

Abstract

In recent years, vehicular edge computing (VEC) has emerged as a promising paradigm. In previous studies on offloading in VEC, a task is always supposed to only request one type of service, limiting the universality of research. To address these limitations, we propose a deep reinforcement learning (DRL)-based joint service caching and task offloading scheme, named DRLSCCO. The advantages of the proposed scheme are as follows: 1) it allows each task to request multiple types of services simultaneously, 2) it enables fine-grained task decomposition based on service types and distributed offloading of subtasks, and 3) it supports both cloud collaboration and edge collaboration. To comprehensively evaluate the performance of the proposed DRLSCCO scheme, we conduct extensive comparative experiments against four benchmark schemes. First, we investigate the convergence behavior of different schemes under dynamic task size and vehicle density. Second, by varying task size and vehicle density, respectively, we reveal the variation pattern of task delay underlying the governing of these factors. Third, with vehicle density and task size held constant, we explore the impact of edge server CPU frequency on energy consumption of mobile network operators (MNOs). Results demonstrate that DRLSCCO outperforms the four benchmark schemes in reducing task delay under various parameter configurations, and achieves the slowest increase of energy consumption as edge server CPU frequency increases.

1. Introduction

elsarticle.cls is a thoroughly re-written document class for formatting L^AT_EX submissions to Elsevier journals. The class uses the environments and commands defined in L^AT_EX kernel without any change in the signature so that clashes with other contributed L^AT_EX packages such as hyperref.sty, preview-latex.sty, etc., will be minimal. elsarticle.cls is primarily built upon the default article.cls. This class depends on the following packages for its proper functioning:

1. natbib.sty for citation processing;
2. geometry.sty for margin settings;
3. fleqn.clo for left aligned equations;
4. graphicx.sty for graphics inclusion;
5. txfonts.sty optional font package, if the document is to be formatted with Times and compatible math fonts;

6. `hyperref.sty` optional packages if hyperlinking is required in the document;
7. `endfloat.sty` optional packages if floats to be placed at end of the PDF.

All the above packages (except some optional packages) are part of any standard L^AT_EX installation. Therefore, the users need not be bothered about downloading any extra packages. Furthermore, users are free to make use of AMS math packages such as `amsmath.sty`, `amsthm.sty`, `amssymb.sty`, `amsfonts.sty`, etc., if they want to. All these packages work in tandem with `elsarticle.cls` without any problems.

2. Major Differences

Following are the major differences between `elsarticle.cls` and its predecessor package, `elsart.cls`:

- `elsarticle.cls` is built upon `article.cls` while `elsart.cls` is not. `elsart.cls` redefines many of the commands in the L^AT_EX classes/kernel, which can possibly cause surprising clashes with other contributed L^AT_EX packages;
- provides preprint document formatting by default, and optionally formats the document as per the final style of models 1+, 3+ and 5+ of Elsevier journals;
- some easier ways for formatting `list` and `theorem` environments are provided while people can still use `amsthm.sty` package;
- `natbib.sty` is the main citation processing package which can comprehensively handle all kinds of citations and works perfectly with `hyperref.sty` in combination with `hypernat.sty`;
- long title pages are processed correctly in preprint and final formats.

3. Installation

The package is available at author resources page at Elsevier (<http://www.elsevier.com/locate/latex>). It can also be found in Comprehensive T_EX Archive Network (CTAN), <https://ctan.org/pkg/elsarticle>.

Please download the `elsarticle.dtx` which is a composite class with documentation and `elsarticle.ins` which is the L^AT_EX installer file. When

we compile the `elsarticle.ins` with L^AT_EX it provides the class file, `elsarticle.cls` by stripping off all the documentation from the `*.dtx` file. The class may be moved or copied to a place, usually, `$TEXMF/tex/latex/elsevier/`, or a folder which will be read by L^AT_EX during document compilation. The T_EX file database needs updation after moving/copying class file. Usually, we use commands like `mktexlsr` or `texhash` depending upon the distribution and operating system.

