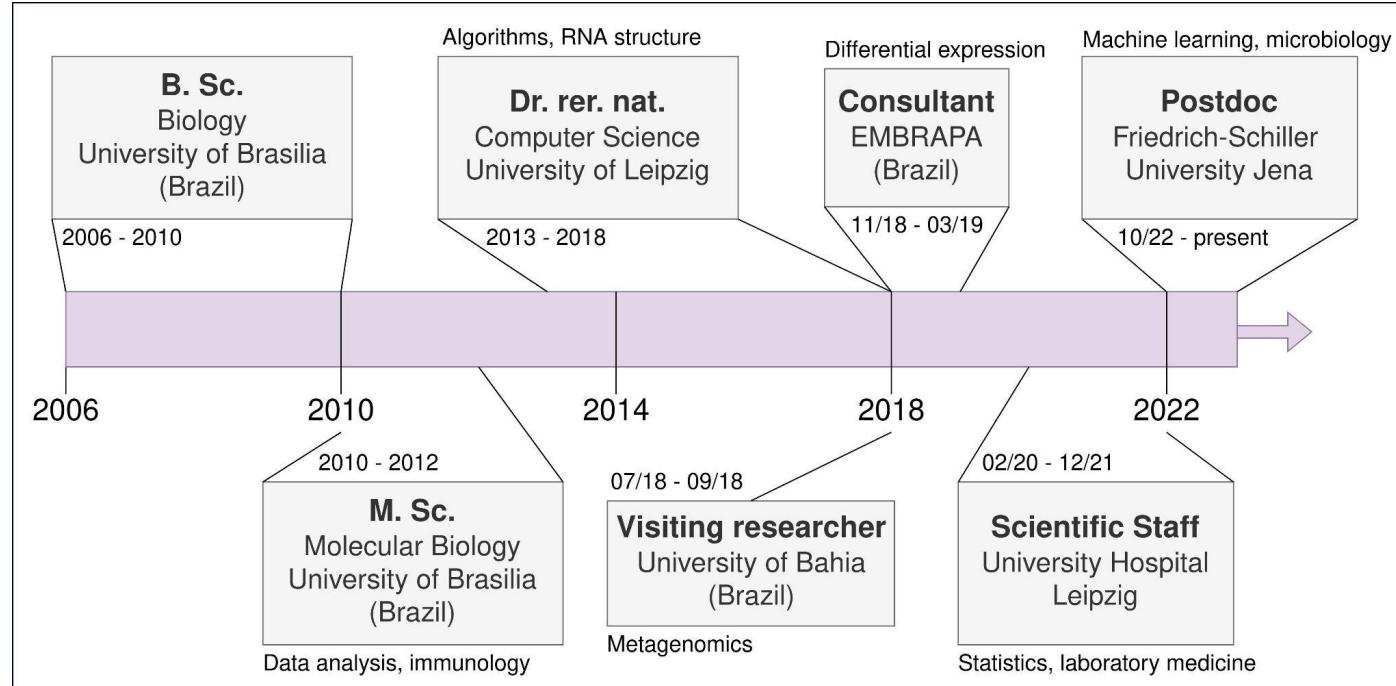


# Introduction to Statistics

Maria Beatriz Walter Costa  
Viral Ecology and Omics (VEO)

# Presenting the lecturer: Dr Maria Beatriz Walter Costa



# Outline

- **What is statistics?**
- **Types of variables**
- **Distributions**
- **Choosing tests**
- **Parametric test**  
t-test
- **Non-parametric test**  
Mann-Whitney U test
- **p-values**
- **Linear regression**
- **Correlation**  
Pearson, Spearman
- **Set Enrichment Analysis**
- **How to continue learning**
- **Slides at:**  
<https://github.com/waltercostamb/statistics>



# Statistics: analysis and interpretation of data

- **Descriptive statistics**

Mean, median, standard deviation

- **Inferential statistics**

Conclusions that extend beyond data you have,  
test ideas/hypothesis

- **Frequentist/classical statistics**

Testing null hypothesis

- **Bayesian statistics**

No rejection of hypothesis, rather degrees of  
belief

- **Shannon diversity index**

Measures diversity of species in community

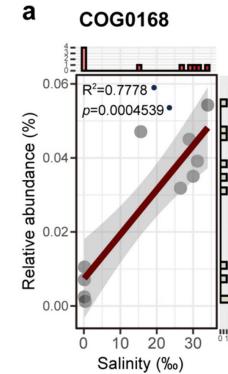
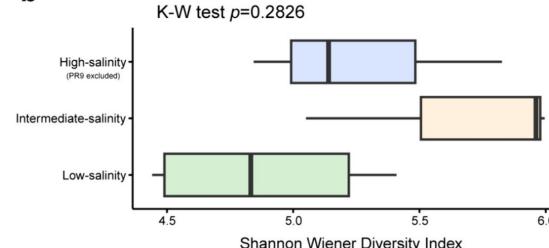
- **Kruskal-Wallis rank sum test**

Tests if samples originate from same distribution

- **Linear regression**

Model that estimates linear relationship between  
response and explanatory variables

b



# Types of variables

- **Qualitative/categorical**

Oxygen tolerance; biomes

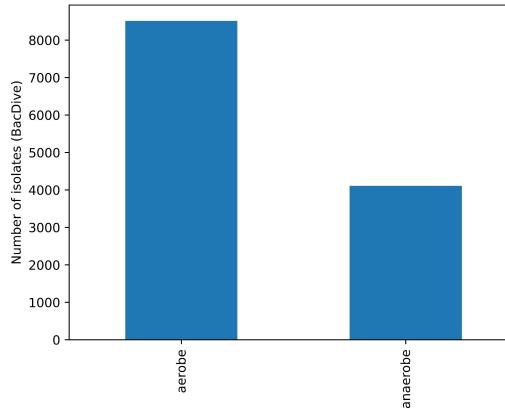
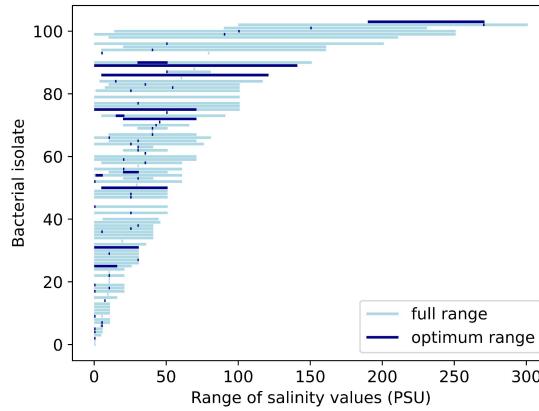
- **Quantitative**

