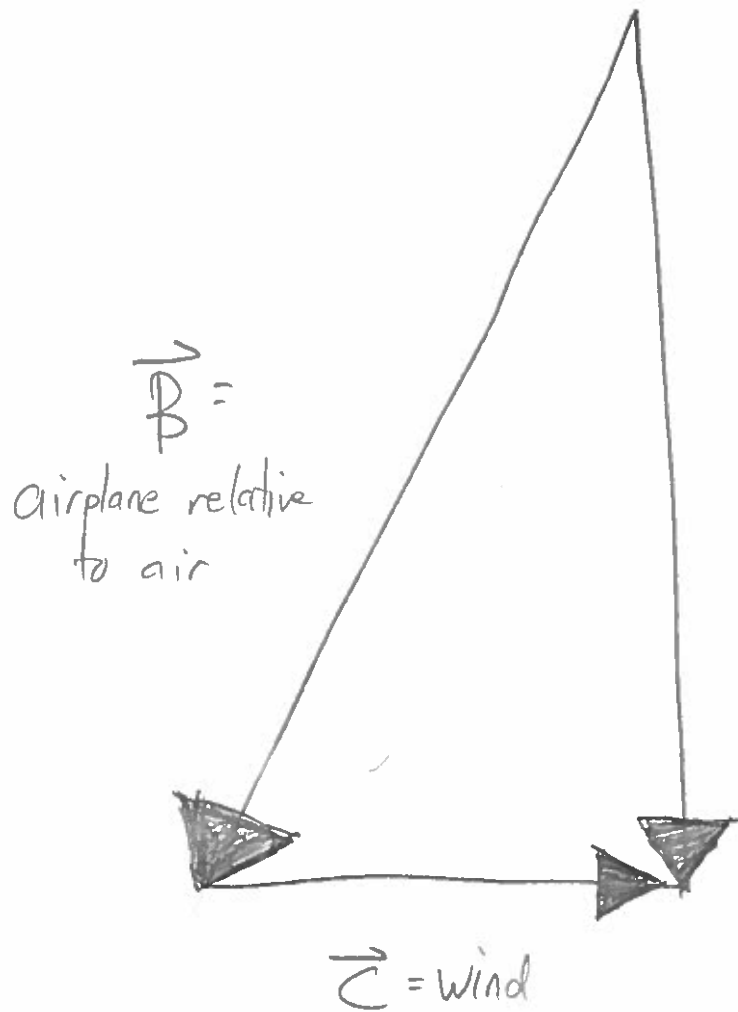


#1 c)



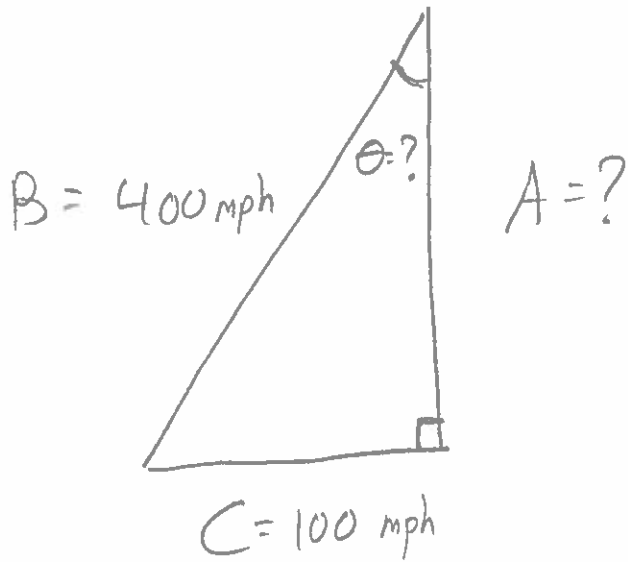
$\vec{A}$  = direction I want  
to go

b)  $\vec{B} + \vec{C} = \vec{A}$

a) I need to angle my plane southwest, so  
once the wind blows me back east, I am going  
south.

d) Now redraw this with numbers:

#1 cont.



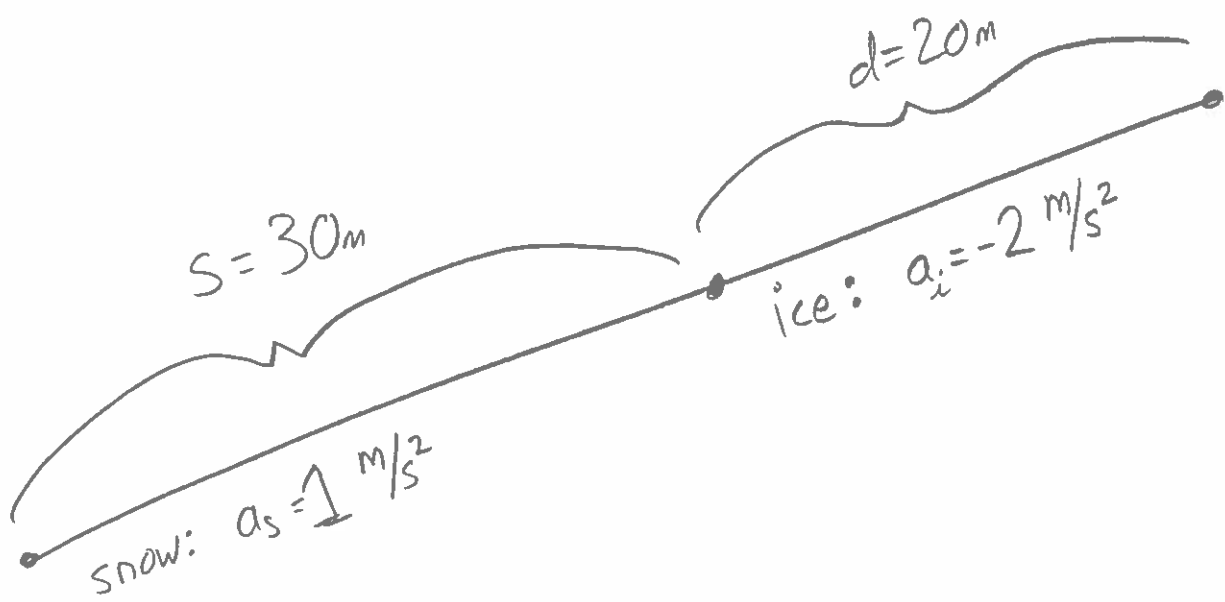
$$\sin \theta = \frac{100 \text{ mph}}{400 \text{ mph}}$$