4. Usage

The class should be loaded with the command:

```
\documentclass[<options>]{elsarticle}
```

where the `options` can be the following:

`preprint` default option which format the document for submission to Elsevier journals.

`review` similar to the `preprint` option, but increases the baselineskip to facilitate easier review process.

`1p` formats the article to the look and feel of the final format of model 1+ journals. This is always single column style.

`3p` formats the article to the look and feel of the final format of model 3+ journals. If the journal is a two column model, use `twocolumn` option in combination.

`5p` formats for model 5+ journals. This is always of two column style.

`authoryear` author-year citation style of `natbib.sty`. If you want to add extra options of `natbib.sty`, you may use the options as comma delimited strings as arguments to `\biboptions` command. An example would be:

```
\biboptions{longnamesfirst,angle,semicolon}
```

`number` numbered citation style. Extra options can be loaded with `\biboptions` command.

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`sort&compress` sorts and compresses the numbered citations. For example, citation [1,2,3] will become [1–3].

`longtitle` if front matter is unusually long, use this option to split the title page across pages with the correct placement of title and author footnotes in the first page.

`times` loads `txfonts.sty`, if available in the system to use Times and compatible math fonts.

`reversenotenum` Use alphabets as author–affiliation linking labels and use numbers for author footnotes. By default, numbers will be used as author–affiliation linking labels and alphabets for author footnotes.

`lefttitle` To move title and author/affiliation block to flushleft. `centertitle` is the default option which produces center alignment.

`endfloat` To place all floats at the end of the document.

`nonatbib` To unload `natbib.sty`.

`doubleblind` To hide author name, affiliation, email address etc. for double blind refereeing purpose.

All options of `article.cls` can be used with this document class.

The default options loaded are `a4paper`, `10pt`, `oneside`, `onecolumn` and `preprint`.

5. Frontmatter

There are two types of frontmatter coding:

- (1) each author is connected to an affiliation with a footnote marker; hence all authors are grouped together and affiliations follow;
- (2) authors of same affiliations are grouped together and the relevant affiliation follows this group.

An example of coding the first type is provided below.

```
\title{This is a specimen title\tnoteref{t1,t2}}
\tnotetext[t1]{This document is the results of the research
  project funded by the National Science Foundation.}
\tnotetext[t2]{The second title footnote which is a longer
  text matter to fill through the whole text width and
  overflow into another line in the footnotes area of the
  first page.}
```

```
\author[1]{J.K. Krishnan\corref{cor1}%
  \fnref{fn1}}
\ead{jkk@example.in}

\author[1,2]{Han Thane\fnref{fn2}}
\ead{han@different.edu}

\author[3]{T. Rafeeq\fnref{fn1,fn3}}
\ead[url]{www.nowhere.com}

\cortext[cor1]{Corresponding author}
\fntext[fn1]{This is the first author footnote.}
\fntext[fn2]{Another author footnote, this is a very long footnote and
  it should be a really long footnote. But this footnote is not yet
  sufficiently long enough to make two lines of footnote text.}
\fntext[fn3]{Yet another author footnote.}
```

```
\affiliation[1]{organization={Department of Physics,  
J.K. Institute of Science},  
addressline={Jawahar Nagar},  
city={Trivandrum},  
% citysep={}, % Uncomment if no comma needed  
% % between city and postcode  
postcode={695013},  
state={Kerala},  
country={India}}  
  
\affiliation[2]{organization={World Scientific University},  
addressline={Street 29},  
postcode={1011 NX},  
postcodesep={},  
city={Amsterdam},  
country={The Netherlands}}  
  
\affiliation[3]{organization={University of Intelligent Studies},  
addressline={Street 15},  
city={Jabaladesh},  
postcode={825001},  
state={Orissa},  
country={India}}
```

The output of the above \TeX source is given in Clips 1 and 2. The header portion or title area is given in Clip 1 and the footer area is given in Clip 2.

