RECITATION EXERCISES APRIL 15

1.	Formula One race cars use a "kinetic energy recovery system" that stores energy in rapidly spinning
	wheels, called flywheels. When the car slows down to make a turn, the car couples the flywheel to
	the transmission; it begins to spin rapidly, storing some of the car's translational kinetic energy in
	its rotation. One type of these systems uses a flywheel of mass $m=5$ kg and radius $r=12$ cm that
	rotates at up to 60,000 revolutions/minute.

You can model the flywheel as a uniform cylinder $(I = \frac{1}{2}mr^2)$.

a) What is its angular velocity in radians per second?

b) How much energy does it store when rotating at full speed?

- c) Suppose the wheel is only spinning at half speed (30,000 rpm). What fraction of its maximum energy does it store? (You should be able to answer this without a calculator. If you are not sure how, ask your instructors for advice.)
- d) When the car accelerates again, this system uses the rotational energy stored in the flywheel to supplement the engine power. If the system provides 100 kW of extra power, how many seconds of "boost power" can the system deliver before it is out of energy?

2. As we did in class, consider rolling different objects down a slope of height h. In this exercise, you will determine how fast they are moving (their final speed v) when they reach the bottom.

First, consider a solid cylinder of mass m and radius r.

For each of the following, your group should guess whether it will be moving faster, slower, or the same speed than the original cylinder when it reaches the bottom. You haven't done any calculations yet, so you may not know for sure – that's okay! Record the result you expect and a brief reason why.

- A more massive solid cylinder of mass 2m with the same radius r
- A larger solid cylinder with the same mass m, but with radius 2r
- A hollow cylinder, also of mass m and radius r
- \bullet A solid sphere, also of mass m and radius r

Now, we'll calculate how fast each of them go down the slope. First, consider a hollow cylinder rolling down the slope. As it rolls, its potential energy at the top is converted into kinetic energy. You may write things in terms of g, m, r, h, etc. here; we don't have any numbers.

- (a) What is its total energy at the top of the slope?
- (b) What is its total energy at the bottom of the slope? (Hint: What kinds of energy does it have there?)
- (c) If you set these two expressions for the total energy equal (since no other force does work here, and since energy is conserved), you will arrive at an equation that you could solve for v, the speed that the ball is moving at the bottom. However, it has another unknown in it: ω , the rate at which it is rotating.

However, the ball is rolling without slipping. What condition relates v to ω if the ball rolls without slipping?



- (e) Here's our list of objects again.
 - ullet A solid cylinder of mass m and radius r
 - A more massive solid cylinder of mass 2m with the same radius r
 - A larger solid cylinder with the same mass m, but with radius 2r
 - \bullet A hollow cylinder, also of mass m and radius r
 - ullet A solid sphere, also of mass m and radius r

Rank them in order of how quickly they'll be moving when they reach the bottom of the ramp. Think about which quantities (m, r, and the shape) appear in your formula and which don't.

3. In the previous exercise, you arrived at a formula for v_f in terms of g, h, and λ .

Suppose that you have some other ramp. You observe that when you roll a hollow sphere down it, it's traveling at 1 m/s. How fast would a solid sphere be traveling? (You do have enough information to provide a number here, even though you don't know m, g, h, or r.)

TABLE 12.2 Moments of inertia of objects with uniform density

Object and axis	Picture	I	Object and axis	Picture	I
Thin rod, about center		$\frac{1}{12}ML^2$	Cylinder or disk, about center	R	$\frac{1}{2}MR^2$
Thin rod, about end		$\frac{1}{3}ML^2$	Cylindrical hoop, about center	R	MR^2
Plane or slab, about center	b a	$\frac{1}{12}Ma^2$	Solid sphere, about diameter	R	$\frac{2}{5}MR^2$
Plane or slab, about edge	b a	$\frac{1}{3}Ma^2$	Spherical shell, about diameter	R	$\frac{2}{3}MR^2$