$$\theta = \arcsin \frac{1}{4} = 22.5^\circ$$

west of south

e) Use Pythagorean theorem:  $A^2 + C^2 = B^2 \rightarrow A^2 = 400^2 - 100^2 = 387 \text{ mph}$ .

$$\text{time} = \frac{\text{distance}}{\text{speed}} = \frac{300 \text{ miles}}{387 \text{ mi/hr}} = 0.78 \text{ hr.}$$



a) "What is  $v$  at the time that  $x = s$ ?"

→ On the snow,  $x = \frac{1}{2}a_s t^2$   
 $v = a_s t$

- Find time that  $x = s$ :  $t = \sqrt{\frac{2s}{a_s}}$
- Find  $v$  at that time:  $v = a_s \sqrt{\frac{2s}{a_s}} = \sqrt{2s a_s}$ .

or use "third kinematics equation":

$$v_f^2 - v_0^2 = 2a_s(x_f - x_0) \rightarrow v_f = \sqrt{2a_s s} = 7.7\text{ m/s}.$$

b) "At what time is  $x = d$ ?"

(using a second set of constant-accel kinematics)

$$x = \frac{1}{2}a_i t^2 + \sqrt{2a_s s} t$$

$$v = a_i t + \sqrt{2a_s s} \leftarrow \text{don't actually need this one}$$



#2 cont'

Set  $x=d$  and solve for  $t$ :