Clip 1: Header of the title page..

This is a specimen a_b title^{*,**}

J.K. Krishnan^{a,1,*}, Han Thane^{a,b,2}, T. Rafeeq^{c,1,3}

^aDepartment of Physics, J.K. Institute of Science, Jawahar Nagar, Trivandrum, 695013, Kerala, India

^bWorld Scientific University, Street 29, 1011 NX Amsterdam, The Netherlands

^cUniversity of Intelligent Studies, Street 15, Jabaladesh, 825001, Orissa, India

Clip 2: Footer of the title page..

*This document is the results of the research project funded by the National Science Foundation.
**The second title footnote which is a longer text matter to fill through the whole text width and overflow into another line in the footnotes area of the first page.
*Corresponding author
Email addresses: jkk@example.in (J.K. Krishnan), han@different.edu (Han Thane)
URL: www.nowhere.com (T. Rafeeq)
¹This is the first author footnote.
²Another author footnote, this is a very long footnote and it should be a really long footnote. But this footnote is not yet sufficiently long enough to make two lines of footnote text.
³Yet another author footnote.

Most of the commands such as `\title`, `\author`, `\affiliation` are self explanatory. Various components are linked to each other by a label-reference mechanism; for instance, title footnote is linked to the title with a footnote mark generated by referring to the `\label` string of the `\tnotetext`. We have used similar commands such as `\tnoteref` (to link title note to title); `\corref` (to link corresponding author text to corresponding author); `\fnref` (to link footnote text to the relevant author names). \TeX needs two compilations to resolve the footnote marks in the preamble part. Given below are the syntax of various note marks and note texts.

```
\tnoteref{<label(s)>}
\corref{<label(s)>}
\fnref{<label(s)>}
\tnotetext[<label>]{<title note text>}
\cortext[<label>]{<corresponding author note text>}
\fnfntext[<label>]{<author footnote text>}
```

where `<label(s)>` can be either one or more comma delimited label strings. The optional arguments to the `\author` command holds the ref label(s) of the address(es) to which the author is affiliated while each `\affiliation` command can have an optional argument of a label. In the same manner, `\tnotetext`, `\fnfntext`, `\cortext` will have optional arguments as their respective labels and note text as their mandatory argument.

The following example code provides the markup of the second type of author-affiliation.

```
\author{J.K. Krishnan\corref{cor1}%  
  \fnref{fn1}}  
\ead{jkk@example.in}  
\affiliation{organization={Department of Physics,  
  J.K. Institute of Science},  
  addressline={Jawahar Nagar},  
  city={Trivandrum},  
  % citysep={}, % Uncomment if no comma needed  
  % % between city and postcode  
  postcode={695013},  
  state={Kerala},  
  country={India}}  
  
\author{Han Thane\fnref{fn2}}  
\ead{han@different.edu}  
\affiliation{organization={World Scientific University},  
  addressline={Street 29},  
  postcode={1011 NX},  
  postcodesep={},  
  city={Amsterdam},  
  country={The Netherlands}}  
  
\author{T. Rafeeq\fnref{fn1,fn3}}  
\ead[url]{www.nowhere.com}  
\affiliation{organization={University of Intelligent Studies},  
  addressline={Street 15},  
  city={Jabaldesh},  
  postcode={825001},  
  state={Orissa},  
  country={India}}
```

```
\cortext[cor1]{Corresponding author}  
\fntext[fn1]{This is the first author footnote.}  
\fntext[fn2]{Another author footnote, this is a very long  
  footnote and it should be a really long footnote. But this  
  footnote is not yet sufficiently long enough to make two lines  
  of footnote text.}
```

The output of the above T_EX source is given in Clip 3.

Clip 3: Header of the title page...