- **Discrete**

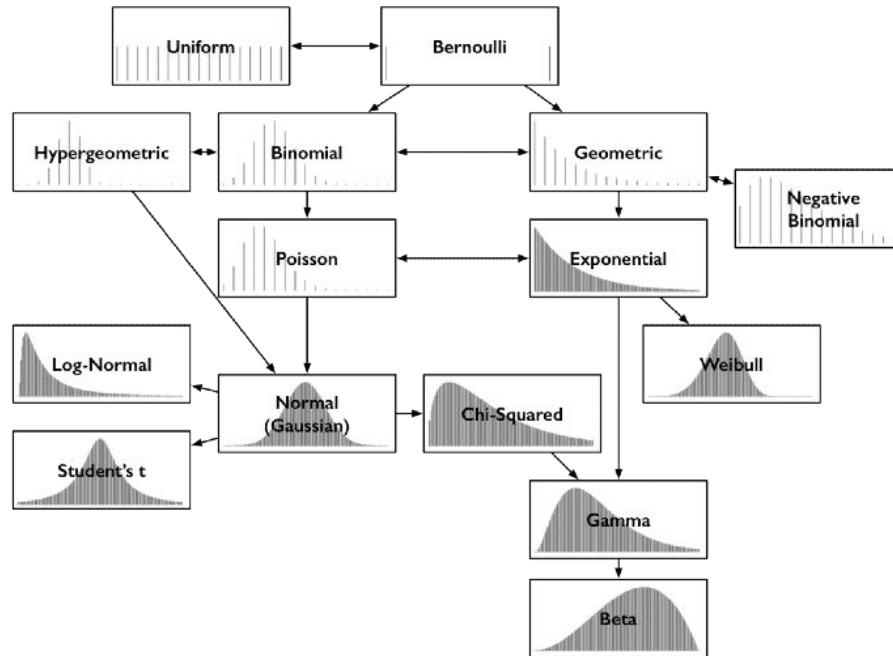
Counts of isolates per class

- **Continuous**

Salinity tolerances



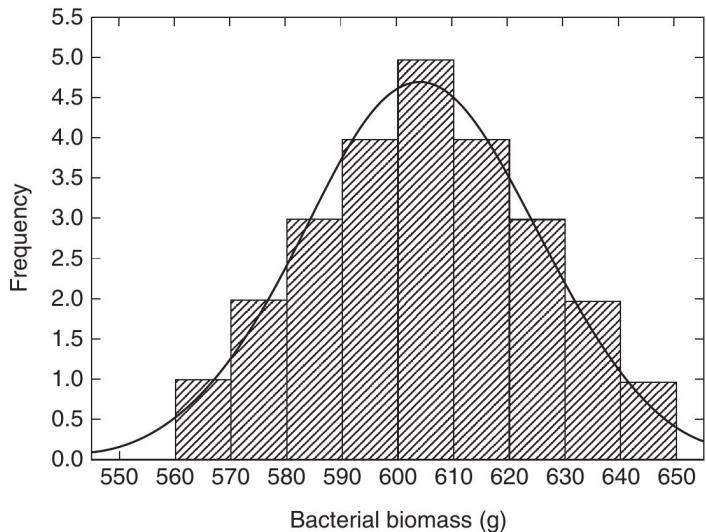
# Distributions: how data spreads across a range of values



# Distributions

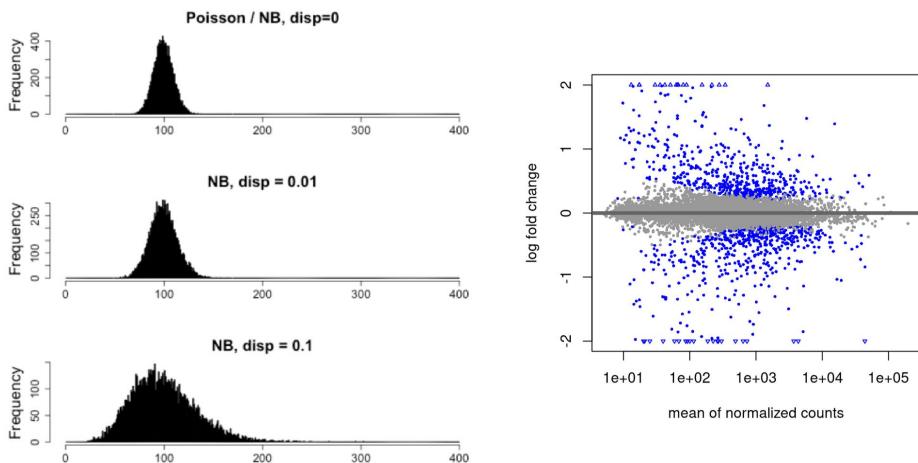
- **Normal**

Mean, st dev; shown by Kolmogorov-Smirnov test



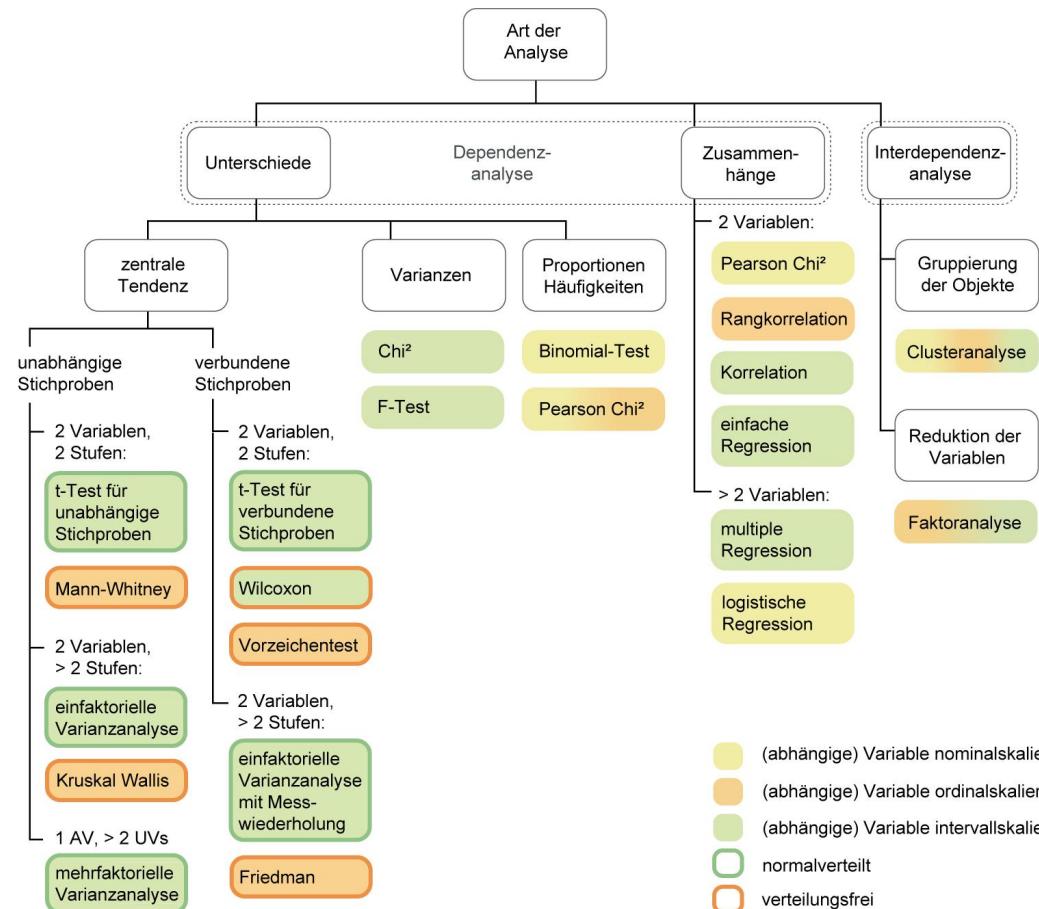
- **Negative binomial**

- expression (RNAseq);
- appropriate for counts
- mean < variance
- DESeq2 for finding fold changes



# Answering questions and choosing tests

| Possible Statistical Procedures        |  |  |
|--|--|--|
| Form of the Data                       | Parametric   | Nonparametric  |
| A single observation $x$               | Is $x$ a member of a specific population (2.5)?                        | —  |
| A sample of $x$ values                 | Construct frequency distribution, calculate $x^*$ , SD, SEM, CI (2.4). | Mode, median, 95th percentile (4)                              |
| Two independent samples ( $x_1, x_2$ ) | Is $X$ normally distributed? (1)<br>Unpaired $t$ test (3.4)            | Mann–Whitney $U$ test (4.7)<br>Wilcoxon signed-rank test (4.8) |
| Two paired samples ( $x_1 - x_2$ )     | Paired $t$ test (3.6)  |  |



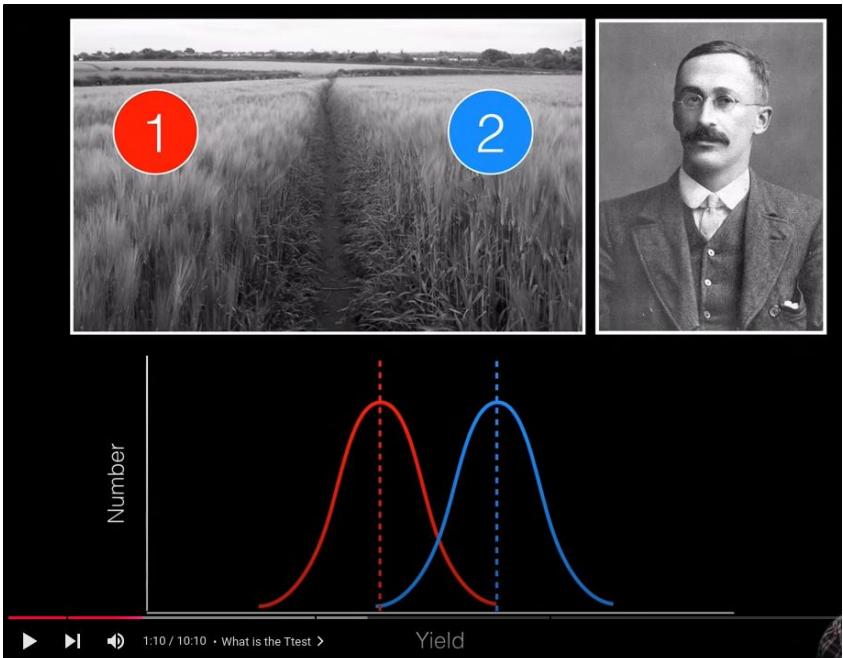
- (abhängige) Variable nominalskaliert
- (abhängige) Variable ordinalskaliert
- (abhängige) Variable intervallskaliert
- normalverteilt
- verteilungsfrei