$$d = \frac{1}{2} a_i t^2 + \sqrt{2a_s s} t$$

$$0 = \frac{1}{2} (-2 \text{ m/s}^2) t^2 + (7.74 \text{ m/s}) t - 20 \text{ m}$$

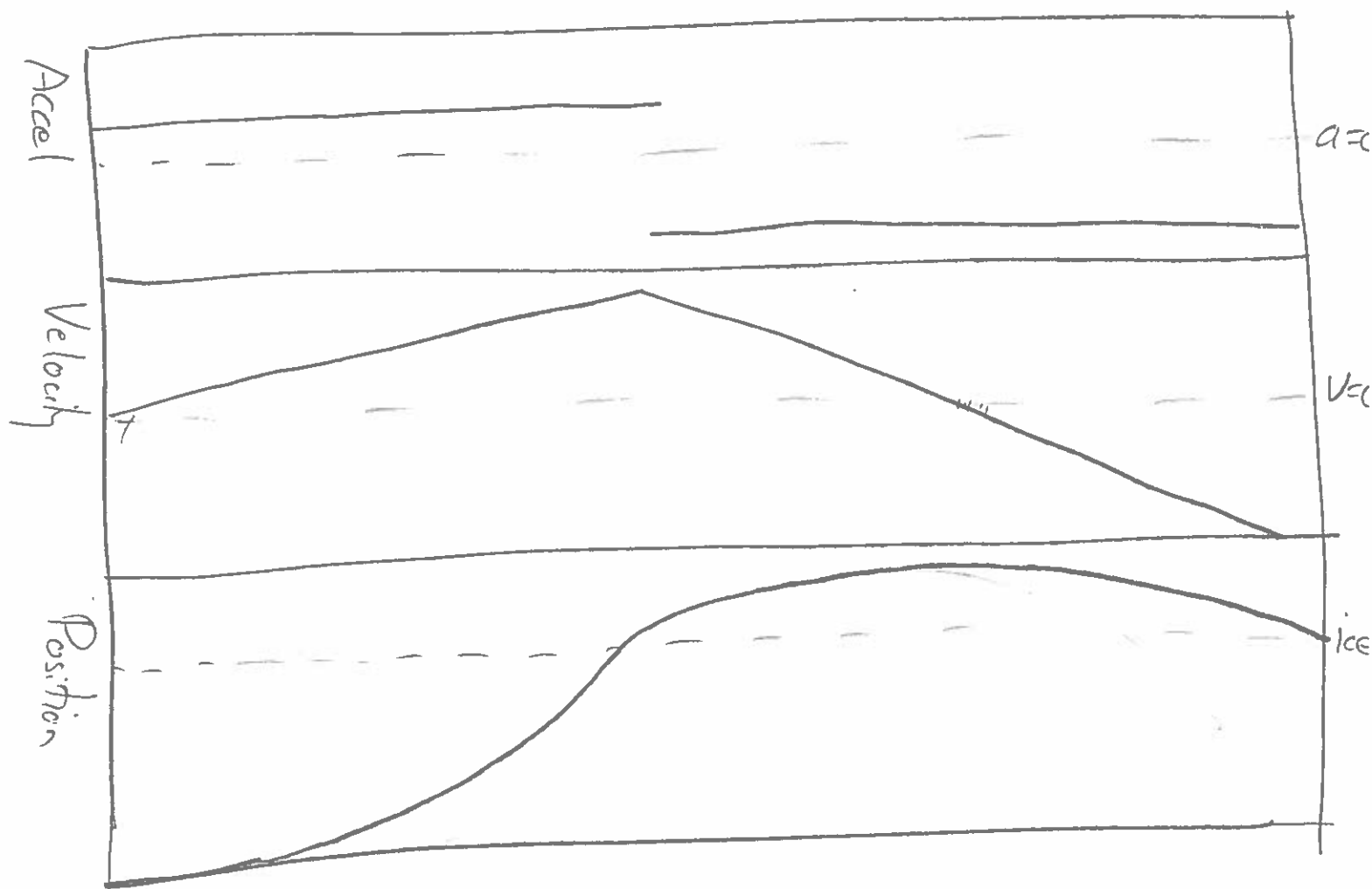
$-1 \text{ m/s}^2$

Quadratic formula:

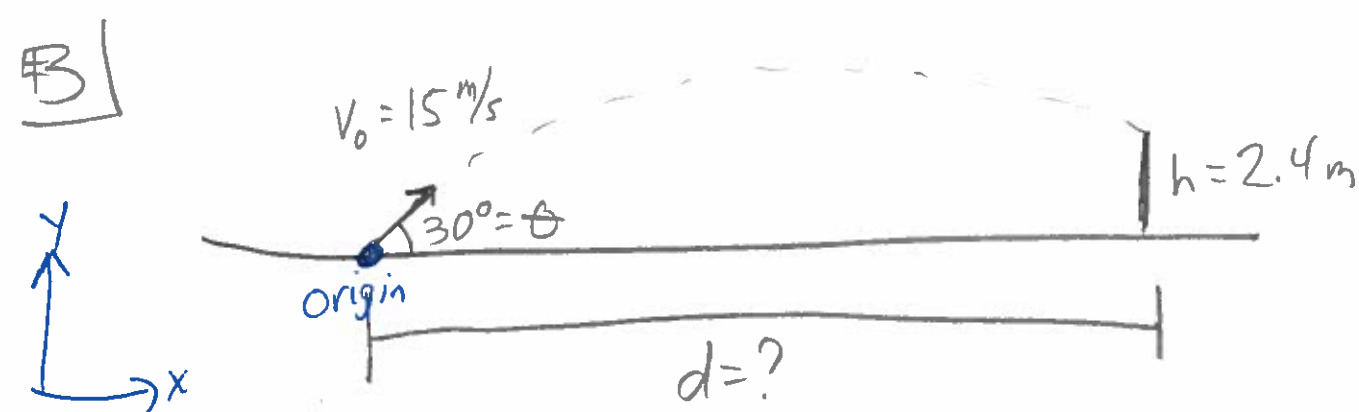
$$t = \frac{-7.74 \pm \sqrt{59.9 - 80}}{-2}$$

← answer is imaginary.

Driver is sad. ;)







a)  $x(t) = (v_0 \cos \theta) t$   
 $y(t) = (v_0 \sin \theta) t - \frac{1}{2} g t^2$

b) "What time is  $y = h$ ?"

$$h = (v_0 \sin \theta) t - \frac{1}{2} g t^2 \rightarrow \frac{1}{2} g t^2 - (v_0 \sin \theta) t + h = 0$$

$$t = \frac{v_0 \sin \theta \pm \sqrt{v_0^2 \sin^2 \theta - 2gh}}{g}$$

b and c): The ball hits the crossbar on the way back down according to the picture.

That corresponds to the  $+$  sign. The  $-$  sign gives you the earlier time the ball was at that height.

