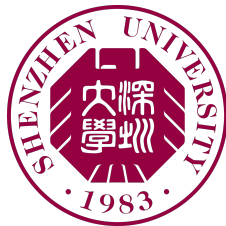


# Towards 'Verifying' a Water Treatment System

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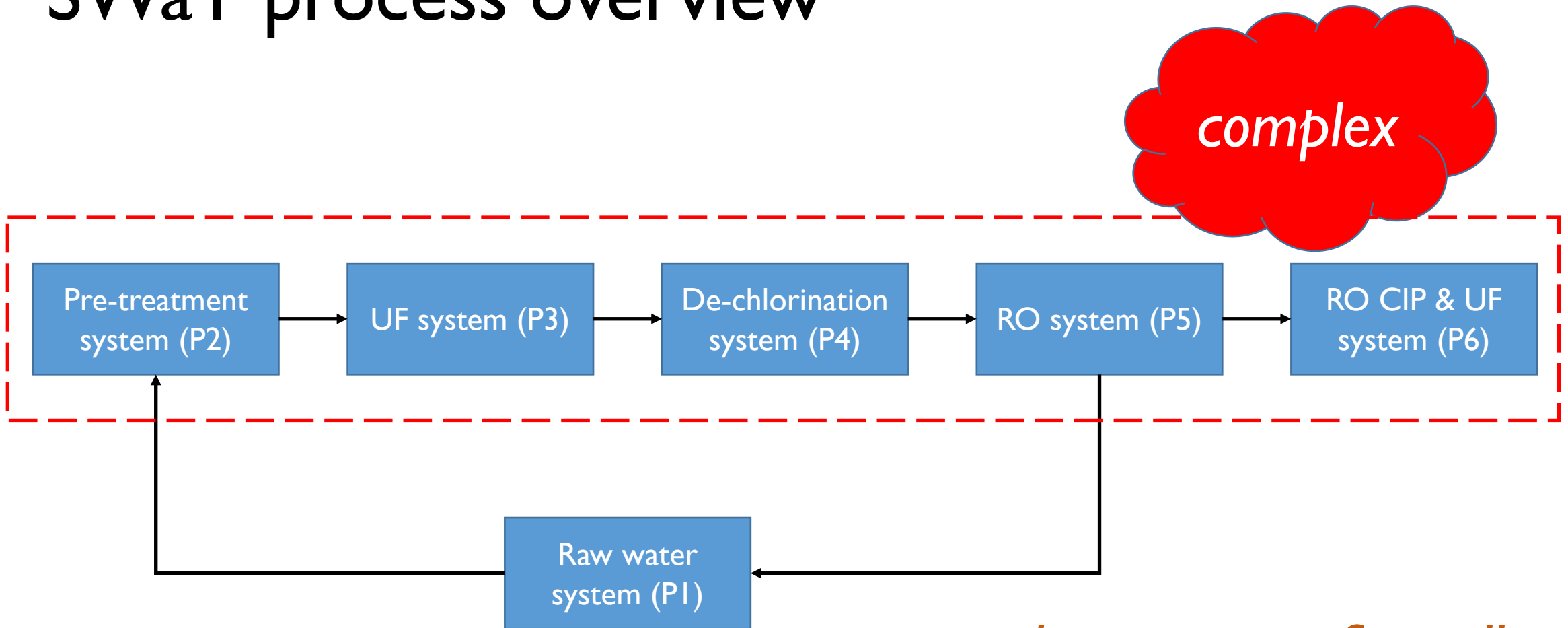


# The Secure Water Treatment System (SWaT)



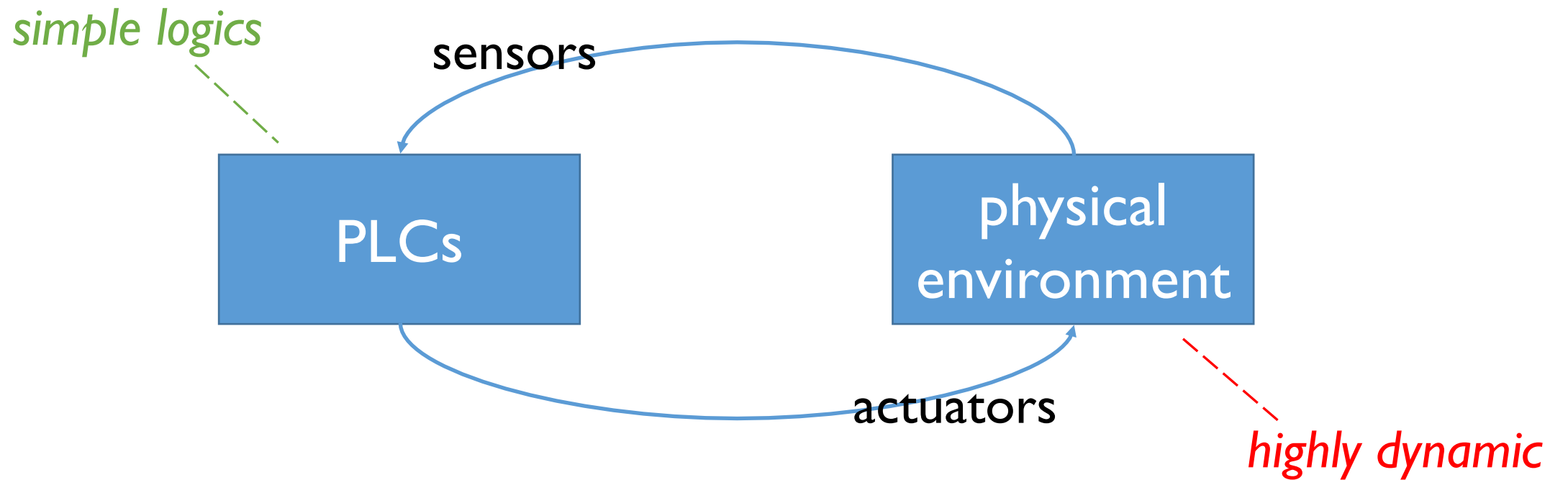
- *fully functioning*
- *supervised experiments*
- *public dataset*
- *a wide range of research areas*