# Parametric test: t-test

- student's t-distribution: gets name from **William Sealy Gosset, worked for Guiness Brewery in Dublin**
- interested in monitoring quality of stout



- **Compares 2 groups**
  - yield of field 1 field 2 of barley



# Parametric test: t-test

- **Compares 2 groups**
  - yield of field 1 field 2 of barley
- **Inferential test for hypothesis testing**
  - Null-hypothesis: means are the same
  - Balance of signal/noise
  - Input: mean, std dev, sample size
- **Are observed differences meaningful or random?**
  - Compare calculated value against a table of standard ones to get p-value
- **Used when data follows normal distribution, similar variances**
- **Suited for small sample sizes (> 40)**

# Non-parametric test: Mann-Whitney U test

- Counterpart to t-test

- Inferential test for hypothesis testing

- Null-hypothesis: rank sums are same
  - Input: ranks (sum), sample size

- Are observed differences meaningful or random?

- Compare calculated values against a table of expected ones to get p-value

- Used when data does not follow normal distribution

| Gender | Reaction time | Rang |
|--------|---------------|------|
| female | 34            | 2    |
| female | 36            | 4    |
| female | 41            | 7    |
| female | 43            | 9    |
| female | 44            | 10   |
| female | 37            | 5    |
| male   | 45            | 11   |
| male   | 33            | 1    |
| male   | 35            | 3    |
| male   | 39            | 6    |
| male   | 42            | 8    |

Calculation of the rank sums

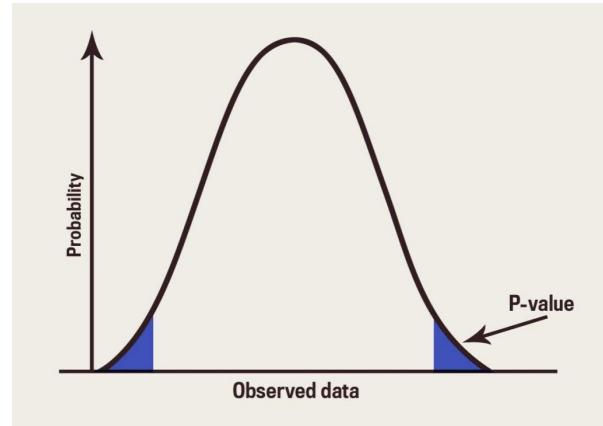
$$T_1 = 2 + 4 + 7 + 9 + 10 + 5 = 37$$

$$T_2 = 11 + 1 + 3 + 6 + 8 = 29$$

# p-value

- **Probability: [0, 1] indicating confidence of result** finding observed or more extreme values for same number of samples (if null hyp. true)
- **Helps decide if we should reject null hypothesis**
- **How close to zero do we have to be to be sufficiently confident?**
- **Rule of thumb: <0.05 to reject null hypothesis** by random chance, we could get similar results 5% of times (false-positives!)

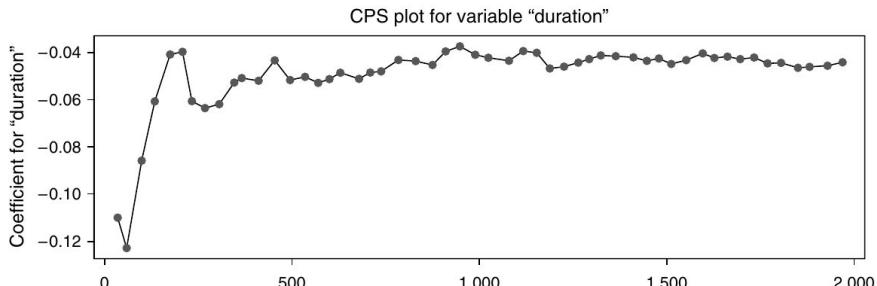
- **p-value does not tell if alternative hypothesis is true**
- **P-value cannot inform on how much difference there is**  
For this, you need to calculate the effect size



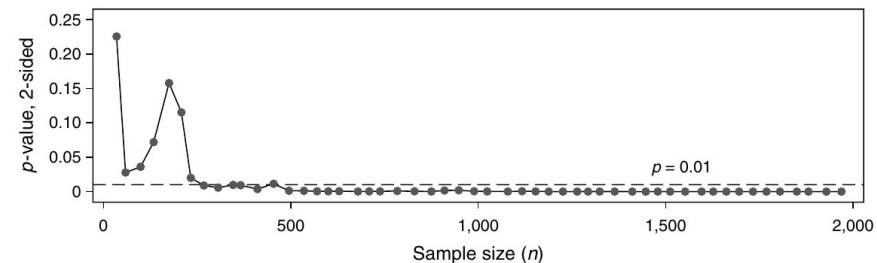
# Effect size is important!

- Traditional tests are appropriate for small sample sizes
- In large samples, even tiny differences will lead to small p-values
- What to do?
  - Present effect sizes
  - Present confidence intervals
  - Use visualization
  - CPS (coefficient, p-value, sample size) charts: sub-sample for different sample sizes and plot
  - Split data into training and “holdout” for validation

CPS Chart for Duration: Coefficient and p-Value vs. Sample Size

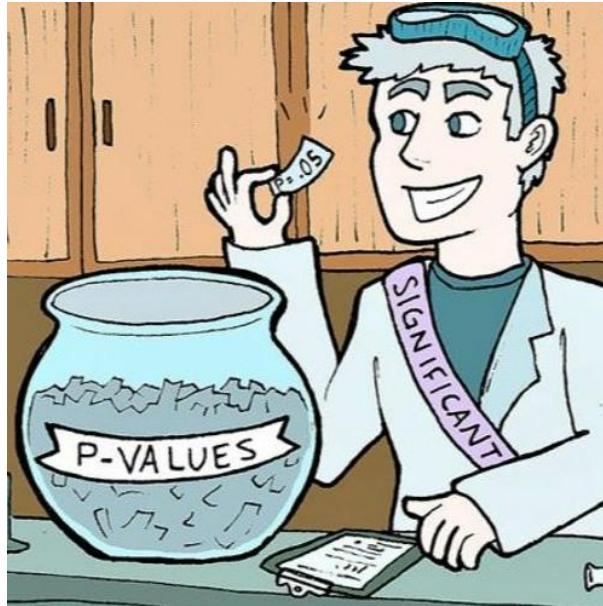


CPS plot for variable "duration"



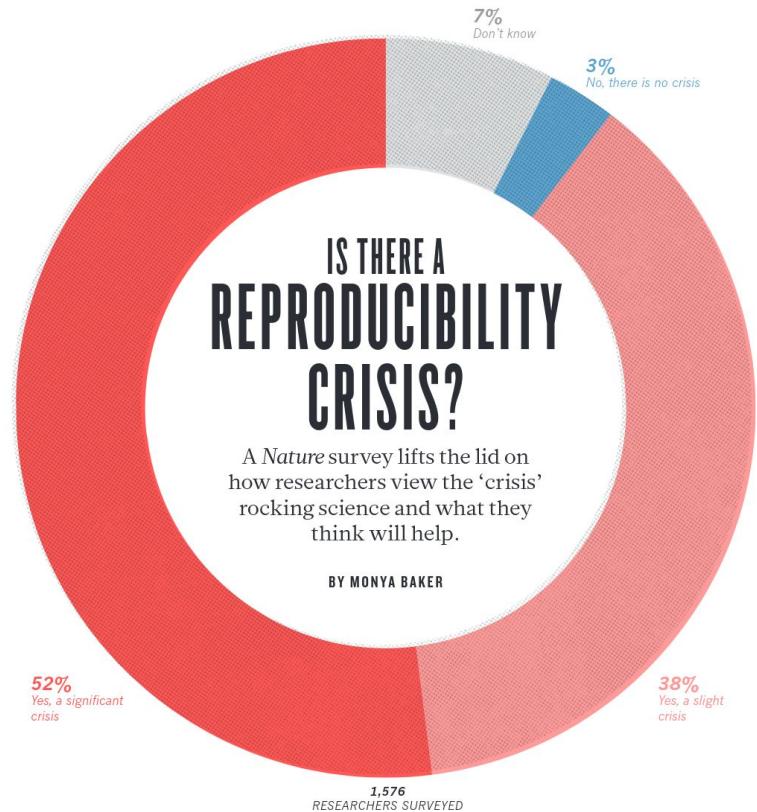
# Replication crisis and p-hacking

- **What are researchers trying to find?** Causality
- P-values help, but aren't proof
  - Correlation does not imply causation
- **Reproducibility** helps further, but is unfortunately discouraged by how publication works
- **P-hacking:** manipulation of data that artificially produces significant results
  - Major player in replication crisis
  - Intention or unintentional
    - Failing to do multiple test correction
- **What to do??**
  - Be transparent
  - ask an expert