This is a specimen a_b title^{*,**}

J.K. Krishnan^{1,*}

Department of Physics, J.K. Institute of Science, Jawahar Nagar, Trivandrum, 695013, Kerala, India

Han Thane²

World Scientific University, Street 29, 1011 NX Amsterdam, The Netherlands

T. Rafeeq^{1,3}

University of Intelligent Studies, Street 15, Jabaladesh, 825001, Orissa, India

Clip 4 shows the output after giving `doubleblind` class option.

Clip 4: Double blind article.

This is a specimen a_b title

Abstract

In this work we demonstrate a_b the formation Y_1 of a new type of polariton

The frontmatter part has further environments such as abstracts and keywords. These can be marked up in the following manner:

```
\begin{abstract}
In this work we demonstrate the formation of a new type of
polariton on the interface between a ....
\end{abstract}
```

```
\begin{keyword}
quadruple exciton \sep polariton \sep WGM
\end{keyword}
```

Each keyword shall be separated by a `\sep` command. msc classifications shall be provided in the keyword environment with the commands `\MSC`. `\MSC` accepts an optional argument to accommodate future revisions. eg., `\MSC[2008]`. The default is 2000.

5.1. New page

Sometimes you may need to give a page-break and start a new page after title, author or abstract. Following commands can be used for this purpose.

```
\newpageafter{title}  
\newpageafter{author}  
\newpageafter{abstract}
```

`\newpageafter{title}` typeset the title alone on one page.

`\newpageafter{author}` typeset the title and author details on one page.

`\newpageafter{abstract}` typeset the title, author details and abstract & keywords one one page.

6. Floats

Figures may be included using the command, `\includegraphics` in combination with or without its several options to further control graphic. `\includegraphics` is provided by `graphic[s,x].sty` which is part of any standard L^AT_EX distribution. `graphicx.sty` is loaded by default. L^AT_EX accepts figures in the postscript format while pdfL^AT_EX accepts *.pdf, *.mps (metapost), *.jpg and *.png formats. pdfL^AT_EX does not accept graphic files in the postscript format.

The `table` environment is handy for marking up tabular material. If users want to use `multirow.sty`, `array.sty`, etc., to fine control/enhance the tables, they are welcome to load any package of their choice and `elsarticle.cls` will work in combination with all loaded packages.

7. Theorem and theorem like environments

`elsarticle.cls` provides a few shortcuts to format theorems and theorem-like environments with ease. In all commands the options that are used with the `\newtheorem` command will work exactly in the same manner. `elsarticle.cls` provides three commands to format theorem or theorem-like environments:

```
\newtheorem{thm}{Theorem}
\newtheorem{lem}[thm]{Lemma}
\newdefinition{rmk}{Remark}
\newproof{pf}{Proof}
\newproof{pot}{Proof of Theorem \ref{thm2}}
```

The `\newtheorem` command formats a theorem in L^AT_EX's default style with italicized font, bold font for theorem heading and theorem number at the right hand side of the theorem heading. It also optionally accepts an argument which will be printed as an extra heading in parentheses.

```
\begin{thm}
For system (8), consensus can be achieved with
 $\|T_{\omega z}\|$ 
...
\begin{eqnarray}\label{10}
....
\end{eqnarray}
\end{thm}
```

Clip 5 will show you how some text enclosed between the above code looks like:

Clip 5: `\newtheorem`.

Theorem 2. For system (8), consensus can be achieved with $\|T_{\omega z}(s)\|_{\infty} < \gamma$ if there exist a symmetric positive definite matrix $P \in \mathcal{R}^{(n-1) \times (n-1)}$ and a scalar $\mu > 0$ satisfying

$$\Gamma = \begin{bmatrix} -\bar{L}^T P - P\bar{L} + U_1^T U_1 + \mu \bar{E} & P U_1^T E_1 & P U_1^T \\ E_1^T U_1 P & -\mu I & 0 \\ U_1 P & 0 & -\gamma^2 I \end{bmatrix} < 0, \quad (10)$$

where $\bar{L} = U_1^T L U_1$ and $\bar{E} = U_1^T E_2^T E_2 U_1$.