# SWaT process overview



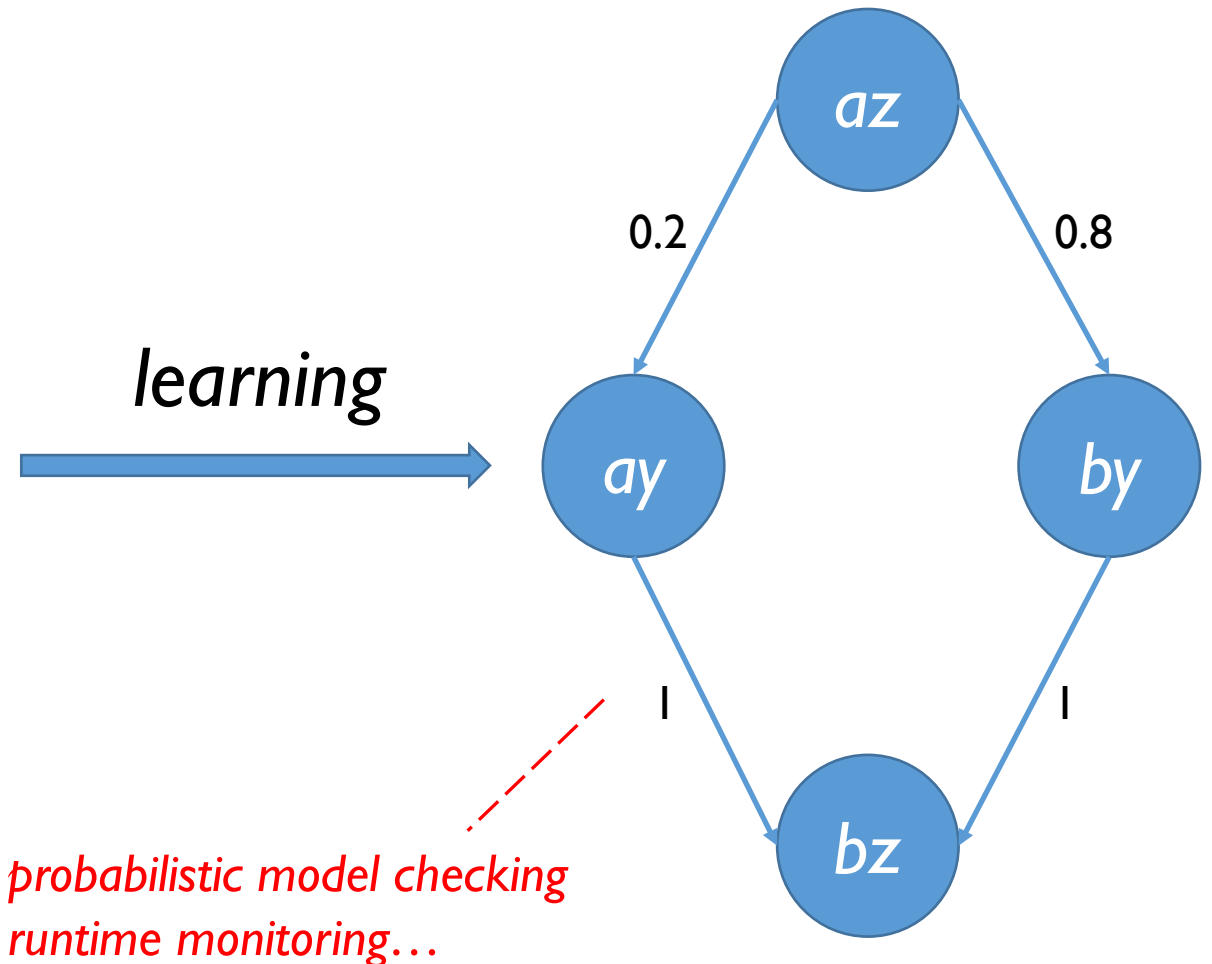
*how can we formally  
'verify' the system?*

# Modelling CPS



# Can we learn a probabilistic model instead?

<i>time</i>	<i>sensors</i>	<i>actuators</i>
<i>t0</i>	<i>a</i>	<i>z</i>
<i>t1</i>	<i>a</i>	<i>y</i>
<i>t2</i>	<i>b</i>	<i>y</i>
<i>t3</i>	<i>b</i>	<i>z</i>
...	...	...



