## Information Integration and Communication in Heterogeneous Internet of Things: A Stochastic Geometry-Based Analytical Modeling\*

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#### ABSTRACT

The heterogeneous Internet of Things (HetIoT), consisting of densely coexisted cellular and device-to-device (D2D) devices, has become a foundational component of 5th generation and beyond networks. Considering the high density of devices, guard zones around base stations (BSs) are introduced to mitigate interference with each other. However, previous studies neglect the impact of cellular devices on D2D transmissions, which is also crucial in HetIoT. To address this issue, this paper presents the use of guard zones around both transmitting BSs and cellular devices. By leveraging a stochastic geometry approach, a novel spatial distribution model is constructed to effectively capture the location randomness and interdependencies between BSs, cellular, and D2D devices. Based on this spatial model, an analytical model is developed to derive expressions for the successful transmission probabilities of BSs, cellular, and D2D devices. This model accounts for the inherent randomness and interrelations between cellular and D2D transmissions, while also characterizing the complex mutual interference resulting from the two types of guard zones. Extensive Monte Carlo simulations confirm the high accuracy of the proposed theoretical model. This analytical model provides practical guidance for practitioners in selecting suitable parameter configurations to enhance performance in HetIoT.

#### 1. Introduction

#### 1.1. Background

In the era of 5th generation (5G) and beyond 5G (B5G) technologies, the growing demand for the Internet of Things (IoT) is driving an exponential increase in the number of connected IoT devices, expected to reach 55 to 80 billion by 2025 [1, 2, 3]. These devices have become ubiquitous, deployed across a wide range of applications including smart cities, environmental monitoring, industrial automation [4], security systems [5], advanced manufacturing [6], and intelligent transportation [7], as illustrated in Fig. 1. They continuously sense and collect various types of data—industrial, environmental, and personal—while transmitting, exchanging, and integrating these data for further processing, significantly enhancing daily lives. Furthermore, 5G/B5G technologies are anticipated to support nearly 10 million devices per km<sup>2</sup> outdoors and 1,000 devices per 100 m<sup>2</sup> indoors [5]. Consequently, it is foreseeable that different IoT devices under diverse communication networks will coexist, thus forming a heterogeneous IoT (HetIoT) system [4, 8].

An HetIoT system integrates various communication networks, including cellular-enabled IoT networks (e.g.,

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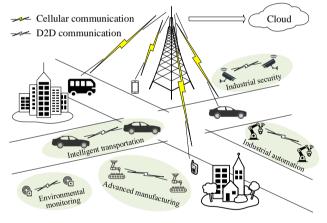


Figure 1: The architecture of information integration and communication in a typical HetloT.

LTE-M [9] and NB-IoT [10]) and self-organized Device-to-Device (D2D) networks (e.g., Zigbee [11] and WiFi HaLow [12]). HetIoT devices encompass a wide range of machines and sensors supported by these diverse networks, such as wearable devices and monitoring sensors. To sum up, IoT devices primarily operate in two categories of networks: cellular networks and D2D networks. We refer to HetIoT devices operating in these two networks as cellular devices and D2D devices, respectively.

In a typical HetIoT system, IoT devices can reuse the licensed cellular spectrum to communicate with one another, either with or without the involvement of base stations (BSs) and the core network. Additionally, unlike the traditional half-duplex (HD) mode, where devices can either transmit or

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receive signals at any given time, advancements in hardware have enabled devices to operate in in-band full-duplex (FD) mode, allowing simultaneous transmission and reception of signals on the same time/frequency resource blocks [13, 14]. Undoubtedly, as the two emerging innovations in 5G/B5G, the integration of D2D communication and FD technology holds significant promise for improving spectrum efficiency and enhancing network capacity [15]. However, the inherent broadcast nature of the wireless medium means that largescale D2D communication can lead to substantial internetwork interference. Moreover, since both cellular and D2D devices are often randomly distributed in space, these mutual interferences exhibit notable spatial randomness and are influenced by location-dependent factors such as large- and small-scale fading. Therefore, effective interference management strategies are crucial for achieving higher system performance in such environments.

To effectively manage interference, establishing guard zones (also known as exclusion zones) is a widely adopted strategy across various network types. A guard zone is typically defined as a circular region with a fixed radius around each transmitter, within which other devices are prohibited from transmitting. This setup ensures sufficient spatial separation to mitigate mutual interference by inhibiting potential concurrent transmissions. In the context of HetIoT, which incorporate both cellular and D2D transmissions, although previous studies have primarily focused on establishing guard zones around BSs to alleviate interference from cellular transmissions [16], there is a growing recognition of the significant impact that interference from large-scale D2D transmissions can have on cellular communications (i.e., the footnote of [17]). Thus, integrating guard zones around both BSs and cellular devices is essential, considering the interactions between cellular and D2D devices. This comprehensive approach is necessary to ensure effective interference management within HetIoT.

#### 1.2. Motivation

Despite advancements in integrating guard zones around both BSs and cellular devices, as well as the flexible deployment of D2D communications with devices operating in either HD or FD mode, implementing these features in HetIoT introduces significant complexities and randomness in terms of interference and spatial distribution. To address this issue, stochastic geometry—a powerful analytical tool that provides a probabilistic framework for modeling spatial point processes—has emerged as an effective method for capturing the intricate spatial configurations of wireless networks [18, 19]. Although stochastic geometry has been applied to cellular and D2D scenarios separately, limited research has explored their interactions in the context of guard zones.

In this study, we aim to fill the gap by leveraging stochastic geometry to analyze system performance in HetIoT. In particular, we need to characterize the spatial distributions of BSs, cellular devices, and D2D devices and analyze critical

performance metrics in HetloT. However, to achieve this goal, we need to overcome the following challenges:

- Firstly, the combination of D2D communication with in-band FD capabilities enables simultaneous transmission and reception, significantly enhancing spectral efficiency. However, as the number of D2D devices adopting FD communication increases, the resulting interference can degrade the performance of cellular communication. Therefore, it is crucial to develop an effective FD mode selection strategy that efficiently mitigates D2D interference by regulating the number of D2D devices utilizing in-band FD communication.
- Secondly, while establishing guard zones around BSs can effectively reduce interference from cellular transmissions, the impact of large-scale D2D transmissions on cellular communications cannot be overlooked. Thus, integrating guard zones around both transmitting BSs and cellular devices offers a promising approach to alleviating overall system interference.
- Finally, the random nature of cellular transmissions leads to the formation of random guard zones around transmitting BSs and cellular devices, which subsequently contributes to random D2D transmissions. This randomness complicates the modeling of the spatial distribution of cellular and D2D devices, their interdependencies, and the complexity of various spatial interferences.

Modeling and analyzing the performance of an Het-IoT requires jointly considering the aforementioned factors. However, existing analytical models often fall short of capturing all these complexities comprehensively [13, 14, 17, 20]. This gap motivates us to develop a novel analytical modeling that accurately analyzes performance and offers configuration insights to enhance overall system efficiency.

#### 1.3. Our contributions

Consider a typical HetIoT, characterized by: 1) densely coexisting cellular and D2D devices; 2) guard zones established around randomly distributed BSs and cellular devices; and 3) D2D devices that can operate in either FD or HD mode for D2D transmissions. Within this context, we build a stochastic geometry-based analytical model to investigate information integration and communication in this network, and theoretically analyze the successful transmission probabilities (STPs) for both cellular and D2D transmissions. Taking all these factors into account, the key contributions of this study are summarized as follows:

 Establish a novel spatial distribution model for Het-IoT. The majority of previous work simply models the spatial distribution of BSs, cellular, and D2D devices by two homogeneous Poisson point processes (HPPPs) [13, 14]. However, their work cannot model the accurate network topology of our focused HetIoT with transmission probabilities and guard zones aroud transmitting devices. Our work applies thinning and approximation operations to HPPPs to cater to the probabilities in transmitting devices. Moreover, we use the superposition of two Poisson hole processes (PHPs) to model the activated D2D devices outside two distinct types of guard zones. This spatial model enables a precise and realistic representation of the network topology.

- Develop a comprehensive analytical model for Het-IoT. The developed analytical model derives accurate expressions for the STPs of both cellular and D2D transmissions, incorporating critical system parameters such as the densities of transmitting cellular devices, D2D devices in HD/FD mode, and the guard zone radius. This model allows us to capture the inherent randomness and interdependencies of cellular and D2D transmissions, as well as the complex spatial interferences within the network.
- Conduct extensive simulations for verification. Extensive Monte Carlo simulations are conducted, which confirm the accuracy of the analytical modeling. These simulation results provide valuable insights for practitioners (e.g., network operators or engineers) in selecting suitable parameter configurations to enhance performance in HetIoT.

The rest of this paper is organized as follows. Section 2 reviews the related work. Section 3 presents the system model of the HetIoT. Section 4 derives a stochastic geometry-based analytical model for three STPs in the HetIoT. Section 5 validates the accuracy of the theoretical model through extensive Monte Carlo simulations. Finally, Section 6 concludes this paper and presents some discussions.

#### 2. Related Work

The HetloT, encompassing large-scale cellular and D2D devices, has emerged as a critical component in 5G/B5G networks. Extensive research has been conducted on the performance modeling and analysis of HetloT, addressing various aspects such as covertness and secrecy [5, 21], resource allocation [22, 23], duplex mode selection [13, 14], and interference management (e.g., via guard zone), among others. In this context, the focus of this work is primarily on the existing literature on performance modeling in HetloT, particularly studies that explore HD/FD-based and guard zone-based approaches, with an emphasis on distinguishing their differences.

#### 2.1. Performance modeling of HetIoT in HD/FD

In HetIoT, full-duplex technology enables devices to simultaneously transmit and receive signals on the same time/frequency resource blocks, thereby improving spectrum efficiency. In this context, previous literature considers two modes of full-duplex technology in HetIoT devices, i.e.,

HD and FD modes. In [24, 25], the authors investigate an HetIoT composed of HD D2D and cellular devices, employing a stochastic geometry approach to model the spatial randomness of these devices and analyze the success probabilities for both cellular and D2D links. However, their models are not applicable to scenarios where D2D devices operate with random HD/FD mode selection. In [13], they propose a fine-tuned selection criterion for HD/FD mode operation in networks where D2D and cellular devices coexist. They develop a stochastic geometry-based model to calculate the outage probabilities of cellular and D2D devices. Similarly, Badri et al. in [14] analyze the interference experienced by cellular users from D2D devices using a stochastic geometry approach, where each D2D device can optimally choose between HD and FD mode to ensure the quality of service for cellular users.

