

# Astromechanics: gravity

Astronomy 101  
Syracuse University, Fall 2018  
Walter Freeman

October 3, 2019

*“Truth is ever to be found in simplicity, and not in the multiplicity and confusion of things.”*

–Newton, *Rules for methodizing the Apocalypse*  
(n.b.: “apocalypse” also means “revealing”)

*“We are to admit no more causes of natural things than such as are both true and sufficient to explain their appearances.”*

–Newton, *Philosophiae Naturalis Principia Mathematica*  
(Mathematical Principles of Natural Philosophy)

*“What is a neutron star?”*

–Paritosh Jain

A neutron star is what happens when gravity crushes dead stars.

- Stars have a huge mass, and thus have huge amounts of gravity
  - While they burn they are supported against that gravity by the heat coming from their cores
  - Once they run out of fuel, their cores collapse.
- 
- Quantum mechanics limits how tightly you can pack particles together. “*Pauli exclusion principle*”
  - Our Sun, when it dies, will be crushed by its own gravity into a ball of carbon atoms – a white dwarf.
  - The quantum exclusion principle, acting on the electrons in the carbon, holds it up.
  - It will sit there forever, slowly cooling down, unless something else hits it.

A neutron star is what happens when gravity crushes dead stars.

- The exclusion principle, holding up the white dwarf left behind on the Sun, acts more weakly on heavy particles.
- Atoms are made of three kinds of particles...

A neutron star is what happens when gravity crushes dead stars.

- The exclusion principle, holding up the white dwarf left behind on the Sun, acts more weakly on heavy particles.
- Atoms are made of three kinds of particles...
  - Positive protons (heavy!)
  - Neutral neutrons (also heavy!)
  - Negative electrons (2000 times lighter!)

A neutron star is what happens when gravity crushes dead stars.

- The exclusion principle, holding up the white dwarf left behind on the Sun, acts more weakly on heavy particles.
- Atoms are made of three kinds of particles...
  - Positive protons (heavy!)
  - Neutral neutrons (also heavy!)
  - Negative electrons (2000 times lighter!)
- If we could get rid of those pesky electrons, we could crush them even tighter!

A neutron star is what happens when gravity crushes dead stars.

- The exclusion principle, holding up the white dwarf left behind on the Sun, acts more weakly on heavy particles.
- Atoms are made of three kinds of particles...
  - Positive protons (heavy!)
  - Neutral neutrons (also heavy!)
  - Negative electrons (2000 times lighter!)
- If we could get rid of those pesky electrons, we could crush them even tighter!
- If a star is massive enough, its gravity is strong enough to crush positive protons and negative electrons together to make neutrons.
- These can be packed incredibly tightly, since the exclusion principle is weaker.
- They are a hundred million billion times denser than water! ( $10^{17}$ )



Today we're learning about gravity.

We'll see that gravity is stronger for objects with larger mass, and also stronger if you get closer.

A neutron star has an extremely large mass (a little more than the Sun), and since it is so small, you can get very close to it...

Today we're learning about gravity.

We'll see that gravity is stronger for objects with larger mass, and also stronger if you get closer.

A neutron star has an extremely large mass (a little more than the Sun), and since it is so small, you can get very close to it...

... so there should be *extreme gravity* on its surface.

It's about 500 billion times as strong as Earth's!

Today we're learning about gravity.

We'll see that gravity is stronger for objects with larger mass, and also stronger if you get closer.

A neutron star has an extremely large mass (a little more than the Sun), and since it is so small, you can get very close to it...

... so there should be *extreme gravity* on its surface.

It's about 500 billion times as strong as Earth's!

Some pictures:

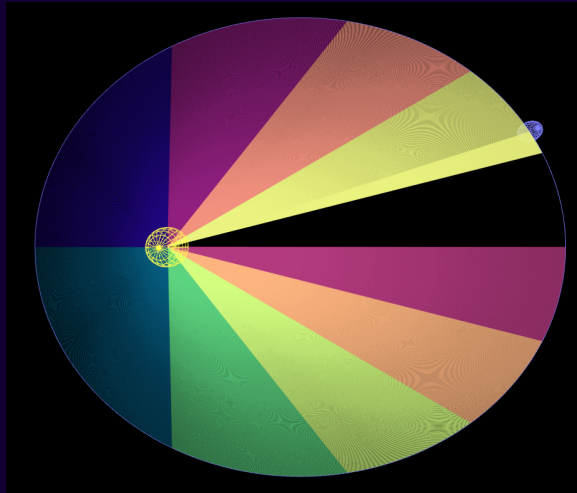
<http://abyss.uoregon.edu/~js/ast122/lectures/lec19.html>

# Kepler's laws, summarized

- 1. Planets travel in elliptical orbits, with the Sun at one focus
- 2. The line going from the Sun to the planet sweeps out equal areas in equal times
- 3. The time that a planet takes to go around the Sun increases as the  $3/2$  power of the long axis of the ellipse.