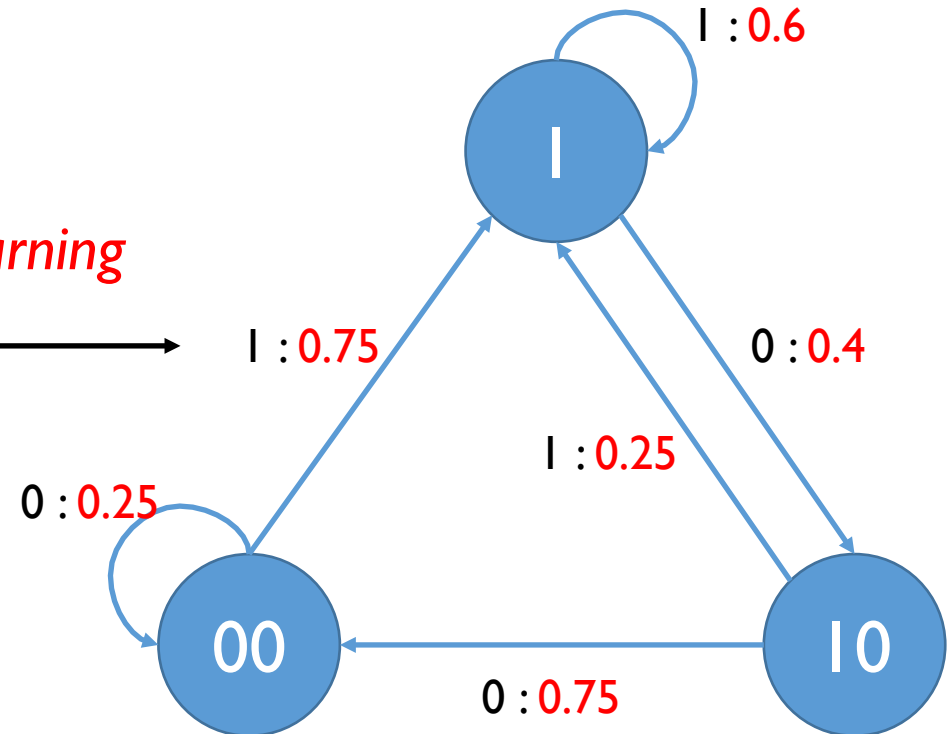
# Probabilistic learning sketch

alphabet:  $\{0, 1\}$

input:  $0010001000111\dots$

*probabilistic learning*

*output model:*



# SWaT dataset

- 26 sensors (*float*) + 25 actuators
- 7 days system log under normal operation + 4 days system log under attacks
- 28800 + 208800



# Predicate abstraction



<i>FIT101</i>	<i>LIT101</i>	<i>MV101</i>	<i>P101</i>	<i>P102</i>	<i>AIT201</i>	<i>AIT202</i>	<i>AIT203</i>	<i>FIT201</i>
2.470294	261.5804	2	2	1	244.3284	8.19008	306.101	2.471278
2.457163	261.1879	2	2	1	244.3284	8.19008	306.101	2.468587
2.439548	260.9131	2	2	1	244.3284	8.19008	306.101	2.467305
2.428338	260.285	2	2	1	244.3284	8.19008	306.101	2.466536
2.424815	259.8925	2	2	1	244.4245	8.19008	306.101	2.466536
2.425456	260.0495	2	2	1	244.5847	8.19008	306.101	2.465127
2.472857	260.2065	2	2	1	244.5847	8.19008	306.101	2.464742

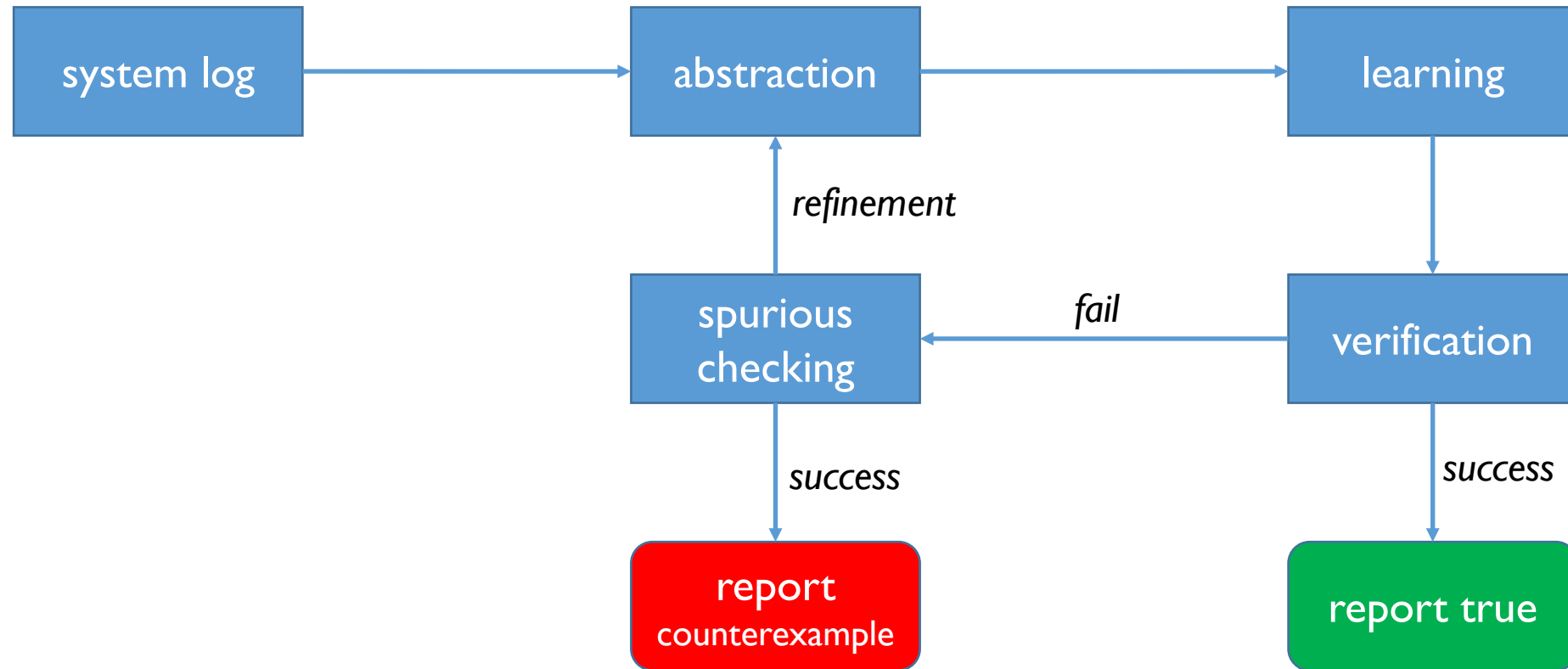
**LIT101 > 1100**



<i>LIT101</i> > 1100
0
0
0
0
0
0
0



# Overall framework



# Safety properties

The diagram shows the formula  $\mathcal{S}_{\leq r}(\varphi)$  with three dashed lines pointing to its components: a blue line from the  $\mathcal{S}$  to the text "steady state probability", a green line from the  $\leq$  to the text "safety threshold", and a red line from the  $r$  to the text "sensors outside its operating range".

