浙江大学 2018-2019 学年 春夏 学期

《Artificial Intelligence》课程期末考试试卷

| | 课程号: | 21191890 | _,开课学院 : | _ 计算机科学与技术学院_ |
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考试试卷: A卷、B卷(请在选定项上打√)

考试形式:闭、开卷(请在选定项上打√),允许带 入场

考试日期: __2019_年_7_月_1_日,考试时间: __120_分钟

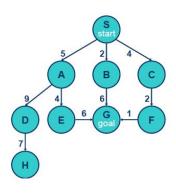
诚信考试,沉着应考,杜绝违纪。

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1. Fill in the blanks (20 points, 1 points/each blank)

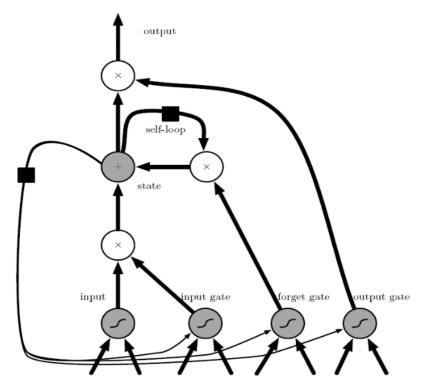
1) As shown in the figure below, we start from the state S and search the path to the goal sate G. Using the depth-first search approach, we expand the search node by going in depth and preserve the node list in a stack. When we reach to the goal state G, the depth-first search expand the node sequence as {S, ______, G} and finally stops at the node list as {______}. With the edge cost on the search tree branches, the returned search cost is . Please write the search sequence of the visiting nodes and the final node list.



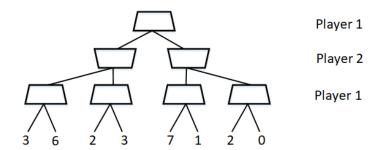
2) To measure the performance of the proposed search algorithm, we will evaluate its _____ ability that guarantees to find a solution when there is one. Moreover, we also want to analyze

| | its, which is whether our sear | ch algorithm can find the optima | al solution. Besides, |
|----|--|---|---------------------------|
| | the time complexity and space complexity | of the algorithm are another two | metrics we want to |
| | know exactly. | | |
| 3) | In a reinforcement learning problem, given | n two reward sequence (1,1,0,0) | and (0,0,1,1)) due |
| | to state transitions, assume γ =0.99, the disc | counted sum of rewards is | and |
| 4) | In an adversarial search, we want to comp | ute an optimal strategy. | tell us how to |
| | evaluate the leaf states at the cut-off. To sp | pare the search time cost, we car | n prune unnecessary |
| | parts of the search tree using the | approaches. | |
| 5) | In the two-player adversarial search, for t | he MIN node achieved α denot | ed in the upper left |
| | site, we can prune the MIN node (at the | e lower-right site) and all its | children when α is |
| | than <i>n</i> . Symmetrically, for a N | MAX node achieved β in the upp | per left site, we also |
| | can prune a MAX node (at the lower-right | site) and all its children when β | isthan |
| | n. | | |
| | | | |
| | MAX | MIN | |
| | NAIN. | MAX R | |
| | MIN W | /IS/ | |
| | | | |
| | MAX | MIN | |
| | MIN | MAX | , m |
| | \bigwedge | | |
| 6) | For the distribution $p(t \mathbf{x}, \mathbf{w}, \beta) = \mathbb{N}(t y(\mathbf{x}, \mathbf{w}, \beta))$ | $(\mathbf{x}, \mathbf{w}), \beta^{-1}$), where we have the | assumption that the |
| | additive noise obeys to the standard norm | al distribution $\mathbb{N}(0, \beta^{-1})$. The r | naximization of the |
| | logarithm likelihood solution of w is equal | ivalent to solve w when the | (between |
| | estimated $y(\mathbf{x}_n, \mathbf{w})$ and the labelled output | t _n) achieves its minimum value | . The maximization |
| | posterior solution of w is equivalent to sol- | ve this cost function with a | term as |
| | the form of $\lambda \mathbf{w}^{\mathrm{T}} \mathbf{w}$. | | |
| 7) | Given the limited training data, we should | divide the available data into the | nree parts, including |
| | the training set, and | We will select the mo | odel with the best |
| | generalization performance. | | |