The `\newdefinition` command is the same in all respects as its `\newtheorem` counterpart except that the font shape is roman instead of italic. Both `\newdefinition` and `\newtheorem` commands automatically define counters for the environments defined.

Clip 6: `\newdefinition.`

Remark 3. We remark that; when the ratio h/λ tends to 0, the expression $\lambda L(r, s) = -(s-r)/(4\left(\frac{h}{\lambda}\right)^2 + (r-s)^2)$ tends to $1/(r-s)$ which is a singular function. This means that the expression $\lambda L(r, s)$ is not well behaved for the small values of h/λ . Consequently, for the solution to converge, the integrals of (10) and (11) must be evaluated with a large number of nodes. In our numerical applications (cf. section 5), we use 100 nodes to evaluate these integrals. With the smallest value of $h/\lambda = 0.02$, the convergence is good with $N = 20$.

The `\newproof` command defines proof environments with upright font shape. No counters are defined.

Clip 7: `\newproof.`

Proof of Theorem 2. Proof follows straightforward from Lemma 3 and Theorem 1. However, it should be emphasized that all possible $\tilde{L}_{\sigma(t)}$ should share a common Lyapunov function $V(\delta) = \delta^T(t)P\delta(t)$ (see the proof of Lemma 3 in Appendix A). \square

Users can also make use of `amsthm.sty` which will override all the default definitions described above.

8. Enumerated and Itemized Lists

`elsarticle.cls` provides an extended list processing macros which makes the usage a bit more user friendly than the default L^AT_EX list macros. With an optional argument to the `\begin{enumerate}` command, you can change the list counter type and its attributes.

```
\begin{enumerate}[1.]
\item The enumerate environment starts with an optional
      argument '1.', so that the item counter will be suffixed
      by a period.
\item You can use 'a' for alphabetical counter and '(i)' for
      roman counter.
\begin{enumerate}[a]
\item Another level of list with alphabetical counter.
\item One more item before we start another.
```

Clip 8: List – Enumerate.

1. The enumerate environment starts with an optional argument '1.' so that the item counter will be suffixed by a period.
2. You can use '(a)' for alphabetical counter and '(i)' for roman counter.
 - a) Another level of list with alphabetical counter.
 - b) One more item before we start another.
 - (i) This item has roman numeral counter.
 - (ii) Another one before we close the third level.
 - c) Third item in second level.
3. All list items conclude with this step.

Further, the enhanced list environment allows one to prefix a string like 'step' to all the item numbers.

```
\begin{enumerate}[Step 1.]
\item This is the first step of the example list.
\item Obviously this is the second step.
\item The final step to wind up this example.
\end{enumerate}
```

Clip 9: List – enhanced.

- Step 1. This is the first step of the example list.
- Step 2. Obviously this is the second step.
- Step 3. The final step to wind up this example.

9. Cross-references

In electronic publications, articles may be internally hyperlinked. Hyperlinks are generated from proper cross-references in the article. For example, the words Fig. 1 will never be more than simple text, whereas the proper cross-reference `\ref{tiger}` may be turned into a hyperlink to the figure itself: [Fig. 1](#). In the same way, the words Ref. [1] will fail to turn into a hyperlink; the proper cross-reference is `\cite{Knuth96}`. Cross-referencing is possible in L^AT_EX for sections, subsections, formulae, figures, tables, and literature references.

10. Mathematical symbols and formulae

Many physical/mathematical sciences authors require more mathematical symbols than the few that are provided in standard L^AT_EX. A useful package for additional symbols is the `amssymb` package, developed by the American Mathematical Society. This package includes such oft-used symbols as \lesssim (`\lessssim`), \gtrsim (`\gtrsim`) or \hbar (`\hbar`). Note that your T_EX system should have the `msam` and `msbm` fonts installed. If you need only a few symbols, such as \square (`\Box`), you might try the package `latexsym`.