## Kepler's second law

The line from the Sun to the planet sweeps out equal areas in equal times.



Each colored wedge has the *same area*, and the planet takes the *same time* to go through each.

# Kepler's Third Law

Kepler's third law of orbital motion says that the square of a planet's *orbital period* is proportional to the cube of its *semimajor axis*.

Simply put: if a planet is further from the Sun, it takes longer to go around.

If the distance is doubled, the time required *more than doubles*.

Let's watch this...

Saturn's orbit is about 10 AU across, while Uranus' orbit is about 20 AU across.

Saturn takes about 30 years to orbit the Sun. About how long does Uranus take?

A: About 30 years

B: Between 30 and 60 years

C: More than 60 years

D: It depends on the masses of Uranus and Saturn

Saturn's orbit is about 10 AU across, while Uranus' orbit is about 20 AU across.

Saturn takes about 30 years to orbit the Sun. About how long does Uranus take?

A: About 30 years

B: Between 30 and 60 years

C: More than 60 years

D: It depends on the masses of Uranus and Saturn

E: I looked it up on Wikipedia...



Complete *Lecture Tutorials* pp. 21-24  
(Kepler's second law) and pp. 25-28  
(Kepler's third law).

We will do something else after this (10-15 min)

Do you think Kepler's laws can apply to things other than planets? Why or why not?

Talk about this with your neighbors. Then write what you think on Slack! (If you and your neighbors have the same idea, only send one message, and tag your neighbors.)

# Asking what vs. asking why

Remember, Kepler only discovered *what* the planets' orbits looked like.

He desperately wanted to know *why* they moved in that way, but he never could figure it out.

It turns out that if we can understand *why*, we can understand some other things, too...

# Natural laws vs. their consequences

Obviously the world around us is very diverse. Some things in it look quite simple:

- The motion of the stars
- The near-perfect-spheres of the planets and moons
- The elliptical motions of the planets (?)
- The colors in a rainbow

# Natural laws vs. their consequences

Obviously the world around us is very diverse. Some things in it look quite simple:

- The motion of the stars
- The near-perfect-spheres of the planets and moons
- The elliptical motions of the planets (?)
- The colors in a rainbow

Others, though, are maddeningly complex:

- Seismic waves and earthquakes
- The colors in the Sun
- The weather
- The diversity of rocks on Earth

# Natural laws vs. their consequences

Obviously the world around us is very diverse. Some things in it look quite simple:

- The motion of the stars
- The near-perfect-spheres of the planets and moons
- The elliptical motions of the planets (?)
- The colors in a rainbow

Others, though, are maddeningly complex:

- Seismic waves and earthquakes
- The colors in the Sun
- The weather
- The diversity of rocks on Earth
- Even the simplest living things

# Natural laws vs. their consequences

Obviously the world around us is very diverse. Some things in it look quite simple:

- The motion of the stars
- The near-perfect-spheres of the planets and moons
- The elliptical motions of the planets (?)
- The colors in a rainbow

Others, though, are maddeningly complex:

- Seismic waves and earthquakes
- The colors in the Sun
- The weather
- The diversity of rocks on Earth
- Even the simplest living things
- ... language, culture, music, art, and all the creations of humankind...

# Elegance, revisited

The laws of the Universe are simple and elegant.  
The things the Universe builds out of them are often complex!





# Elegance, revisited

The laws of the Universe are simple and elegant.  
The things the Universe builds out of them are often complex!





Isaac Newton (1642-1727 or 1726) finally figured out the laws that eluded Kepler.

He discovered...

- Forces cause objects to change their speed or direction of motion
- Calculus – the mathematics of changes
- Gravity is such a force
- The mathematical description of gravity



Isaac Newton (1642-1727 or 1726) finally figured out the laws that eluded Kepler.

He discovered...

- Forces cause objects to change their speed or direction of motion
- Calculus – the mathematics of changes
- Gravity is such a force
- The mathematical description of gravity
- Principles of optics
- The mathematics of cooling
- ... and much more

“Forces cause objects to accelerate”

$$F = ma$$

$$F/m = a$$

“The strength of a force, divided by the mass of the thing it acts on,  
gives that thing's acceleration”

# The law of gravity

Newton showed mathematically what Kepler suspected: that “there is a force in the Earth that causes the Moon to move”.

That thing, of course, is gravity.