Although the above studies consider HD/FD mode selection devices for spectrum efficiency and model HetIoT in stochastic geometry. However, they cannot solve the interference issues among cellular and D2D transmissions. This is also a crucial problem in HetIoT, i.e., the devices in different network types suffer interference with each other because of their co-existence.

### 2.2. Performance modeling of guard-zone based HetIoT

Establishing guard zones is a widely adopted strategy to mitigate interference across various network types, including ad hoc networks [26, 27], UAV networks [28], and D2D-enabled HetIoT [16]. Some related work, guard zones are generally positioned around both cellular and D2D devices, as discussed below. Establishing guard zones is a widely adopted strategy to mitigate interference across various network types, including ad hoc networks [26, 27], UAV networks [28], and D2D-enabled HetIoT [16]. Some studies explored the use of guard zones in HetIoT. For instance, [29] develops a stochastic geometry-based theoretical model study the STPs for both cellular and D2D devices in D2D underlaid cellular network. In this network, guard zones are implemented centered around BSs to mitigate the interference. Within these zones, D2D devices are required to operate in cellular mode; outside the zones, they operate in D2D mode. In [20], they investigate a D2D and cellular coexisting network, where D2D devices outside the guard zones around BSs are active, while cellular devices are divided into "central" users within the guard zones and "edge" users outside them. Utilizing stochastic geometry, their model characterize the location randomness of various types devices. Similarly, Chen et al. in [30] combine SIRaware link activation with guard zones around BSs to evaluate the impact of guard zone radius and SIR threshold on D2D throughput and cellular coverage. Shi et al. in [31] set exclusion regions around cellular users in D2D-aided uplink cellular networks and analyze the coverage probabilities for both cellular and D2D devices using a stochastic geometry approach. Beyond guard zones around BSs, other works,

such as [17, 32], establish guard zones around D2D transmitters, primarily aiming to reduce interference from cellular transmissions.

In summary, the majority of previous studies focus on setting guard zones around BSs to reduce interference from transmitting BSs on other network components, they often overlook the impact of transmitting cellular devices on D2D communications. In a dense HetIoT network, cellular and D2D devices closely coexist, the interference generated by transmitting cellular devices can significantly affect D2D transmission performance. In comparison, our work considers two distinct types of guard zones around both BSs and cellular devices to ensure sufficient spatial separation between cellular and D2D transmissions.

#### 3. System Model

#### 3.1. Network deployment

Fig. 2 illustrates a guard-zone-based HetIoT comprising base stations (BSs), cellular devices, and D2D devices. The BSs, cellular devices, and D2D devices are assumed to be randomly distributed according to three independent homogeneous Poisson point processes (HPPPs).  $\Phi_b, \Phi_c, \Phi_d$  with densities  $\lambda_b, \lambda_c, \lambda_d$  ( $\lambda_c \gg \lambda_b, \lambda_d \gg \lambda_b$ ), respectively. Each cellular device is associated with its geographically nearest BS, thereby a whole cellular network forms a topology of a Voronoi tessellation, as shown in Fig. 2(a). Let  $S_v$  be the area of a Voronoi cell, then  $\mathbb{E}\left[S_v\right] = 1/\lambda_b$  [19]. Each Voronoi cell is approximated as a circle with radius  $R_v$  [33], then  $R_v = \sqrt{\mathbb{E}\left[S_v\right]/\pi} = \sqrt{1/\pi\lambda_b}$ . In HetIoT, the BSs, cellular devices and D2D devices transmit data with a fixed transmission power  $P_b, P_c$  and  $P_d$ , respectively.

Considering the spectrum limit, all cellular transmissions and D2D transmissions among the three devices share the same band, then causing interference with each other. In particular, cellular transmissions between BSs and cellular devices, including both downlink (from BS to cellular device) and uplink (from cellular device to BS) transmissions, are performed in a Voronoi cell. Given one carrier in a Voronoi cell, only a downlink or uplink transmission can in use at the same time. As in Fig. 2(a) shows, the cellular devices in the Voronoi cell of a BS under transmission cannot initiate a new transmission via the same carrier; in contrast, the cellular devices in a Voronoi cell can transmit data to the BS when it is not under transmission. For D2D transmissions, we assume that a D2D device may choose to operate in either HD or FD mode with a maximum transmission distance  $d_d$ . Since the cellular and D2D transmissions may interfere with each other, guard zones at the sides of transmitting BSs and cellular devices are set. In the guard zone centered at each transmitting BS with radius  $d_h$  or in the guard zone centered at each transmitting cellular device with radius  $d_c$ , the D2D devices cannot be activated to perform any transmission. As Fig. 2(a) shows, D2D devices in the guard zones of transmitting BSs or cellular devices are nonactivated; in contrast, D2D devices outside the guard zones

Table 1
Key notations and their descriptions.

Notations	Descriptions of BSs' Parameters								
$\Phi_b, \lambda_b$	HPPP of BSs with density $\lambda_b$								
$\Phi^t_b, \lambda^t_b$	HPPP of transmitting BSs with density $\lambda_b^t$								
$p_b^i$	Transmission probability of each BS								
$d_b$	Radius of BS's guard zone Distance between BS and cellular device with PDF								
$R_b$									
$I_b^*$	$f_{R_b}(r_b)$ Interference at BS from transmitting devices								
Notations	Descriptions of cellular devices' Parameters								
$\Phi_c, \lambda_c$	HPPP of cellular devices with density $\lambda_c$								
$\Phi_{\underline{\mathcal{C}}_{t}}^{t}, \lambda_{c}^{t}$	Point process of transmitting cellular devices with $\lambda_c^t$								
$\Phi_c^t$	Approximated HPPP of activated cellular devices								
$p_t$	Probability that cellular device accesses the channel								
$p_c^t$	Transmission probability of each cellular device								
$d_c$	Radius of cellular device's guard zone								
$R_c$	Distance from cellular device to BS with PDF $f_{R_c}(r_c)$								
$I_c^*$	Interference at cellular device from transmitting de-								
	vices								
Notations	Descriptions of D2D devices' Parameters								
$\Phi_d, \lambda_d$	HPPP of D2D devices with density $\lambda_d$								
$\Phi^a_d, \lambda^a_d$	Point process of activated D2D devices with density								
~	$\lambda_d^a$								
$\widetilde{\Phi}^a_d$	Approximated HPPP of activated D2D devices								
$\Phi_H$ , $\lambda_H$	HPPP of activated HD D2D devices with density $\lambda_H$								
$\Phi_F^{}, \lambda_F^{} \ \Phi_H^t, \lambda_H^t$	HPPP of activated FD D2D devices with density $\lambda_F$								
$\Phi_H^t, \lambda_H^t$	HPPP of transmitting HD D2D devices with density								
	$\lambda_H^t$								
$\Phi_F^t, \lambda_F^t$	HPPP of transmitting FD D2D devices with density								
m /m	$\lambda_F^I$								
$\mathbb{P}_b/\mathbb{P}_c$	Probability that a D2D device locates outside the guard zones of transmitting BSs/CUs								
n	Probability that a D2D device is activated								
$rac{p_a}{p_H/p_F}$	Probability that a D2D device operates in HD/FD								
PH/PF	mode								
$d_d$	Maximum transmission distance of each D2D device								
$R_d$	Distance between two D2D devices with PDF $f_{R_d}(r_d)$								
ĸ	Self-interference cancellation factor								
$I_d^*$	Interference at D2D device from transmitting devices								
Notations	Descriptions of Public Parameters								
$\mathbb{E}[S_n]$	Mean area of each Voronoi cell $S_v$								
$R_v$	Approximated radius of circular Voronoi cell								
$p_d/p_u$	Probability of DL/UL transmission in a cell								
$\theta/\theta_{dB}$	SINR threshold (unitless/dB)								
H	Channel power fading coefficient								
α	Path-loss exponent								
$\sigma^2$	Additive white Gaussian noise with variance $\sigma^2$								
*	$* \in \{b, c, d\}$ denotes BS, cellular device, D2D device,								
	respectively								
$SINR_*$	Received SINR at *								
$S_*$	*'s received signal power								
$P_*$	Transmission power of each *								
$\mathcal{P}_*$	Successful transmission probability of *								

are activated. The main notations used in this paper and their descriptions are summarized in Table 1.

#### 3.2. Channel model

Without loss of generality, all the wireless signals in cellular and D2D transmissions undergo both large-scale and small-scale channel fading. The former is characterized by

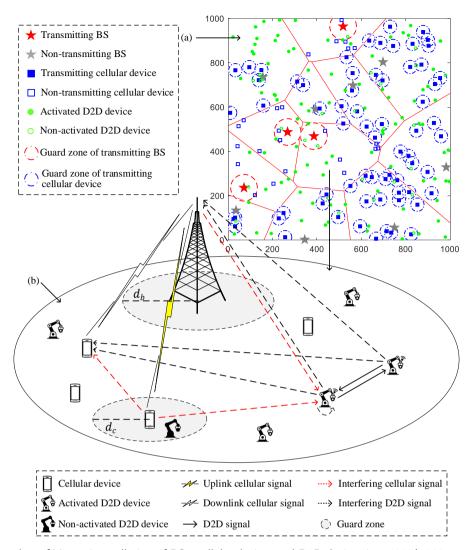


Figure 2: (a) A snapshot of Voronoi tessellation of BSs, cellular devices and D2D devices in a 1000\*1000 m square region, where  $\lambda_b=10$  BSs km<sup>-2</sup>,  $\lambda_c=100$  cellular devices km<sup>-2</sup>,  $\lambda_d=100$  D2D devices km<sup>-2</sup>,  $d_b=60$  m,  $d_c=30$  m,  $p_d=0.5$ ,  $p_t=1.0$ . (b) A cell of a guard-zone based HetloT.

the distance-dependent power-law path loss model in which the signal power decays at the rate  $R^{-\alpha}$  [34], where R is Euclidean distance between a transmitter and a receiver, and  $\alpha$  is the path-loss exponent which usually satisfies  $2 < \alpha < 6$  [35]. The latter is modeled by an independent and identically distributed (i.i.d.) channel power gain H, which follows exponential distribution with mean  $1/\mu$ , i.e.,  $H \sim \exp(\mu)$  [36, 37]. Besides, the noise at the receiver is modeled as an additive white Gaussian variable with zero mean and variance  $\sigma^2$  [38, 39].