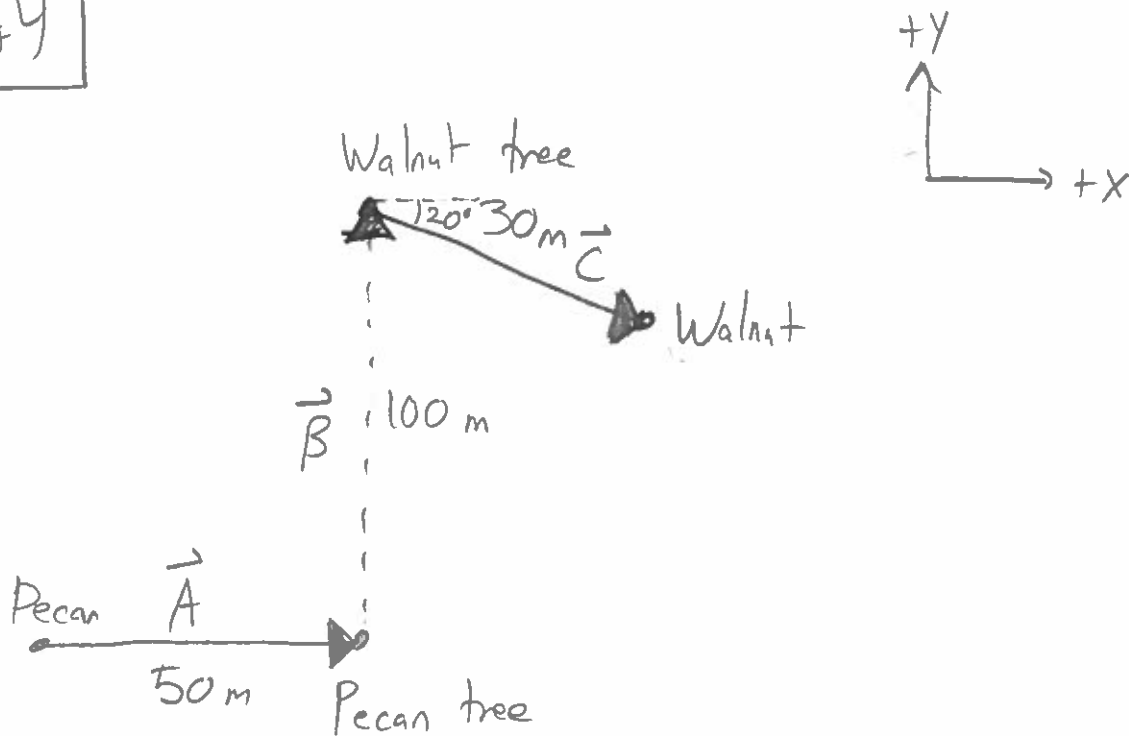
d) Find  $x(t)$  at that time:

$$d = (v_0 \cos \theta) t = v_0 \cos \theta \frac{v_0 \sin \theta + \sqrt{v_0^2 \sin^2 \theta - 2gh}}{g}$$





#4



$$\vec{A} = (50, 0)$$

$$\vec{B} = (0, 100)$$

$$\vec{C} = (30 \cos 20^\circ, -30 \sin 20^\circ)$$

$$\text{Pecan to walnut} = \vec{A} + \vec{B} + \vec{C} = (50 + 30 \cos 20^\circ, 100 - 30 \sin 20^\circ)$$

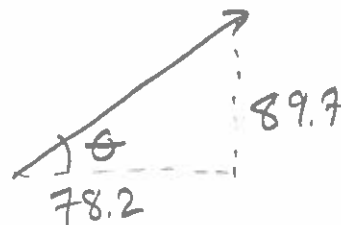
$$= (78.2, 89.7)$$

a)

Use Pythagorean theorem to find magnitude of  $(\vec{A} + \vec{B} + \vec{C})$

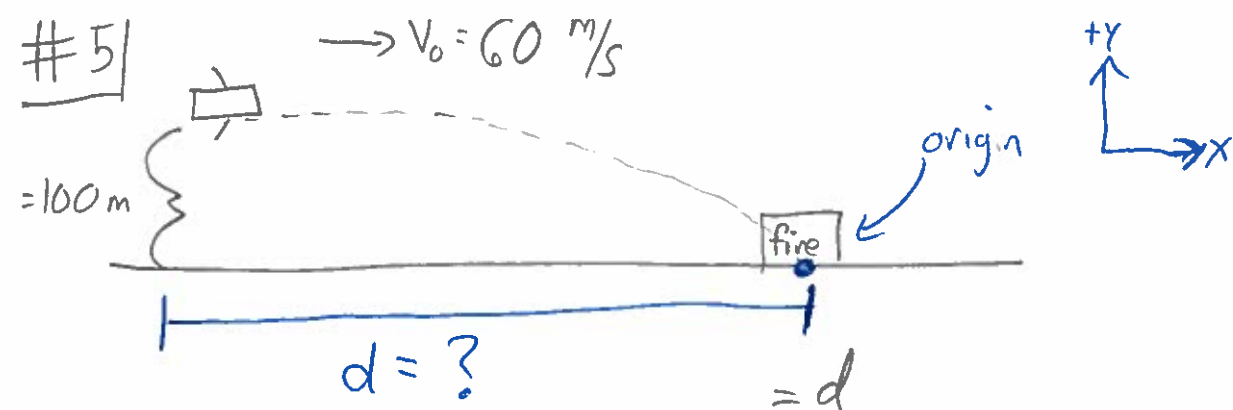
$$= \sqrt{78.2^2 + 89.7^2} = 119 \text{ m.}$$

b) Find direction of that vector:



$$\theta = 48.9^\circ \text{ north of east}$$





a) "What value of  $x_0$  makes it so that  $x=0$  at the same time that  $y=0$ ?"