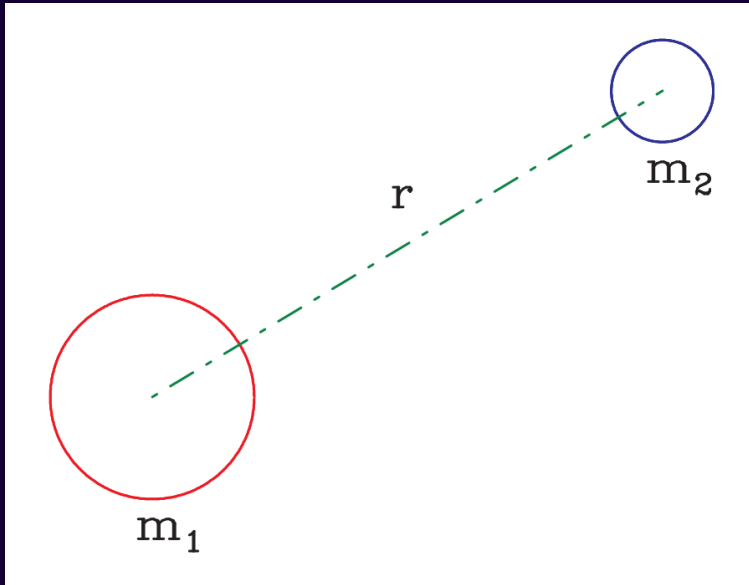
Newton discovered:

All objects attract all other objects with a force that is:

- Proportional to the product of their masses
- Inversely proportional to the distance between their centers, squared

In symbols:

$$F = \frac{Gm_1m_2}{r^2}$$



The gravitational force between these two planets is

$$F_g = \frac{Gm_1m_2}{r^2}.$$

Suppose two asteroids are floating out in space. Asteroid A is twice as massive as asteroid B.

If the force of A's gravity on B is ten tons, the force of B's gravity on A will be...

A: 5 tons

B: 10 tons

C: 20 tons

D: 40 tons

# The law of gravity

All objects attract all other objects with a force that is:

- Proportional to the product of their masses
- Inversely proportional to the distance between them squared

In symbols:

$$F = \frac{Gm_1m_2}{r^2}$$

Notice I didn't say which mass was which. It doesn't matter!



Suppose two asteroids are floating out in space, 20 miles apart. Asteroid A is twice as massive as asteroid B, and the force of A's gravity on B is ten tons.

Suppose I now move the two asteroids closer, so they're only 10 miles apart. What will the force of A's gravity on B be now?

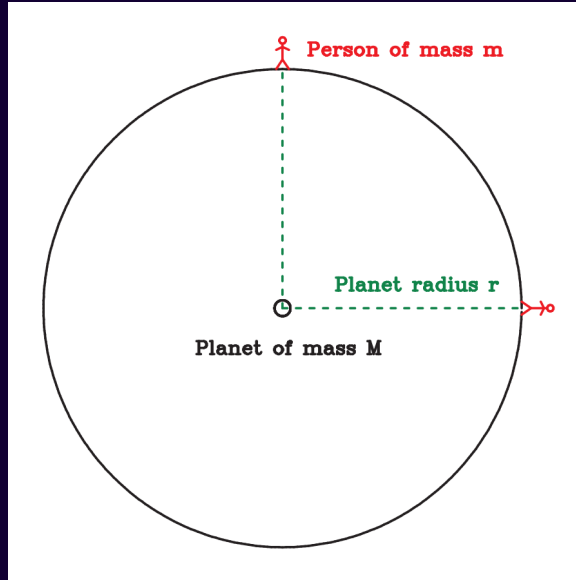
A: 5 tons

B: 10 tons

C: 20 tons

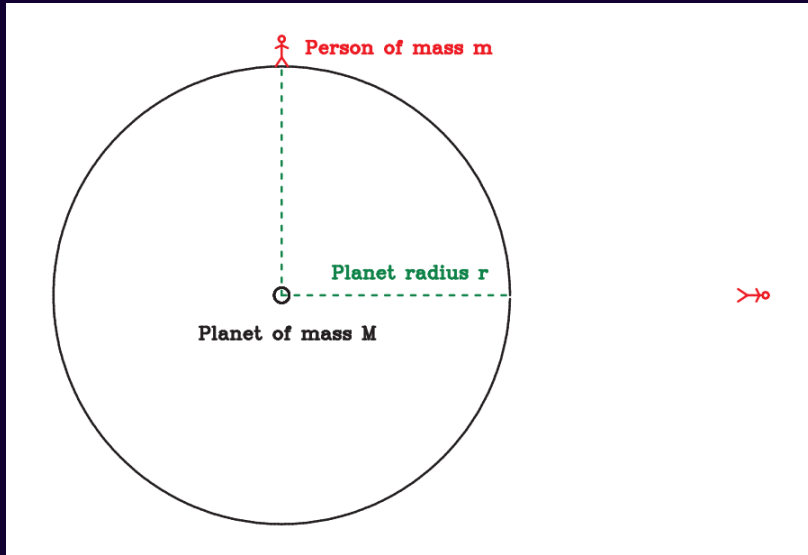
D: 40 tons

The distance is measured between the *centers* of the objects.



This lets you calculate the force of a planet's gravity on people on its surface!

Earth has a radius of about 6,000 km. If we move this person 6,000 km away from Earth's surface, how does the strength of Earth's gravity change?



A: It stays the same

B: It becomes twice as strong

C: It becomes half as strong

D: It becomes one-quarter as strong

E: There's no gravity in space, so it goes away totally