- 8) There are several approaches to solving decision problems in statistical learning method, all of which have been used in practical applications. One (i.e., the generative models) solves the inference problem usually by modeling the ______ distribution for each class individually, especially in the Bayesian learning theory. The second method (i.e., discriminant models) inferences the class label by calculating the _____ probability directly.
- As shown in the black diagram of the long-short term memory (LSTM) recurrent network "cell", an input feature is computed with a regular artificial neuron unit. Its value can be accumulated into the state if the sigmoidal ______ gate allows it. The state unit has a linear self-loop whose weight is controlled by the ______ gate. Please find the answer words in the following LSTM figure.



10) Fill in the values of each of the nodes in the following Minimax tree. The upward pointing trapezoids correspond to maximizer nodes (layer 1 and 3 for Player 1), and the downward pointing trapezoids correspond to minimizer nodes (layer 2 for Player 2). Each node has two actions available, Left and Right. Mark the sequence of actions in the following figure that correspond to Minimax play.



2. Single Choice (50 points, only one of the options is correct. 2 points/one question)

- Consider a graph search problem where for every action, the cost is at least ϵ , with $\epsilon > 0$. Assume the used heuristic is consistent. Which of the following statement is TRUE?
 - A. Depth-first graph search is guaranteed to return an optimal solution
 - B. Greedy graph search is guaranteed to return an optimal solution
 - C. A* graph search is guaranteed to expand no more nodes than depth-first graph search.
 - D. A* graph search is guaranteed to expand no more nodes than uniform-cost graph search.
- 2) Which of the following statement(s) is / are TRUE for Gradient Decent (GD) and Stochastic Gradient Decent (SGD)?
 - (i) In GD and SGD, you update a set of parameters in an iterative manner to minimize the error function. (ii) In SGD, you have to run through all the samples in your training set for a single update of a parameter in each iteration. (iii) In GD, you either use the entire data or a subset of training data to update a parameter in each iteration.

A.i B. ii C. iii D. i, ii E. ii, iii F. i, ii, iii

3) Below are the 8 actual values [0,0,0,1,1,1,1,1] of target variable in the train file. What is the entropy of the target variable?

A. $- (5/8 \log(5/8) + 3/8 \log(3/8))$ B. $5/8 \log(5/8) + 3/8 \log(3/8)$

C.
$$-(3/8 \log(5/8) + 5/8 \log(3/8))$$
 D. $5/8 \log(3/8) - 3/8 \log(5/8)$

4) Here are the defining equations for a LSTM cell.

$$i_{t} = \sigma \left(W^{(i)} x_{t} + U^{(i)} h_{t-1} \right)$$

$$f_{t} = \sigma \left(W^{(f)} x_{t} + U^{(f)} h_{t-1} \right)$$

$$o_{t} = \sigma \left(W^{(o)} x_{t} + U^{(o)} h_{t-1} \right)$$

$$\widetilde{c}_{t} = \tanh \left(W^{(c)} x_{t} + U^{(c)} h_{t-1} \right)$$

$$c_{t} = f_{t} \circ c_{t-1} + i_{t} \circ \widetilde{c}_{t}$$

$$h_{t} = o_{t} \circ \tanh \left(c_{t} \right)$$

Recall that \circ denotes element-wise multiplication and that σ denotes the sigmoid function. Which of the following statement is TRUE?