$$\begin{cases} x(t) = V_0 t - d \\ y(t) = h - \frac{1}{2}gt^2 \end{cases} \quad \begin{cases} V_x(t) = V_0 \\ V_y(t) = -gt \end{cases}$$

$$0 = V_0 t - d$$

$$0 = h - \frac{1}{2}gt^2 \Rightarrow t = \sqrt{\frac{2h}{g}}$$

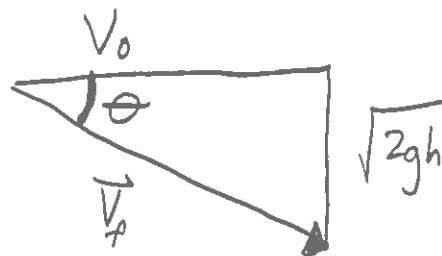
Substitute:

$$d = V_0 \sqrt{\frac{2h}{g}} = 271 \text{ m.}$$

b) "What is the direction of  $\vec{v}$  at the time  $y=0$ ?"

$$V_x = V_0 \quad V_y = -g\sqrt{\frac{2h}{g}} = -\sqrt{2gh}$$

$$\tan \theta = \frac{\sqrt{2gh}}{V_0} ; \theta = \tan^{-1} \frac{\sqrt{2gh}}{V_0}$$



$$\theta = 36.4 \text{ degrees below horizontal}$$

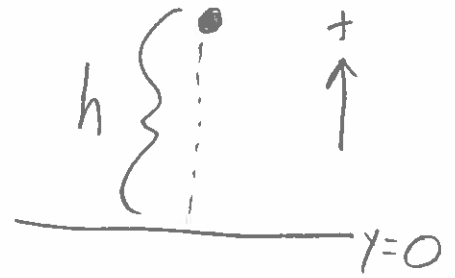
5 cont.

Directly above. The sand accelerates downward, but this doesn't affect its horizontal motion; in the x-direction it continues moving at the same rate as the plane.

#6] a) This is just freefall in one dimension from rest.

$$y(t) = -\frac{1}{2}gt^2 + h$$

"When is  $y=0$ ?"  $\Rightarrow 0 = -\frac{1}{2}gt^2 + h$   
 $\Rightarrow t = \sqrt{2h/g}$



b) "What is  $v$  at the time when  $y=0$ ?"

$$v(t) = v_0 - gt \rightarrow v = -g\sqrt{2h/g} = -\sqrt{2gh}$$

c) After bounce, need a new "set" of kinematics relations, with  $V_0 = -\frac{1}{2}V_f$  from the previous phase:  $\frac{\sqrt{2gh}}{2} = \sqrt{\frac{2gh}{4}} = \sqrt{\frac{gh}{2}}$ .

So:

$$y(t) = -\frac{1}{2}gt^2 + \sqrt{\frac{gh}{2}}t \quad \text{and} \quad v(t) = -gt + \sqrt{\frac{gh}{2}}$$

Highest point happens at the time  $v=0$ :

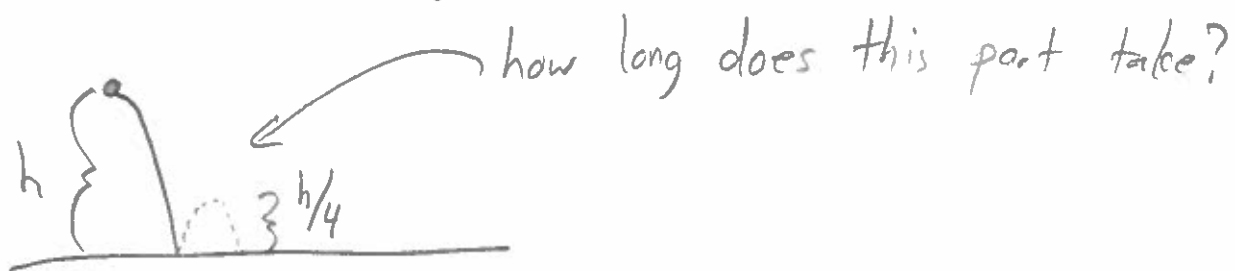
$$0 = -gt + \sqrt{\frac{gh}{2}} \rightarrow t = \sqrt{\frac{h}{2g}}$$

Height at that time:

$$y(t) = -\frac{1}{2}g\left[\frac{h}{2g}\right] + \sqrt{\frac{gh}{2}}\sqrt{\frac{h}{2g}} = -\frac{1}{4}h + \frac{1}{2}h = \frac{1}{4}h$$

#6  
cont.

d) We have time from first drop to hitting ground the first time — now we need how long it takes to land again.