#### 3.3. Density of transmitting cellular devices

Recall that both downlink and uplink cellular transmissions are performed in a Voronoi cell. In all cellular transmissions of HetIoT, let  $p_d$  and  $p_u$  be the distribution ratio of downlink and uplink transmissions, respectively. Then  $p_d + p_u = 1$ . The transmission probability of a BS can be given by the downlink transmission ratio  $p_b^t = p_d$ . Accordingly, we can apply the thinning operation to the BS

distribution  $\Phi_b$  and generate a new distribution  $\Phi_b^t$  with density  $\lambda_b^t$  for all BSs under transmissions (we called it transmitting BSs). The value of  $\lambda_b^t$  is given by  $\lambda_b^t = p_b^t \lambda_b$  [18, 19]. For the uplink transmissions, all cellular devices adopt ALOHA mechanism to access the channel with probability  $p_t$  [14]. Hence, the transmission probability of each cellular device  $p_c^t = p_u p_t$ . After excluding the cellular devices in the Voronoi cell of each transmitting BS and the cellular devices that do not attempt to transmit data, the remained transmitting cellular devices form a general point process  $\Phi_c^t$  with density  $\lambda_c^t$ . The density of transmitting cellular devices  $\lambda_c^t$  can be given by  $\lambda_c^t = p_c^t \lambda_c^u$ .

#### 3.4. Density of transmitting D2D devices

In D2D transmissions, a D2D device can be activated under two necessary conditions:

- C1: A D2D device is located outside the guard zones of transmitting BSs, the probability of which is denoted by P<sub>b</sub>; and
- C2: A D2D device is located outside the guard zones of transmitting cellular devices, the probability of which is denoted by  $\mathbb{P}_c$ .

The conditions C1 and C1 are independent of each other. Let  $p_a$  be the activated probability of a D2D device, which is given by

$$p_a = \mathbb{P}(\mathbf{C1}, \mathbf{C2}) = \mathbb{P}(\mathbf{C1})\mathbb{P}(\mathbf{C2}) = \mathbb{P}_b\mathbb{P}_c. \tag{1}$$

Next we need to calculate  $\mathbb{P}_b$  and  $\mathbb{P}_c$ , respectively.

Given the distributions of transmitting BSs  $\Phi_b^t$  and and the D2D devices  $\Phi_d$ , the D2D devices outside the guard zones (i.e., holes) centered at transmitting BSs with radius  $d_b$  form a Poisson hole process (PHP)  $\Phi_d^b$  [18, 19]. In  $\Phi_d^b$ , the activated probability a D2D device  $\mathbb{P}_b$  is given by

$$\mathbb{P}_b = \exp\left(-\lambda_b^t \pi d_b^2\right). \tag{2}$$

We use an HPPP  $\widetilde{\Phi}_c^t$  with the density  $\lambda_c^t$  to approximate the general point process  $\Phi_c^t$  of transmitting cellular devices  $\widetilde{\Phi}_c^t$  and D2D devices  $\Phi_d$ , the D2D devices outside the guard zones (i.e., holes) centered at transmitting cellular devices with radius  $d_c$  form another PHP  $\Phi_d^c$ . In  $\Phi_d^c$ , the activated probability a D2D device  $\mathbb{P}_c$  is given by

$$\mathbb{P}_c = \exp\left(-\lambda_c^t \pi d_c^2\right). \tag{3}$$

Substituting (22) and (11) into (4), we have

$$p_a = \mathbb{P}_b \mathbb{P}_c = \exp\left(-\pi \left(\lambda_b^t d_b^2 + \lambda_c^u d_a^2\right)\right). \tag{4}$$

According to (4), we can see that the activated D2D devices form a point process  $\Phi^a_d$  with density  $\lambda^a_d$  given by  $\lambda^a_d = p_a \lambda_d$ . A D2D device is assumed to operate in HD and FD with probability  $p_H$  and  $p_F$ , respectively, where  $p_H + p_F = 1$ . Let an HPPP  $\widetilde{\Phi}^a_d$  with the density  $\lambda^a_d$  approximate the general point process  $\Phi^a_d$  of activated D2D devices [40].  $\widetilde{\Phi}^a_d$  is the union of two independent PPPs  $\Phi_H$  of activated HD D2D devices with density  $\lambda_H$  and  $\Phi_F$  of activated FD D2D devices with density  $\lambda_F$  [14]. Then we have

$$\widetilde{\Phi}_d^a = \Phi_H \cup \Phi_F, \lambda_H = p_H \cdot \lambda_d^a, \lambda_F = p_F \cdot \lambda_d^a.$$
(5)

We consider a general case in D2D transmissions, i.e., half of the HD D2D devices are transmitters and half of them are receivers [14]. The transmitting HD D2D devices form an HPPP  $\Phi_H^t$  with density  $\lambda_H^t$ , where  $\lambda_H^t = \lambda_H/2$ . For FD mode D2D devices, all users are transceivers at the same time. The transmitting FD D2D devices form an HPPP  $\Phi_F^t$  with density  $\lambda_F^t$ , where  $\lambda_F^t = \lambda_F$ .

#### 4. Analytical Model

This section develops a stochastic geometry-based analytical model to derive the expressions of STPs for the BSs, cellular and D2D transmissions.

We first introduce a general expression of the STP. Consider a wireless transmission signal from a tagged transmitter x to a tagged receiver y within a distance  $R_x$ , where the location distribution of x follows the point process  $\Phi$ , and  $R_x \in [0, \hat{R}_x]$ . Let  $P_x$  and  $H_x$  denote the transmission power of x and the channel power gain between x and y, respectively. Let SINR $_y$  denote the signal-to-interference-plus-noise ratio (SINR) between y received x's signal power  $S_y$  and its suffered interference signal power  $I_y$  plus noise power  $\sigma^2$ . The value of SINR $_y$  can be given by [41, 42]

$$SINR_y \left( R_x, I_y \right) = \frac{S_y}{I_v + \sigma^2} = \frac{P_x H_x R_x^{-\alpha}}{I_v + \sigma^2}.$$
 (6)

In (6),  $I_y = \sum_{x' \in \Phi'} P_{x'} H_{x'} R_{x'}^{-\alpha}$ , where  $x' \in \Phi'$  is the interfering transmitter with set  $\Phi'$ ,  $P_{x'}$  denotes the transmission power of x',  $H_{x'}$  and  $R_{x'}$  are the channel power gain and the transmission distance between x' and y, respectively.

For the tagged receiver y, the signal from x can be successfully received and decoded only when SINR $_y$  (Unitless) at y exceeds a certain SINR threshold  $\theta_{dB}$  (in decibel (dB)) <sup>2</sup>. Let  $\mathbb{P}_x$  denote the conditional success probability (CSP) of x's transmission, which is given by

$$\mathbb{P}_{x} = \mathbb{P}\left(\mathrm{SINR}_{y}\left(R_{x}, I_{y}\right) > \theta \middle| \Phi\right). \tag{7}$$

Let  $\mathcal{P}_x$  denote the STP of x. The overall network performance can be defined as the mean value of  $\mathbb{P}_x$ , i.e.,

$$\begin{split} \mathcal{P}_{x} &= \mathbb{E}_{\Phi} \left[ \mathbb{P}_{x} \middle| \Phi \right] \\ &= \mathbb{E}_{R_{x}, I_{y}} \left[ \mathbb{P} \left( \operatorname{SINR}_{y} \left( R_{x}, I_{y} \right) > \theta \right) \middle| \Phi \right] \\ &= \int_{0}^{\hat{R}_{x}} \mathbb{P} \left( \operatorname{SINR}_{y} \left( r_{x}, I_{y} \right) > \theta \middle| \Phi \right) \cdot f_{R_{x}} \left( r_{x} \right) \mathrm{d}r_{x}, \end{split} \tag{8}$$

where  $f_{R_x}\left(r_x\right)$  is the probability density function (PDF) of  $R_x$ . In (8),  $\mathbb{P}\left(\mathrm{SINR}_y\left(r_x,I_y\right)>\theta\middle|\Phi\right)$  can be further calculated as follows.

$$\mathbb{P}\left(\operatorname{SINR}_{y}\left(r_{x}, I_{y}\right) > \theta \middle| \Phi\right) = \mathbb{P}\left(\frac{P_{x}H_{x}r_{x}^{-\alpha}}{I_{y} + \sigma^{2}} > \theta \middle| \Phi\right)$$

$$= \mathbb{P}\left(H_{x} > \frac{\theta r_{x}^{\alpha}}{P_{x}}\left(I_{y} + \sigma^{2}\right) \middle| \Phi\right)$$

$$\stackrel{(a)}{=} \mathbb{E}_{I_{y}}\left[\exp\left(\frac{\mu\theta r_{x}^{\alpha}}{P_{x}}\left(I_{y} + \sigma^{2}\right)\right)\right]$$

$$= \exp(-s\sigma^{2})\mathbb{E}_{I_{y}}\left[\exp(-sI_{y})\right]$$

$$\stackrel{(b)}{=} \exp(-s\sigma^{2})\mathcal{L}_{I_{y}}(s),$$

$$(9)$$

<sup>&</sup>lt;sup>1</sup>The approximation can be found in many existing works [40]. The approximated PPP is inhomogeneous with constant positive density.