- A. If x_t is the 0 vector, then $h_t = h_{t-1}$.
- B. If f_t is very small or zero, then error will not be back-propagated to earlier time steps.
- C. The entries of f_t , i_t , o_t are non-negative.
- D. f_t , i_t , o_t can be viewed as probability distributions. (i.e., their entries are non-negative and their entries sum to 1.)
- 5) Minmax is the canonical game search algorithms, which can return an optimal action assuming we have a perfect opponent play. Which one of the following options is FALSE:
 - A. When the search tree are too large, Minmax is completely infeasible
 - B. We can limit the search depth to spare the memory space
 - C. Theoretically, Minmax is complete and optimal
 - D. The space complexity of minmax is $O(b^m)$, where b is the branching factor, m is the search depth.
- 6) Cut-off strategy is usually used to reduce the search space. The effectivity of the cut-off strategy depends on the heuristic evaluation function, which can tune nonterminal nodes into terminal leaves. Which choice is FALSE:

- A. The proposed evaluation function should order the terminal states in the same way as the true utility function.
- B. To make the search faster, the computation of the heuristic evaluation function cannot cost too long time.
- C. Cut-off strategy is an imperfect real-time decision making approach;
- D. The heuristic evaluation function of nonterminal states should not correlated with the actual chances of winning.
- 7) A data set $X = \{x_1, x_2, ..., x_N\}^T$, which are drawn independently (independent and identically distributed, i.i.d) from a Gaussian distribution $\mathbb{N}(\mu, \sigma^2)$ whose mean μ and variance σ^2 are unknown. We can get the likelihood function for the Gaussian as:
 - A. $\prod_{n=1}^T \mathbb{N}(x_n|\mu,\sigma^2)$
- B. $\prod_{n=1}^{N} \mathbb{N}(x_n | \mu, \sigma^2)$
- C. $\sum_{n=1}^{N} \mathbb{N}(x_n | \mu, \sigma^2)$
- D. $\sum_{n=1}^{T} \mathbb{N}(x_n | \mu, \sigma^2)$
- 8) The Fisher's linear discriminant criterion is defined as be _____

A. the ratio of the distance between the projected mean of the two classes vs. the projected mean of the whole data set

- B. the ratio of the projected mean of the whole data set vs. the distance between the projected mean of the two classes
- C. Generalized Rayleigh quotient
- D. the sum of the within-class variance and the between-class variance.
- For the perceptron, we minimize the perceptron criterion to seek the weight vector w. Given dataset $X = \{x_1, x_2, ..., x_N\}^T$, Denote \mathcal{M} as the set of all misclassified patterns, ϕ_n as the feature of the input pattern x_n , and t_n as the output class label for the input x_n . We want to minimize the error function ______ using the stochastic gradient descent algorithm in the iterative form as ______. η is the learning rate parameter and τ is the iterative step number.

A.
$$-\sum_{n\in\mathcal{M}} \mathbf{w}^{\mathsf{T}} \phi_n t_n$$
, $\mathbf{w}^{(\tau+1)} = \mathbf{w}^{\tau} + \eta \phi_n t_n$

B.
$$-\sum_{n=1}^{N} \mathbf{w}^{\mathsf{T}} \phi_n t_n$$
, $\mathbf{w}^{(\tau+1)} = \mathbf{w}^{\tau} + \eta \phi_n t_n$

C.
$$-\sum_{n=1}^{N} \mathbf{w}^{\mathsf{T}} \phi_n t_n, \ \mathbf{w}^{(\tau+1)} = \mathbf{w}^{\tau} - \eta \phi_n t_n$$

D.
$$-\sum_{n\in\mathcal{M}} \mathbf{w}^{\mathsf{T}} \phi_n t_n$$
, $\mathbf{w}^{(\tau+1)} = \mathbf{w}^{\tau} - \eta \phi_n t_n$