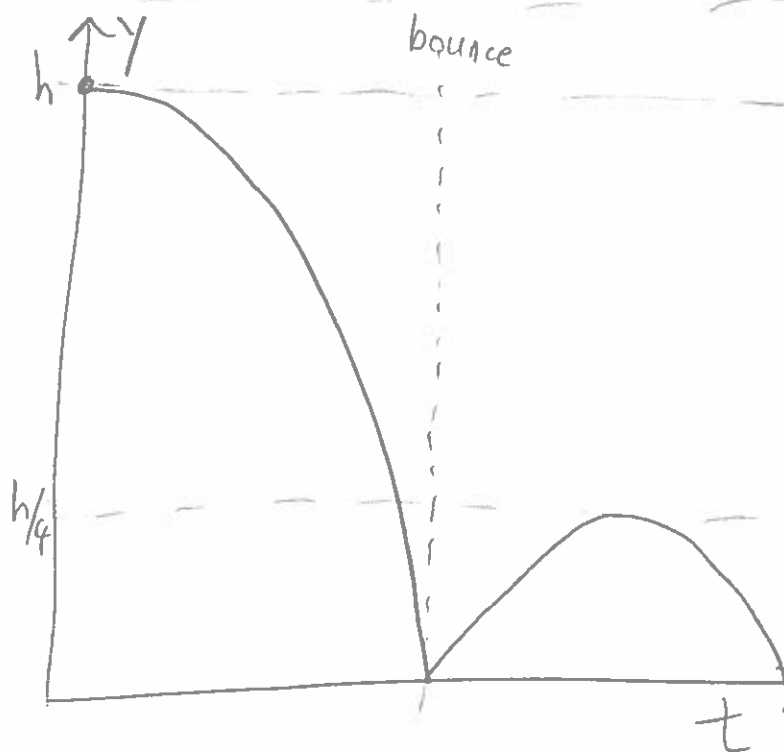
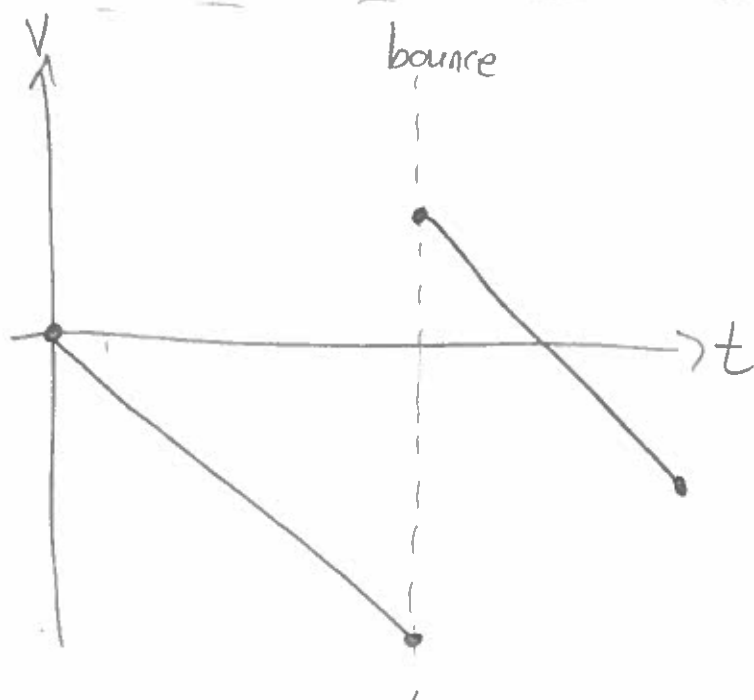


"What is  $t$  when  $y=0$ ?" (again)

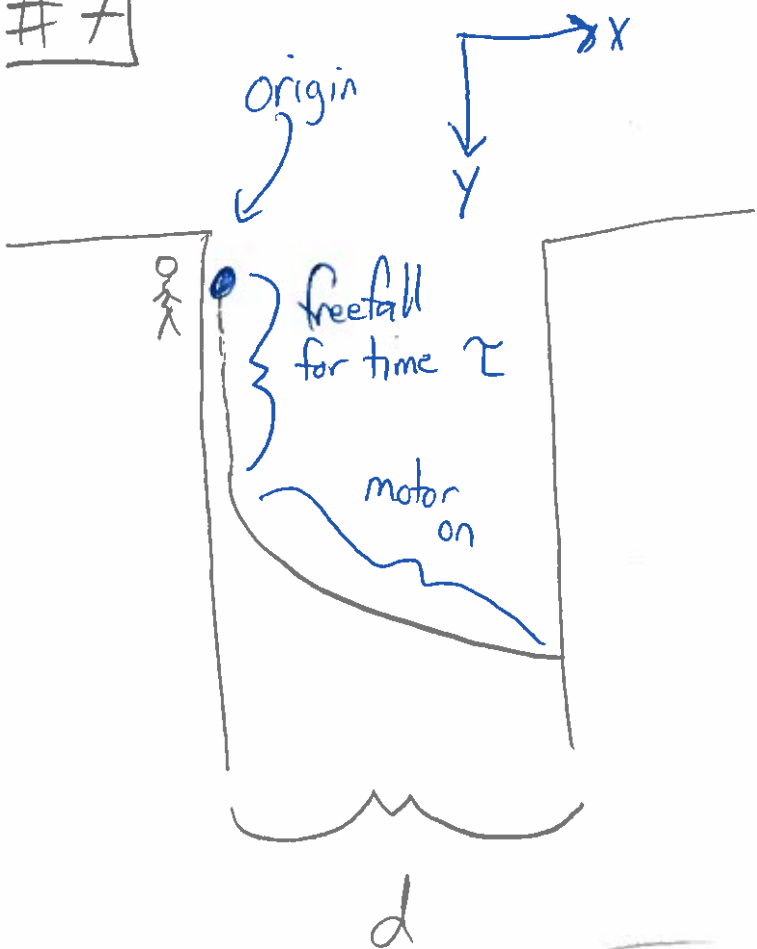
$$y(t) = -\frac{1}{2}gt^2 + \sqrt{\frac{gh}{2}}t = 0 \quad \text{factor this}$$

$$\Rightarrow t = \left(\frac{2}{g}\right)\left(\sqrt{\frac{gh}{2}}\right) = \sqrt{\left(\frac{4}{g^2}\right)\left(\frac{gh}{2}\right)} = \sqrt{\frac{2h}{g}}$$

• Total is the sum of this time plus the time to hit the first time:  $t_{\text{total}} = \sqrt{\frac{2h}{g}} + \sqrt{\frac{2h}{g}} = 2\sqrt{\frac{2h}{g}}$ .