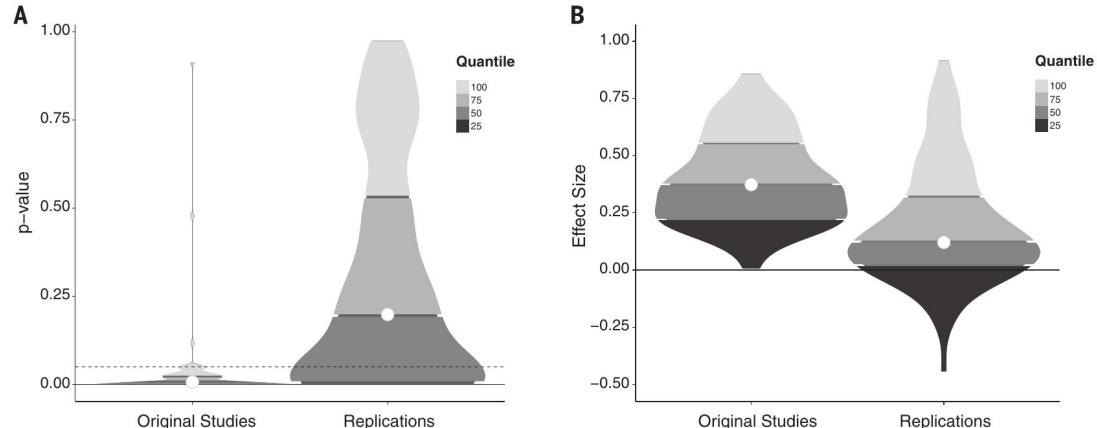
# How many scientific studies are reproducible?

- “Estimating the reproducibility of psychological science”, Open science collaboration (300 authors), Science, 2015
- Replicated 100 experimental studies
- Compared: p-values, effect sizes, subjective assessments



# How many scientific studies are reproducible?

- “**Estimating the reproducibility of psychological science**”, Open science collaboration (300 authors), Science, 2015
- Replicated 100 experimental studies
- Compared: p-values, effect sizes, subjective assessments
- 36% of original studies were reproducible
- Effect size of reproduced studies had half the magnitude of original ones



# Guidelines of Scientific Reports

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nature > scientific reports



## Statistical guidelines

If your paper contains statistical testing, it should state the name of the statistical test, the n value for each statistical analysis, the comparisons of interest, a justification for the use of that test (including, for example, a discussion of the normality of the data when the test is appropriate only for normal data), the alpha level for all tests, whether the tests were one-tailed or two-tailed, and the actual P value for each test (not merely "significant" or " $P < 0.05$ "). Please make it clear what statistical test was used to generate every P value. Use of the word "significant" should always be accompanied by a P value; otherwise, use "substantial," "considerable," etc.

Data sets should be summarised with **descriptive statistics**, which should include the **n value for each data set**, a clearly labelled **measure of centre** (such as the mean or the median), and a clearly labelled **measure of variability** (such as standard deviation or range).

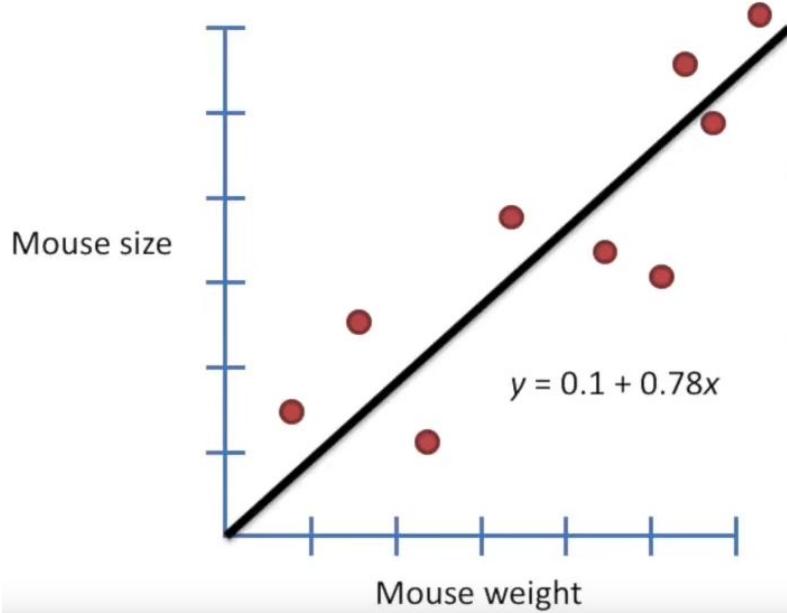
Ranges are more appropriate than standard deviations or standard errors for small data sets. Graphs should include clearly labelled error bars. You must state whether a number that follows the ± sign is a standard error (s.e.m.) or a standard deviation (s.d.).

You must justify the use of a particular test and explain whether the data conforms to the assumptions of the tests. Three errors are particularly common:

- Multiple comparisons: when making multiple statistical comparisons on a single data set, you should explain how you adjusted the alpha level to avoid an inflated Type I error rate, or you should select statistical tests appropriate for multiple groups (such as ANOVA rather than a series of t-tests).
- Normal distribution: many statistical tests require that the data be approximately normally distributed; when using these tests, you should explain how you tested your data for normality. If the data does not meet the assumptions of the test, you should use a non-parametric alternative instead.
- Small sample size: when the sample size is small (less than about 10), you should use tests appropriate to small samples or justify the use of large-sample tests.

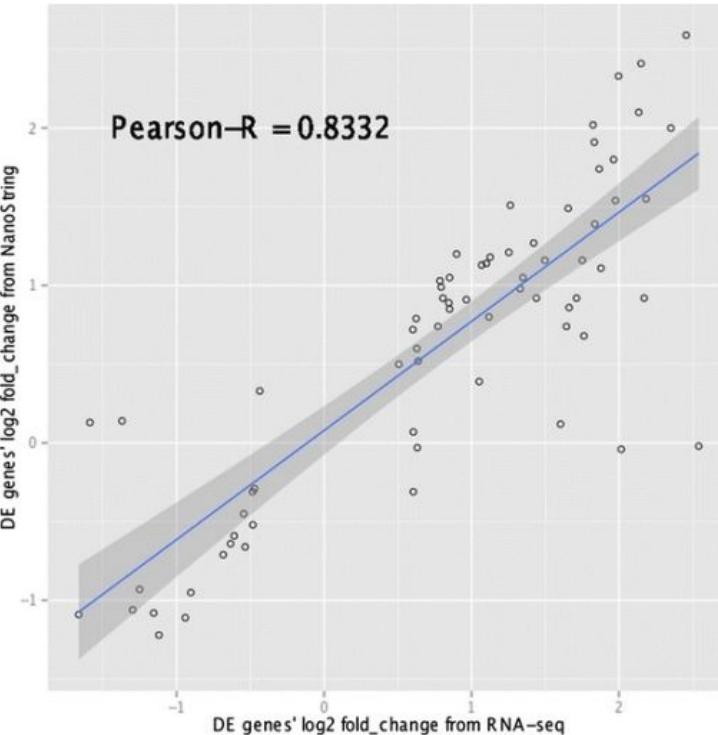
# Linear regression

- Models relationship between independent (x) and dependent (y) variables
- $f(x) = a + bx$ 
  - a = intercept in y axis
  - b = slope
- Use least squares to fit straight line to data
- Calculate R squared
  - Distance between prediction and actual values (residuals)
  - How much weight explains size
- Calculate p-value for R squared
  - prob that random dots result in similarly stronger relationship or higher