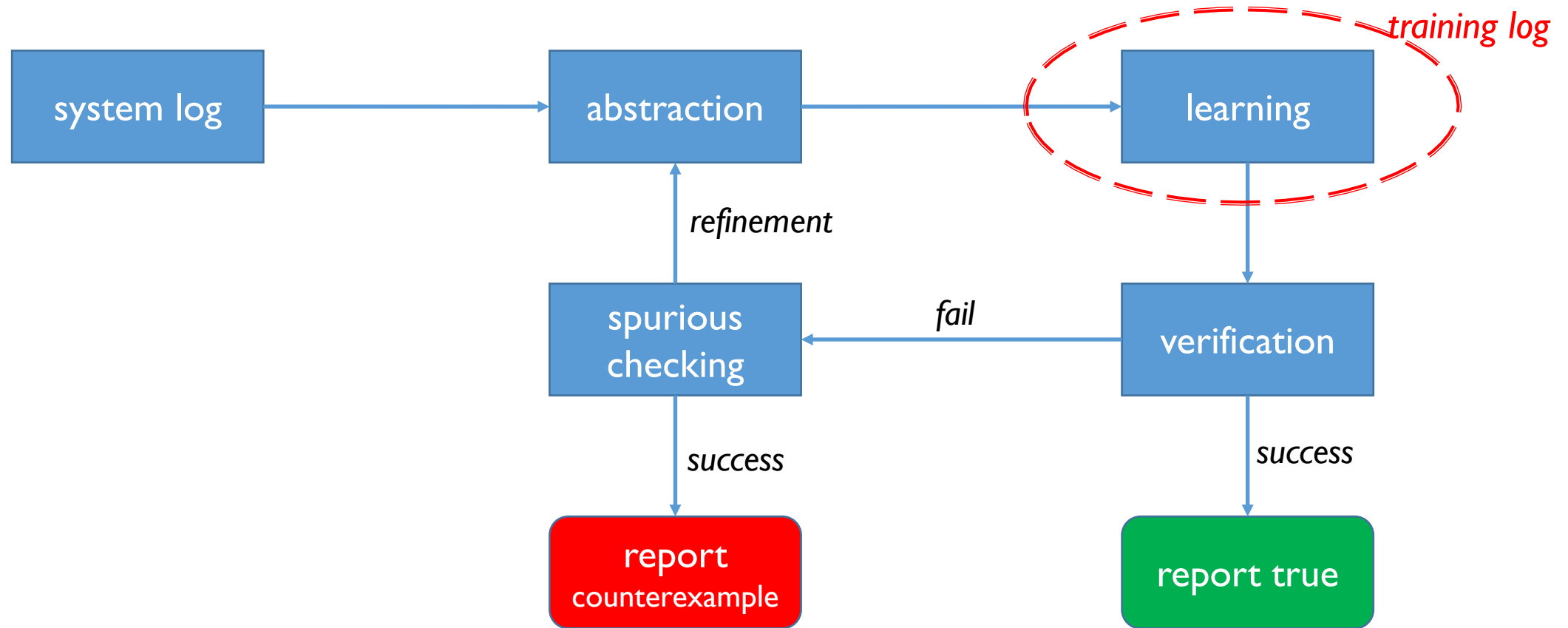
$$\mathcal{S}_{\leq r}(\varphi)$$

*steady state probability*

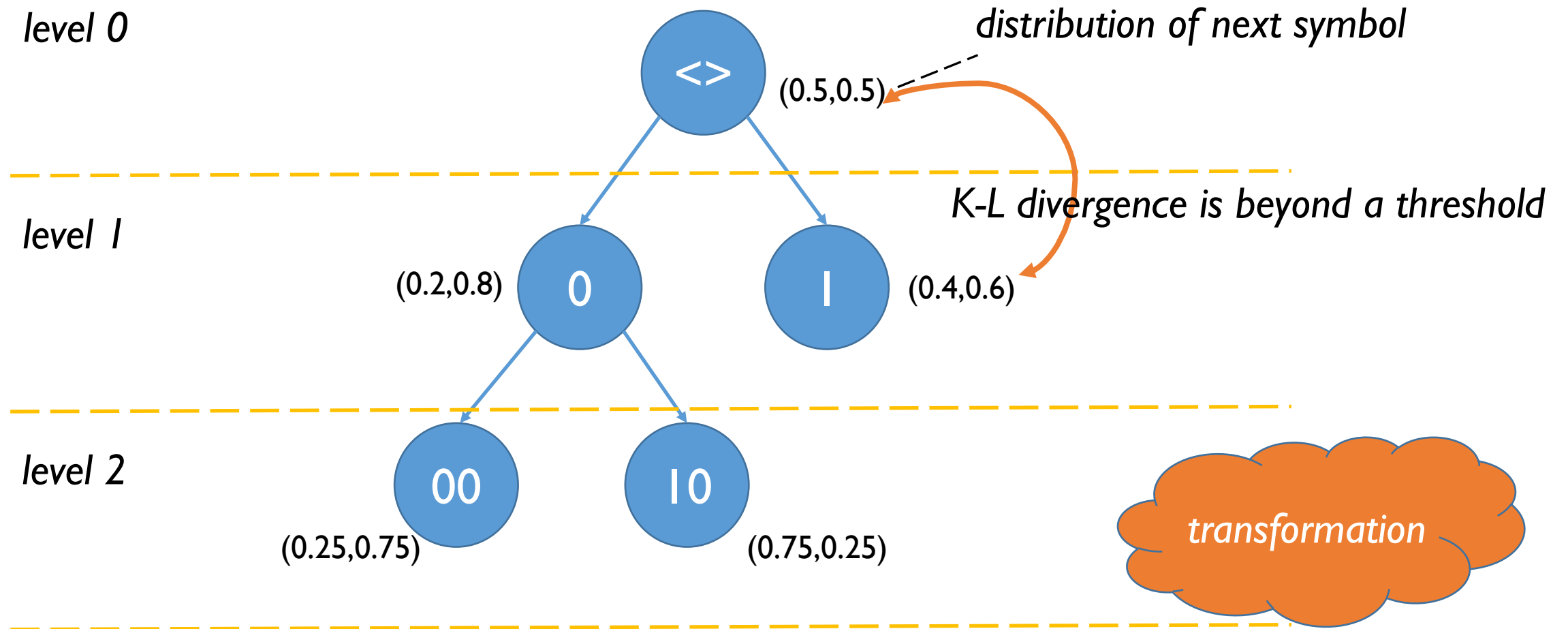
*sensors outside its operating range*