- 10) Since K-means clustering is an iterative process, we need to set its iteration termination conditions. Which of the following sentences correctly describes the iteration termination condition of K-means clustering?
 - A. Has formed K clustering sets, or has reached the upper limit of iteration times.
 - B. Has reached the upper limit of iteration times, or the centroid of clustering remains basically unchanged in the two iterations before and after.
 - C. Has reached the upper limit of iteration times, or each sample to be clustered belongs to a unique cluster set.
 - D. K clustering sets have been formed, or each sample to be clustered belongs to a unique clustering set.
- 11) Assume q(z) is a distribution defined over the latent variables, and we have defined $L(\mathbf{q}, \boldsymbol{\theta}) = \sum_{z} q(z) \ln\{\frac{p(X, Z|\boldsymbol{\theta})}{q(z)}\} \text{ and } KL(\mathbf{q}||\mathbf{p}) = -\sum_{z} q(z) \ln\{\frac{p(Z|X, \boldsymbol{\theta})}{q(z)}\}, \text{ for any choice of } \mathbf{p}(Z, \mathbf{q}) = \sum_{z} q(z) \ln\{\frac{p(Z|X, \boldsymbol{\theta})}{q(z)}\}$ q(z), which of the following decomposition holds? _____

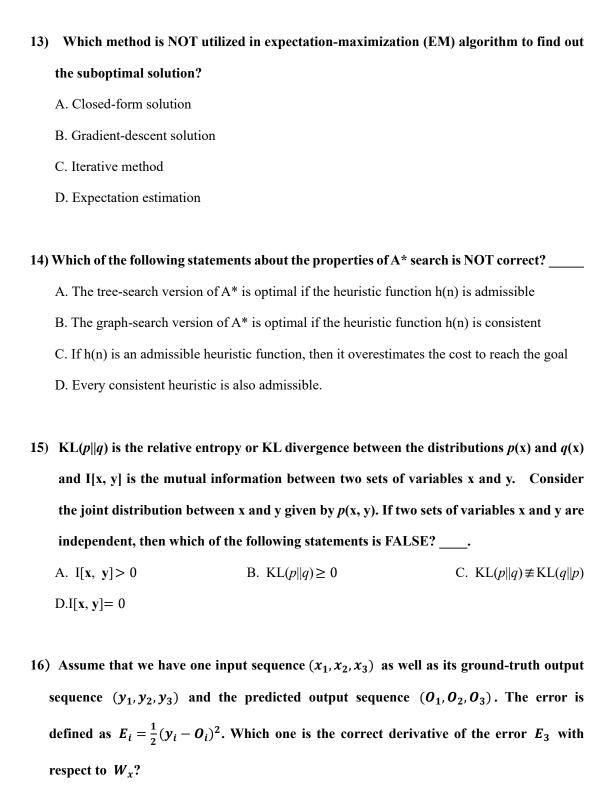
A
$$L(a|A) = lnn(X|A) + KL(a|ln)$$

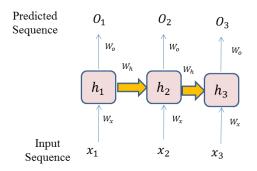
A.
$$L(q, \theta) = lnp(X|\theta) + KL(q||p)$$
 B. $lnp(X|\theta) = L(q, \theta) + KL(q||p)$

C.
$$KL(q||p) = lnp(X|\theta) + L(q,\theta)$$
 D. $L(q,\theta) = lnp(X, Z|\theta) + KL(q||p)$

D.
$$L(q, \theta) = lnp(X, Z|\theta) + KL(q||p|)$$

- 12) According to the intuitive definition of reinforcement learning, which one is TRUE in the following choices?
 - A. Reinforcement Learning learns the map from environment input x to the corresponding label y
 - B. Reinforcement Learning discover data structures and patterns of the dataset in the unsupervised manner
 - C. With the environment feedback, reinforcement learning conducts the sequential decision process to find the optimal trajectory
 - D. Reinforcement learning algorithms require a fully-observable and accurately sensible





$$\text{A.} \quad \frac{\partial E_3}{\partial W_x} = \frac{\partial E_3}{\partial O_3} \frac{\partial O_3}{\partial h_3} \frac{\partial h_3}{\partial W_x} + \frac{\partial E_3}{\partial O_3} \frac{\partial O_3}{\partial h_3} \frac{\partial h_3}{\partial h_2} \frac{\partial h_2}{\partial W_x} + \frac{\partial E_3}{\partial O_3} \frac{\partial O_3}{\partial h_3} \frac{\partial h_3}{\partial h_2} \frac{\partial h_2}{\partial h_1} \frac{\partial h_1}{\partial W_x}$$