<sup>&</sup>lt;sup>2</sup>The real ratio value of  $\theta_{dB}$  is given by  $\theta = 10^{\theta_{dB}/10}$  (Unitless).

where  $s = \mu \theta r_x^\alpha/P_x$ ,  $\mathbb{E}_X [f(X)]$  is the expectation of f(X) with respect to X. (a) is resulted from the exponential distribution of  $H_x$  with mean  $1/\mu^3$ , i.e.,  $H_x \sim \exp(\mu)$ . According to the cumulative distribution function of an exponential distribution, if  $f_{H_x}(h_x) = \mu e^{-\mu h_x}$ ,  $P(H_x > h_0) = 1 - F_{H_x}(h_0) = 1 - P(H_x \le h_0) = 1 - \int_0^{h_0} \mu e^{-\mu h_x} dh_x = \exp\left(-\mu h_0\right)$ . (b) comes from the definition of Laplace transform (LT) of interference  $I_y$ , evaluated at s, that is  $\mathcal{L}_{I_y}(s) = \mathbb{E}\left[\exp\left(-sI_y\right)\right]$ .

Based on the general expression of STP, we can express the STPs of BSs, cellular devices and D2D devices in sequence.

#### 4.1. STP of BSs $P_b$

In a Voronoi cell, a tagged BS  $b_0$  performs the downlink transmission to a tagged cellular device  $c_0$ . When  $c_0$  receives the desired signal from  $b_0$ , it also suffers from the interference of the other transmitting BSs, cellular devices, D2D devices in HD/FD mode. Let  $\mathrm{SINR}_c\left(R_b,I_c\right)$  denote the SINR at the cellular device  $c_0$ . The value of  $\mathrm{SINR}_c\left(R_b,I_c\right)$  is given by

SINR<sub>c</sub> 
$$(R_b, I_c) = \frac{S_c}{I_c + \sigma^2} = \frac{P_b H_b R_b^{-\alpha}}{I_c^b + I_c^c + I_c^H + I_c^F + \sigma^2},$$
(10)

where  $S_c$ ,  $I_c$  and  $\sigma^2$  are the desired signal power, aggregate interference power and noise power at  $c_0$ , respectively.  $P_b$  is the transmission power of BS,  $H_b$  and  $R_b$  are the channel power gain and transmission distance between  $b_0$  and  $c_0$ , respectively. The terms  $I_c^b$ ,  $I_c^c$ ,  $I_c^H$ ,  $I_c^F$  are interferences caused by the other transmitting BSs, cellular devices, D2D devices in HD/FD mode at  $c_0$ , respectively. Their values are given as follow.

$$\begin{split} I_c^b &= \sum_{i \in \Phi_b^I / \left\{b_0\right\}} P_b H_i R_i^{-\alpha}, I_c^c = \sum_{i \in \Phi_c^I} P_c H_i R_i^{-\alpha}, \\ I_c^H &= \sum_{i \in \Phi_H^I} P_d H_i R_i^{-\alpha}, I_c^F = \sum_{i \in \Phi_F^I} P_d H_i R_i^{-\alpha}. \end{split}$$

Let  $\mathcal{P}_b$  denote the STP of BSs. Based on Eq. (7)-(9),  $\mathcal{P}_b$  can be calculated by

$$\mathcal{P}_{b} = \mathbb{E}_{R_{b},I_{c}} \left[ \mathbb{P} \left( \text{SINR}_{c} \left( R_{b}, I_{c} \right) > \theta \right) \middle| \Phi \right]$$

$$= \int_{0}^{R_{v}} \mathbb{E}_{I_{c}} \left[ \mathbb{P} \left( \text{SINR}_{c} \left( r_{b}, I_{c} \right) > \theta \right) \middle| \cdot f_{R_{b}} \left( r_{b} \right) dr_{b},$$
(11)

where  $f_{R_b}(r_b)$  is PDF of  $R_b$ ,  $R_b \in [0, R_v]$  and  $R_v$  is the approximated radius of circular Voronoi cell. In Eq. (11),  $f_{R_b}(r_b)$  can be calculated by [43]

$$\begin{split} f_{R_b}\left(r_b\right) &= \mathrm{d}\frac{F_{R_b}\left(r_b\right)}{\mathrm{d}r_b} = \mathrm{d}\frac{\mathbb{P}\left(R_b \leq r_b\right)}{\mathrm{d}r_b} \\ &= \mathrm{d}\frac{r_b^2/R_v^2}{\mathrm{d}r_b} = 2r_b/R_v^2 = 2\pi\lambda_b r_b. \end{split}$$

where  $F_{R_b}\left(r_b\right) = \mathbb{P}\left(R_b \leq r_b\right)$  is the cumulative distribution function of  $R_b$  [44, 45]. In Eq. (11), we can calculate  $\mathbb{E}_{I_c}\left[\mathbb{P}\left(\mathrm{SINR}_c\left(r_b,I_c\right)>\theta\right)\right]$  as

$$\mathbb{E}_{I_{c}} \left[ \mathbb{P} \left( \text{SINR}_{c} \left( r_{b}, I_{c} \right) > \theta \right) \right]$$

$$= \mathbb{E}_{I_{c}^{b}, I_{c}^{c}, I_{c}^{H}, I_{c}^{F}} \left[ \exp \left( -\frac{\mu \theta r_{b}^{\alpha}}{P_{b}} \left( I_{c}^{b} + I_{c}^{c} + I_{c}^{H} + I_{c}^{F} + \sigma^{2} \right) \right) \right]$$

$$= \exp \left( -s_{c} \sigma^{2} \right) \mathcal{L}_{I_{c}^{b}} \left( s_{c} \right) \mathcal{L}_{I_{c}^{c}} \left( s_{c} \right) \mathcal{L}_{I_{c}^{H}} \left( s_{c} \right) \mathcal{L}_{I_{c}^{F}} \left( s_{c} \right),$$

$$(12)$$

where  $s_c = \frac{\mu \theta r_b^a}{P_b}$ . The terms  $\mathcal{L}_{I_c^b}\left(s_c\right)$ ,  $\mathcal{L}_{I_c^c}\left(s_c\right)$ ,  $\mathcal{L}_{I_c^H}\left(s_c\right)$ , and  $\mathcal{L}_{I_c^F}\left(s_c\right)$ , are LTs of  $I_c^b$ ,  $c_b^c$ ,  $c_b^H$ , and  $c_b^F$  evaluated at  $s_c$ , respectively. We derive their expressions below.

First, the LT of  $I_c^b$  at  $c_0$  is given by

$$\mathcal{L}_{I_c^b}\left(s_c\right) = \exp\left(-2\pi\lambda_b^t r_b^2 \theta^{2/\alpha} \int_{\frac{R_U}{r_b \theta^{1/\alpha}}}^{\infty} \frac{y}{1 + y^\alpha} dy\right). \tag{13}$$

Proof:

$$\mathcal{L}_{I_{c}^{b}}(s_{c}) = \mathbb{E}_{I_{c}^{b}}\left[\exp\left(-s_{c}I_{c}^{b}\right)\right]$$

$$= \mathbb{E}_{R_{i},H_{i}}\left[\exp\left(-\frac{\mu\theta r_{b}^{\alpha}}{P_{b}}\sum_{i\in\Phi_{b}^{i}/\{b_{0}\}}P_{b}H_{i}R_{i}^{-\alpha}\right)\right]$$

$$\stackrel{(a)}{=}\mathbb{E}_{R_{i}}\left[\mathbb{E}_{H_{i}}\left[\exp\left(-\sum_{i\in\Phi_{b}^{i}/\{b_{0}\}}\mu\theta r_{b}^{\alpha}H_{i}R_{i}^{-\alpha}\right)\right]\right]$$

$$\stackrel{(b)}{=}\mathbb{E}_{R_{i}}\left[\prod_{i\in\Phi_{b}^{i}/\{b_{0}\}}\mathbb{E}_{H_{i}}\left(\exp\left(-\mu\theta r_{b}^{\alpha}R_{i}^{-\alpha}H_{i}\right)\right)\right]$$

$$\stackrel{(c)}{=}\mathbb{E}_{R_{i}}\left[\prod_{i\in\Phi_{b}^{i}/\{b_{0}\}}\int_{0}^{\infty}\exp\left[-\mu\theta r_{b}^{\alpha}R_{i}^{-\alpha}h_{i}\right]f_{H_{i}}\left(h_{i}\right)dh_{i}\right]$$

$$\stackrel{(d)}{=}\mathbb{E}_{R_{i}}\left[\prod_{i\in\Phi_{b}^{i}/\{b_{0}\}}\int_{0}^{\infty}\exp\left[-\mu\theta r_{b}^{\alpha}R_{i}^{-\alpha}h_{i}\right]\mu\exp\left(-\mu h_{i}\right)dh_{i}\right]$$

$$=\mathbb{E}_{R_{i}}\left[\prod_{i\in\Phi_{b}^{i}/\{b_{0}\}}\left(\frac{\mu}{\mu+\mu\theta r_{b}^{\alpha}R_{i}^{-\alpha}}\right)\right]$$

$$(14)$$

In Eq. (14), (a) comes from the fact that  $R_i$  and  $H_i$  are mutually independent. (b) results from the property of exponential distribution, i.e.,  $\exp\left(\sum_i H_i\right) = \prod_i \exp\left(H_i\right)$ . (c) is due to the definition of expectation of  $H_i$ . (d) holds because  $H_i$  follows an exponential distribution with mean  $1/\mu$ , i.e.,  $f_{H_i}\left(h_i\right) = \mu e^{-\mu h_i}$ . According to the probability generation functional (PGFL) of an HPPP  $\Phi$  with density  $\lambda$ , i.e.,  $\mathbb{E}\left[\prod_{x\in\Phi} f(x)\right] = \exp\left(-\lambda \int_{\mathbb{R}^d} (1-f(x)) \,\mathrm{d}x\right)$ , we

<sup>&</sup>lt;sup>3</sup>In our simulation, we set  $\mu = 1$ , i.e.,  $\mu \sim \exp(1)$ .