*safety threshold*

# Learning

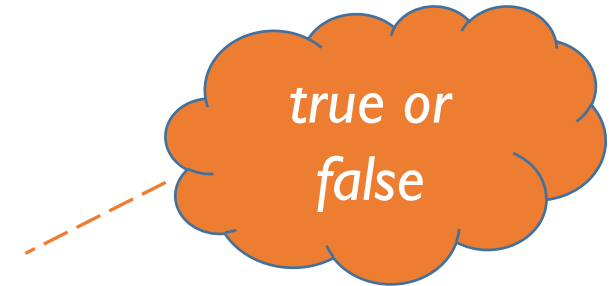


# Learning



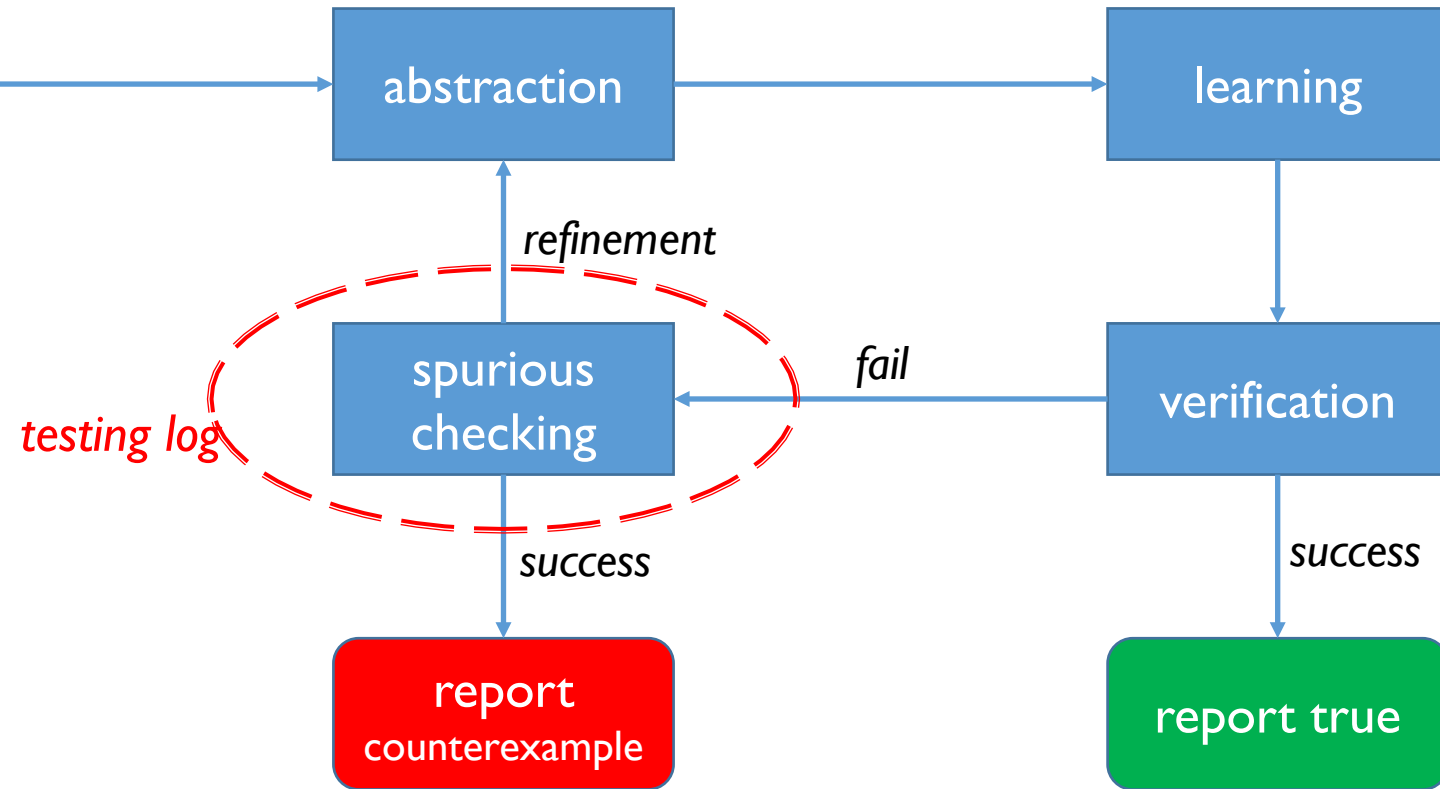
# Verify a safety property

$$\mathcal{S}(\varphi) \leq r \quad ?$$

