

Energy methods – problem solving

Physics 211
Syracuse University, Physics 211 Spring 2015
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Announcements

- Mastering Physics due Monday
- If your exam was misgraded, grade appeals will be handled the same way as before (and faster!)

Where we've been, where we're going

- Last time: we saw that “potential energy” is both a statement about nature and a bookkeeping trick to keep track of work
 - Potential energy only applies to conservative forces (gravity, springs)
 - Lets us account for the work done by these forces with no integrals required
 - Potential energy due to Earth's gravity: $U_g = mgy$
 - Potential energy due to universal gravity: $U_G = -\frac{GMm}{r}$
 - Potential energy in a spring: $U_e = \frac{1}{2}k(\Delta x)^2$
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- This time: we'll introduce the idea of **power**, a rate of doing work
- ... then we'll spend most of today just doing practice problems.

- We've been concerned with quite a few “rates” in this class:
 - Velocity: the rate of changing position, measured in meters per second
 - Angular velocity: the rate of changing angle, measured in radians per second
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- This quantity is called **power**
- It's measured in joules per second: $1 \text{ J/s} = 1 \text{ watt}$

When does this idea of a rate of transferring energy or doing work come up?

- Rates of energy transfer: “Sunlight delivers about 1000 watts per square meter to the ground”
- Rates of energy “consumption”: “My laptop uses about 20 watts of power”
- Rates of doing work: “This car’s engine can put out 75 kW of power”

Most of our ideas here are stepping stones to understanding something else.

The idea of power is more of a standalone concept: a useful application.

Many of our machines are limited by the **rate** that they can convert energy from one form to another.

Power: rate of doing work

A bit of mathematics that will be useful to you:

“An object moves at a constant speed \vec{v} , subject to some force \vec{F} ; at what rate does that force do work on the object?”

An example: an airplane flies at $v=1000$ m/s, and its engines exert $F=300$ kN of thrust. What is the rate at which the engines do work (power)?

$$\text{Work} = \text{force} \times \text{distance}$$

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$$P = \vec{F} \cdot \vec{v} = 300\text{MW}$$

- The engines output 300 MW of power: this is around 10 liters per second of fuel even at 100% efficiency!
- Some of that 300 MW of energy dissipated by drag heats up the airplane...

Sample problems

A truck pulling a heavy load with mass $m = 4000$ kg wants to drive up a hill at a 30° grade.

If the truck's engine can produce 100 kW of power (134 hp), how fast can the truck go? (Neglect drag.)

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At low speeds: static friction limits acceleration

At high speeds: engine power limits acceleration

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$$\frac{1}{2}mv_0^2 - \frac{GMm}{r} = 0$$

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How can I “cheat” here?

42. || A 1000 kg elevator accelerates upward at 1.0 m/s^2 for 10 m, starting from rest.
- How much work does gravity do on the elevator?
 - How much work does the tension in the elevator cable do on the elevator?
 - Use the work-kinetic energy theorem to find the kinetic energy of the elevator as it reaches 10 m.
 - What is the speed of the elevator as it reaches 10 m?

Sample problems

57. || The spring shown in **FIGURE P11.57** is compressed 50 cm and used to launch a 100 kg physics student. The track is frictionless until it starts up the incline. The student's coefficient of kinetic friction on the 30° incline is 0.15.
- What is the student's speed just after losing contact with the spring?
 - How far up the incline does the student go?

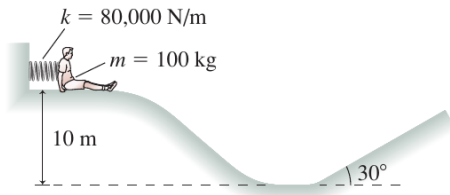


FIGURE P11.57

49. || Truck brakes can fail if they get too hot. In some mountainous areas, ramps of loose gravel are constructed to stop runaway trucks that have lost their brakes. The combination of a slight upward slope and a large coefficient of rolling resistance as the truck tires sink into the gravel brings the truck safely to a halt. Suppose a gravel ramp slopes upward at 6.0° and the coefficient of rolling friction is 0.40. Use work and energy to find the length of a ramp that will stop a 15,000 kg truck that enters the ramp at 35 m/s (≈ 75 mph).