have

$$\mathcal{L}_{I_{c}^{b}}(s_{c})$$

$$\stackrel{(a)}{=} \exp\left(-\lambda_{b}^{t} \int_{\mathbb{R}^{2}/B(c_{0},R_{v})} \left(1 - \frac{1}{1 + \theta r_{b}^{\alpha} r_{i}^{-\alpha}}\right) dr_{i}\right)$$

$$\stackrel{(b)}{=} \exp\left(-\lambda_{b}^{t} \int_{0}^{2\pi} \int_{R_{v}}^{\infty} \left(\frac{\theta r_{b}^{\alpha} r_{i}^{-\alpha}}{1 + \theta r_{b}^{\alpha} r_{i}^{-\alpha}}\right) r_{i} dr_{i} d\alpha\right)$$

$$= \exp\left(-2\pi \lambda_{b}^{t} \int_{R_{v}}^{\infty} \frac{1}{1 + \frac{1}{\theta r_{b}^{\alpha} r_{i}^{-\alpha}}} r_{i} dr_{i}\right)$$

$$\stackrel{(c)}{=} \exp\left(-2\pi \lambda_{b}^{t} \int_{\frac{R_{v}}{r_{b}\theta^{1/\alpha}}}^{\infty} \left(\frac{1}{1 + y^{\alpha}}\right) y r_{b}^{2} \theta^{2/\alpha} dy\right)$$

$$= \exp\left(-2\pi \lambda_{b}^{t} r_{b}^{2} \theta^{2/\alpha} \int_{\frac{R_{v}}{r_{b}\theta^{1/\alpha}}}^{\infty} \frac{y}{1 + y^{\alpha}} dy\right).$$

$$(15)$$

In Eq. (15)(a),  $R^2/B\left(c_0,R_v\right)$  is the area in which the interfering BSs locate, which excludes the current Voronoi cell that the origin receiving tagged cellular device  $c_0$  locates,  $B\left(c_0,R_v\right)$  is a circular region centered at the origin  $c_0$  with radius  $R_v$ . (b) converts the expression from orthogonal coordinates to polar coordinates, where  $\alpha$  is the polar angle which is uniformly distributed in  $[0,2\pi]$ ; in Eq. (f), the integration limits are from  $R_v$  to  $\infty$  since the closest interfering BS is at least at a distance  $R_v$ . (c) follows by changing the variable  $y^\alpha = \frac{1}{\theta r_b^\alpha r_i^{-\alpha}}$ , i.e,  $y = \frac{r_i}{r_b \theta^{1/\alpha}}$ , hence y belongs to  $\left(\frac{R_v}{r_b \theta^{1/\alpha}}, \infty\right)$ . For the special case  $\alpha = 4$ , we have

$$\mathcal{L}_{I_{c}^{b}}(s_{c}) = \exp\left(-2\pi\lambda_{b}^{t}r_{b}^{2}\sqrt{\theta}\int_{\frac{R}{r_{b}\theta^{1/4}}}^{\infty} \frac{y}{1+y^{4}} dy\right)$$

$$\stackrel{(a)}{=} \exp\left(-\pi\lambda_{b}^{t}r_{b}^{2}\sqrt{\theta} \cdot \left(\frac{\pi}{2} - \tan^{-1}\left(\frac{R^{2}}{r_{b}^{2}\sqrt{\theta}}\right)\right)\right),$$
(16)

where (a) follows  $\int_A^\infty \frac{x}{1+x^\alpha} dx = \frac{1}{4} \left(\pi - 2 \tan^{-1} \left(A^2\right)\right)$ . In (12), the LT of  $I_c^c$  at  $c_0$  is given as

$$\mathcal{L}_{I_c^c}\left(s_c\right) = \exp\left(-\lambda_b^t \left(s_c P_c\right)^{2/\alpha} \cdot \frac{2\pi^2}{\alpha \sin\left(2\pi/\alpha\right)}\right) \tag{17}$$

Proof:

$$\mathcal{L}_{I_{c}^{b}}(s_{c}) = \mathbb{E}_{I_{c}^{b}}\left[\exp\left(-s_{c}I_{c}^{b}\right)\right]$$

$$= \mathbb{E}_{R_{i},H_{i}}\left[\exp\left(-s_{c}\sum_{i\in\Phi_{b}^{t}/\{b_{0}\}}P_{c}H_{i}R_{i}^{-\alpha}\right)\right]$$

$$= \mathbb{E}_{R_{i}}\left[\mathbb{E}_{H_{i}}\left[\exp\left(-\sum_{i\in\Phi_{b}^{t}/\{b_{0}\}}s_{c}P_{c}H_{i}R_{i}^{-\alpha}\right)\right]\right]$$

$$\stackrel{(a)}{=}\exp\left(-\lambda_{c}^{t}\int_{\mathbb{R}^{2}}\left(1 - \frac{1}{1 + s_{c}P_{c}r_{i}^{-\alpha}}\right)dr_{i}\right)$$

$$\stackrel{(b)}{=}\exp\left(-\lambda_{c}^{t}\int_{0}^{2\pi}\int_{0}^{\infty}\left(\frac{s_{c}P_{c}r_{i}^{-\alpha}}{1 + s_{c}P_{c}r_{i}^{-\alpha}}\right)r_{i}dr_{i}d\alpha\right)$$

$$= \exp\left(-2\pi\lambda_{c}^{t}\left(s_{c}P_{c}\right)^{2/\alpha}\int_{0}^{\infty}\frac{y}{1 + y^{\alpha}}dy\right)$$

$$\stackrel{(c)}{=}\exp\left(-\pi\lambda_{c}^{t}\left(s_{c}P_{c}\right)^{2/\alpha}\cdot\frac{2}{\alpha}\cdot\Gamma\left(\frac{2}{\alpha}\right)\cdot\Gamma\left(1 - \frac{2}{\alpha}\right)\right)$$

$$\stackrel{(d)}{=}\exp\left(-\lambda_{c}^{t}\left(s_{c}P_{c}\right)^{2/\alpha}\cdot\frac{2\pi^{2}}{\alpha\sin\left(2\pi/\alpha\right)}\right)$$

In the above proof, (a) follows from the probability generation functional (PGFL) of HPPP; in (a),  $R^2$  is the area in which the interfering cellular devices locate. (b) converts the expression from orthogonal coordinates to polar coordinates, where  $\alpha$  is the polar angle which is uniformly distributed in  $[0, 2\pi]$ . (c) can refer to Eq. 3.241.4 in [46]. (d) follows from the Euler's reflection formula  $\Gamma(x) \cdot \Gamma(1-x) = \frac{\pi}{\sin(\pi x)}$  where  $\Gamma(x)$  is the complete gamma function  $\Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt$ .

Following the similar derivation process in  $\mathcal{L}_{I_c^c}$ , the LT of  $I_c^H$  and  $I_c^F$  at  $c_0$  are given as follows.

$$\mathcal{L}_{I_c^H}\left(s_c\right) = \exp\left(-\lambda_H^t \left(s_c P_d\right)^{2/\alpha} \cdot \frac{2\pi^2}{\alpha \sin\left(2\pi/\alpha\right)}\right),\tag{19}$$

$$\mathcal{L}_{I_c^F}\left(s_c\right) = \exp\left(-\lambda_F^t \left(s_c P_d\right)^{2/\alpha} \cdot \frac{2\pi^2}{\alpha \sin\left(2\pi/\alpha\right)}\right).\tag{20}$$

#### 4.2. STP of a cellular device $\mathcal{P}_c$

In a Voronoi cell, a tagged cellular device  $c_0'$  can perform the uplink transmission to a tagged BS  $b_0'$ . When  $b_0'$  receives the desired signal from  $c_0'$ , it also suffers from the interference cause by the other transmitting BSs, cellular devices, D2D devices in HD/FD mode. Let  $\mathrm{SINR}_b\left(R_c,I_b\right)$  denote the SINR at the BS  $b_0'$ . The value of  $\mathrm{SINR}_b\left(R_c,I_b\right)$  is given by

$$SINR_{b}(R_{c}, I_{b}) = \frac{S_{b}}{I_{b} + \sigma^{2}} = \frac{P_{c}H_{c}R_{c}^{-\alpha}}{I_{b}^{b} + I_{b}^{c} + I_{b}^{H} + I_{b}^{F} + \sigma^{2}},$$
(21)

where  $S_b$ ,  $I_b$  and  $\sigma^2$  are the desired signal power, aggregate interference power and noise power at  $b_0'$ , respectively.  $P_c$ 

is the transmission power of cellular device,  $H_c$  and  $R_c$  are the channel power gain and transmission distance between  $c'_0$ and  $b'_0$ , respectively. Besides,  $I^b_b, I^c_c, I^H_c, I^F_c$  are interference from the other transmitting BSs, cellular devices, HD D2D devices and FD D2D devices at  $b'_0$ , respectively. Their values are given by

$$\begin{split} I_b^b &= \sum_{i \in \Phi_b^t} P_b H_i R_i^{-\alpha}, I_c^c = \sum_{i \in \Phi_c^t / \left\{ c_0' \right\}} P_c H_i R_i^{-\alpha}, \\ I_c^H &= \sum_{i \in \Phi_H^t} P_d H_i R_i^{-\alpha}, I_c^F = \sum_{i \in \Phi_F^t} P_d H_i R_i^{-\alpha}. \end{split}$$