#7



a) Before the rocket fires, it is in freefall:

$$y(t) = \frac{1}{2}gt^2$$

→  $\frac{1}{2}g\tau^2$  below the window

$$v_y(t) = gt$$

→ velocity of  $g\tau$  in the y-direction and 0 in x

b) After motor is fired:

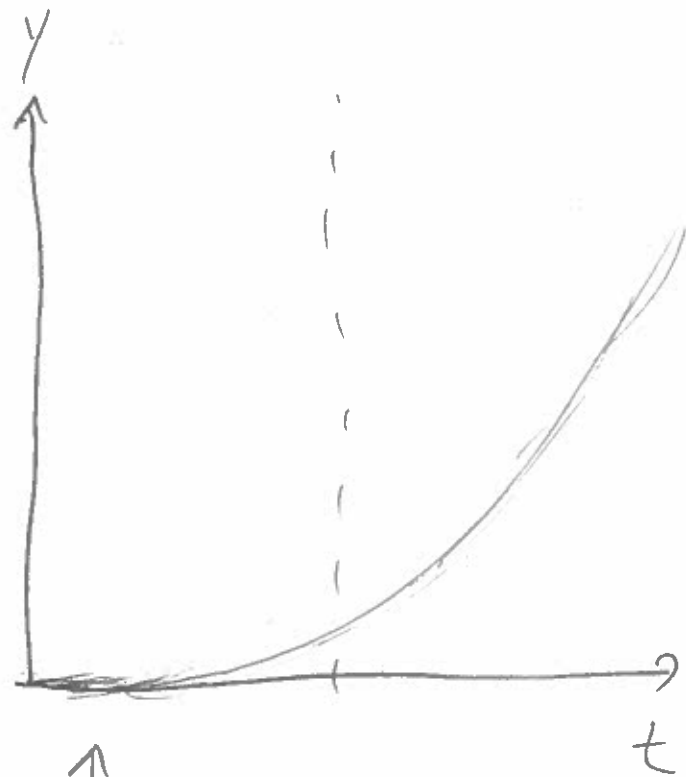
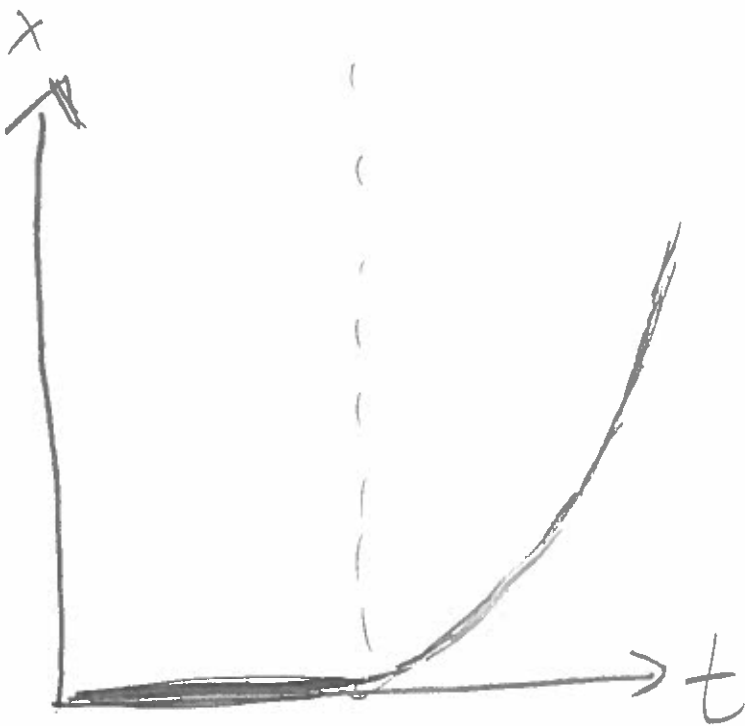
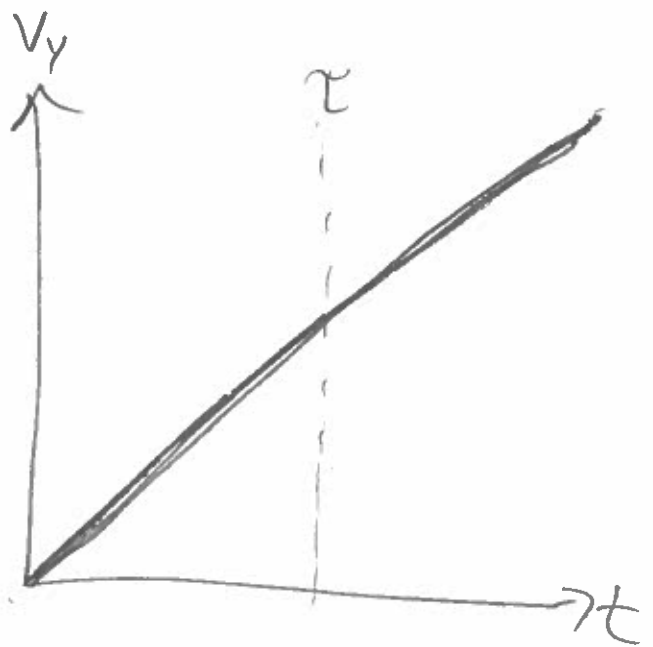
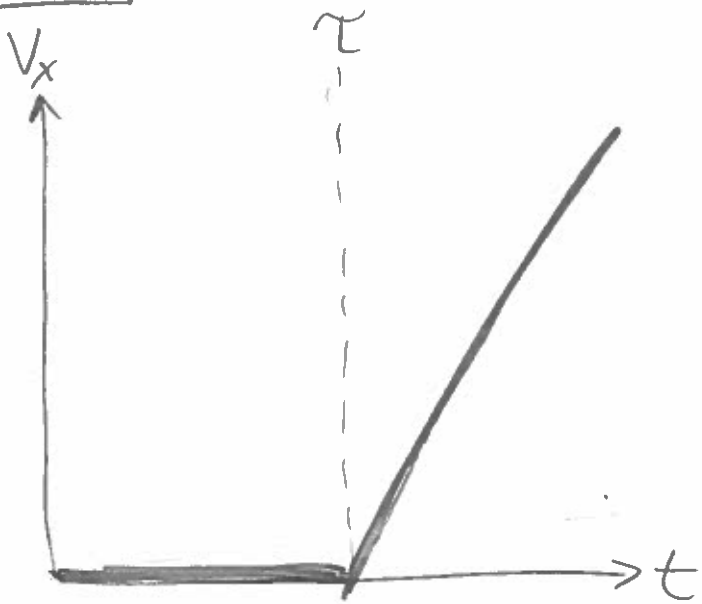
$$x(t) = \frac{1}{2}(2g)t^2$$