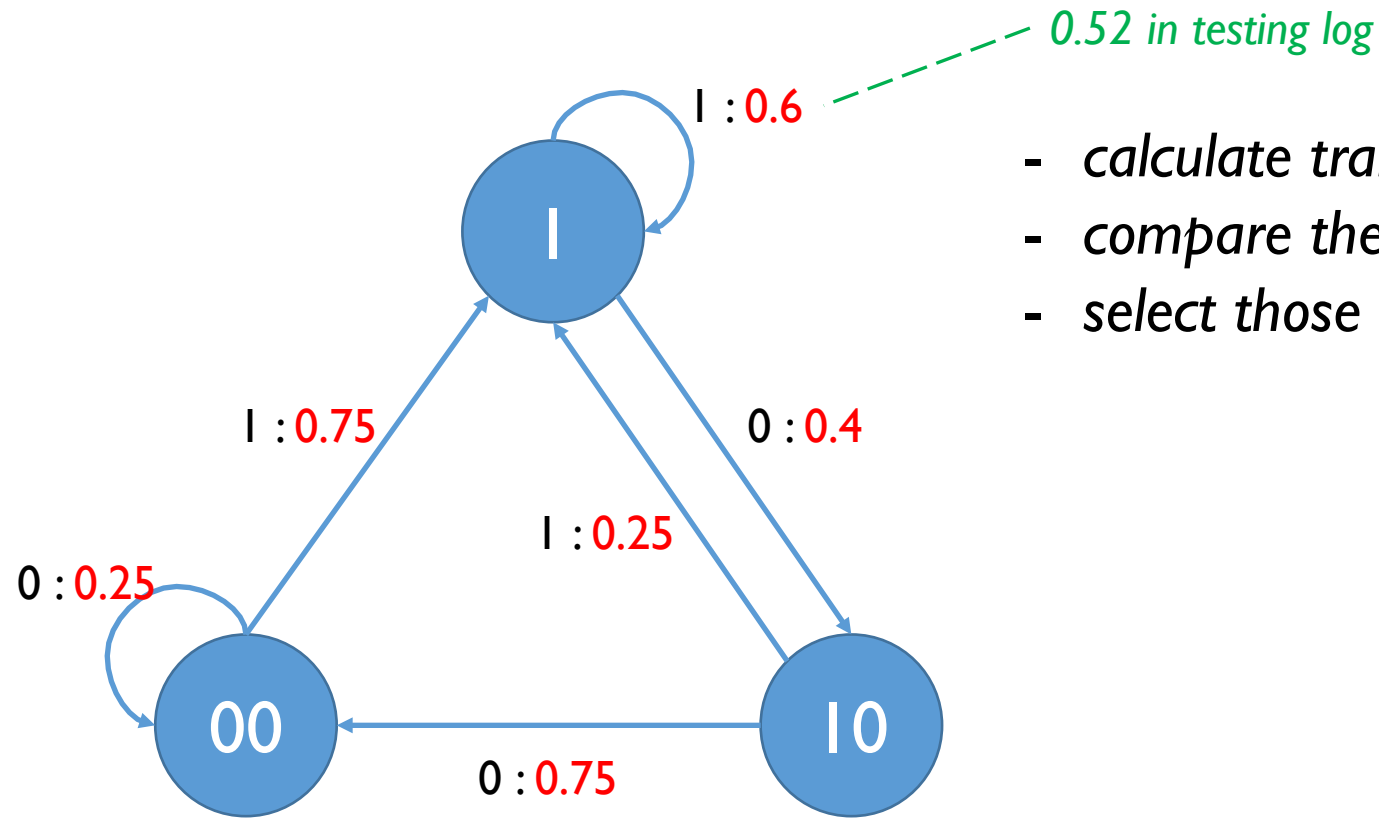


1. *compute steady state probability distribution of the learned model*
2. *sum up the probability of unsafe states*