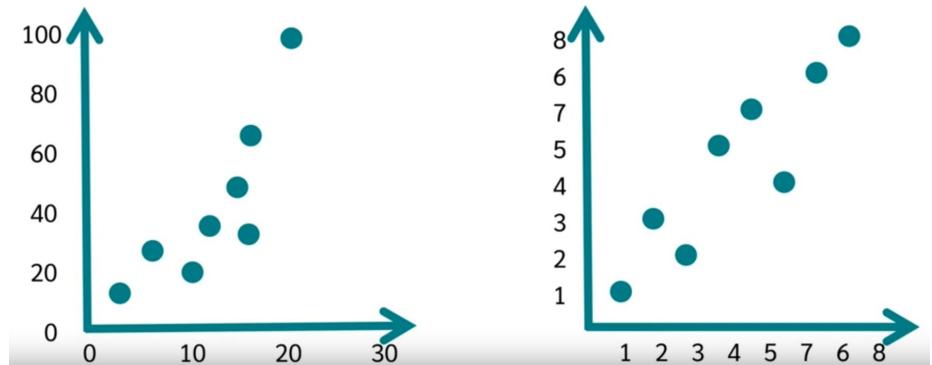
# Parametric correlation: Pearson

- Models relationships between two numeric variables
- Inferential model, can be used to predict new data based on trend
  - Measures strength of relationship (strong, moderate, weak)
  - [-1, 0, 1]
- P-values: prob that random dots result in similarly stronger relationship or higher; confidence on model
- Assumes linear relationships
  - check with visualization
- NO CAUSAL assumptions
  - A 3rd factor could cause the variables



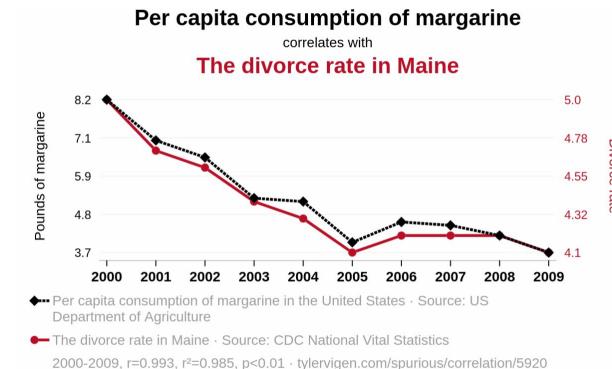
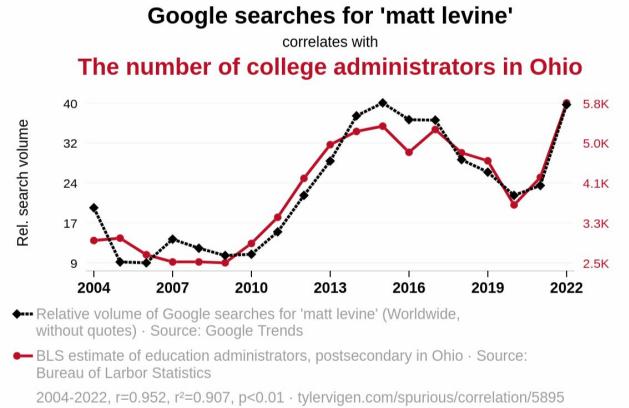
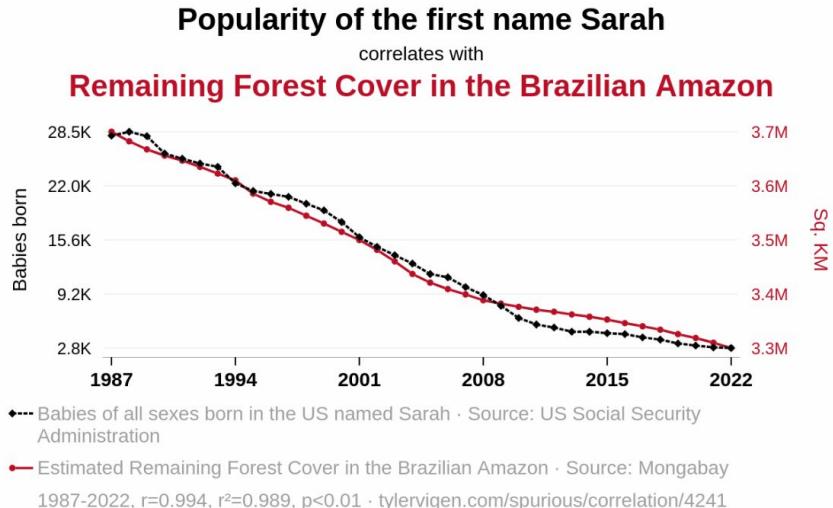
# Non-parametric correlation: Spearman

- Non-param counterpart of Pearson
- Applies Pearson on ranks instead of raw values
- Inferential model
  - strength of relationship (strong, moderate, weak)
  - $[-1, 0, 1]$
- P-values: prob that random dots result in similarly stronger relationship or higher
- NO CAUSAL assumptions