Let  $\mathcal{P}_c$  denote the STP of cellular devices. Based on Eqs. (7)-(9),  $\mathcal{P}_c$  can be calculated by

$$\mathbb{P}_{c} = \mathbb{E}_{R_{c},I_{b}} \left[ \mathbb{P} \left( \text{SINR}_{b} \left( R_{c} \right) > \theta \right) \middle| \Phi \right]$$

$$= \int_{0}^{R_{v}} \mathbb{E}_{I_{b}} \left[ \mathbb{P} \left( \text{SINR}_{b} \left( r_{c}, I_{b} \right) > \theta \right) \right] \cdot f_{R_{c}} \left( r_{c} \right) dr_{c}$$
(22)

where  $f_{R_c}(r_c)$  is PDF of  $R_c$ , and  $R_c \in [0, R_v]$ . Since the cellular devices in each Voronoi cell follow the same location distribution,  $R_c$  has the same PDF as  $R_b$ , i.e.,  $f_{R_c}\left(r_c\right)$  =  $2\pi\lambda_b r_c$ . In Eq. (22),  $\mathbb{E}_{I_b}\left[\mathbb{P}\left(\mathrm{SINR}_b\left(r_c,I_b\right)>\theta\right)\right]$  can be calculated by

$$\begin{split} &\mathbb{E}_{I_{b}}\left[\mathbb{P}\left(\mathrm{SINR}_{b}\left(r_{c},I_{b}\right)>\theta\right)\right] \\ &=\mathbb{E}_{I_{b}^{b},I_{b}^{c},I_{b}^{H},I_{b}^{F}}\left[\mathbb{P}\left(\frac{P_{c}H_{c}R_{c}^{-\alpha}}{I_{b}^{b}+I_{b}^{c}+I_{b}^{H}+I_{b}^{F}+\sigma^{2}}>\theta\right)\right] \\ &=\exp\left(-s_{b}\sigma^{2}\right)\mathcal{L}_{I_{b}^{b}}\left(s_{b}\right)\mathcal{L}_{I_{b}^{c}}\left(s_{b}\right)\mathcal{L}_{I_{b}^{H}}\left(s_{b}\right)\mathcal{L}_{I_{b}^{F}}\left(s_{b}\right), \end{split} \tag{23}$$

where  $s_b = \frac{\mu\theta r_c^a}{P_c}$ . The terms  $\mathcal{L}_{I_b^b}\left(s_b\right)$ ,  $\mathcal{L}_{I_b^c}\left(s_b\right)$ ,  $\mathcal{L}_{I_b^H}\left(s_b\right)$ , and  $\mathcal{L}_{I_F}(s_b)$  are LTs of  $I_b^b, I_b^c, I_b^H$ , and  $I_b^F$  evaluated at  $s_b$ , respectively. Their values are given as follows.

$$\mathcal{L}_{I_{b}^{b}}(s_{b}) = \exp\left(-2\pi\lambda_{b}^{t}\left(s_{b}P_{b}\right)^{2/\alpha}\int_{\frac{R_{v}}{\left(s_{b}P_{b}\right)^{1/\alpha}}}^{\infty}\frac{y}{1+y^{\alpha}}\mathrm{d}y\right), \quad \mathbb{E}_{I_{d}}\left[\mathbb{P}\left(\mathrm{SINR}_{d}\left(r_{d},I_{d}\right)>\theta\right)\right]$$

$$= \mathbb{E}_{I_{d}^{b},I_{d}^{c},I_{d}^{H},I_{d}^{F}}\left[\mathbb{P}\left(\frac{P_{d}H_{d}r_{d}^{-\alpha}}{I_{d}^{b}+I_{d}^{c}+I_{d}^{H}+I_{d}^{F}}\right)\right]$$

$$= \mathbb{E}_{I_{d}^{b},I_{d}^{c},I_{d}^{H},I_{d}^{F}}\left[\mathbb{P}\left(\frac{P_{d}H_{d}r_{d}^{-\alpha}}{I_{d}^{b}+I_{d}^{c}+I_{d}^{H}+I_{d}^{F}}\right)\right]$$

$$= \exp\left(-s_{d}\sigma^{2}\right)\exp\left(-s_{d}I_{d}^{s}\right).$$

$$\mathcal{L}_{I_{d}^{b}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{c}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right),$$

$$\mathcal{L}_{I_{d}^{b}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{c}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right),$$

$$\mathcal{L}_{I_{b}^{H}}\left(s_{b}\right) = \exp\left(-\lambda_{H}^{t}\left(s_{b}P_{d}\right)^{2/\alpha}\cdot\frac{2\pi^{2}}{\alpha\sin\left(2\pi/\alpha\right)}\right),$$

$$\exp\left(-\lambda_{H}^{t}\left(s_{b}P_{d}\right)^{2/\alpha}\cdot\frac{2\pi^{2}}{\alpha\sin\left(2\pi/\alpha\right)}\right),$$

$$\exp\left(-\lambda_{H}^{t}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right)\right)$$

$$\exp\left(-\lambda_{H}^{t}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right)\right)$$

$$\exp\left(-\lambda_{H}^{t}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right)\right)$$

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$$\exp\left(-\lambda_{H}^{t}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right)\right)$$

$$\exp\left(-\lambda_{H}^{t}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{$$

$$\mathcal{L}_{I_{b}^{F}}\left(s_{b}\right) = \exp\left(-\lambda_{F}^{t}\left(s_{b}P_{d}\right)^{2/\alpha} \cdot \frac{2\pi^{2}}{\alpha\sin\left(2\pi/\alpha\right)}\right). \tag{27}$$

#### 4.3. STP of D2D device $\mathcal{P}_d$

For a D2D transmission from a tagged D2D device  $d_0^t$  to the other tagged D2D device  $d_0^r$ , the SINR<sub>d</sub>  $(R_d, I_d)$  at  $d_0^r$ can be expressed as

$$SINR_{d}(R_{d}, I_{d}) = \frac{S_{d}}{I_{d} + \sigma^{2}} = \frac{P_{d}H_{d}R_{d}^{-\alpha}}{I_{d}^{b} + I_{d}^{c} + I_{d}^{H} + I_{d}^{F} + I_{d}^{s} + \sigma^{2}}$$
(28)

where  $S_d$ ,  $I_d$  and  $\sigma^2$  are the desired signal power, aggregate interference power and noise power at  $d_0^r$ , respectively.  $P_d$ is the transmission power of D2D device,  $H_d$  and  $R_d$  are the channel power gain and transmission distance between  $d_0^t$  and  $d_0^r$ , respectively. Besides,  $I_b^b, I_c^c, I_c^H, I_c^F$  are interferences caused by the other transmitting BSs, cellular devices, HD D2D devices and FD D2D devices at  $d_0^r$ 's, respectively. Their values are given as follows.

$$\begin{split} I_b^b &= \sum_{i \in \Phi_b^t} P_b H_i R_i^{-\alpha}, I_c^c = \sum_{i \in \Phi_c^t} P_c H_i R_i^{-\alpha}, \\ I_c^H &= \sum_{i \in \Phi_H^t / \left\{d_0^t\right\}} P_d H_i R_i^{-\alpha}, \\ I_c^F &= \sum_{i \in \Phi_E^t / \left\{d_0^t\right\}} P_d H_i R_i^{-\alpha}. \end{split}$$

In addition,  $I_d^s = \kappa P_d \mathbb{1}_{FD}$  is the self-interference due to the FD D2D transmission,  $\kappa$  is the self-interference cancellation factor,  $\mathbb{1}_{FD}$  is the indicator function which takes value 1 representing D2D device operating in FD mode and 0 representing D2D device operating in HD mode.

Hence,  $\mathbb{P}_d$  can be expressed as

$$\mathbb{P}_{d} = \mathbb{E}_{I_{d},R_{d}} \left[ \mathbb{P} \left( \text{SINR}_{d} \left( R_{d}, I_{d} \right) > \theta \right) \right]$$

$$= \int_{0}^{d_{d}} \mathbb{E}_{I_{d}} \left[ \mathbb{P} \left( \text{SINR}_{d} \left( r_{d}, I_{d} \right) > \theta \right) \right] \cdot f_{R_{d}} \left( r_{d} \right) dr_{d}$$
(29)

where  $d_d$  is the maximum transmission distance of each D2D device, and  $f_{R_d}(r_d)$  is PDF of  $r_d$ . Considering  $r_d \in$  $[0,d_d], f_{R_d}\left(r_d\right) = 2 r_d/d_d^2. \text{ Then, } \mathbb{E}_{I_d}\left[\mathbb{P}\left(\text{SINR}_d\left(r_d,I_d\right) > \theta\right)\right])$ can be calculated by

$$\mathcal{L}_{I_{b}^{c}}\left(s_{b}\right) = \exp\left(-2\pi\lambda_{b}^{t}\left(s_{b}P_{b}\right)^{2/\alpha}\int_{\frac{R_{v}}{\left(s_{b}P_{b}\right)^{1/\alpha}}}^{\infty}\frac{y}{1+y^{\alpha}}\mathrm{d}y\right), \quad \mathbb{E}_{I_{d}}\left[\mathbb{P}\left(\mathrm{SINR}_{d}\left(r_{d},I_{d}\right)>\theta\right)\right]$$

$$= \mathbb{E}_{I_{d}^{b},I_{d}^{c},I_{d}^{H},I_{d}^{F}}\left[\mathbb{P}\left(\frac{P_{d}H_{d}r_{d}^{-\alpha}}{I_{d}^{b}+I_{d}^{c}+I_{d}^{H}+I_{d}^{F}+I_{d}^{S}+\sigma^{2}}>\theta\right)\right]$$

$$= \exp\left(-s_{d}\sigma^{2}\right)\exp\left(-s_{d}I_{d}^{S}\right).$$

$$\mathcal{L}_{I_{b}^{c}}\left(s_{b}\right) = \exp\left(-s_{d}\sigma^{2}\right)\exp\left(-s_{d}I_{d}^{S}\right).$$

$$\mathcal{L}_{I_{d}^{c}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{c}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right)\mathcal{L}_{I_{d}^{F}}\left(s_{d}\right),$$

$$(30)$$

where  $s_d = \frac{\mu \theta r_d^{\alpha}}{P_d}$ . The terms  $\mathcal{L}_{I_d^b}\left(s_d\right)$ ,  $\mathcal{L}_{I_d^c}\left(s_d\right)$ ,  $\mathcal{L}_{I_d^H}\left(s_d\right)$ and  $\mathcal{L}_{I_d^F}(s_d)$  are LTs of  $I_d^b$ ,  $I_d^c$ ,  $I_d^H$ , and  $I_d^F$  evaluated at  $s_d$ , respectively. Their values are given as follows.

$$\mathcal{L}_{I_d^b}\left(s_d\right) = \exp\left(-2\pi\lambda_b^t \left(s_d P_b\right)^{2/\alpha} \int_{\frac{d_b}{r_0\theta_c^{1/\alpha}}}^{\infty} \frac{y}{1 + y^{\alpha}} \mathrm{d}y\right),\tag{31}$$

Table 2 Parameters settings for simulations. Herein the notation 'x:y:z' indicates that a parameter varies from x to z in increments of y, while 'x, y' signifies that a parameter can take on the values x and y. For example, in the first row of Table 2, '-20:1:20' indicates that the parameter  $\theta$  ranges from -20 dB to 20 dB in steps of 1 dB, and '4, 5' denotes that the parameter  $\alpha$  can take the values 4 and 5, respectively.