# Spurious checking

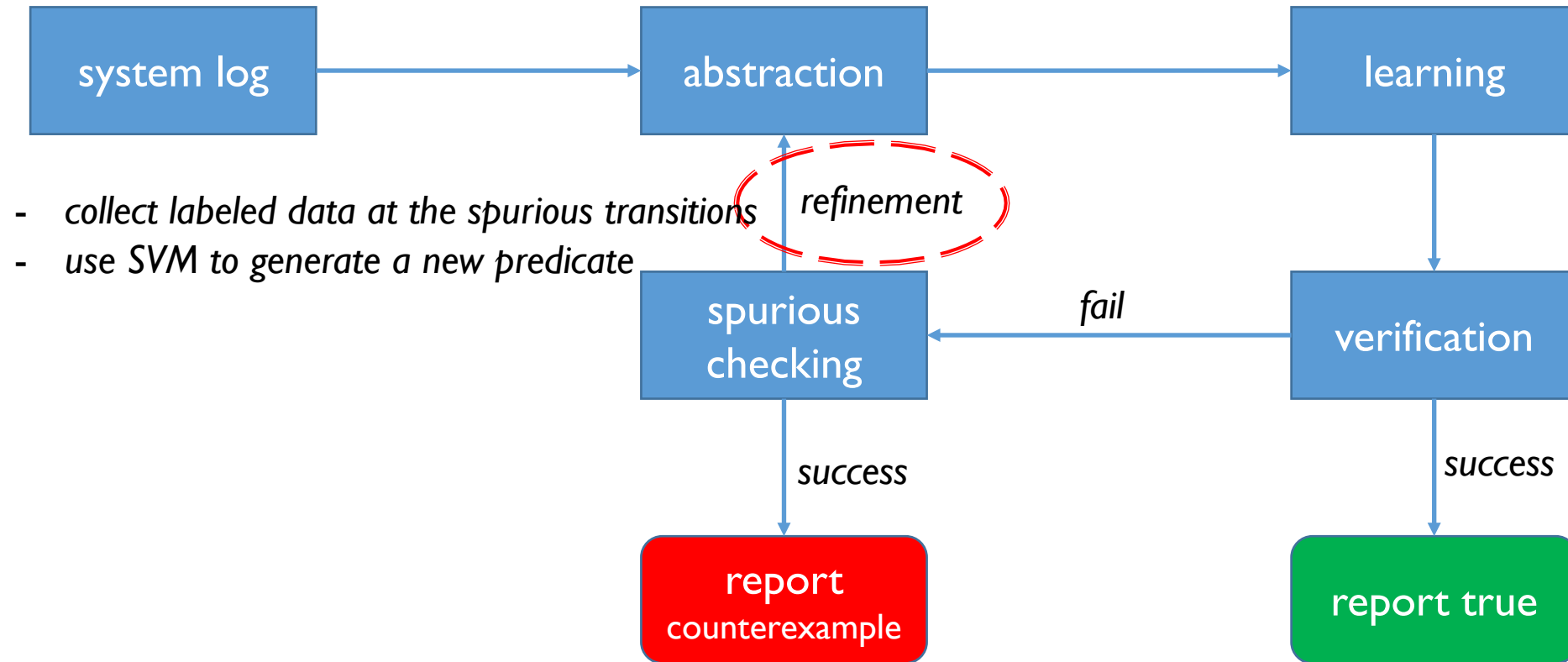


# Find spurious transitions



- calculate transition probabilities in the testing log
- compare the differences with the learned probability
- select those inflated transitions

# Refinement






# Collect labeled data

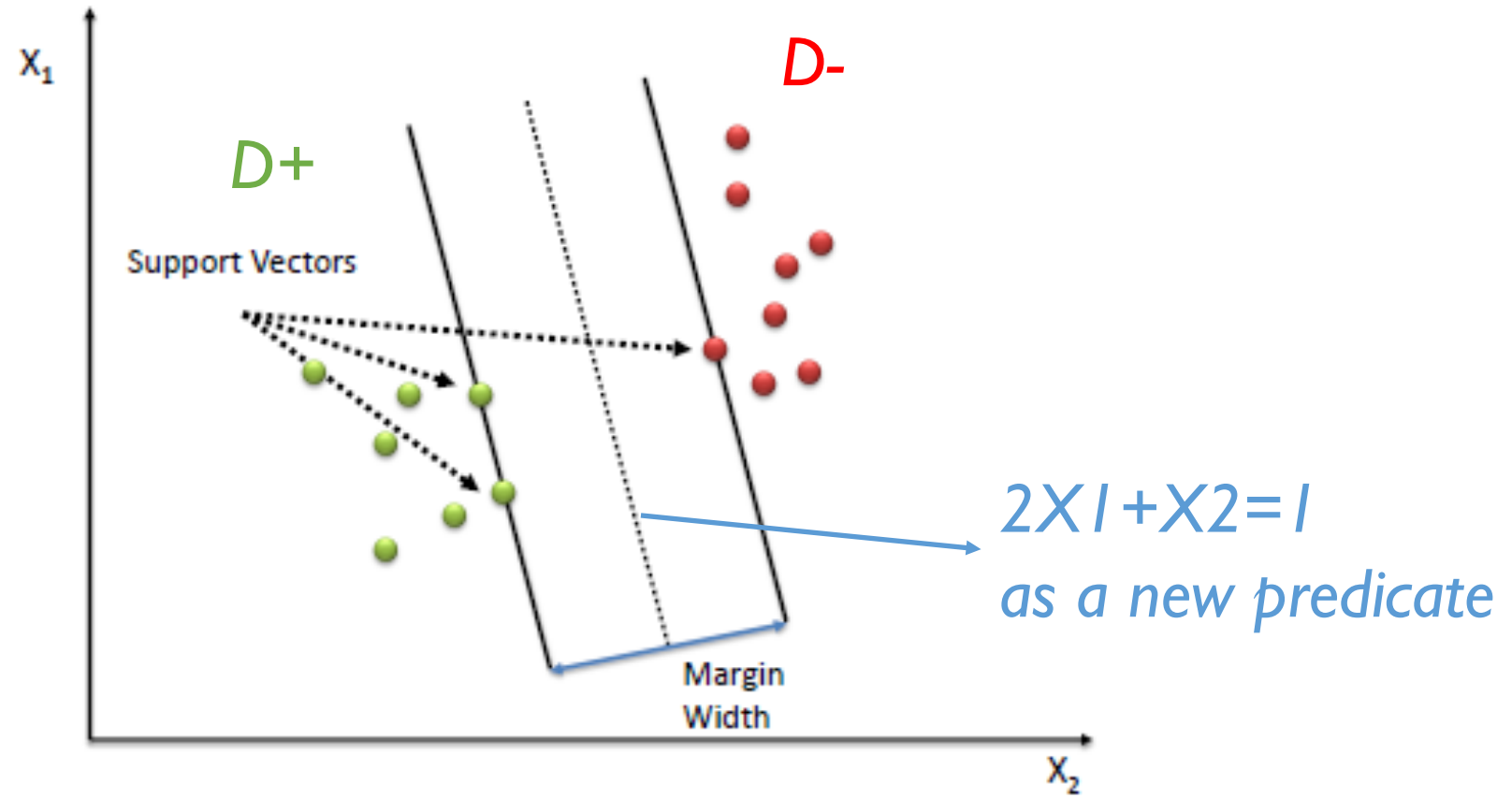
*spurious transition:*  $1 \xrightarrow{1} 1$

*system log:*      0   0   1   0   0   0   1   1   0   0   ...