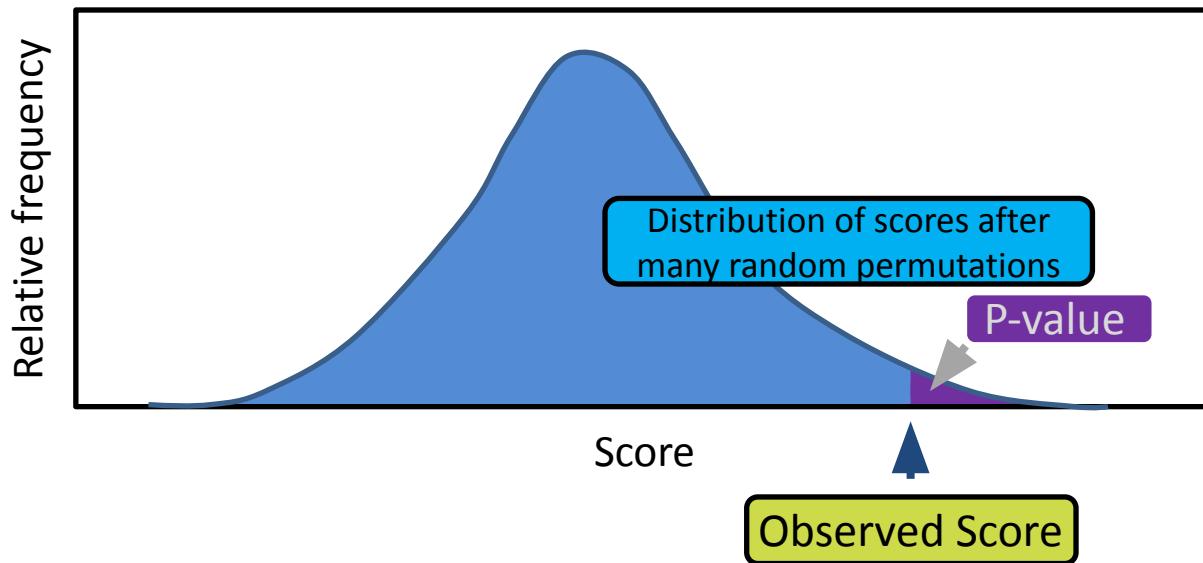


# Spurious correlations

- Correlation does not imply causation

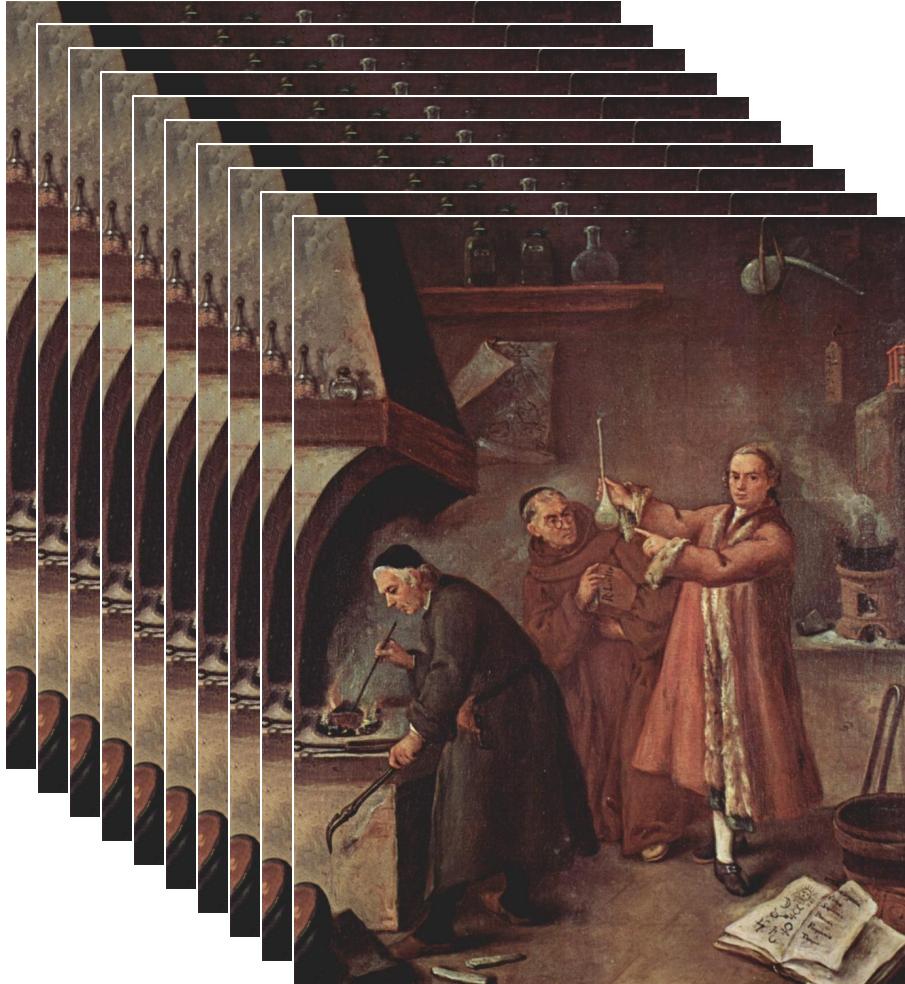
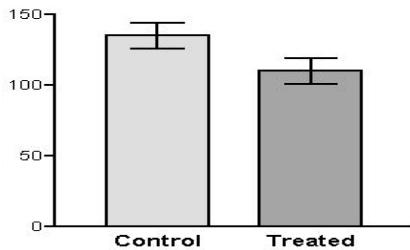


# Permutation statistics

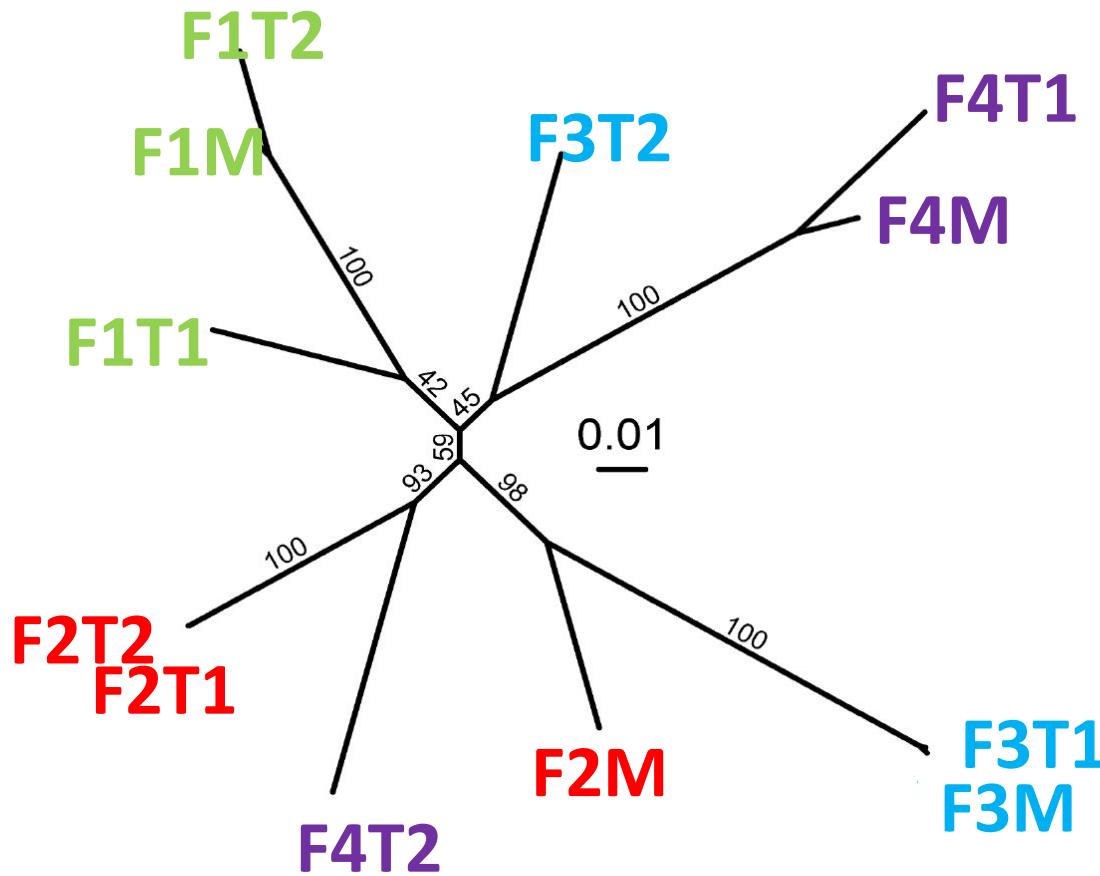


# Statistics

- We use statistics to assess confidence in an experimental result
  - We repeat the experiment  $N$  times and test how robust the result is
  - How much variation is there in the result?

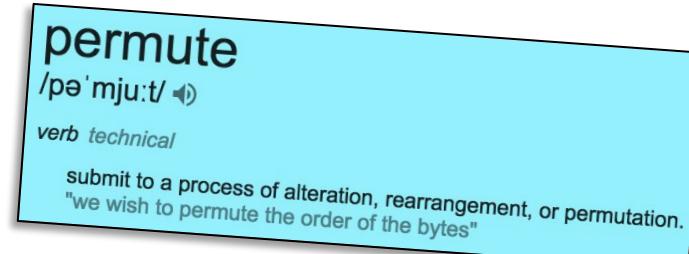


# Are the viruses from family members closely related?



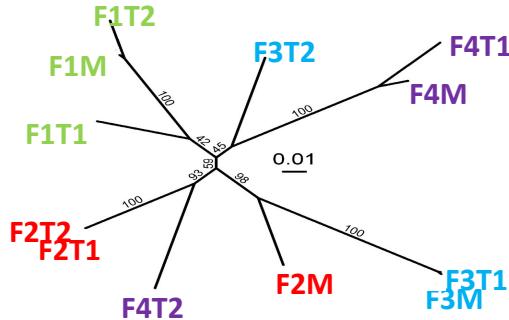
# A question of statistics

- What do we mean by “closely” related?
  - More closely than expected!
  - This is a question of statistics
- Statistics are not well defined for many bioinformatic analyses
  - For example, we need to consider the number of leaves in the tree, the shape of the tree, the number of families and family members in the analysis, and possibly many other variables
- A simple solution is data permutation:
  - Permute (shuffle) the leaves in the tree 1000\* times
  - Register if the family members cluster together better than in the original tree
    - If they often cluster better, this suggests they originally did not cluster so well
    - If they rarely cluster better, this suggests they originally clustered pretty well