B.
$$\frac{\partial E_3}{\partial W_x} = \frac{\partial E_3}{\partial O_3} \frac{\partial O_3}{\partial h_3} \frac{\partial h_3}{\partial W_x}$$

C.
$$\frac{\partial E_3}{\partial W_x} = \frac{\partial E_3}{\partial O_3} \frac{\partial O_3}{\partial h_3} \frac{\partial h_3}{\partial W_x} + \frac{\partial E_2}{\partial O_2} \frac{\partial O_2}{\partial h_2} \frac{\partial h_2}{\partial W_x} + \frac{\partial E_1}{\partial O_1} \frac{\partial O_1}{\partial h_1} \frac{\partial h_1}{\partial W_x}$$

D.
$$\frac{\partial E_3}{\partial W_x} = \frac{\partial E_3}{\partial O_3} \frac{\partial O_3}{\partial h_3} \frac{\partial h_3}{\partial W_x} + \frac{\partial E_3}{\partial O_3} \frac{\partial O_3}{\partial h_3} \frac{\partial h_3}{\partial W_h}$$

17) Which sentence is FALSE in terms of the traditional recurrent neural network (RNN) and LSTM (long short-term memory) model?

- A. In LSTM, there are input gate, output gate and forget gate.
- B. LSTM can avoid the problem of gradient vanishing.
- C. Unlike LSTM, RNN cannot encode the temporal dependence among sequential data.
- D. The parameters in LSTM and RNN can be optimized by error backpropagation.

18) We can structure the correlation degree between two groups of variables to a certain value range. The Pearson Correlation between X and Y is denoted as corr(X,Y). Which description sentence is FALSE in the following sentence?

- A. Pearson Correlation coefficient measures the degree of linear correlation between variable X and Y. The bigger |corr(X, Y)|, the greater linear correlation between these two variables is.
- B. |corr(X, Y)| = 0 means no linear correlation between X and Y (There might be nonlinear correlation between them).
- C. If X and Y are independent, then |corr(X,Y)| = 0, and there is no linear or nonlinear relationship between X and Y.

D. If X and Y are uncorrelated, they must be independent.

19) What are some practical problems with the sigmoidal activation function in neural nets?

- A. It is convex, and convex functions cannot solve nonconvex problems.
- B. It can have negative values.
- C. It does not work well with the entropy loss function.
- D. Gradients are small for values away from 0, leading to the "Vanishing Gradient" problem for large or recurrent neural nets.

20) Which of the following statements is FALSE in describing probability approximately correct (PAC)?

- A. Strong learnable model means that the learning model can recognize and classify most samples with high accuracy.
- B. Strong learnable model means that the learning model can only recognize and classify some samples, and its accuracy is slightly higher than that of random guess.
- C.Strong learning and weak learning are equivalent, that is, if a "weak learning algorithm" has been found, it can be boosted to a "strong learning algorithm".
- D. Under the background of approximate correctness of probability, there are "strong learnable model" and "weak learnable model".

21) Which search algorithm imposes a fixed depth limit on nodes?

- A. Depth-limited search
- B. Depth-first search
- C. Iterative deepening search
- D. Bidirectional search

22) Which of the following machine learning methods does not utilize annotated data?

- A. Semi-supervised Learning
- B. Unsupervised Learning
- C. Regression analysis

D. Supervised learning

23) Since K-means clustering is an iterative process, we need to set its iteration termination conditions. Which of the following sentences correctly describes the iteration termination condition of K-means clustering?

- A. Has formed K clustering sets, or has reached the upper limit of iteration times.
- B. Has reached the upper limit of iteration times, or the centroid of clustering remains basically unchanged in the two iterations before and after.
- C. Has reached the upper limit of iteration times, or each sample to be clustered belongs to a unique cluster set.
- D. K clustering sets have been formed, or each sample to be clustered belongs to a unique clustering set.

24) In reinforcement learning, through which two steps of iteration, to learn the best strategy?