Another point which would require authors' attention is the breaking up of long equations. When you use `elsarticle.cls` for formatting your submissions in the `preprint` mode, the document is formatted in single column style with a text width of 384pt or 5.3in. When this document is formatted for final print and if the journal happens to be a double column journal, the text width will be reduced to 224pt at for 3+ double column and 5+ journals respectively. All the nifty fine-tuning in equation breaking done by the author goes to waste in such cases. Therefore, authors are requested to check this problem by typesetting their submissions in final format as well just to see if their equations are broken at appropriate places, by changing appropriate options in the document class loading command, which is explained in section 4, [Usage](#). This allows authors to fix any equation breaking problem before submission for publication. `elsarticle.cls` supports formatting the author submission in different types of final format. This is further discussed in section 13, [Final print](#).

Displayed equations and double column journals

Many Elsevier journals print their text in two columns. Since the preprint layout uses a larger line width than such columns, the formulae are too wide for the line width in print. Here is an example of an equation (see equation 6) which is perfect in a single column preprint format:

In normal course, articles are prepared and submitted in single column format even if the final printed article will come in a double column format journal. Here the problem is that when the article is typeset by the typesetters for paginating and fit within the single column width, they have to break the lengthy equations and align them properly. Even if most of the tasks in preparing your proof is automated, the equation breaking and aligning requires manual judgement, hence this task is manual. When there comes a manual operation that area is error prone. Author needs to check that equation pretty well.

However if authors themselves break the equation to the single column width typesetters need not want to touch these area and the proof authors get will be without any errors.

Clip 10: See equation (6).

Here e, m are the electron charge and mass; \mathbf{p} is the electron momentum. For the quadrupole $1S$ transition in cuprous oxide the energy of interaction can be written as:

$$\hbar g = \langle {}^3\Gamma_{5,xz}^+ | H_{int} | {}^1\Gamma_1^+ \rangle = \langle {}^3\Gamma_{5,1,2}^+ | H_{int} | {}^1\Gamma_{1,0,0}^+ \rangle \quad (5)$$

Here we introduced the initial state of the system, which transforms as irreducible representation ${}^1\Gamma_1^+$ of the cubic centered group O_h . The final state is the *ortho*-exciton state which transforms as ${}^3\Gamma_{5,xz}^+$ in Cartesian system or as ${}^3\Gamma_{5,1,2}^+$ in the corresponding spherical basis.

Hence, using (1, 3, 4, 5), one can deduce that the coupling of the spherical harmonic compared to the plane wave ($\hbar g_{1,2} = 124 \mu\text{eV}$) is resonantly enhanced:

$$\frac{g_{1,39}}{g_{1,2}} = -i0.06b_{1,39} (kr_0) A_{1,39}^{1,2} (r_0 + \delta r) \quad (6)$$

Here we utilized the fact that $B_{1,39}^{1,2} \ll A_{1,39}^{1,2}$. While the resonant enhancement is provided by the $b_{1,39}$ Mie coefficient here, the translational coefficient reduces the effect. That is why if one tries to couple the evanescent light to the dipole transition the effect is much weaker as $A_{1,39}^{0,1} \ll A_{1,39}^{1,2}$. The resulting exciton - evanescent light coupling is shown in Fig. 1 Both dipole and quadrupole

When this document is typeset for publication in a model 3+ journal with double columns, the equation will overlap the second column text matter if the equation is not broken at the appropriate location.

Clip 11: See equation (6) overprints into second column.

Here $A_{1,39}$ and $B_{1,39}$ are the translational coefficients. Their explicit expression can be found, for instance, in [12, 9] and are explicitly listed in the Appendix.