Fi	gure	$\theta$ (dB)	α	$\kappa(dB)$	$\sigma^2(dBm)$	$d_b(m)$	$p_b^t$	$p_c^t$	$p_H$	$\lambda_b(/\mathrm{Km}^2)$	$\lambda_c(/\mathrm{Km}^2)$	$d_c(m)$	$P_d$ (dBm)	$\lambda_d(/\mathrm{Km}^2)$	$P_b(dBm)$	$P_c(dBm)$
4	(a)	-20:1:20	4,5	-70	-100	50	0.5	0.5	0.5	5	50	20	1	50	23	10
	(b)	-20:1:20	4	-60, -70	-100	50	0.5	0.5	0.5	5	50	20	1	50	23	10
	(c)	-20:1:20	4	-70	-100, -50	50	0.5	0.5	0.5	5	50	20	1	50	23	10
5	(a)	5	4	-70	-100	20:20:100	0.2, 0.8	0.5	0.5	20	50	20	1	50	23	10
	(b)	5	4	-70	-100	20:20:100	0.5	0.2, 0.8	0.5	20	50	20	1	50	23	10
	(c)	5	4	-70	-100	20:20:100	0.5	0.5	0.2, 0.8	20	50	20	1	50	23	10
6	(a)	5	4	-70	-100	50	0.5	0.5	0.5	5:5:30	20, 50	20	1	50	23	10
	(b)	5	4	-70	-100	0, 50	0.5	0.5	0.5	5:5:30	50	0, 30	1	50	23	10
	(c)	5	4	-70	-100	50	0.5	0.5	0.5	5:5:30	50	20	1, 5	50	23	10

$$\mathcal{L}_{I_d^c}\left(s_d\right) = \exp\left(-2\pi\lambda_c^u \left(s_d P_c\right)^{2/\alpha} \int_{\frac{d_c}{\left(s_d P_c\right)^{1/\alpha}}}^{\infty} \frac{y}{1 + y^{\alpha}} \mathrm{d}y\right),$$

$$(32)$$

$$\mathcal{L}_{I_d^H}\left(s_d\right) = \exp\left(-\lambda_H^t \left(s_d P_d\right)^{2/\alpha} \cdot \frac{2\pi^2}{\alpha \sin\left(2\pi/\alpha\right)}\right),$$

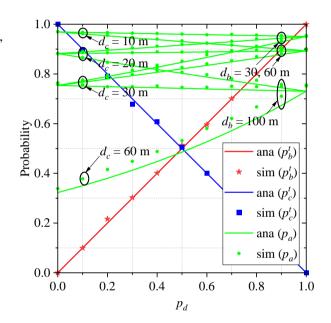
$$(33)$$

$$\mathcal{L}_{I_d^F}\left(s_d\right) = \exp\left(-\lambda_F^t \left(s_d P_d\right)^{2/\alpha} \cdot \frac{2\pi^2}{\alpha \sin\left(2\pi/\alpha\right)}\right).$$

$$(34)$$

#### 5. Performance Evaluation

This section presents extensive Monte Carlo simulations conducted in MATLAB to validate the accuracy of the proposed theoretical model. The simulation environment is built upon the system model detailed in Section 3. Table 2 summarizes the network parameter settings in our results, which are consistent with state-of-the-art research [13, 14, 47]<sup>4</sup>.Herein  $P_d=1$ dBm we used adapts for the practical power ranges (from 1mW to 1W) of D2D devices operating in WiFi HaLow [12]. In each simulation, the simulation region is defined as a circular disk with a radius of  $10^4$  m. A total of  $10^4$  iterations are performed for each simulation to obtain the average value. In all figures, the labels 'ana' and 'sim' represent the theoretical and simulation results, respectively.



**Figure 3:**  $p_b^t$ ,  $p_c^t$  and  $p_a$  versus  $p_d$ , where  $d_b$ = 30, 60, 100 m,  $d_c$ = 10, 20, 30, 60m.

## 5.1. Probabilities of transmitting BSs, transmitting cellular devices and activated D2D devices

Fig. 3 shows the variance of the probabilities of transmitting BSs  $p_b^t$ , transmitting cellular devices  $p_c^t$  and activated D2D devices  $p_a$  versus the changing values of downlink transmission probability  $p_d$ , BS guard zone's radius  $d_b$ , and cellular device guard zone's radius  $d_c$ . In the results, we have the following observations:

• As  $p_d$  increases,  $p_c^t$  decreases. This occurs because that either downlink or uplink transmission can happen in each Voronoi cell; thus, a higher  $p_d$  results in a lower  $p_c^t$ .

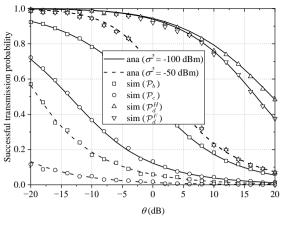
<sup>&</sup>lt;sup>4</sup>Due to page limitations, the parameter settings, such as the transmission power of BSs and cellular devices, are not comprehensively explored. In future work, one can choose suitable values for these parameter values to reflect the respective characteristics of the devices in diverse communication networks. For example,  $P_b$ =35 dBm for BSs and  $P_c$ =22 dBm for IoT devices in NB-IoT networks [10].

- For a given  $d_b$ ,  $p_a$  decreases as  $p_d$  increases when  $d_c$  is small. Conversely,  $p_a$  increases as  $p_d$  increases when  $d_c$  is large. The reasoning is as follows: with a small  $d_c$ , as  $p_d$  increases, the probability of a D2D device being within the guard zone of a transmitting BS rises, increasing the likelihood that the D2D device cannot be activated, hence  $p_a$  decreases. In contrast, with a large  $d_c$ , as  $p_d$  increases,  $p_c^t$  decreases, reducing the probability of a D2D device being within the guard zone of a transmitting cellular device, which subsequently decreases the likelihood that the D2D device cannot be activated, causing  $p_a$  to increase.
- For a given d<sub>c</sub>, p<sub>a</sub> increases as p<sub>d</sub> increases when d<sub>b</sub> is small, while p<sub>a</sub> decreases as p<sub>d</sub> increases when d<sub>b</sub> is large. The reasons are similar to those mentioned above.
- Given  $p_d$  and  $d_b$ , a larger  $d_c$  results in a smaller  $p_a$ . When  $p_d = 1$ ,  $p_a$  remains constant across different values of  $d_c$ , because there are no cellular devices transmitting in any Voronoi cells. Similarly, given  $p_d$  and  $d_c$ , a larger  $d_b$  results in a smaller  $p_a$ . When  $p_d = 0$ ,  $p_a$  remains constant across different values of  $d_b$ , because there are no BSs transmitting in any Voronoi cells
- For small values of  $d_b$  and  $d_c$  compared to the radius  $R_v$  of each Voronoi cell, the theoretical results closely align with the corresponding simulation ones, thereby validating the accuracy of our model. However, for large values of  $d_b$  and  $d_c$  relative to  $R_v$ , the theoretical and simulation results diverge, as D2D devices are more likely to be located in the overlap areas of the guard zones of BSs and D2D devices, leading to simulation results that exceed the theoretical predictions.

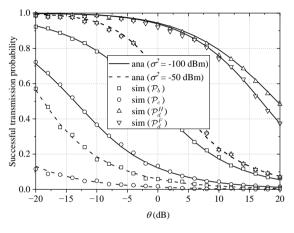
#### 5.2. STPs vs. $\theta$

Figs. 4 shows the varieties of STPs for BSs  $\mathcal{P}_b$ , cellular devices  $\mathcal{P}_c$ , D2D devices in HD mode  $\mathcal{P}_d^H$  and D2D devices in FD mode  $\mathcal{P}_d^F$  versus the changing values of the SINR threshold  $\theta$ , path-loss exponent  $\alpha$ , self-interference cancellation factor  $\kappa$ , and noise power  $\sigma^2$ . In the results, we have the following observations:

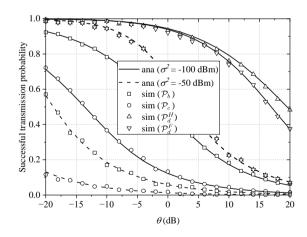
- Given  $\alpha$ ,  $\kappa$  and  $\sigma^2$ ,  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  decreases as  $\theta$  increases, as shown in Figs. 4(a)-(c). This is because an increase in  $\theta$  make it more difficult to decode signals from the cellular device, BS, and D2D device, respectively.
- For a fixed  $\theta$ , a larger  $\alpha$  leads to higher values of  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$ , as illustrated in Fig. 4(a). This is due to the fact that a larger  $\alpha$  results in greater attenuation of interference signals as they propagate through space, which in turn leads to higher SINRs at the BS, cellular device and D2D device. With increased SINRs, the probabilities  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  also rise.



(a)  $\alpha = 3, 4$ 



(b)  $\kappa = -60$ , -70 dB



(c)  $\sigma^2 = -50$ , -100 dBm

Figure 4:  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  versus  $\theta$ .

• For a fixed  $\theta$ , an increase  $\kappa$  results in a decrease in  $\mathcal{P}_d^F$ , while  $\mathcal{P}_d^H$ ,  $\mathcal{P}_b$  and  $\mathcal{P}_c$  remain relatively unchanged, as shown in Fig. 4(b). Note that the actual ratio value of  $\kappa$  (dB [14]) is expressed as  $10^{\kappa/10}$  (unitless [13]). Thus, a larger  $\kappa$  signifies greater self-interference at the FD D2D device, leading to a decrease in its STP. However,

the STPs of each BS, cellular device and HD D2D device are not significantly affected.

• For a fixed  $\theta$ , an increase in  $\sigma^2$  results in lower values of  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$ , as shown in Fig. 4(c). This is because that a larger  $\sigma^2$  leads to lower SINRs at each BS, cellular device and HD D2D device. Consequently, With decreased SINRs, the probabilities  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  also decline.