Rocket hits building when  $x(t) = d \rightarrow d = gt^2$ ,  $\tau_2$

so it hits the building a time  $\tau_2 = \sqrt{d/g}$  after motor fires

So the total time in the air is  $\tau + \tau_2 = \tau + \sqrt{d/g}$

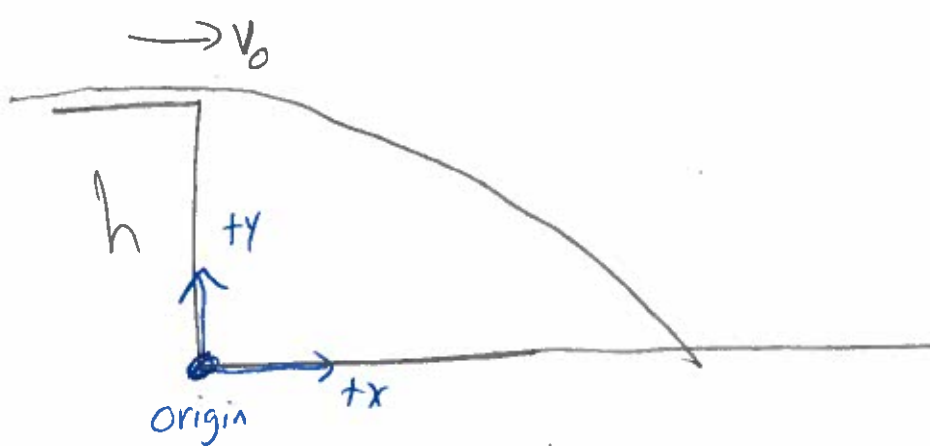
7 cont.



note: remember down  
is positive



#8



a) "What is the time when  $y=0$ ?"

$$y = h - \frac{1}{2}gt^2 \rightarrow 0 = h - \frac{1}{2}gt^2 \Rightarrow t = \sqrt{\frac{2h}{g}}.$$

b) "What is  $x$  at that time?"

$$x = v_0 t \rightarrow x = v_0 \sqrt{\frac{2h}{g}}.$$

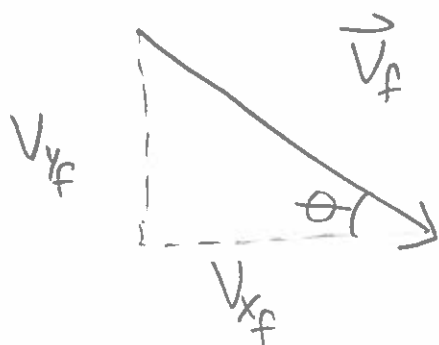
c) Find magnitude of  $\vec{v}$  at that time.

$$\bullet v_x = v_0$$

$$\bullet v_y = -gt \rightarrow \text{at floor, } v_y = -\sqrt{2gh}$$

$$\text{Magnitude} = \sqrt{v_x^2 + v_y^2} = \sqrt{v_0^2 + 2gh}$$

d) Find direction of  $\vec{v}$ :



$$\theta = \tan^{-1} \frac{v_{yf}}{v_{xf}} = \tan^{-1} \frac{\sqrt{2gh}}{v_0}$$

below the horizontal

#8 cont.

e) Now I need to decompose the initial velocity vector into x- and y-components, and

$$V_x = V_0 \cos \theta, \quad V_y = V_0 \sin \theta.$$

Nothing else changes in the approach.