- A. Dynamic Programming and Q-Learning
- B.Q-learning and greedy strategy optimization
- C. Policy improvement and policy evaluation
- D. Value function calculation and action-value function calculation

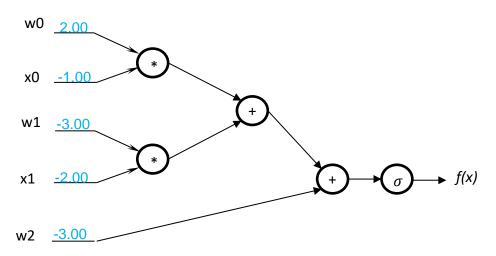
25) Boosting is a typical ensemble learning method to construct a strong leaner by:

- A. training the weak base classifiers in parallel
- B. the items in the dataset are treated equally with the same weight
- C. the prediction is achieved by the weighted majority voting schema
- D. only apply to the classification problem

3. Calculus and Analysis (30 points)

1) (Neural Network, 8 points) Backpropagation is used to efficiently train neural networks (NNs) following a gradient descent approach that exploits the chain rule. Given some function f(x)

where x is a vector of inputs and we are interested in computing the gradient of f(x) at x. Let $f(x) = \sigma(w_0x_0 + w_1x_1 + w_2)$, where w_0, w_1 and w_2 are the parameters and $\sigma()$ is sigmoid function ($\frac{\mathrm{d}\sigma(x)}{\mathrm{d}x} = (1 - \sigma(x))\sigma(x), \sigma(1) = 0.73, \frac{\mathrm{d}\sigma(x)}{\mathrm{d}x}|_{x=1} = 0.2$), please compute the gradient $\frac{\partial f}{\partial w_0}$, $\frac{\partial f}{\partial x_0}$, $\frac{\partial f}{\partial w_1}$ and $\frac{\partial f}{\partial x_1}$, and at $(w_0, x_0, w_1, x_1, w_2) = (2, -1, -3, -2, -3)$:



(a)
$$\frac{\partial f}{\partial w_0} =$$
 _____ (b) $\frac{\partial f}{\partial x_0} =$ _____ (c) $\frac{\partial f}{\partial w_1} =$ _____ (d) $\frac{\partial f}{\partial x_1} =$ _____

2) (Deep learning, 8 points)

(a) Convolution is very important in deep convolutional neural network. Given 7*7 input shown in Figure (1) and 3*3 convolutional kernel in Figure (2), please calculate the convolution output of the top line with stride 2 and no padding. (2 points)

| 1 | 1 | 2 | 4 | 5 | 6 | 7 |
|---|---|---|---|---|---|---|
| 0 | 1 | 2 | 3 | 3 | 2 | 9 |
| 2 | 0 | 0 | 2 | 1 | 2 | 4 |
| 1 | 2 | 2 | 1 | 1 | 8 | 8 |
| 5 | 6 | 7 | 7 | 7 | 8 | 3 |
| 8 | 7 | 4 | 4 | 9 | 0 | 1 |
| 2 | 5 | 3 | 9 | 4 | 3 | 1 |

| 1 | 1 | 0 |
|---|----|----|
| 1 | 0 | -1 |
| 0 | -1 | -1 |

Figure (2)

- (b) Given same input and filter as (a), please calculate the convolution output at the upper left corner with stride 1 and zero padding. (2 points)
- (c) what are the output sizes of convolution layer in (a) and (b), respectively? (2 points)
- (d) Given a single depth slice in Figure (3), please give out the max-pooling value of this slice with 2×2 filters and stride 2. (2 points)

| 1 | 1 | 2 | 4 |
|---|---|---|---|
| 5 | 6 | 7 | 8 |
| 3 | 2 | 1 | 0 |
| 1 | 2 | 3 | 4 |

Figure (3)