The bulk (incident) and evanescent polaritons in cuprous oxide are formed through the quadrupole part of the light-matter interaction:

$$H_{int} = \frac{ie}{m\omega_{1S}} \mathbf{E}_{i,S} \cdot \mathbf{p}$$

Here e, m are the electron charge and mass; \mathbf{p} is the electron momentum. For the quadrupole $1S$ transition in cuprous oxide the energy of interaction can be written as:

$$\hbar g = \langle {}^3\Gamma_{5,xz}^+ | H_{int} | {}^1\Gamma_1^+ \rangle = \langle {}^3\Gamma_{5,1,2}^+ | H_{int} | {}^1\Gamma_{1,0,0}^+ \rangle \quad (5)$$

Here we introduced the initial state of the system, which transforms as irreducible representation ${}^1\Gamma_1^+$ of the cubic centered group O_h . The final state is the *ortho*-exciton

Figure 1: The evanescent light - $1S$ quadrupole coupling ($g_{1,1}$) scaled to the bulk exciton-photon coupling ($g_{1,2}$). The size parameter kr_0 is denoted as x and the PMS is placed directly on the cuprous oxide sample ($\delta r = 0$, See also Fig.2).

3. Results and discussion

In this section let us utilize the above calculated WGM-QE interaction to obtain the evanescent polariton (EP) dispersion in the framework of the coupled oscillator model that has been widely used for describing coupled atom-photon or exciton-photon modes in microcavity systems [13]. Near the resonance between WGM and the quadrupole exciton $\omega_{1l} \approx \omega_{1S}$ the EP branches are given by the eigenvalues of the following Hamiltonian:

$$H/\hbar = \omega_{1l} a_x^\dagger a_x + \omega_{1S} b_x^\dagger b_x + g_{1l}(x) (a_k^\dagger b_x + a_x b_x^\dagger), \quad (7)$$

The typesetter will try to break the equation which need not necessarily be to the liking of the author or as it happens, typesetter's break point may be semantically incorrect. Therefore, authors may check their submissions for the incidence of such long equations and break the equations at the correct places so that the final typeset copy will be as they wish.

11. Bibliography

Three bibliographic style files (*.bst) are provided — elsarticle-num.bst, elsarticle-num-names.bst and elsarticle-harv.bst — the first one can be used for the numbered scheme, second one for numbered with new options of natbib.sty. The third one is for the author year scheme.

In L^AT_EX literature, references are listed in the thebibliography environment. Each reference is a \bibitem and each \bibitem is identified by a label, by which it can be cited in the text:

\bibitem[Elson et al.(1996)]{ESG96} is cited as \citet{ESG96}.

In connection with cross-referencing and possible future hyperlinking it is not a good idea to collect more than one literature item in one \bibitem. The so-called Harvard or author-year style of referencing is enabled by the L^AT_EX package natbib. With this package the literature can be cited as follows:

- Parenthetical: \citep{WB96} produces (Wettig & Brown, 1996).
- Textual: \citet{ESG96} produces Elson et al. (1996).
- An affix and part of a reference: \citep[e.g.] [Ch. 2]{Gea97} produces (e.g. Governato et al., 1997, Ch. 2).

In the numbered scheme of citation, \cite{<label>} is used, since \citep or \citet has no relevance in the numbered scheme. natbib package is loaded by elsarticle with numbers as default option. You can change this to author-year or harvard scheme by adding option authoryear in the class loading command. If you want to use more options of the natbib package, you can do so with the \biboptions command, which is described in the section 4, Usage. For details of various options of the natbib package, please take a look at the natbib documentation, which is part of any standard L^AT_EX installation.

In addition to the above standard .bst files, there are 10 journal-specific .bst files also available. Instruction for using these .bst files can be found at <http://support.stmdocs.in>

12. Graphical abstract and highlights

A template for adding graphical abstract and highlights are available now. This will appear as the first two pages of the PDF before the article content begins.

Please refer below to see how to code them.

```
....  
....  
  
\end{abstract}  
  
%%Graphical abstract  
\begin{graphicalabstract}  
%\includegraphics{grabs}  
\end{graphicalabstract}  
  
%%Research highlights  
\begin{highlights}  
\item Research highlight 1  
\item Research highlight 2  
\end{highlights}  
  
\begin{keyword}  
%% keywords here, in the form: keyword \sep keyword  
....  
....
```

13. Final print

The authors can format their submission to the page size and margins of their preferred journal. `elsarticle` provides four class options for the same. But it does not mean that using these options you can emulate the exact page layout of the final print copy.