D-                      D+

# Learn a new predicate by SVM



# Summary of result

<i>47 properties</i>	<i>19 never violated</i>
	<i>24 verified</i>
	<i>4 violations</i>

*details at <https://github.com/wang-jingyi/Ziqian>*

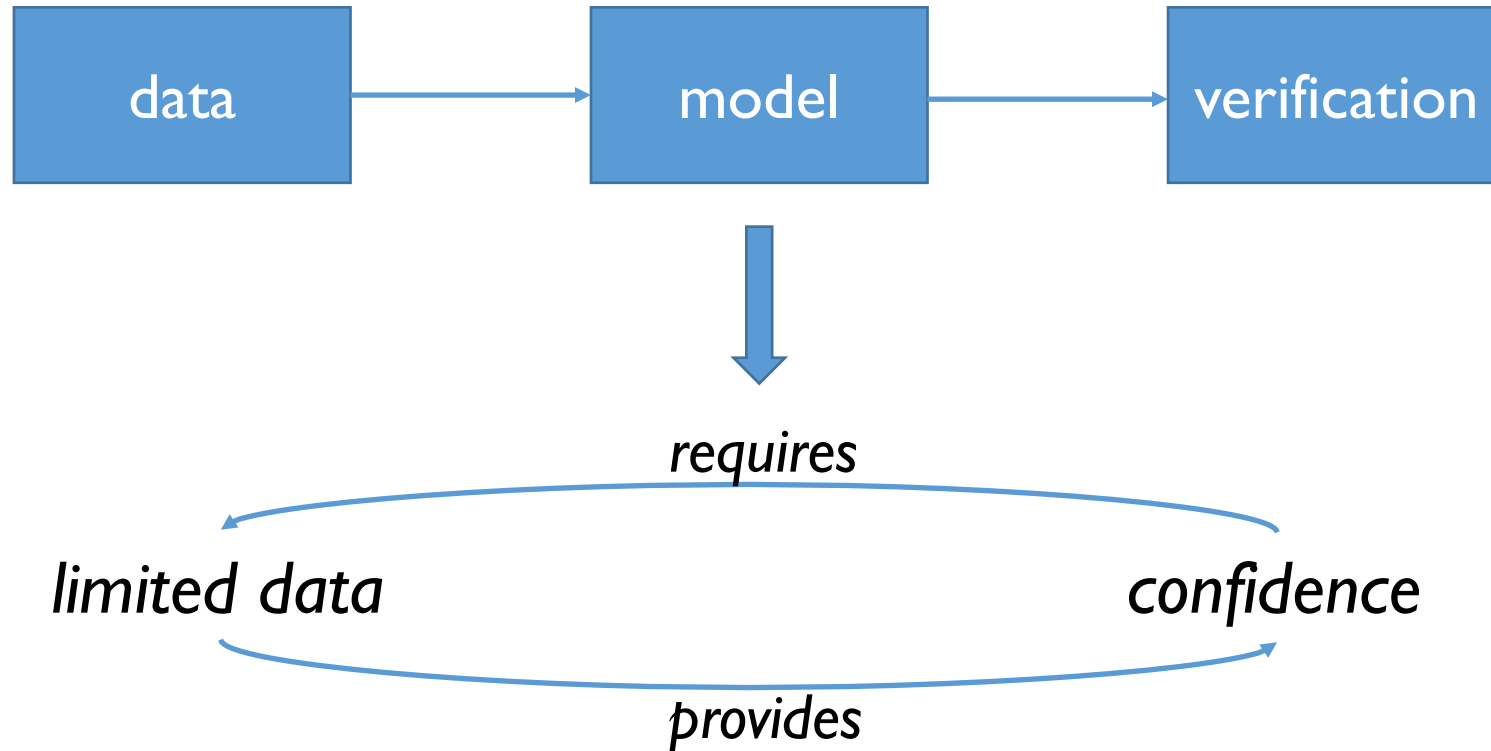
# Observations

- *the learned models are precise*
- *the learned models are small*
  - *2 to 208 states*
- *group behaviors*
  - *$FIT401 < 1.5$ ,  $FIT502 < 1.1$ ,  $FIT503 < 0.7$ ,  $FIT504 < 0.25$*
  - *$FIT501 < 1$ ,  $PIT501 < 20$ ,  $PIT503 < 10$*
- *safety violations*
  - *$AIT401 > 100$ ,  $PIT501 > 30$ ,  $PIT502 > 0.2$ ,  $PIT503 > 20$*
  - *high in the training log, 1 in learned model and the testing log*

# Discussions

- *safety margin: 20%*
- *hyper parameter in the learning algorithm*
- *sub-sampling*
- *limited data*

# Ongoing and future work



some preliminary results at [https://link.springer.com/chapter/10.1007/978-3-319-66335-7\\_23](https://link.springer.com/chapter/10.1007/978-3-319-66335-7_23)

# Our facilities are available!



# Take-home points

- *experience on **automatic verification** of a real-world CPS from data*
- *applied an **abstraction-based learning algorithm***
- *the learned models are potentially **used for subsequent analysis***