问题

给定下推自动机

$$M = (\{q_0, q_1, q_2\}, \{a, b\}, \{c, z\}, \delta, q_0, z, \{q_2\}),$$

其中转移函数为

$$\delta(q_0, b, z) = \{(q_1, ccz)\},$$
 $\delta(q_0, a, c) = \{(q_1, \varepsilon)\},$ $\delta(q_1, a, c) = \{(q_1, \varepsilon)\},$ $\delta(q_1, a, z) = \{(q_1, z), (q_2, \varepsilon)\},$

试给出下推自动机M对应的上下文无关文法。

解答

先将转移函数改造为满足定理7.2要求的形式,可得转移函数集合:

$$\delta(q_0, b, z) = \{(q_4, cz)\}, & \delta(q_4, \varepsilon, c) = \{(q_0, cc)\}, \\
\delta(q_0, a, c) = \{(q_1, \varepsilon)\}, & \delta(q_1, a, c) = \{(q_1, \varepsilon)\}, \\
\delta(q_1, a, z) = \{(q_3, cz)\}, & \delta(q_3, \varepsilon, c) = \{(q_1, \varepsilon)\}, \\
\delta(q_1, a, z) = \{(q_2, \varepsilon)\}, & \delta(q_3, \varepsilon, c) = \{(q_1, \varepsilon)\}, \\
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\delta(q_3, \varepsilon,$$

由第一个转移函数,可得产生式集合:

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由第二个转移函数,可得产生式集合:

由第三个转移函数,可得产生式集合:

$$(q_0cq_1) \rightarrow a$$
.

由第四个转移函数,可得产生式集合:

$$(q_1cq_1) \rightarrow a$$
.

由第五个转移函数,可得产生式集合:

$$\begin{array}{rcl} q_1zq_0 & \to & a(q_3cq_0)(q_0zq_0)|a(q_3cq_1)(q_1zq_0)|a(q_3cq_2)(q_2zq_0)| \\ & & a(q_3cq_3)(q_3zq_0)|a(q_3cq_4)(q_4zq_0), \\ q_1zq_1 & \to & a(q_3cq_0)(q_0zq_1)|a(q_3cq_1)(q_1zq_1)|a(q_3cq_2)(q_2zq_1)| \\ & & a(q_3cq_3)(q_3zq_1)|a(q_3cq_4)(q_4zq_1), \\ q_1zq_2 & \to & a(q_3cq_0)(q_0zq_2)|a(q_3cq_1)(q_1zq_2)|a(q_3cq_2)(q_2zq_2)| \\ & & a(q_3cq_3)(q_3zq_2)|a(q_3cq_4)(q_4zq_2), \\ q_1zq_3 & \to & a(q_3cq_0)(q_0zq_3)|a(q_3cq_1)(q_1zq_3)|a(q_3cq_2)(q_2zq_3)| \\ & & a(q_3cq_3)(q_3zq_3)|a(q_3cq_4)(q_4zq_3), \\ q_1zq_4 & \to & a(q_3cq_0)(q_0zq_4)|a(q_3cq_1)(q_1zq_4)|a(q_3cq_2)(q_2zq_4)| \\ & & a(q_3cq_3)(q_3zq_4)|a(q_3cq_4)(q_4zq_4). \end{array}$$

由第六个转移函数,可得产生式集合:

$$(q_3cq_1) \to \varepsilon$$
.

由第七个转移函数,可得产生式集合:

$$(q_1zq_2) \rightarrow a$$
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文法的初始变量为 (q_0zq_2) 。