1p: 1+ journals with a text area of 384pt × 562pt or 13.5cm × 19.75cm or 5.3in × 7.78in, single column style only.

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This is a specimen a_b title^{*,**}

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Abstract

In this work we demonstrate a_b the formation Y_1 of a new type of polariton on the interface between a cuprous oxide slab and a polystyrene micro-sphere placed on the slab. The evanescent field of the resonant whispering gallery mode (WGM) of the micro sphere has a substantial gradient, and therefore effectively couples with the quadrupole 1S excitons in cuprous oxide. This evanescent polariton has a long life-time, which is determined only by its excitonic and WGM component. The polariton lower branch has a well pronounced minimum. This suggests that this excitation is localized and can be utilized for possible BEC. The spatial coherence of the polariton can be improved by assembling the micro-spheres into a linear chain.

Keywords: quadrupole exciton, polariton, WGM, BEC

JEL: 71.35.-y, 71.35.Lk, 71.36.+c

1. Introduction

Although quadrupole excitons (QE) in cuprous oxide crystals are good candidates for BEC due to their narrow line-width and long life-time there are some factors impeding BEC [1, 2]. One of these factors is that due to the small but non negligible coupling to the photon bath, one must consider BEC of the corresponding mixed light-matter states called polaritons [3]. The photon-like part of the polariton has a large group velocity and tends to escape from the crystal. Thus, the temporal coherence of the condensate is effectively broken [4, 5]. One proposed solution to this issue is to place the crystal into a planar micro-cavity [6]. But even state-of-the-art planar micro-cavities can hold the light no longer than 10 μ s. Besides, formation of the polaritons in the planar cuprous oxide micro-cavity is not effective due to quadrupole origin of the excitons.

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¹This is the first author footnote.

²Another author footnote, this is a very long footnote and it should be a really long footnote. But this footnote is not yet sufficiently long enough to make two lines of footnote text.

³Yet another author footnote.

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Theorem 1. *In this work we demonstrate the formation of a new type of polariton on the interface between a cuprous oxide slab and a polystyrene micro-sphere placed on the slab. The evanescent field of the resonant whispering gallery mode*

(WGM) of the micro sphere has a substantial gradient, and therefore effectively couples with the quadrupole 1S excitons in cuprous oxide. This evanescent polariton has a long life-time, which is determined only by its excitonic and WGM component. The polariton lower branch has a well pronounced minimum. This suggests that this excitation is localized and can be utilized for possible BEC. The spatial coherence of the polariton can be improved by assembling the micro-spheres into a linear chain.

Therefore in this work we propose to prevent the polariton escaping by trapping it into a whispering gallery mode (WGM)⁴ of a polystyrene micro-sphere (PMS).

We develop a model which demonstrates formation of a strongly *localized* polariton-like quasi-particle. This quasi-particle is formed by the *resonant* interaction between the WGM in PMS and QE in the adjacent layer of cuprous oxide. The QE interacts with the *gradient* of the WGM evanescent field.

There are few experiments concerned with resonant interaction of the WGM and dipole allowed exciton (DE) [7, 8]. But the DE has some disadvantages compared to QE when it comes to interaction with the WGM. First, the evanescent light has small intensity. Therefore it is not effective for the dipole allowed coupling. But it has a large gradient, so it can effectively couple through a quadrupole part. Second, the DE has short life time compared to the QE and therefore is not suitable for BEC. Third, the kinetic energy of the DE is comparable with the interaction energy. Hence the localization is effectively impeded.

⁴WGM occur at particular resonant wavelengths of light for a given dielectric sphere size. At these wavelengths, the light undergoes total internal reflection at the sphere surface and becomes trapped within the particle for timescales of the order of ns .

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