

# RECITATION QUESTIONS – ANGULAR MOMENTUM

APRIL 9

Recall that the angular momentum  $L$  of an object can be found two ways:

$$L = I\omega \text{ (an object rotating around its center)}$$

or

$$L = mv_{\perp}r = mvr_{\perp} \text{ (a separate object moving past an object that can rotate)}$$

- Consider the demo you saw in class: a person stands on a platform that is free to rotate. You can approximate the person as a cylinder (with radius  $r_p$  and mass  $m_p$ ) in calculating their moment of inertia. Someone hands the person a horizontal bicycle wheel of radius  $r_w$  of mass  $m_w$  that is rotating rapidly around its vertical axis at angular velocity  $\omega_0$ .
  - When the person turns the bicycle wheel over (so it is rotating counterclockwise as seen from above rather than clockwise, for instance), how quickly and in which direction will they begin to rotate?
  - In class, the bicycle wheel was filled with concrete; its mass was likely around  $m_w = 5$  kg. Estimate  $r_p$  and  $m_p$  for an average person, and estimate  $r_w$ . Is your result for the final angular velocity of the person reasonable?
- We return to our astronaut using a jet pack to maneuver in space.

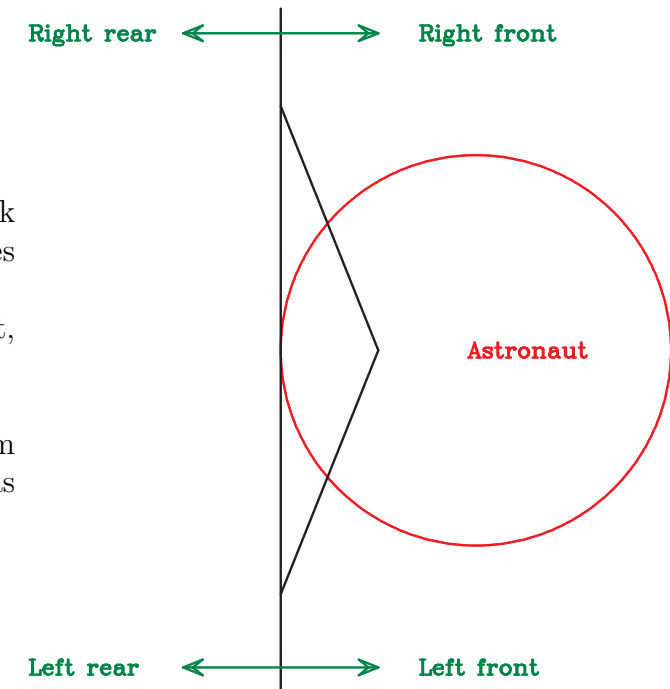
Several engineers are debating how to design this jet pack:

Alex: We're making a rocket, right? We just need one jet that can spit out gas. Let's build a backpack and put the gas exhaust in the middle of the astronaut's back. Gas comes out their back, astronaut goes forward, easy!

Beth: Don't do that – then they can't go backwards! We need to put one in the back and one in the front, one behind their back pointing backwards and one in front of their stomach pointing forwards.

Charlie: Wait. Don't we need them to be able to turn around, too?

They settle on this design – a backpack worn by the astronaut with a horizontal bar sticking out from their hips, with four thrusters on the ends of the bar. These thrusters are capable of emitting puffs of gas at 300 m/s.



- Why does this design need *four* thrusters, off center, to allow the astronaut to maneuver? (*Reference the conservation of angular momentum in your explanation.*)
  - If the astronaut wishes to accelerate forward, which thrusters should they fire?
  - If the astronaut fires the left rear thruster by itself, how will their velocity change? What about their angular velocity?
  - Suppose the astronaut doesn't want to accelerate, but just wants to generate a clockwise angular velocity. Which thrusters should they fire?
- An astronaut wearing this design of jetpack is floating in space, conducting a repair on a satellite, when someone throws them a 20 kg tool at 1 m/s. However, they throw it to the side; the astronaut must reach their arm one meter to the left to catch the tool.

- (a) Explain why the astronaut begins to rotate after they catch the tool.
- (b) What will the astronaut's angular velocity and what will their velocity be after they catch it?
- (c) If the astronaut has a mass of 200 kg, and their mass distribution can be approximated by a cylinder of radius 20 cm, how fast will they be rotating?
- (d) They would like to use this jetpack to stop themselves from rotating. Which thrusters should they fire, and how much gas should they release from each one?
- (e) What will their velocity be after this maneuver? What should the astronaut do if they want to reduce their velocity back to zero?