3) (Reinforcement Learning, 8 points) In robot movement problem, the definitions of state, action, decay factor, initial/terminal state, and reward are as follows:

states:
$$S = \{s_1, s_2, ..., s_9, s_d\}$$

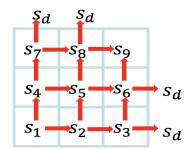
actions:
$$A = \{up, right\}$$

decay factor:
$$\gamma = 0.99$$

initial state:
$$S_0 = s_1$$

terminal state:
$$S_T = \{s_9, s_d\}$$

$$\text{reward: } \mathbf{R} = \left\{ \begin{array}{rl} 1, & \text{if } S_{t+1} = s_9 \\ -1, & \text{if } S_{t+1} = s_d \\ 0, & \text{otherwise} \end{array} \right.$$



Referring to the given Q-learning algorithm and initialization, compute the corresponding q value function and policy after the first and second episode. (The q function and policy is required to provide in separate tables. Keep 3 digits after the decimal point.)

Initialize q_{π} : a/b represents $q_{\pi}(s, up) = a$, $q_{\pi}(s, right) = b$. The value of the q function of all terminal states is set to 0/0, and the rest of the state can be randomly initialized, here set 0.2/0.

Initialize s: s_1 .

The algorithm of Q-Learning is as follows:

```
Initialize q_{\pi}
Loop:
   initialize s as initial state loop:
   a = \operatorname{argmax}_{a'} q_{\pi}(s, a')
   conduct action a, observe reward R and next state s'
   update q_{\pi}(s, a) \leftarrow q_{\pi}(s, a) + \alpha \left[ R + \gamma \max_{a'} q_{\pi}(s', a') - q_{\pi}(s, a) \right]
   s \leftarrow s'
   until s is the terminal state
Until q_{\pi} converges
```

- (a) Please list out the initial state and the action policy before the first episode (both in a 3*3 table) (2 points)
- (b) Please denote all the terminal states in the state table (2 points).
- (c) Please calculate the q value and present the policy for each state after the first episode (2 points)
- (d) Please calculate the q value and present the policy for each state after the second episode (2 points)
- 4) (PCA, 6 points) Eigenface method is a principal component analysis method for face image dimensionality reduction.
 - a) Please give out the summary description of the Eigenface method (3 points).

b) Please describe the advantages and disadvantages of the Eigenface method (3 points).

《Artificial Intelligence》

Final Examination Answer Sheet

| Name: | | | | | Student ID |
|------------|----------------------|-------------|---------------|---|------------|
| Dept.: | | | | | |
| Section | 1 | 2 | | 3 | Total |
| Score | | | | | |
| Reviewer | | | | | |
| 1. Fill in | the blanks (20 point | s, 1pt/per) | | | |
| 1) | ,, | | , | | |
| 2) | | | | | |
| 3) | ,, | | | | |
| | | | | | |
| 5) | ,, | | | | |
| | | | | | |
| 7) | , | | - | | |
| 8) | , | | | | |
| 9) | , | | | | |
| 10). | | | | | |
| | | | Player 1 | | |
| | | 7 | Player 2 | | |
| | A A | | Player 1 | | |
| 3 6 | 2 3 7 1 | | Player 1 | | |

2. Multiple Choice (50 points, 2pt/per)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|----|----|----|----|----|----|----|----|----|
| | | | | | | | | | |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| | | | | | | | | | |
| 21 | 22 | 23 | 24 | 25 | | | | | |
| | | | | | | | | | |

- 3. Calculus and Analysis (30 points)
- 1) (Neural Network, 8 points)

(a)
$$\partial f/\partial w_0 =$$

(b)
$$\partial f/\partial x_0 =$$

(c)
$$\partial f/\partial w_1 =$$

(d)
$$\partial f/\partial x_1 =$$

- 2) (Deep Learning, 8 points)
 - (a) (2 points)
 - (b) (2 points)
 - (c) (2 points)

| (d) (2 points) | |
|--------------------------------------|---------------------|
| 3) (Reinforcement (a) (2 points) | Learning, 8 points) |
| (b) (2 points) | |
| (c) (2 points) | |
| (d) (2 points) | |
| 4) (PCA, 6 points) (a) (3 points) | |

(b) (3 points)