#### 5.3. STPs vs. $d_h$

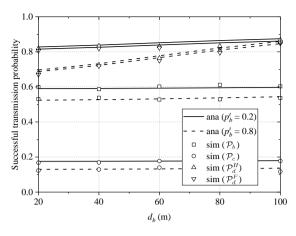
Figs. 5 shows the varieties of STPs of BSs  $\mathcal{P}_b$ , cellular devices  $\mathcal{P}_c$  and D2D devices in HD mode  $\mathcal{P}_d^H$  and D2D devices in FD mode  $\mathcal{P}_d^F$  versus the different settings of the radius of guard zone for BSs  $d_b$ , the transmission probability for BSs  $p_b^t$ , the transmission probability for cellular devices  $p_c^t$ , and the probability of HD D2D devices  $p_H$ . In the results, we have the following observations:

- Given  $p_b^t$ ,  $p_c^t$  and  $p_H$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  increase as  $d_b$  increases, while  $\mathcal{P}_b$  and  $\mathcal{P}_c$  remain relatively unchanged. This occurs because as  $d_b$  increases, the activated probability of D2D devices  $p_a$  decreases, fewer D2D transmissions lead to increased  $\mathcal{P}_d^H$  and  $\mathcal{P}_c^F$ . In contrast, the increase of  $d_b$  does not significantly affect  $\mathcal{P}_b$  and  $\mathcal{P}_c$ .
- Given d<sub>b</sub>, a larger p<sup>t</sup><sub>b</sub> results in lower values of P<sub>b</sub>, P<sub>c</sub>,
   P<sup>H</sup><sub>d</sub> and P<sup>F</sup><sub>d</sub>, as shown in Fig. 5(a). This is because increased transmissions from BSs to cellular devices may introduce more mutual interference, negatively impacting the STPs of BSs, cellular devices and D2D devices.
- Given  $d_b$ , a larger  $p_c^t$  similarly leads to lower values of  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$ , as depicted in Fig. 5(b). The reasons for this are analogous to those discussed above.
- Given d<sub>b</sub>, a larger p<sub>H</sub> results in higher values of P<sub>b</sub>,
   P<sub>c</sub>, P<sub>d</sub><sup>H</sup> and P<sub>d</sub><sup>F</sup>, as shown in Fig. 5(c). This occurs
   because increased HD D2D transmissions lead to a
   reduction in FD D2D transmissions, thereby decreasing the interference affecting the transmission of BSs,
   cellular devices and D2D devices, respectively.

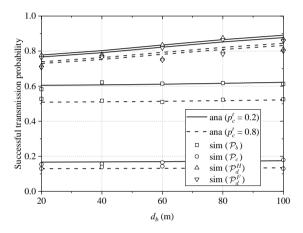
#### 5.4. STPs vs. $\lambda_b$

Figs. 6 shows the varieties of STPs of BSs  $\mathcal{P}_b$ , cellular devices  $\mathcal{P}_c$  and D2D devices in HD mode  $\mathcal{P}_d^H$  and D2D devices in FD mode  $\mathcal{P}_d^F$  versus the different settings of the density of BSs  $\lambda_b$ , the density of cellular devices  $\lambda_c$ , the radius of the guard zone of cellular devices  $d_c$  and the transmission power of D2D devices  $P_d$ . In the results, we have the following observations:

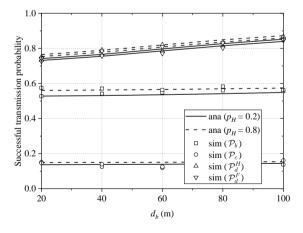
• Given  $\lambda_c$ ,  $d_b$ ,  $d_c$  and  $P_d$ ,  $\mathcal{P}_b$  and  $\mathcal{P}_c$  increase as  $\lambda_b$  increases, while  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  decrease. This is because an increase in  $\lambda_b$  reduces the area of each Voronoi cell, thus shortening the transmission distance of the



(a)  $p_h^t = 0.2, 0.8$ 



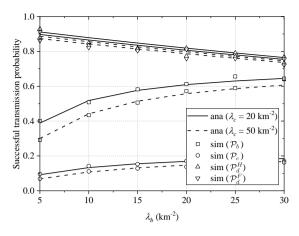
(b)  $p_c^t = 0.2, 0.8$ 



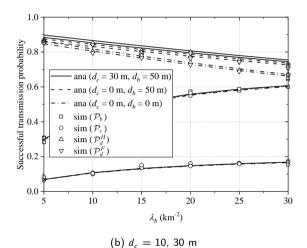
(c)  $p_H = 0.2, 0.8$ 

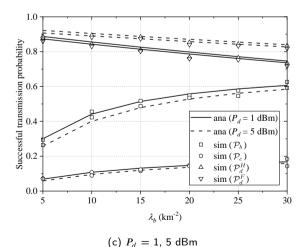
**Figure 5:**  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  versus  $d_b$ .

desired signal between the BS and cellular device pair, leading to higher  $\mathcal{P}_b$  and  $\mathcal{P}_c$ . Conversely, the increased density of BSs also elevates the interference power experienced by D2D devices, resulting in decrease in  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$ .



(a) 
$$\lambda_c = 10, 50 \text{ km}^{-2}$$





**Figure 6:**  $\mathcal{P}_b$ ,  $\mathcal{P}_c$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  versus  $\lambda_b$ 

For a given λ<sub>b</sub>, a larger λ<sub>c</sub> results in lower values of P<sub>b</sub>, P<sub>c</sub>, P<sub>d</sub><sup>H</sup> and P<sub>d</sub><sup>F</sup>, as shown in Fig. 6(a). This occurs because more transmissions from cellular devices can introduce additional interference to the transmissions of BSs, cellular devices and D2D devices, thereby decreasing their STPs.

- For a given  $\lambda_b$ ,  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$  are maximized when guard zones are set at both transmitting BSs and cellular devices, while they are minimized when no guard zones are implemented for either. Furthermore,  $\mathcal{P}_b$  and  $\mathcal{P}_c$  remain relatively unchanged, as illustrated in Fig. 6(b). This is because establishing guard zones reduces the activated probability of D2D devices  $p_a$ , leading to fewer D2D transmissions and thus increased  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$ , with negligible effects on  $\mathcal{P}_b$  and  $\mathcal{P}_c$ .
- For a given  $\lambda_b$ , a larger  $P_d$  results in higher  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$ ; conversely, a larger  $P_d$  leads to lower  $\mathcal{P}_b$  and  $\mathcal{P}_c$ , as shown in Fig. 6(c). This occurs because a higher  $P_d$  correlates with increased received desired signal power at the D2D device, enhancing  $\mathcal{P}_d^H$  and  $\mathcal{P}_d^F$ . However, a larger  $P_d$  also increases the undesired interference power received by the BSs and cellular devices, thus reducing  $\mathcal{P}_b$  and  $\mathcal{P}_c$ .

#### 5.5. Summary and Insights

**Summary**: All simulation results closely align with the theoretical ones, thus validating the accuracy of our analytical modeling<sup>5</sup>. From the results, we summarize three key observations below.

- Dense Coexistence of Cellular and D2D Devices: Increasing the density of BSs improves the STPs for both BSs and cellular devices.
- Guard Zones Around BSs and Cellular Devices: Expanding the radii of the two types of guard zones enhances the STP of D2D devices.
- HD/FD Mode Selection: Reducing the probability of D2D devices operating in FD mode increases their STP

*Insights*: Based on the above observations, our analytical modeling can assist practitioners, such as network operators or engineers, in estimating the practical performance of SAGINs. For instance, it allows for configuring key network parameters—including the density of deployed BSs, the radii of the two types of guard zones, and the probability of D2D devices operating in full-duplex mode—across various application scenarios.

#### 6. Conclusion and Discussions

#### 6.1. Conclusion

The HetIoT, integrating large-scale cellular and D2D devices, has become a foundational component for 5G/B5G networks. In the context of full-duplex D2D communications within HetIoT, guard zones are introduced around both

<sup>&</sup>lt;sup>5</sup>The minor discrepancies between some simulation values and theoretical predictions can be attributed to the limited simulations region or number of iterations. These issues can be mitigated by either improving the simulation parameters or enhancing computational hardware.

transmitting BSs and cellular devices to mitigate interference between concurrent cellular and D2D transmissions. This paper presents a novel spatial distribution model that effectively captures the location randomness and interdependencies of cellular and D2D devices. Using this model, it develops an analytical model to derive the expressions for the STPs of BSs, cellular, and D2D devices, accounting for the inherent randomness and interrelations between cellular and D2D transmissions, while also characterizing the complex mutual interference resulting from the two types of guard zones. Extensive Monte Carlo simulations validate the high accuracy of the proposed theoretical model. In future work, this modeling can be further explored to identify optimal parameter configurations, such as the radii of guard zones and the probability of D2D devices operating in FD mode, to enhance network performance.

#### 6.2. Discussions

From the perspective of technical applications, our analytical modeling can integrate several emerging technologies into HetIoT, including mobile edge computing (MEC) [48, 49], edge artificial intelligence (AI) [50], and digital twin [51]. For instance, when deploying MEC within HetIoT, local model training involves a large number of edge IoT devices and requires efficient transmission of model updates. Our model can be utilized to analyze transmission performance, providing insights that guide suitable parameter configurations to enhance efficiency and reliability in MEC environments. Similarly, the integration of edge AI in HetIoT applications necessitates rapid and reliable data exchange for real-time decision-making and adaptive learning. Our modeling can help assess the communication performance between distributed edge devices and identify suitable network parameters, such as device density and transmission power, to support low-latency AI tasks effectively. In the case of digital twin technology, HetIoT facilitates real-time mirroring of physical assets in the digital world, which requires high-throughput and low-latency data transmission. Our model can assist in analyzing the required network configurations to ensure seamless data synchronization and reliable communication between the physical and virtual layers, thereby enhancing the accuracy and responsiveness of digital twins.

By applying our analytical modeling, practitioners can optimize HetIoT deployments to support these advanced technologies, thereby unlocking new possibilities for industrial automation, intelligent transportation, and other IoT-driven domains.

#### CRediT authorship contribution statement

Yulei Wang: Conceptualization, Methodology, Formal analysis, Software, Validation, Writing—original draft, Writing—review & editing. Li Feng: Supervision, Writing—review & editing, Project administration, Funding acquisition. Yalin Liu: Supervision, Writing—review & editing. Zhongjie Li: Writing—review & editing.

#### **Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### **Data Availability**

The data underlying the results presented in the study are available within the paper.

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