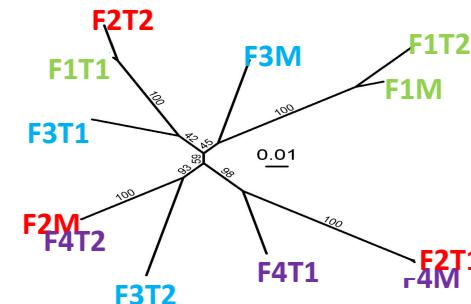
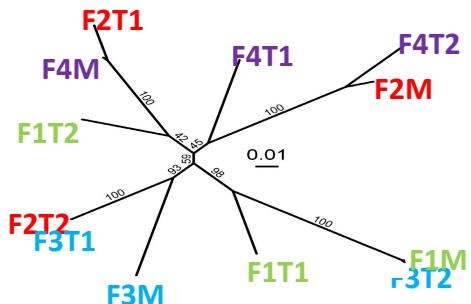
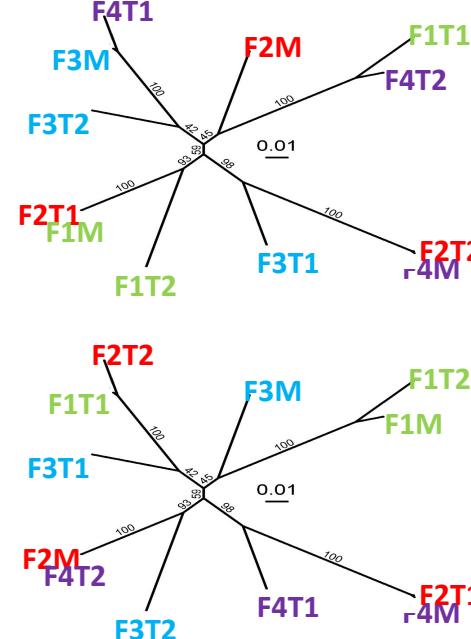
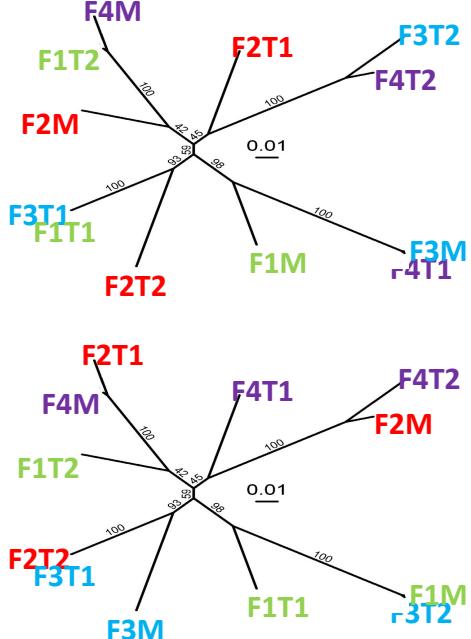
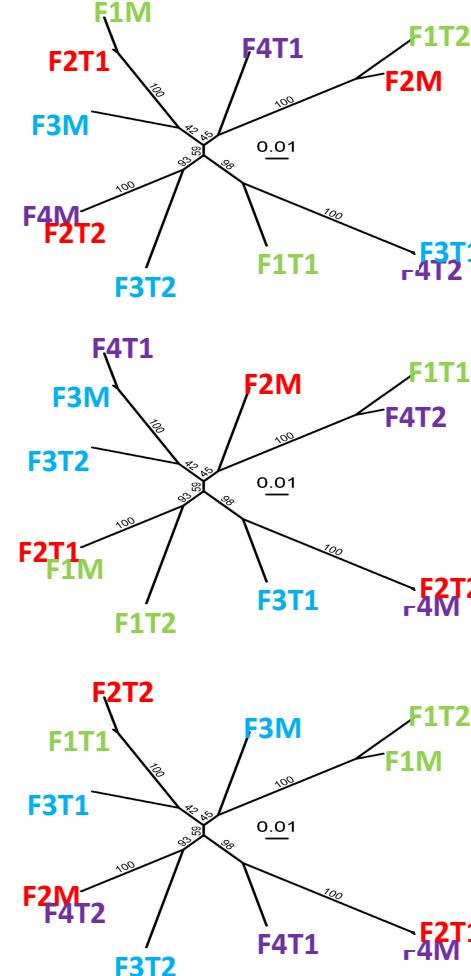
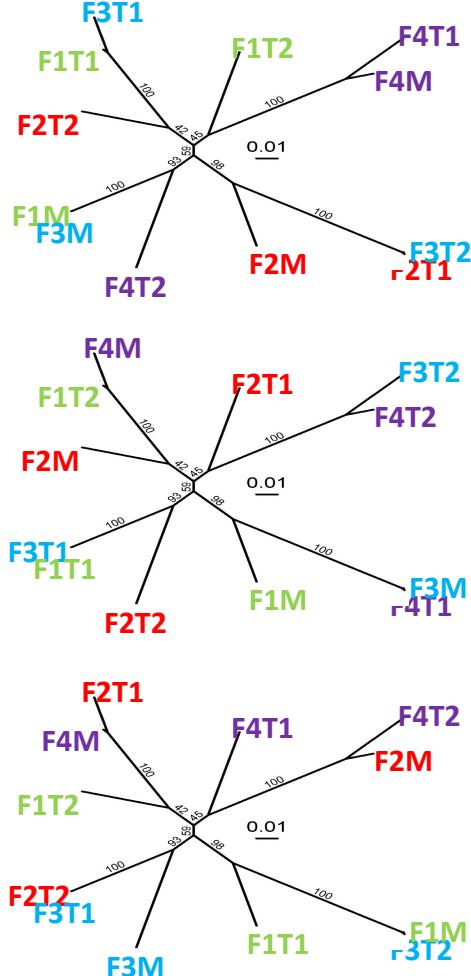
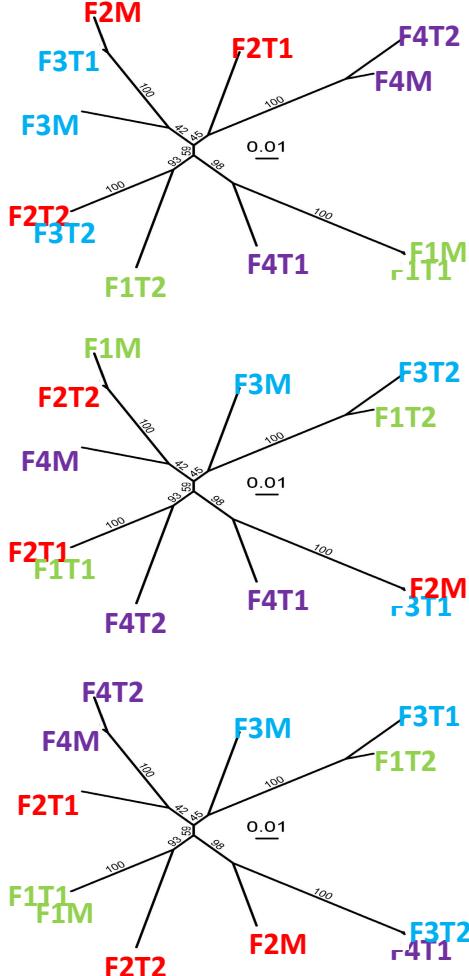
\* or another high number

# First, we need a “score”



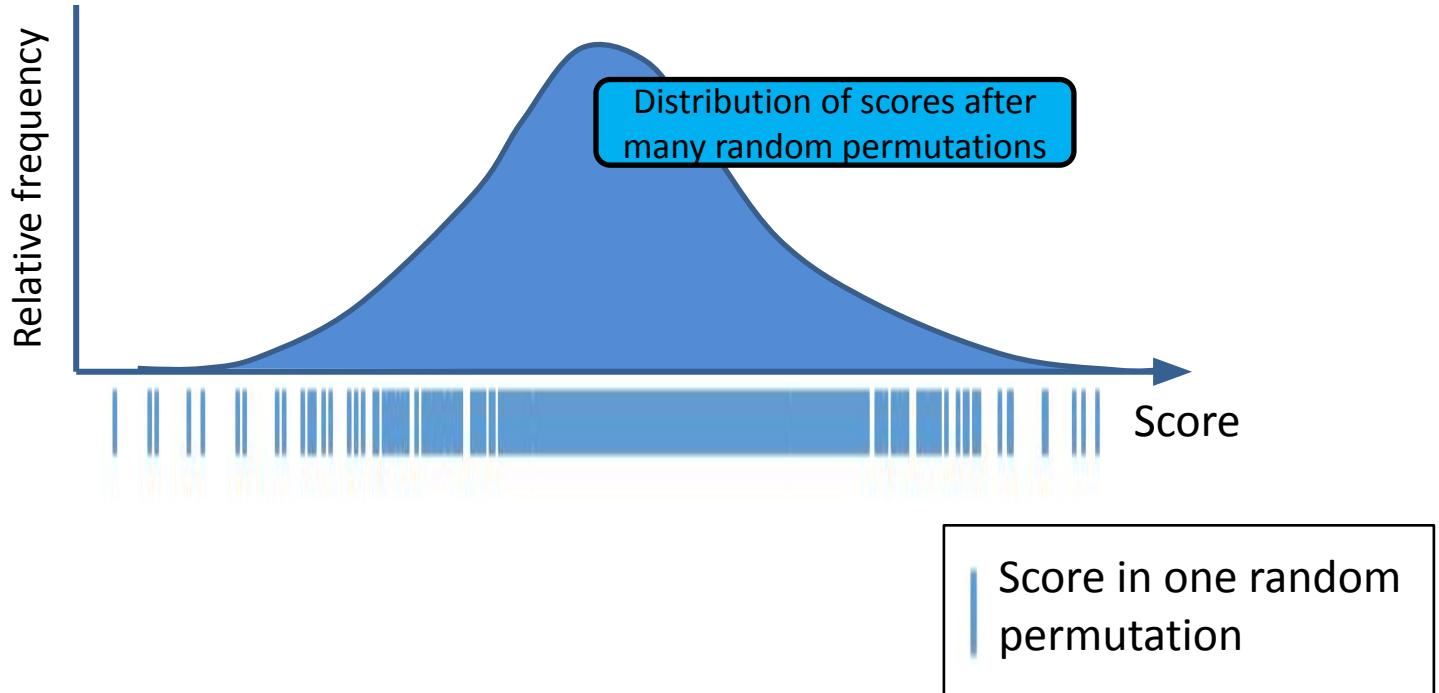
- In our example, the score should register “how well” the family members are clustered
  - For example:
    - The number of leaves whose closest other leaf is from the same family
    - The number of branches that you can break off the tree, that contain only leaves from one family
    - The minimum number of branches you need to switch around before the tree is perfect (reversed)
    - etc...
- This score is known as a “statistic”
  - For some bioinformatic questions, robust statistics have already been developed

# How high is the score by random chance?



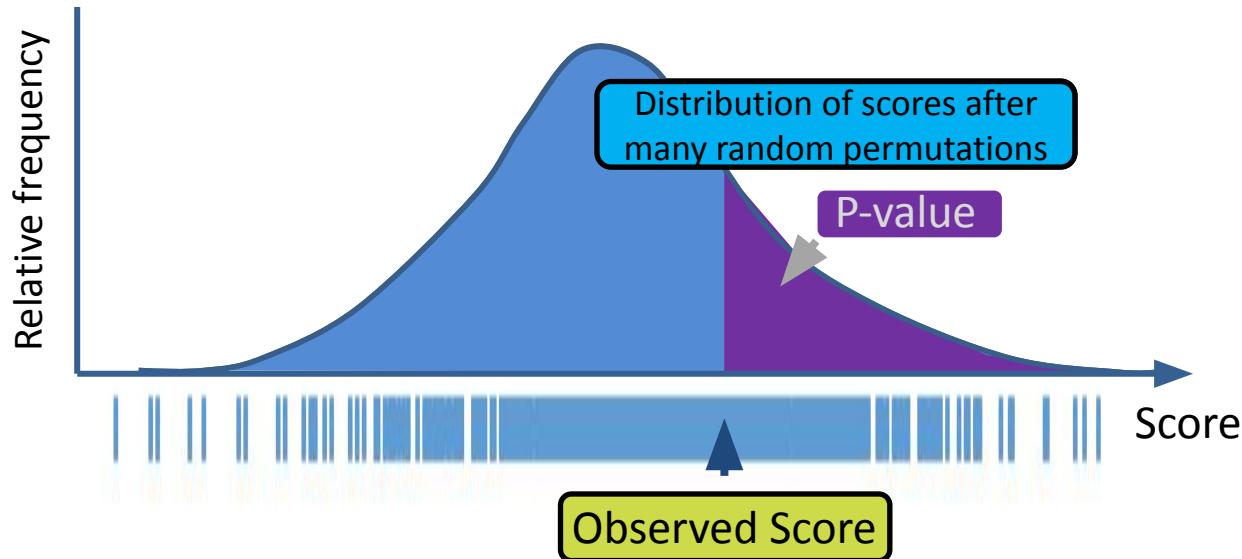
1000x

# How often is every score found?



# Probability value (P-value)

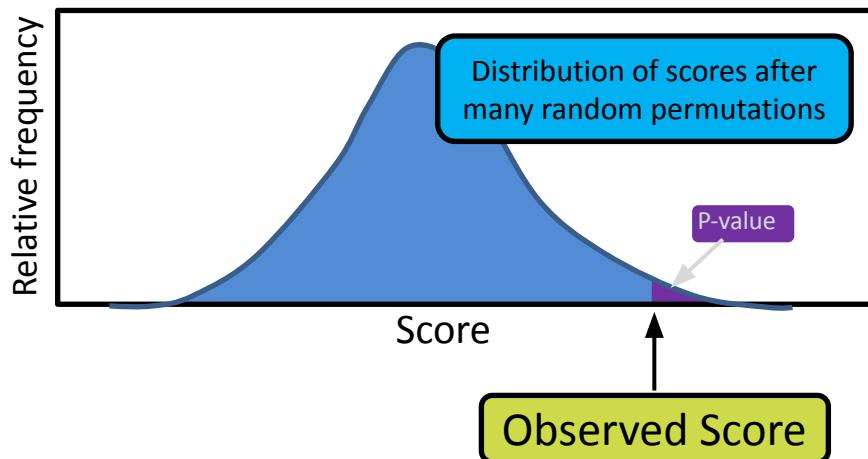
- The P-value is defined as the probability of observing a score as good as, or better than your Observed Score by chance



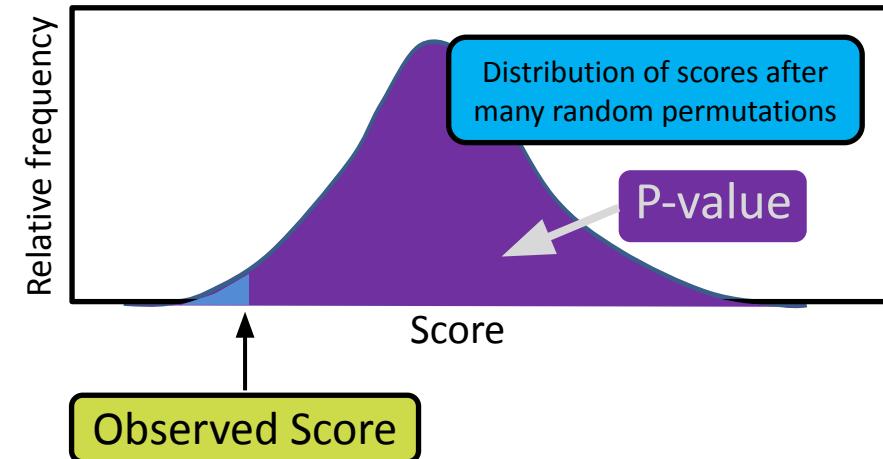
- In permutation statistics, this corresponds to the fraction of times that the permuted score is equal or higher than Your Score

# Permutation statistics (shuffling)

- If the randomly permuted data rarely has a higher score than your **Observed Score**, then the P-value is low, and your observation is **meaningful (significant)**



- If the randomly permuted data often has a higher score than your **Observed Score**, then the P-value is high, and your observation is **not meaningful (not significant)**



## Youtube videos

- CrashCourse, “What is statistics”  
<https://www.youtube.com/watch?v=sxQaBpKfDRk>
- Bozeman science, “Student’s t-test”  
<https://www.youtube.com/watch?v=pTmLQvMM-1M>
- StatQuest, “p-values: What they are and how to interpret them”  
<https://www.youtube.com/watch?v=vemZtEM63GY>
- DATAbab, “Mann-Whitney U test”  
<https://www.youtube.com/watch?v=Twk6lBhBl88>
- StatQuest, “Pearson’s correlation”  
[https://www.youtube.com/watch?v=xZ\\_z8KWkhXE](https://www.youtube.com/watch?v=xZ_z8KWkhXE)
- DATAbab, “Spearman Rank Correlation”  
[https://www.youtube.com/watch?v=XV\\_W1w4Nwoc](https://www.youtube.com/watch?v=XV_W1w4Nwoc)
- StatQuest, “Linear Regression”  
<https://www.youtube.com/watch?v=7ArmBVF2dCs>

## Papers

- Open science collaboration, “Estimating the reproducibility of psychological science”, Science, 2015  
<https://www.science.org/doi/10.1126/science.aac4716>
- Baker 2016, “1,500 scientists lift the lid on reproducibility”, Nature, 2016  
<https://www.nature.com/articles/533452a>

## Other material

- Science fictions links  
<https://www.sciencefictions.org/p/science-fictions-links-for-october>
- Scientific reports, submission guidelines  
<https://www.nature.com/srep/author-instructions/submitting-guidelines>

# How to continue your learning



- **StatQuest with Josh Starmer YouTube channel**

<https://www.youtube.com/@statquest>

- Frequentist statistics
- Short introduction videos on many different topics

- Course “Statistical Rethinking”, by Richard McElreath from MPI Leipzig

[https://github.com/rmcelreath/stat\\_rethinking\\_2024](https://github.com/rmcelreath/stat_rethinking_2024)

- Bayesian statistics
- Chapters 1 - 3: Foundation of Bayesian inference
- Chapter 4: Linear regression
- Chapters 5 - 17: Advanced statistics (including generalized linear models)

- Book (in portuguese): “Introdução à Estatística para Ciência de Dados”, by Tatiana Escovedo, Thiago Marques, Marcos Kalinowski



—  
Thank you!

